6898: Advanced Topics in Software Design MIT Lab for Computer Science February 11, 2002 Daniel Jackson



### course admin

# new version of bill's notes online

### schedule

- › today: Alloy language
- weds: modelling idioms
- first problem set out; due 2 weeks later
- > mon: holiday
- > weds: peer review
- > mon: JML, OCL, Z

### peer review

> 4 students present models for discussion

#### tasks

- scribe for today
- > organizer for peer review
- > presenters on JML, OCL, Z

# software blueprints

#### what?

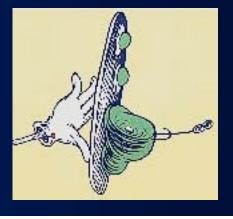
- > clear abstract design
- captures just essence

#### why?

- fewer showstopper flaws
- major refactoring less likely
- easier coding, better performance

#### how?

- > identify risky aspects
- › develop model incrementally
- > simulate & analyze as you go



# alloy: a new approach

#### alloy

- language & analyzer designed hand-in-hand
- fully automatic checking of theorems
- > simulation without test cases

### language

- a flexible notation for describing structure
- static structures, or dynamic behaviours
- > a logic, so declarative: incremental & implicit

#### analyzer

- > mouse-click automation
- generates counterexamples to theorems
- > based on new SAT technology

# roots & influences

Z notation (Oxford, 1980-1992)

elegant & powerful, but no automation

SMV model checker (CMU, 1989)

> 10<sup>100</sup> states, but low-level & for hardware

Nitpick (Jackson & Damon, 1995)

Z subset (no quantifiers), explicit search

Alloy (Jackson, Shlyakhter, Sridharan, 1997-2002)

- full logic with quantifiers & any-arity relations
- flexible structuring mechanisms
- SAT backend, new solvers every month

# experience with alloy

### applications

- Chord peer-to-peer lookup (Wee)
- Access control (Wee)
- Intentional Naming (Khurshid)
- Microsoft COM (Sullivan)
- Classic distributed algorithms (Shlyakhter)
- > Firewire leader election (Jackson)
- Red-black tree invariants (Vaziri)

### taught in courses at

CMU, Waterloo, Wisconsin, Rochester, Kansas State, Irvine, State, Twente Georgia Tech, Queen's, Michigan State, Imperial, Colorado

# elements of alloy project



language design flexible, clean syntax, all F.O.

scheme for translation to SAT skolemization, grounding out exploiting symmetry & sharing

customizable visualization

framework for plug-in solvers currently Chaff & BerkMin decouples Alloy from SAT

## alloy type system

#### types

- a universe of atoms, partitioned into basic types
- relational type is sequence of basic types
- sets are unary relations; scalars are singleton sets

### examples

- > basic types ROUTER, IP, LINK
- relations

Up: 〈ROUTER〉 ip: 〈ROUTER, IP〉 from, to: 〈LINK,ROUTER〉 table: 〈ROUTER, IP, LINK〉

the set of routers that's up maps router to its IP addr maps link to routers maps router to table

# relational operators

#### join

for set s and relation r, s.r is relational image **q**[**p**] is syntactic variant of **p**.**q** for binary relations, p.q is composition  $\mathbf{p} \cdot \mathbf{q} = \{ (\mathbf{p}_1, \dots, \mathbf{p}_{n-1}, \mathbf{q}_2, \dots, \mathbf{q}_m) \mid (\mathbf{p}_1, \dots, \mathbf{p}_n) \in \mathbf{p} \land (\mathbf{q}_1, \dots, \mathbf{q}_m) \in \mathbf{q} \land \mathbf{p}_n = \mathbf{q}_1 \}$ 

#### product

 $p \rightarrow q = \{(p_1, \dots, p_n, q_1, \dots, q_m) \mid (p_1, \dots, p_n) \in p \land (q_1, \dots, q_m) \in q\}$ for sets s and t, s → t is cross product

### set operators

for scalar e and set s, e in s is set membership p+q, p-q, p&q union, difference, intersection p in q = 'every tuple in p is also in q' for relations p and q, p in q is set subset

# alloy declarations

module routing -- declare sets & relations sig IP {}

sig Link {from, to: Router}

sig Router { ip: IP, table: IP ->? Link, nexts: set Router

sig Up extends Router {}

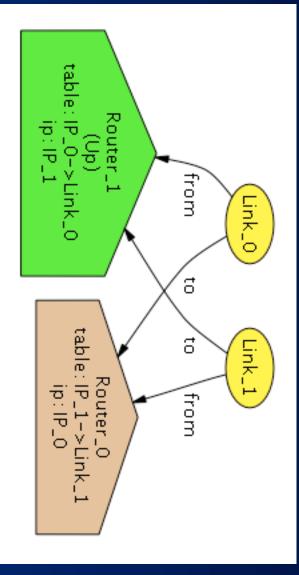
IP:  $\langle IP \rangle$ 

Link: (LINK) from, to: (LINK,ROUTER)

Router: (ROUTER) ip: (ROUTER, IP) table: (ROUTER, IP, LINK) nexts: (ROUTER,ROUTER)

Up: (ROUTER)

# a sample network



# interlude: identity etc

### constants

- iden[t] identity: maps each atom of type of t to itself
- > univ [t] universal: contains every tuple of type t
- > none [t] zero: contains no tuple of type t

### examples

- > sig Router {
   ip: IP,
   table: IP ->? Link,
   nexts: set Router
  }
- fact NoSelfLinks {all r: Router | r !in r.nexts}
- fact NoSelfLinks' {no Router\$nexts & iden [Router]}

## alloy constraints

fact Basics { all r: Router { no disj r1, r2: Router | r1.ip = r2.ip } // ip addresses are unique no r.table[r.ip] } // router doesn't forward to itself r.nexts = r.table[IP].to // nexts are routers reachable in one step r.table[IP].from = r// router table refers only to router's links

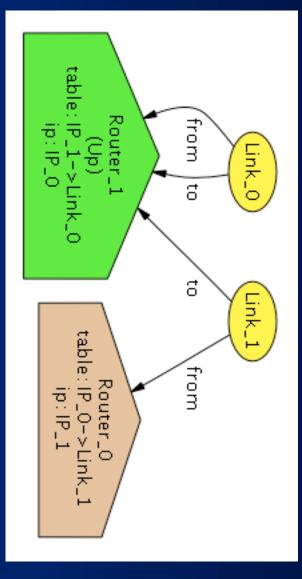
fun Consistent () { all r: Router, i: IP | r.table[i].to in i.~ip.\*~nexts } // table forwards on plausible link

# simulation commands

run Consistent for 2 -- show me a network that satisfies the Consistent constraint

-- show me one that doesn't fun Inconsistent () {not Consistent ()} run Inconsistent for 2

# an inconsistent state

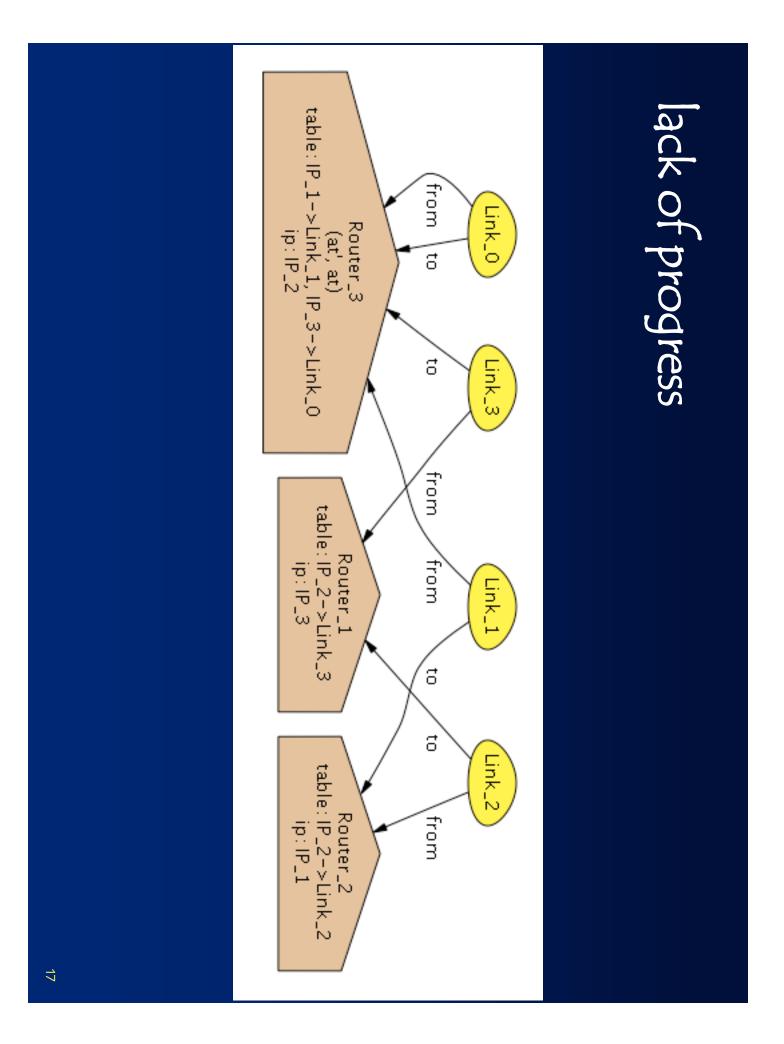


### assertions & commands -- define forwarding operation

fun Forward (d: IP, at, at': Router) { -- packet with destination d goes from at to at' at' = at.table[d].to

assert Progress { -- assert that packet doesn't get stuck in a loop all d: IP, at, at': Router Consistent() && Forward (d, at, at') => at != at'

-- issue command to check assertion check Progress for 4



# introducing mutation

-- links now depend on state sig Link {from, to: State ->! Router}

sig Router {ip: IP, table: State -> IP ->? Link} -- one table per state

- -- state is just an atom
- -- put router connectivity here
- sig State {nexts: Router -> Router}

# state in constraints

```
fact {
                                                                                                                                                           all r: Router, s: State {
no disj r1, r2: Router | r1.ip = r2.ip
                                                                                            s.nexts[r] = (r.table[s] [IP].to)[s]
                                                             no r.table[s][r.ip]
                                                                                                                          (r.table[s][IP].from)[s] = r
```

```
fun Consistent (s: State) {
                                  all r: Router, i: IP
(r.table[s][i].to)[s] in i.~ip.*~(s.nexts)
```

### propagation

in one step, each router can ...

- > incorporate a neighbour's entries
- > drop entries

fun Propagate (s, s': State) { all r: Router r.table[s'] in r.table[s] + r.~(s.nexts).table[s]

declarative spec

- > more possibilities, better checking
- easier than writing operationally

# does propagation work?

assert PropagationOK { all s, s': State l Consistent (s) && Propagate (s,s') => Consistent (s')

check PropagationOK for 2

#### 0

from

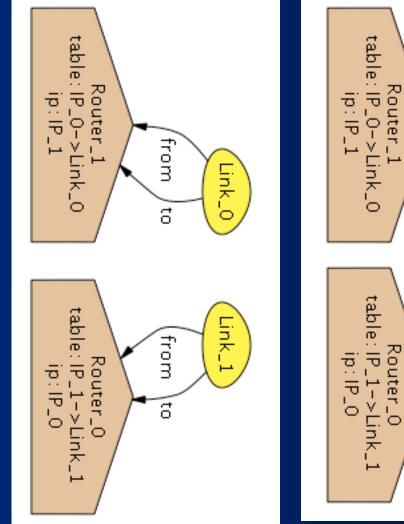
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from

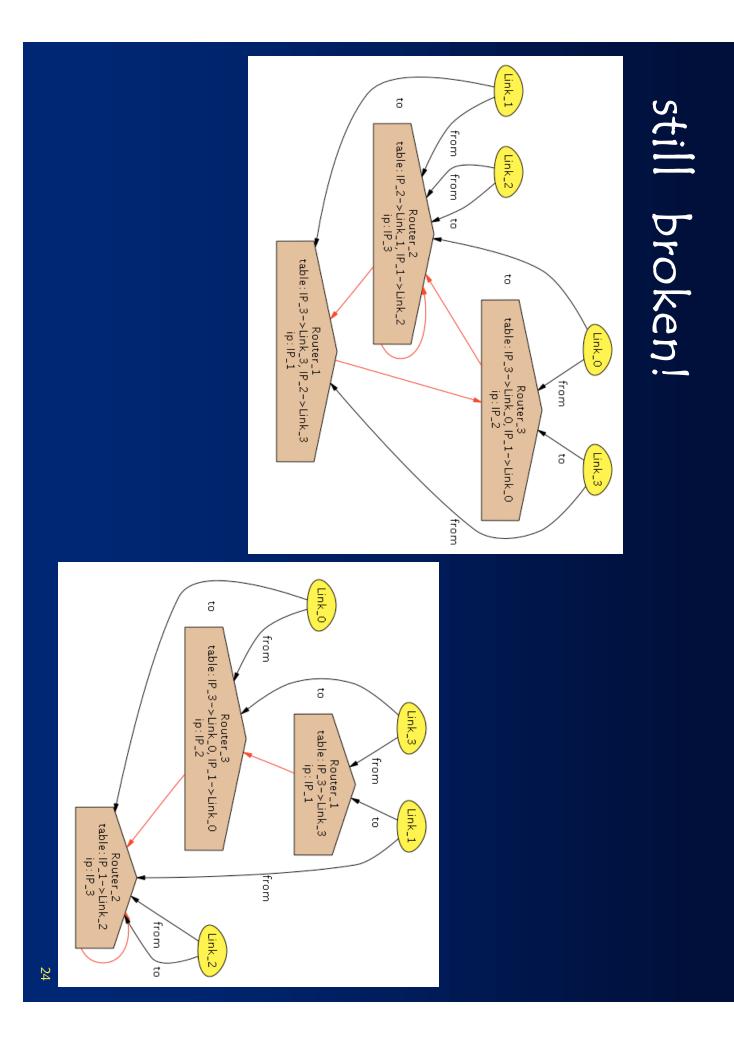
Link\_0

Link\_1









### language recap (1)

### sig X {f: Y} declares

- a set X
- a type TX associated with X
- a relation f with type 〈TX,TY〉 a constraint (all x: X | x.f in Y && one x.f)

### fact {...} introduces a global constraint

### declares a constraint to be instantiated fun F (...) {...}

declares a theorem intended to follow from the facts assert A  $\{\ldots\}$ 

# language recap (2)

run F for 3 instructs analyzer to

- > find example of F
- v using 3 atoms for each type

check A for 5 but 2 X instructs analyzer to

- > find counterexample of A
- v using 5 atoms for each type, but 2 for type TX

# other features (3)

arbitrary expressions in decls > sig PhoneBook {friends: set Friend, number: friends -> Num}

signature extensions

> sig Man extends Person {wife: option Woman}

polymorphism

> fun Acyclic[t] (r: t->t) {no ^r & iden[t]}

modules

> open models/trees

integers > #r.table[IP] < r.fanout</pre>

# models, validity & scopes

### semantic elements

- assignment: function from free variables to values
- meaning functions
- E : Expression -> Ass -> Relation
- F : Formula -> Ass -> Bool

### examples

- > expression: Alice.~likes
- > assignment: Alice – {(al
- Alice = {(alice)} Person = {(alice),(bob),(carol)} likes = {(bob, alice),(carol, alice)}
- $\cdot \text{ value: } \{(bob), (carol)\}$

- > formula: Alice in p.likes
- > assignment:

 $p = \{(bob)\}$ 

Alice = {(alice)} Person = {(alice),(bob),(carol)} likes = {(bob, alice),(carol, alice)}

- value: true
- › formula: all p: Person | Alice in p.likes
- assignment:

Alice = {(alice)} Person = {(alice),(bob),(carol)} likes = {(bob, alice),(carol, alice)}

value: false

# validity, satisfiability, etc

meaning of a formula

- Ass (f) = {set of all well-typed assignments for formula f}
- > Models (f) =  $\{a: Ass(f) \mid F[f]a = true\}$
- Valid (f) = all a: Ass (f) | a in Models(f)
- Satisfiable (f) = some a: Ass (f) | a in Models(f)
- > ! Valid (f) = Satisfiable (!f)

checking assertion

- > SYSTEM => PROPERTY
- intended to be valid, so try to show that negation is sat
- > model of negation of theorem is a counterexample

### scope

a scope is a function

From basic types to natural numbers

assignment a is within scope s iff

> for basic type t,  $#a(t) \le s(t)$ 

'small scope hypothesis'

- many errors can be found in small scopes
- > ie,

for the theorems f that arise in practice if f has a counterexample, it has one in a small scope

## what you've seen

tractable inexpressive

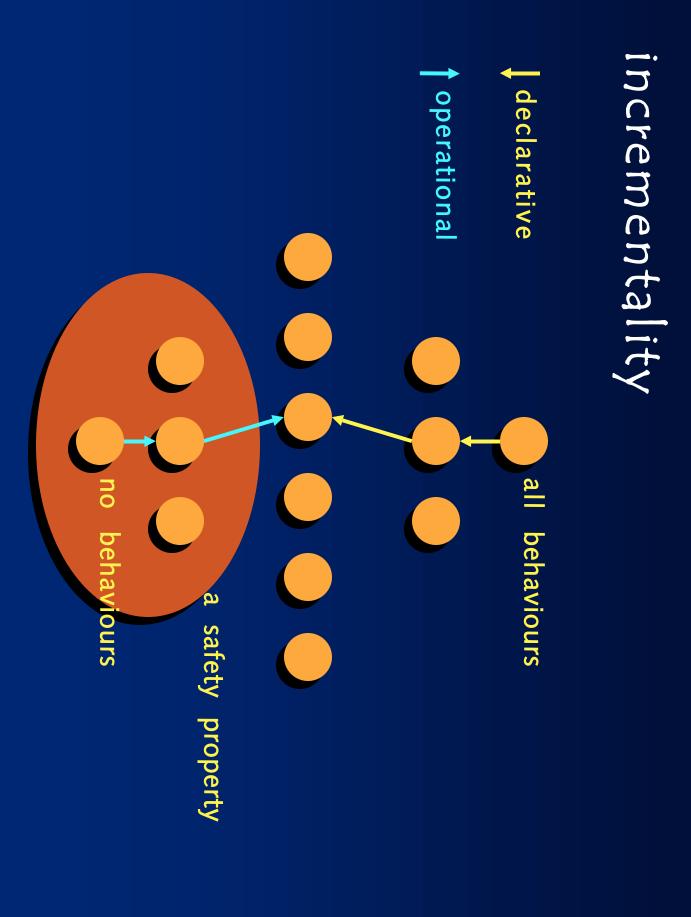
### simple notation

- > expressive but first-order
- > properties in same notation
- static & dynamic constraints
- > flexible: no fixed idiom

### fully automatic analysis

- simulation, even of implicit operations
- checking over large spaces
- > concrete output

expressive intractable



### next time

#### idioms

- > mutation
- frame conditions
- object-oriented structure
- > operations and traces

### reading

- > questions are on web page
- > answers to me by mail before class