

**Recitation 5, Friday February 23**

**List (+ Recursion + Orders of Growth) Problems**

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Fill in the code for these recursive procedures. Assume recursive processes (not iterative).

1. This procedure returns the length (i.e., number of elements) in a list.

```
(define (length lst)
  (if (null? lst)
      0
      (+ 1 (length (cdr lst)))))
```

time =  $\Theta(n)$   
 space =  $\Theta(n)$   
 n is length of list arg

2. This procedure returns the nth element of a list, where the first element index is 0.

```
(define (list-ref lst n)
  (if (= n 0)
      (car lst)
      (list-ref (cdr lst) (- n 1))))
```

time =  $\Theta(n)$   
 space =  $\Theta(n)$   
 n is the element index n

3. This procedure returns #t if obj is an element of a list; #f if it is not.  
 (Hint: Use the procedure equal?.)

```
(define (member? obj lst)
  (cond ((null? lst) #f)
        ((equal? obj (car lst)) #t)
        (else (member? obj (cdr lst)))))
```

time =  $\Theta(n)$   
 space =  $\Theta(1)$   
 n is length of list arg

4. The procedure returns a new list that has exactly one instance of each element in the original list.  
 (Hint: Use the procedure member?.) e.g., (remove-duplicates (list 1 2 1 2 3 4)) => (1 2 3 4)

```
(define (remove-duplicates lst)
  (cond ((null? lst) '())
        ((member? (car lst) (cdr lst))
         (remove-duplicates (cdr lst)))
        (else (cons (car lst)
                     (remove-duplicates (cdr lst))))))
```

time =  $\Theta(n^2)$  } for worst-case  
 space =  $\Theta(n)$   
 n is length of list arg

*lists are  $\Theta(n)$*  (with arrow pointing to the recursive call)

*or lst, since it's empty* (with arrow pointing to the null case)

*1 pending operation* (with arrow pointing to the cons operation)