

## Actor-Critic Policy Learning in Cooperative Planning

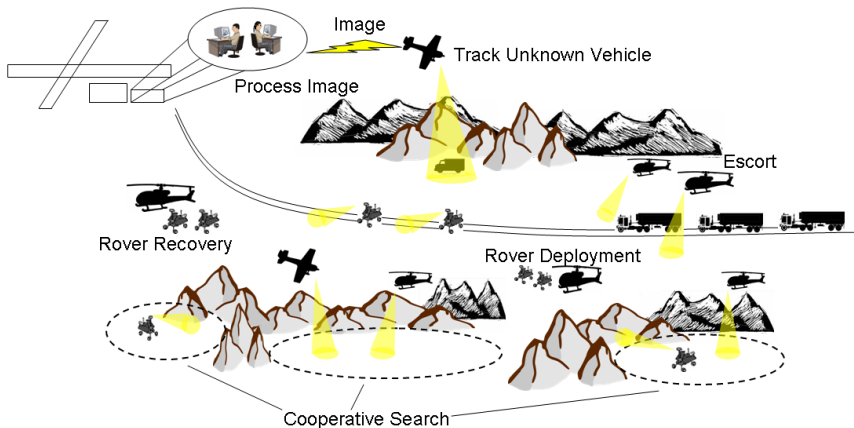
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# Motivating Example



A. Whitten, 2010

# Challenges of Cooperative Planning



- ① Cooperative planning uses **models**
  - E.g. vehicle dynamics, fuel use, rules of engagement, embedded strategies, desired behaviors, etc...
  - Models enable anticipation of likely events & prediction of resulting behavior
- ② Models are **approximated**
  - Planning with stochastic models is time consuming → Model **simplification**
  - Un-modeled uncertainties, parameter uncertainties
- ③ Result is **sub-optimal** planner output
  - Sub-optimality range from  $\epsilon$  to catastrophic
  - **Mismatch** between actual and expected performance

## Open Questions



- ① How can current multi-agent planners balance between robustness and performance **better**?
- ② How should the learning algorithms be formulated to best **address the errors and uncertainties** present in the multi-agent planning problem?
- ③ How can a learning algorithm be formulated to **enable a more intelligent planner response**, given stochastic models?

# Research Objectives



## Focus

- ▶ How can a learning algorithm be formulated to **enable a more intelligent planner response**, given stochastic models?

## Objectives

- ▶ Increase model fidelity to narrow the **gap** between expected and actual performance
- ▶ Increase cooperative planner **performance** over time

## Two Worlds



- ▶ Cooperative Control
  - Provides **fast** solutions
  - **Sub-optimal**
- ▶ Online Learning Techniques
  - Handles **stochastic** system and unknown models
  - **High** sample complexity
  - Might **crash** the plane to learn!
- ▶ Can we take the best of the both worlds?

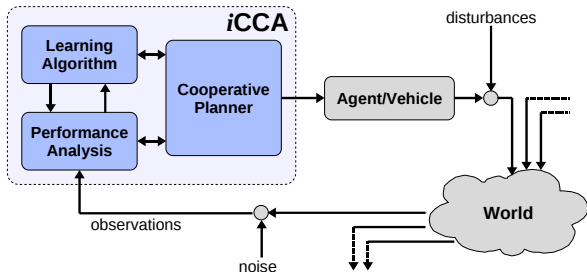
## Best of the Both Worlds



- ▶ Cooperative control scheme that **learns** over time
  - Learning → Improve Sub-optimal Solutions
  - Fast Planning → Reduce Sample Complexity
  - Fast Planning → Avoid Catastrophic plans



# A Framework for Planning + Learning



- ▶ **Template** architecture for multi-agent planning and learning
- ▶ A cooperative planner **coupled** with learning and analysis algorithms to **improve future plans**
  - Distinct elements cut combinatorial complexity of full integration and enable decentralized planning and learning
- ▶ Intelligent cooperative control architecture (iCCA)





## Merging Point

- ▶ Deterministic  $\rightarrow$  Stochastic
  - Plan (Trajectory)  $\rightarrow$  Policy (Behavior)
- ▶ Import a plan into a policy
  - **Bias** the policy for those states on the planned trajectory
  - Need a method to **explicitly** represent the policy
- ▶ Avoid taking actions with unsustainable outcome
  - **Override** with the safe (planned) action
  - Provide a **virtual** negative feedback

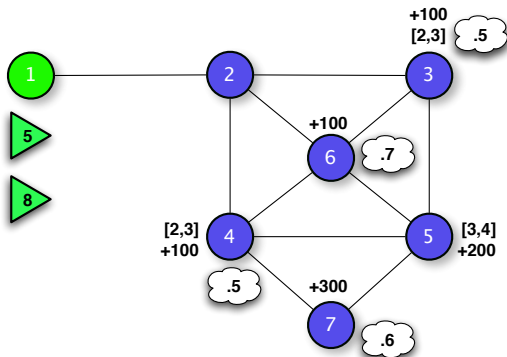
# Stochastic Weapon-Target Assignment



- ▶ **Scenario:** A small team of fuel-limited UAVs (triangles) in a simple, uncertain world cooperate to visit a set of targets (circles) with stochastic rewards

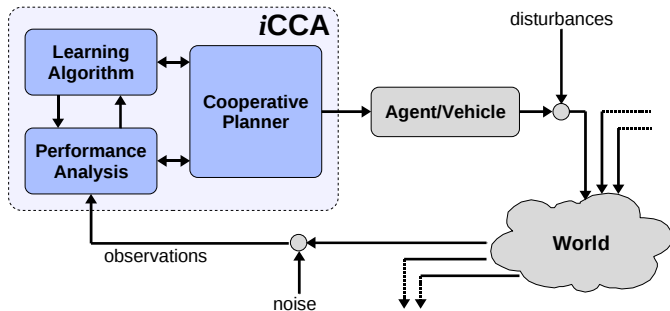
- ▶ **Objective:** Maximize collective reward
- ▶ **Key features:**

- Stochastic target rewards (probability shown in nearest cloud)
- Specific windows for target visit-times





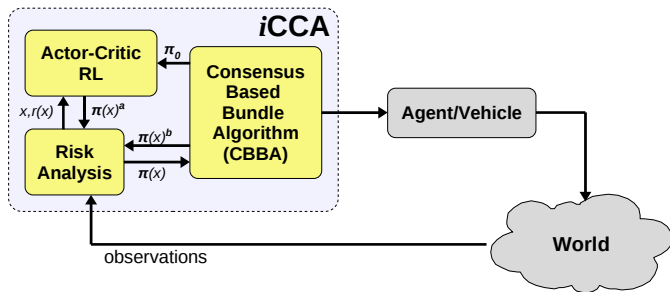
# Stochastic WTA Formulation under iCCA



- ▶ Apply iCCA template [Redding et al, 2010]
- ▶ **Cooperative Planner** ← Consensus-Based Bundle Algorithm (CBBA)
- ▶ **Learning Algorithm** ← Actor-Critic Reinforcement Learning
- ▶ **Performance Analysis** ← Risk Assessment



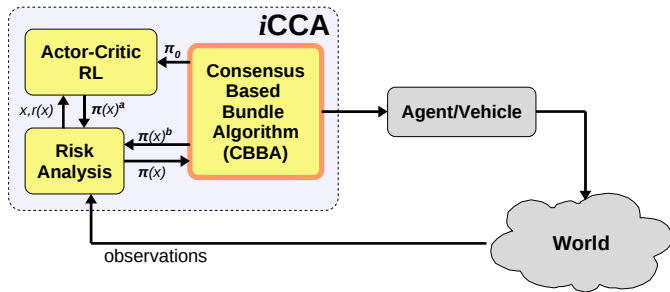
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- ▶ Apply iCCA template [Redding et al, 2010]
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# Stochastic WTA Formulation under iCCA



## ► Consensus-Based Bundle Algorithm (CBBA)

- CBBA is a deterministic planner
- Applying CBBA to a stochastic problem introduces sub-optimality
- CBBA provides a “plan”, which seeds an initial policy  $\pi_0$
- $\pi_0$  provides contingency actions

# Consensus Based Bundle Algorithm



- ▶ Current approach is inspired by the Consensus-Based Bundle Algorithm (CBBA) [Choi, Brunet, How TRO 2009]
  - Key new idea: Focus on agreement of plans Combines auction mechanism for decentralized task selection and consensus protocol for resolving conflicted selections
  - Note: auction without auctioneer
- ▶ Consensus on information & winning bids, winning agents
  - Situational awareness used to improve score estimates
  - Best bid for each task used to allocate tasks w/o conflicts
    - $y_i(j)$  = what agent  $i$  thinks is the maximum bid on task  $j$
    - $z_i(j)$  = who agent  $i$  thinks bid max value on task  $j$
- ▶ Distributed algorithm, but also provides a fast central solution

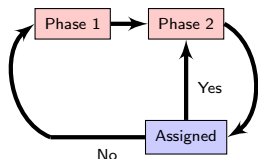


## Consensus Based Bundle Algorithm

- ▶ Distributed multi-task assignment algorithm: CBBA
  - Each agent carries a single bundle of tasks that is populated by greedy task selection process
  - Consensus on marginal score of each task not overall bundle score  
 ⇒ suboptimal, but avoids bundle enumeration

### ▶ Phase 1: Bundle construction

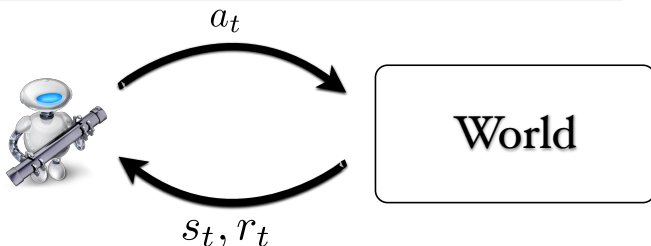
- Add task that gives largest marginal score improvement
- Populate bundle to its full length  $L_t$  (or feasibility)



### ▶ Phase 2: Conflict resolution – locally exchange $y, z, t_i$

- Sophisticated decision map needed to account for marginal score dependency on previous selections
- If an agent is outbid for a task in its bundle, it releases all tasks in bundle following that task

# Reinforcement Learning



## ► Value Function:

$$Q^\pi(s, a) = E_\pi \left[ \sum_{t=0}^{\infty} \gamma^{t-1} r_t \mid s_0 = s, a_0 = a, \right]$$

## ► Temporal Difference TD Learning

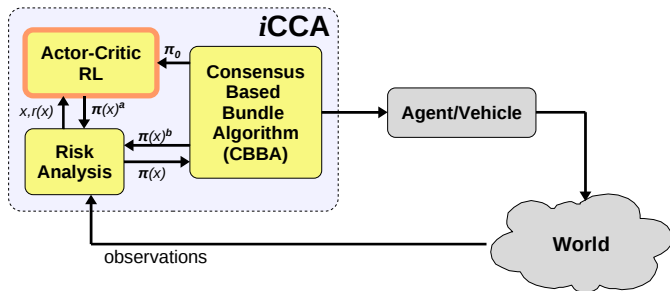
$$Q^\pi(s_t, a_t) = Q^\pi(s_t, a_t) + \alpha \delta_t(Q^\pi)$$

$$\delta_t(Q^\pi) = r_t + \gamma Q^\pi(s_{t+1}, a_{t+1}) - Q^\pi(s_t, a_t)$$





# Stochastic WTA Formulation under iCCA



## ► Actor-Critic Reinforcement Learning

- Combination of two popular RL thrusts
  - Policy search methods (Actor)
  - Value based techniques (Critic)
- Reduced variance of the policy gradient estimate
- Natural Actor Critic [Bhatnagar et al. 2007] - more reduced variance
- Convergence Guarantees

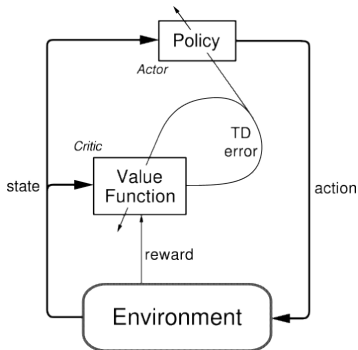


## Actor-Critic Reinforcement Learning

- ▶ Explore parts of world likely to lead to better system performance
- ▶ Actor-critic learning:  $\pi(s)$  (actor) and  $Q(s, a)$  (critic)

### Actor handles the policy

- ▶  $\pi(s) = \frac{e^{P(s,a)/\tau}}{\sum_b e^{P(s,b)/\tau}}$
- ▶  $P(s, a)$ : Preference of taking action  $a$  from state  $s$
- ▶  $\tau \in [0, \infty)$  acts as **temperature** (greedy  $\rightarrow$  random action selection)
- ▶  $P(s, a) \leftarrow P(s, a) + \alpha Q(s, a)$



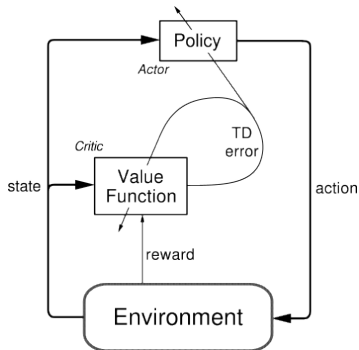
# Actor-Critic Reinforcement Learning



- ▶ Explore parts of world likely to lead to better system performance
- ▶ Actor-critic learning:  $\pi(s)$  (actor) and  $Q(s, a)$  (critic)

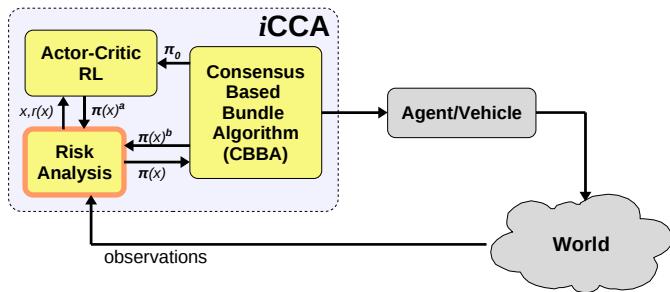
## Critic handles the value function

- ▶ Associates reward received with recent state/action pair
- ▶ Updates  $Q(s, a)$  via Temporal-Difference (TD) algorithm





# Stochastic WTA Formulation under iCCA



## ► Risk Analysis

- Heuristic check of the candidate action  $\pi(x)^a$ , suggested by learner
- Rejects  $\pi(x)^a$  if too “risky”,  $\pi(x) \leftarrow \pi(x)^b$
- Reward  $r(x)$  is virtual if  $\pi(x)^a$  is too “risky”

## Risk Analysis



- ▶ **Objective:** Ensure the agent remains safely within its operational envelope and away from undesirable or catastrophic states
- ▶ Exploration can tend toward dangerous states as **all** information is valuable to learning algorithms - even negative information
- ▶ A **virtual reward** is introduced
  - Large negative value given to the learner for actions deemed too risky, where “risk” is defined according to domain-dependent rules
  - Learner is dissuaded from suggesting that action again due to its large negative value

# Simulation Setup



- ▶ Mixed Matlab C/C++ implementation
- ▶ Two stochastic WTA scenarios:
  - ① 2 UAVs, 7 Targets
  - ② 2 UAVs, 10 Targets
- ▶ Four test cases per scenario:
  - ① Optimal: Dynamic programming
  - ② CBBA only: No learning to augment the baseline plan
  - ③ Actor-Critic only: Learning not seeded with baseline plan.
  - ④ Actor-Critic + CBBA: Instance of iCCA framework

## Simulation Setup II



### ▶ Parameter Initialization

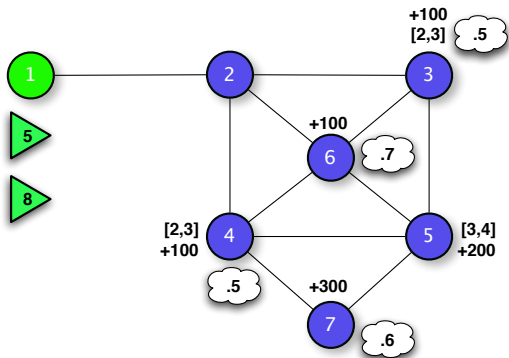
- $P(s, a) = \begin{cases} 100 & \text{If } (s, a) \text{ is on the CBBA planned trajectory} \\ 0 & \text{otherwise} \end{cases}$
- $Q(s, a) = 0, \tau \leftarrow 1$

### ▶ Risk Analyzer

- Given  $(s, a)$ , calculate the shortest path from the successive state to the base.
- If remaining fuel is not **sufficient**
  - Action  $a$  is replaced with CBBA solution ran from state  $s$ .
  - Set virtual reward so that  $P(s, a) = -100$ .



## 2 UAVs, 7 Targets



- ▶ UAVs (triangles) and Targets (circles)
- ▶ Acceptable windows for target visit times in brackets, e.g. [2,3]
- ▶ Target visit rewards
- ▶ Probability of receiving reward shown in cloud
- ▶  $\approx$  100 million state-action pairs

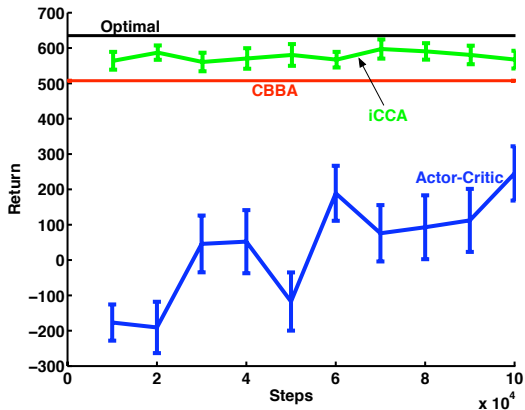
- ▶ iCCA and Actor-Critic test cases were run for 60 episodes
- ▶ CBBA was run on the deterministic version of the stochastic problem for 10,000 episodes



## 2 UAVs, 7 Targets: Simulation Results



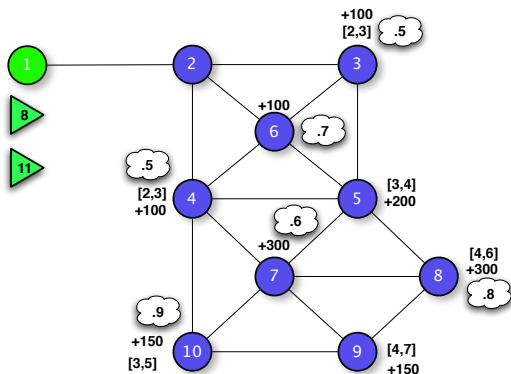
### Comparison of Collective Rewards



- ▶ (Black) Optimal as calculated via dynamic programming
- ▶ (Red) CBBA only
- ▶ (Blue) Actor-critic only
- ▶ (Green) Coupled CBBA + actor-critic via iCCA



## 2 UAVs, 10 Targets



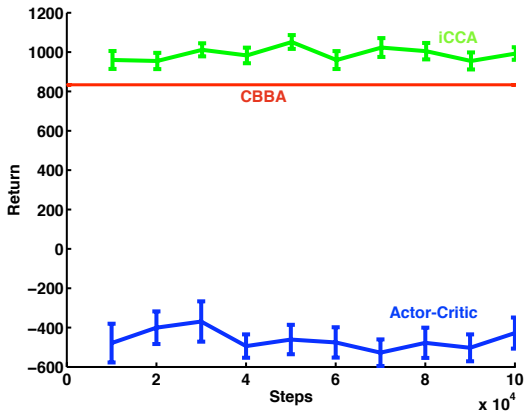
- ▶ UAVs (triangles) and Targets (circles)
- ▶ Acceptable windows for target visit times in brackets, e.g. [2,3]
- ▶ Target visit rewards
- ▶ Probability of receiving reward shown in cloud
- ▶  $\approx 9$  billion state-action pairs

- ▶ iCCA and Actor-Critic test cases were run for 30 episodes
- ▶ CBBA was run on the deterministic version of the stochastic problem for 10,000 episodes

## 2 UAVs, 10 Targets: Simulation Results



### Comparison of Collective Rewards



- ▶ Optimal solution intractable
- ▶ (Red) CBBA only
- ▶ (Blue) Actor-critic only
- ▶ (Green) Coupled CBBA + actor-critic via iCCA

## Conclusions



- ▶ A reinforcement learning algorithm was implemented under iCCA to **improve planner response** under stochastic models
- ▶ A safe initial policy was incrementally adapted by a natural actor-critic learning algorithm to increase planner performance over time
- ▶ Approach successfully demonstrated in simulation with limited-fuel UAVs visiting stochastic targets
- ▶ Current Work:
  - Extend to other *forms* of cooperative planners
  - Extend tabular representation to function approximation to improve scalability of problem formulation
  - Formally define the notion of “risk”
  - Implement virtual forward search for suggested actions