# **Robust Textual Inference using Diverse Knowledge Sources**

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### Abstract

We present a machine learning approach to robust textual inference, in which parses of the text and the hypothesis sentences are used to measure their asymmetric "similarity", and thereby to decide if the hypothesis can be inferred. This idea is realized in two different ways. In the first, each sentence is represented as a graph (extracted from a dependency parser) in which the nodes are words/phrases, and the links represent dependencies. A learned, asymmetric, graph-matching cost is then computed to measure the similarity between the text and the hypothesis. In the second approach, the text and the hypothesis are parsed into the logical formula-like representation used by (Harabagiu et al., 2000). An abductive theorem prover (using learned costs for making different types of assumptions in the proof) is then applied to try to infer the hypothesis from the text, and the total "cost" of proving the hypothesis is used to decide if the hypothesis is entailed.

## 1 Introduction

Below, we illustrate our methods with the following toy example of entailment:

TEXT: Chris purchased a BMW.

HYPOTHESIS: Chris bought a car.

Using relationships derived from syntactic dependencies, we can represent the text and hypothesis sentences equivalently as either a directed graph, or as a set of logical terms, as shown in Figure 1 and Section 3.1. In the graph, a vertex typically represents a word, but can also represent a phrase that is interpreted as a single entity. Labeled edges represent syntactic and semantic relationships tagged by various modules. The logical formula is derived by constructing a term for each node in the graph, and representing the dependency links with appropriately shared arguments. After presenting the inference methods, we show how the representations over which they work are derived from plain text.

## 2 Entailment by graph matching

We take the view that a hypothesis can be inferred from the text when the cost of matching the hypothesis graph to the text graph is low. For the remainder of this section, we outline a model for assigning a match cost to graphs.

For hypothesis graph H, and text graph T, a matching M is a mapping from the vertices of H to those of T; we allow nodes in H to map to a fictitious NIL vertex if necessary. Suppose the cost of matching M is Cost(M). Then we define the cost of matching H to T:  $MatchCost(H,T) = min_M Cost(M)$ .

One simple cost model is given by the normalized sum of costs SubCost(v, M(v)) for substituting each vertex v in H for M(v) in T:

$$\operatorname{Cost}(M) = \frac{1}{Z} \sum_{v \in H_V} w(v) \operatorname{SubCost}(v, M(v)) \quad (1)$$

Here, w(v) represents the weight or relative importance for vertex v, and  $Z = \sum w(v)$  is a normalization constant. In our implementation, the weight of each vertex was based on the part-of-speech tag of the word or the type of named entity, if applicable. For hypothesis vertex v and text vertex M(v), the substitution cost (in [0, 1]) is progressively higher for the following conditions:

- v and M(v)'s stem and POS / only stem match
- v is a synonym / hypernym of M(v) (WordNet)
- v and M(v)'s stems are similar according to the word similarity modules (described later).

As (Punyakanok et al., 2004) demonstrated, models which also match syntactic relationships between words can outperform bag-of-words models for TREC QA answer extraction. As in (1), we can measure how relationally similar H and T are by a normalized sum of costs for substituting each edge relation (v, v') in H with the edge relation (M(v), M(v')) in T. We assign a substitution cost for edge (v, v') in H based on the following conditions on path length:

- M(v) is a parent/ancestor of M(v')
- M(v) and M(v') share a parent/ancestor



Figure 1: Example graph matching ( $\alpha = 0.55$ ) for example pair in Section 2. Dashed lines represent mapping.

As in the vertex case we have weights for each hypothesis edge, w(e), based upon the edge's label; typically subject and object relations are more important to match than others. Our final matching cost is given by a convex mixture of the vertex and relational match costs:

 $Cost(M) = \alpha VertexCost(M) + (1 - \alpha)RelationCost(M).$ 

Notice that minimizing Cost(M) is computationally hard since RelationCost(M) = 0 if and only if H is isomorphic to a subgraph of T. As an approximation, we can efficiently find the matching  $M^*$  which minimizes  $VertexCost(\cdot)$  using the Hungarian method (Kuhn, 1955); we then perform local greedy hillclimbing search, beginning from  $M^*$ , to approximate the minimal matching.

## **3** Abductive theorem proving

This method works with a logical formula-like representation (Harabagiu et al., 2000) of the syntactic dependencies in the text and hypothesis sentences. The basic idea is that a hypothesis that can be logically derived from the text is entailed by it. Such a logical derivation is called a "proof" of the hypothesis.

The logical formulae capture only the syntactic dependencies in the sentences. Consequently, several entailed hypotheses that require semantic rewrites (such as "a *BMW* is a *car*") can be derived from the corresponding text formulae only by using additional assumptions in the proof. We do not use explicit logical axioms ("rules") for these assumptions; instead, each assumption that unifies one term in the hypothesis with another in the text is assigned a cost based on the judged plausibility of that assumption. This cost is computed using particular features of the assumption.

Using such a cost model, the inference procedure searches for a minimum cost proof for the hypothesis. The

hypothesis is judged to be entailed from the text if it has a proof with cost below a certain learned threshold value.

We also provide a procedure to learn good costs for assumptions from a training set containing examples of entailed and non-entailed hypotheses.

## 3.1 Representation

For the example, the following logical representation is derived, with each number/letter representing a constant:

T: Chris(1) BMW(2) purchased(3,1,2)

H: Chris(x) car(y) bought(e,x,y)

Each predicate and each argument is also annotated with other linguistic information not shown here (such as semantic roles and named entity tags) for use in assigning costs to assumptions.

## 3.2 Inference

For our representation, proof steps that unify one term from the text with one term of the hypothesis suffice. We allow any pair of terms to unify with each other, with a cost assigned by the *assumption cost model*. We relax the requirements for logical unification in several ways, adding cost penalties for each such relaxation:

- 1. Terms with different predicates can be unified; the cost penalty is obtained using the term similarity measures (described later) and the linguistic annotations on the predicates.
- 2. The terms can have differing number of arguments, and the arguments of one term can be matched with those of the other term in any order. Each argument matching is assigned a cost based on the compatibility of the annotations of those arguments. A term pair might be unified in many ways corresponding to different argument matchings.
- 3. Constants can be unified with each other at an appropriate cost. This cost is precomputed for all constant pairs in a particular example, and is lowered for specific pairs—such as when there is possible coreference or appositive reference.

We developed a specialized abductive theorem prover to discover the minimum cost proof using uniform cost search. For our running example, the minimum cost proof unifies BMW with car, and purchased with bought, at small costs.

### 3.3 Learning good costs for assumptions

Given a training set of labeled text-hypothesis pairs (such as the RTE development set), we propose a learning algorithm that tries to learn good assumption costs.<sup>1</sup>

<sup>&</sup>lt;sup>1</sup>Details are omitted here due to space constraints. See (Raina et al., 2005) for details.

# 4 Producing representations and similarities for inference

### 4.1 Syntactic processing

The first steps of the front-end deal with tokenization and parsing. Beyond this base level, the performance of the inference methods depends critically on our ability to identify similarities and differences between our fairly syntactic representations of the text and the hypothesis. This is largely dependent on being able to perform normalization and enrichment tasks that will reveal essential similarities, and on having good measures of lexical semantic similarity between words and larger units.

We do deterministic tokenization and then use full sentence parsing to reveal syntactic dependencies. The parser used was a variant of (Klein and Manning, 2003). The most important addition was training on an extra dozen sentences that gave the parser some exposure to topics in the news in 2005 rather than only those appearing in 1989. Exploiting headedness relations and hand-written patternmatching rules, the parse tree is converted into a set of typed dependencies between words, representing grammatical relations (like subject and object) and other modifier dependencies, including such things as appositives, negations, and temporal modifiers. This is the basis of the graph structure in Figure 1. Various collapsings are then done to normalize and improve this dependency representation. Prepositions and possessive 's are changed from being vertices to relation names, and coordinations explicitly represent the conjuncts. A conditional random field (Lafferty et al., 2001) named entity recognition system is run to identify seven classes (Person, Organization, Location; Percent, Time, Money, and Date). The first three are collapsed into single nodes tagged NNP (proper noun) prior to parsing, while the latter four are grouped after parsing, but before the conversion to a dependency representation, and their values are normalized into a canonical form using hand-written regular expressions. This includes representing approximate and relative quantities (around \$40 and less than 2 dollars) as well as exact amounts. At the same time, we also collapse collocations, which are found in WordNet, like *back off* and *throw up* to a single node.

#### 4.2 Additional dependencies between nodes

We augment the syntactic dependency graph with semantic role arcs using a Propbank-trained semantic role labeler (Toutanova et al., 2005). For each verb, we added edges between that verb and the head word of each of its arguments, and labeled the edges with the appropriate semantic role. This allowed us to add relations (between words) that were not captured by surface syntax, and also to classify modifying phrases as temporal, locative, and other categories. We added coreference relations between noun phrases and named entities using a maximum entropy coreference classifier modeled after (Soon et al., 2001).

Dataset	Gener	al	ByTask		
	Accuracy	CWS	Accuracy	CWS	
DevSet1	64.8%	0.778	65.5%	0.805	
DevSet2	52.1%	0.578	55.7%	0.661	
DevSet1 + DevSet2	58.5%	0.679	60.8%	0.743	
Test set	56.2%	0.620	55.2%	0.686	

Table 1: Accuracy and confidence weighted score (CWS) on RTE datasets.

Task	General		ByTask		
	Accuracy	CWS	Accuracy	CWS	
CD	79.3%	0.903	84.0%	0.926	
IE	47.5%	0.493	55.0%	0.590	
IR	56.7%	0.590	55.6%	0.604	
MT	46.7%	0.480	47.5%	0.479	
PP	58.0%	0.623	54.0%	0.535	
QA	48.5%	0.478	43.9%	0.466	
RC	52.9%	0.523	50.7%	0.480	

Table 2: Accuracy and confidence weighted score (CWS) split by task on the RTE test set.

### 4.3 Methods for discovering term similarity

As in other work, e.g., (Moldovan et al., 2000), we relied on WordNet (Miller, 1995) heavily for lexical knowledge. The WordNet::Similarity module (Pedersen et al., 2004) was used to compute a symmetric similarity score between two phrases. If the queried phrases are listed as antonyms in WordNet, the match is given a very high cost in the inference procedures. Derivational forms in Word-Net are used to detect nominalized events and modify the representation (e.g., murder of police officer entails police officer killed). WordNet does not include prepositions. We semi-automatically constructed a matrix of preposition similarity values using synonyms (e.g., over and above) and antonyms (e.g., over and under). Synonyms were found by grouping prepositions into clusters. Antonym pairs were added manually. Finally, we compiled a list of 206 countries and their derivatives manually (e.g., Philippines - Filipino), and collected a list of 276 frequently occurring acronyms in a large corpus, and recorded their expansions.

The inference procedures require considerable semantic knowledge to infer some rewrites using just phrasal dependencies; for example, *won victory in Presidential election* might entail *became President*. We attempted to discover such rewrites by looking for similarly placed phrases in a large corpus, using a backed-off modification of the similarity measure described in (Lin and Pantel, 2001).

Sometimes both of these methods are too precise. Words that are used in the same context often do not have explicit relationships between them; for instance *marathon* and *run* clearly have a semantic relationship not considered in the WordNet hierarchy. To overcome this we used Infomap,<sup>2</sup>

<sup>&</sup>lt;sup>2</sup>Available at http://infomap.stanford.edu.

Text	Hypothesis	Our answer	Conf	Comments
A Filipino hostage in Iraq was re-	A Filipino hostage was freed in	True	0.61	Verb rewrite is handled. Phrasal or-
leased.	Iraq. (TRUE)			dering does not affect cost.
The government announced last	Oil prices drop. (FALSE)	False	0.69	High cost given for substituting
week that it plans to raise oil prices.				word for its antonym.
Shrek 2 rang up \$92 million.	Shrek 2 earned \$92 million.	False	0.51	Collocation "rang up" is not known
	(TRUE)			to be similar to "earned".
Sonia Gandhi can be defeated in the	Sonia Gandhi is defeated by	True	0.66	"can be" does not indicate the com-
next elections in India by BJP.	BJP. (FALSE)			plement event occurs.
Fighters loyal to Moqtada al-Sadr	Fighters loyal to Moqtada al-	True	0.67	Should recognize non-Location
shot down a U.S. helicopter Thursday	Sadr shot down Najaf. (FALSE)			cannot be substituted for Location.
in the holy city of Najaf.				
C and D Technologies announced	Datel Acquired C and D tech-	True	0.59	Failed to penalize switch in seman-
that it has closed the acquisition of	nologies. (FALSE)			tic role structure enough
Datel, Inc.				

Table 3: Analysis of results on some RTE examples.

an open-source implementation of Latent Semantic Analysis (Deerwester et al., 1990), to score words according to distributional similarity (measured using the British National Corpus). To further exploit distributional similarity, we also implemented a measure of similarity that is computed as the ratio between the number of search results from google.com for two phrases when queried separately and in combination.

## 5 **Results and analysis**

Our overall system is a combination of the two systems described in Sections 2 and 3. Each system produces a real number score that is normalized to have zero mean and unit variance, and then converted to a confidence value using the cumulative distribution function for a normal distribution. These individual scores are then linearly combined using logistic regression, with the weights trained on the RTE development sets. The first version (called General) trained one set of weights for all RTE tasks; the second version (called ByTask) trained separate weights per task. All parameters except the classifier weights were identical.

Table 1 reports the performance of our final classifiers on different datasets. Table 2 shows the performance separately on each task in the test set.

A random guessing baseline achieves accuracy 50% and confidence weighted score (CWS) 0.50. Our test set accuracy is only a few points above random guessing; however, the CWS is significantly higher. Thus, our predictions are well-calibrated and more robust; this is probably because our learning and classifier combination procedures maximize the likelihood of the full predicted distribution rather than just a binary accuracy value.

Table 3 has an analysis of some examples from the RTE datasets. The term similarity routines seemed most important for good performance, while many of the other modules are useful in specific cases. Many of the language resources used were sparse (e.g., antonyms in WordNet); high-recall resources would be extremely beneficial.

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