

idioms

Daniel Jackson

MIT Lab for Computer Science
6898: Advanced Topics in Software Design

February 13, 2002

issues

state change

- › how do you describe change in a logic?

mutation

- › how do you modularize the change?

frame conditions

- › how do you control unwanted changes?

"the relational model"

ideas

- › view behaviour as a relation on states
- › represent as a simple formula
- › distinct variables for pre- and post-state

example

- › a procedure that returns the index of an element in an array

```
fun Find (t: Index ->? Elt, e: Elt): Index {  
    t[result] = e  
}
```

this procedure is

- › partial: some pre-states have no post-states
- › non-deterministic: some pre-states have >1 post-state

preconditions

what does partiality mean?

- > guard
 - a control: won't allow invocation in bad state
- > precondition
 - a disclaimer: havoc if invoked in bad state

the VDM/Larch approach

make precondition explicit

```
> op Find (t: Index ->? Elt, e: Elt): Index
  pre  e in Index.(t.map)
  post t[result] = e
```

do ‘implementability check’

```
> all s: State | pre(s) => some s': State | post(s,s')
```

the Z approach

precondition is implicit

› $\text{Find} = [t: \text{Index} \rightarrow? \text{Elt}, e? : \text{Elt}, i! : \text{Index} \mid t[i!] = e?]$

compute precondition

› $\text{Pre}(\text{Find}) = \text{some } s : \text{State} \mid \text{Find}(s, s')$

and check properties

› $\text{Pre}(\text{Find}) = \text{true} ??$

the Alloy approach

roll your own!

- › can split pre/post into distinct functions
- › can combine in different ways
- › can interpret as guard or precondition

```
fun FindPre (t: Index ->? Elt, e: Elt) { e in Index.t }
```

```
fun FindPost (t: Index ->? Elt, e: Elt): Index { t[result] = e }
```

```
fun Find (t: Index ->? Elt, e: Elt): Index {  
    FindPre (t, e) => FindPost (t, result, e)  
}
```

frame conditions

procedure that removes dupls

```
> fun RemoveDupls (t, t': Index ->? Elt) {  
    Index.t = Index.t'  
    #Index.t' = #t'  
}
```

procedure that sorts array without dupls

```
> fun Sort (t, t': Index ->? Elt) {  
    Index.t = Index.t'  
    all i, j; t.Elt | i->j in Index$lt => t[i]->t[j] in Elt$lt  
}
```

are these constrained enough?

summary so far

declarative style is powerful

- › spec by conjunction
- › separation of concerns

declarative style is dangerous

- › implicit preconditions
- › underconstraint

frame conditions

- › subtle for non-deterministic operations
- › subtle in OO programs
- › important stylistic issue, even when not subtle

modularizing change

- 3 approaches
 - > global state machine
 - > local state machines
 - > object oriented

a static model of router tables

```
module routing
sig IP {}
sig Link {from, to: Router}
sig Router {ip: IP, table: IP ->? Link, nexts: set Router}
{
    table[IP].from in this
    nexts = table[IP].to
    no table[ip]
}

fact {inj (Router$ip)}
fun Consistent () {
    all r: Router, i: IP | r.table[i].to in i.^ip.^nexts
}

fun inj [t,t'] (r: t->t') {all x: t' | sole r.x}
```

a dynamic model

```
sig State {}  
sig IP {}  
sig Link {from, to: State ->! Router}  
sig Router {ip: IP, table: State -> IP ->? Link,  
    nexts: State -> Router}  
{  
    all s: State {  
        (table[s][IP].from) [s] in this  
        nexts[s] = (table[s][IP].to)[s]  
        no table[s] [ip]  
    }  
}  
fun Consistent (s: State) {  
    let rnexsts = {r,r': Router | r->s->r' in Router\$nexts} |  
    all r: Router, i: IP | (r.table[s][i].to) [s] in i.^ip.*rnexsts}
```

propagation

```
fun Propagate (s, s': State) {  
    let rnexts = {r,r': Router | r->s->r' in Router$nexts} |  
    all r: Router | r.table[s'] in r.table[s] + r.~rnexts.table[s] }
```

```
assert PropagationOK {  
    all s, s': State |
```

```
        Consistent (s) && Propagate (s,s') => Consistent (s') }
```

can you write NoTopologyChange?

```
fun NoTopologyChange (s,s': State) {  
    all x: Link {  
        x.from[s] = x.from[s'] && x.to[s] = x.to[s']  
    }  
}
```

global state version

```
sig IP {} sig Link {} sig Router {}

sig LinkState {
    from, to: Link -> Router }

sig NetworkState extends LinkState {
    ip: Router -> IP,
    table: Router -> IP ->? Link,
    nexts: Router -> Router } {

    all r: Router {
        table[r][IP].from in r
        nexts[r] = table[r][IP].to
        no table[r][r.ip] }
    inj (ip) }
```

operations for global version

```
fun Consistent (s: NetworkState) {  
    all r: Router, i: IP |  
        s.table[r][i].to[s] in i.~(ip[s]).*~(nexts[s]) }
```

```
fun Propagate (s, s': NetworkState) {  
    all r: Router {  
        s'.table[r] in s.table[r] + r.~(nexts[s]).(table[s])  
        s.ip[r] = s'.ip[r] } }
```

can you write NoTopologyChange?

```
fun NoTopologyChange (s,s': NetworkState) {  
    s.from = s'.from  
    s.to = s'.to  
}
```

object oriented version

```
sig IP {}  
sig Link {from, to: RouterRef}  
sig Router {ip: IP, table: IP ->? LinkRef, nexts: set RouterRef} {  
    no table[ip] }  
fact {inj (Router$ip)}  
sig LinkRef {}  
sig RouterRef {}  
  
sig State {  
    robj: RouterRef ->! Router,  
    lobj: LinkRef ->! Link  
}
```

invariants

router invariant is now recognized as ‘cross object’

```
fact {
  all s: State, r: RouterRef {
    r.(s.robj).table[IP].(s.lobj).from in r
    r.(s.robj).nexts = r.(s.robj).table[IP].(s.lobj).to
  }
}
```

operations in OO version

```
fun Consistent (s: State) {  
    all r: RouterRef, i: IP |  
        r.(s.robj).table[i].(s.lobj).to in  
        i.~ip.~(s.robj).*~(s.robj.nexts) }
```

```
fun Propagate (s, s': State) {  
    let rnexts = {r,r': Router | r->s->r' in Router$.nexts} |  
    all r: RouterRef |  
        r.(s'.robj).table in r.(s.robj).table  
        + r.~(s.robj.nexts).(s.robj).table }
```

can you write NoTopologyChange?

```
fun NoTopologyChange (s,s': State) {  
    s.lobj = s'.lobj }
```

comparison

how do the approaches compare?

- > ease of expression
- > degree of modularity
- > how systematic
- > frame conditions

didn't get round to discussing this