

Probabilistic modeling and Inference in Astronomy

Dan Foreman-Mackey

Sagan Fellow, University of Washington

github.com/dfm // [@exoplaneteer](https://twitter.com/exoplaneteer) // dfm.io



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A high-resolution photograph of Earth from space, showing the curvature of the planet and the blue atmosphere. The landmasses are visible in shades of brown and green, with white clouds scattered across the surface. In the bottom left corner, a bright sun is partially visible, creating a lens flare effect. The background is a deep black space filled with numerous small, distant stars.

I study
astronomy.

Photo credit [NASA Ames/SETI Institute/JPL-Caltech](#)

this isn't what
my data look like



I study
astronomy.

Why Astronomy?

simple but **interesting** physical models

precise **open-access** data

observational only

Why Astronomy?

simple but **interesting** physical models

precise **open-access** data

observational only

no chance of financial gain **ever**

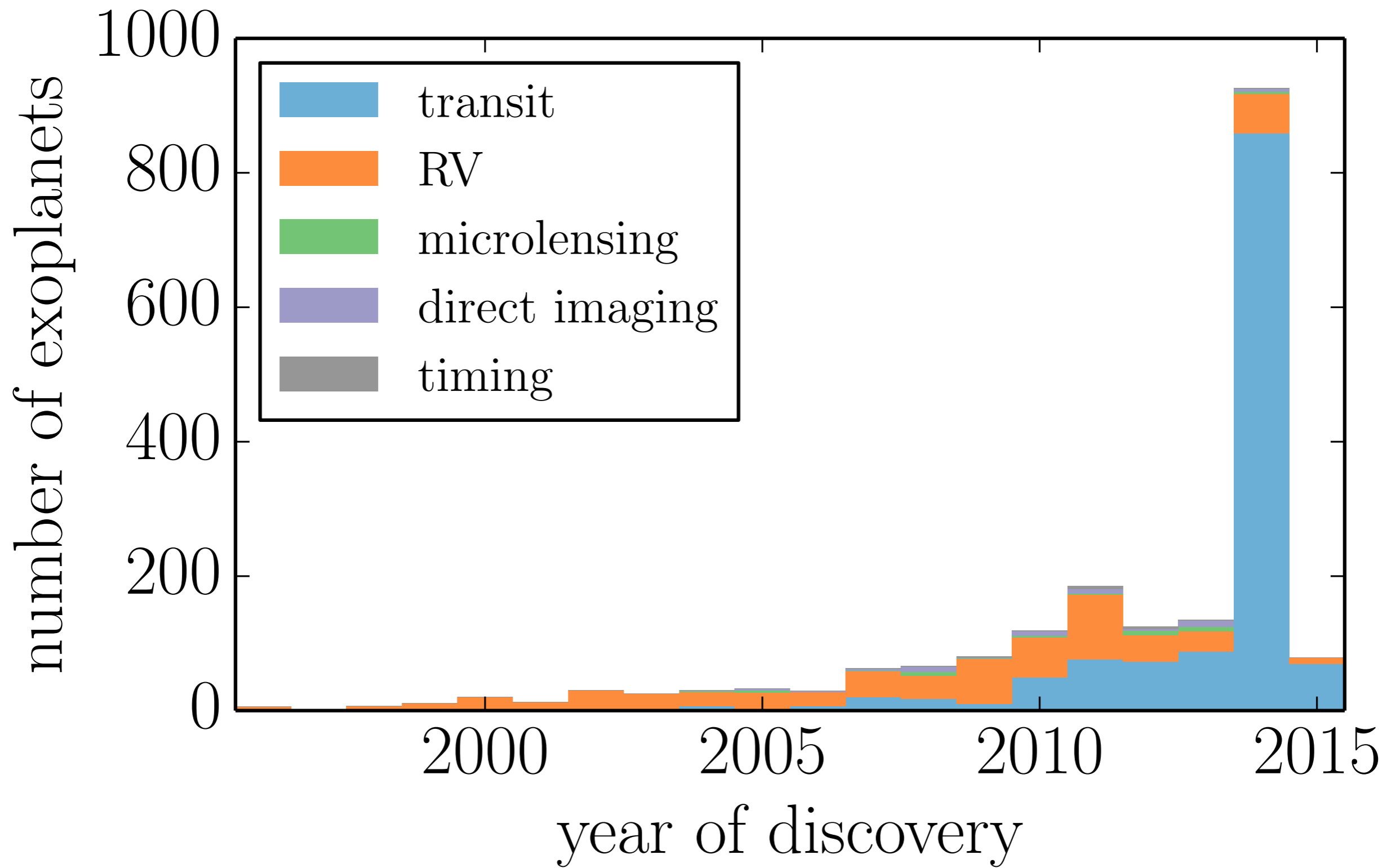
ex·o·plan·et

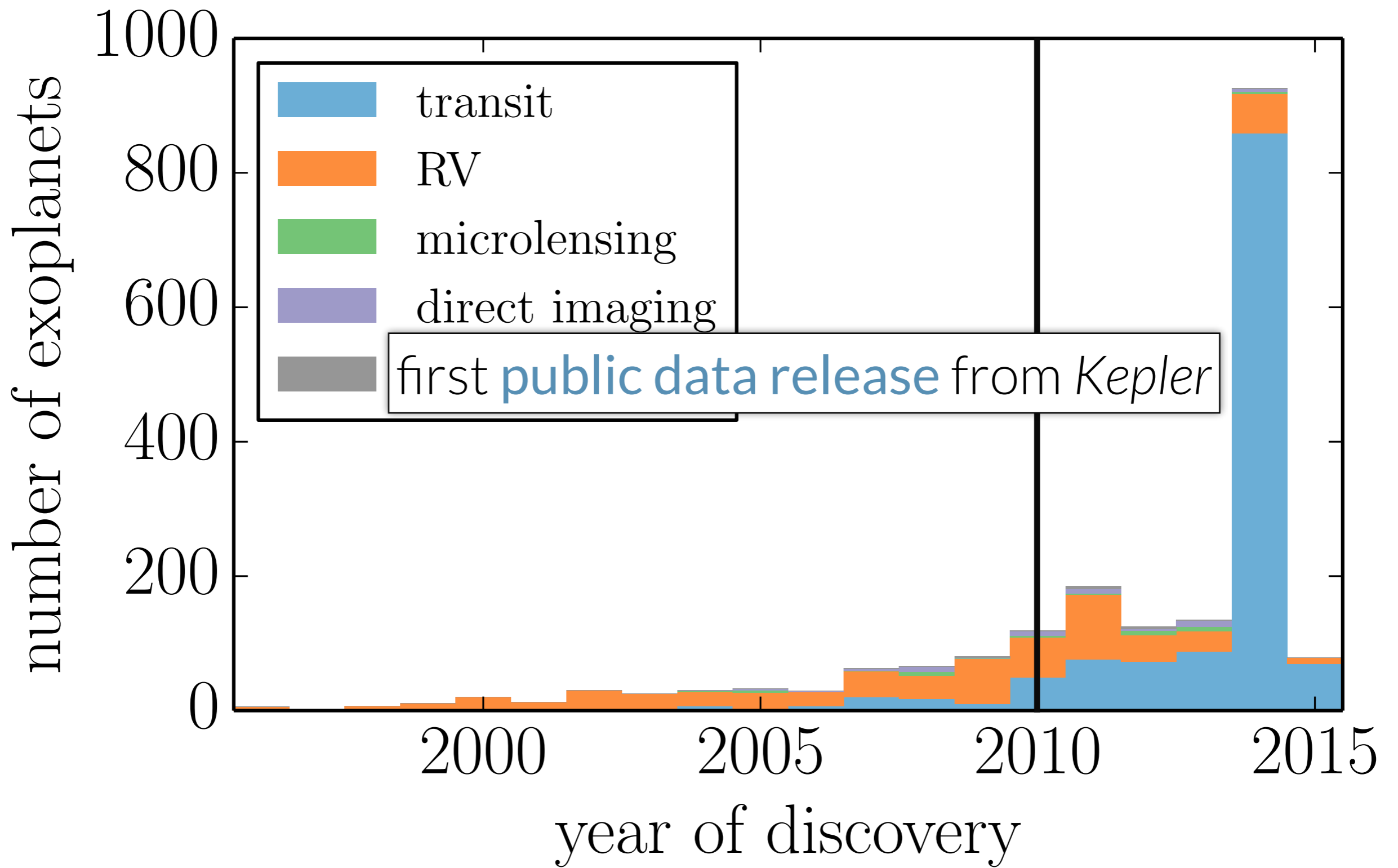
'eksō,planət/

noun. a planet that orbits a star outside the solar system.

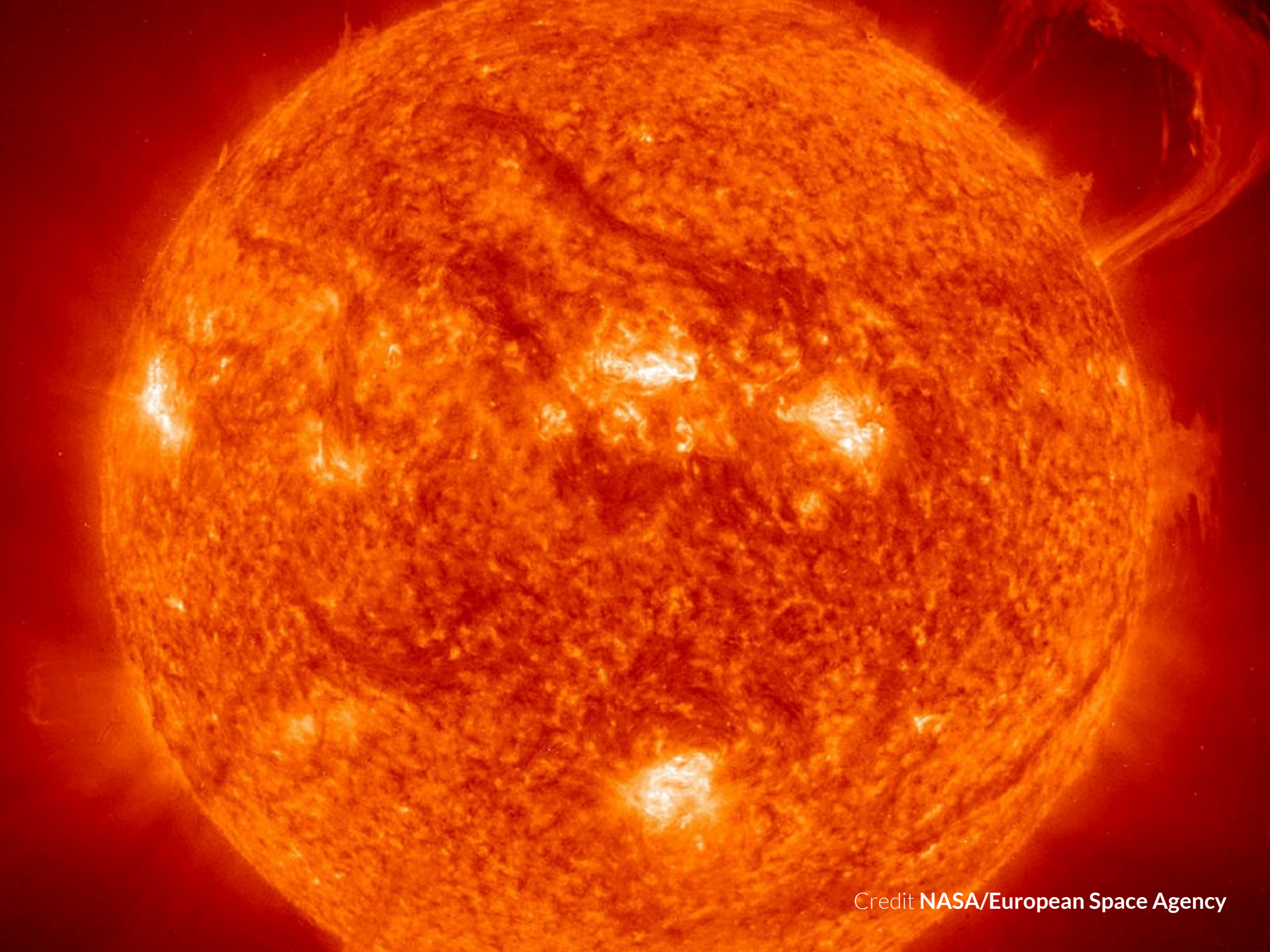
How do we **find & study** exoplanets?

1281 transit
616 radial velocity
45 direct imaging
32 microlensing
20 timing
0 astrometry

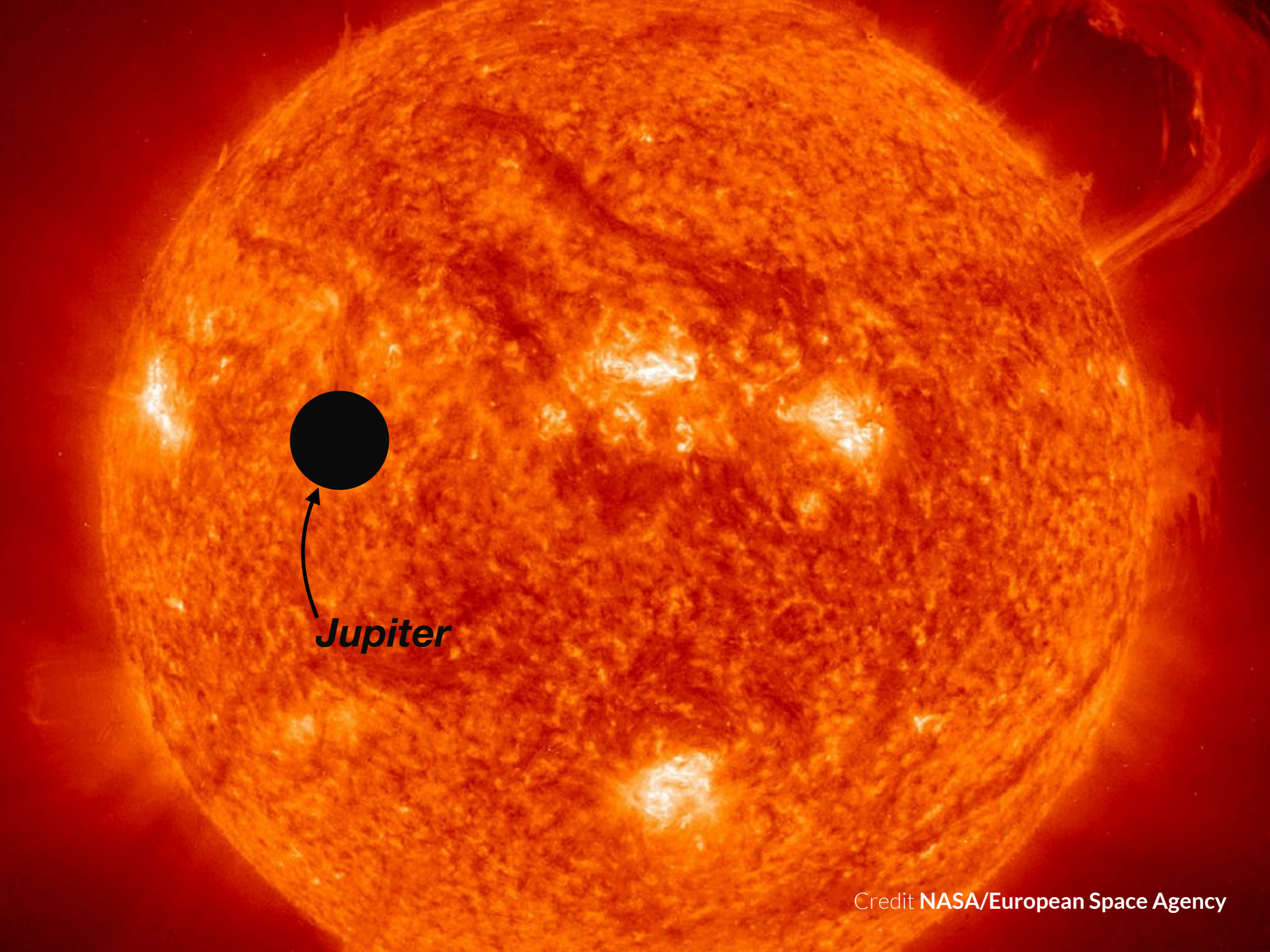




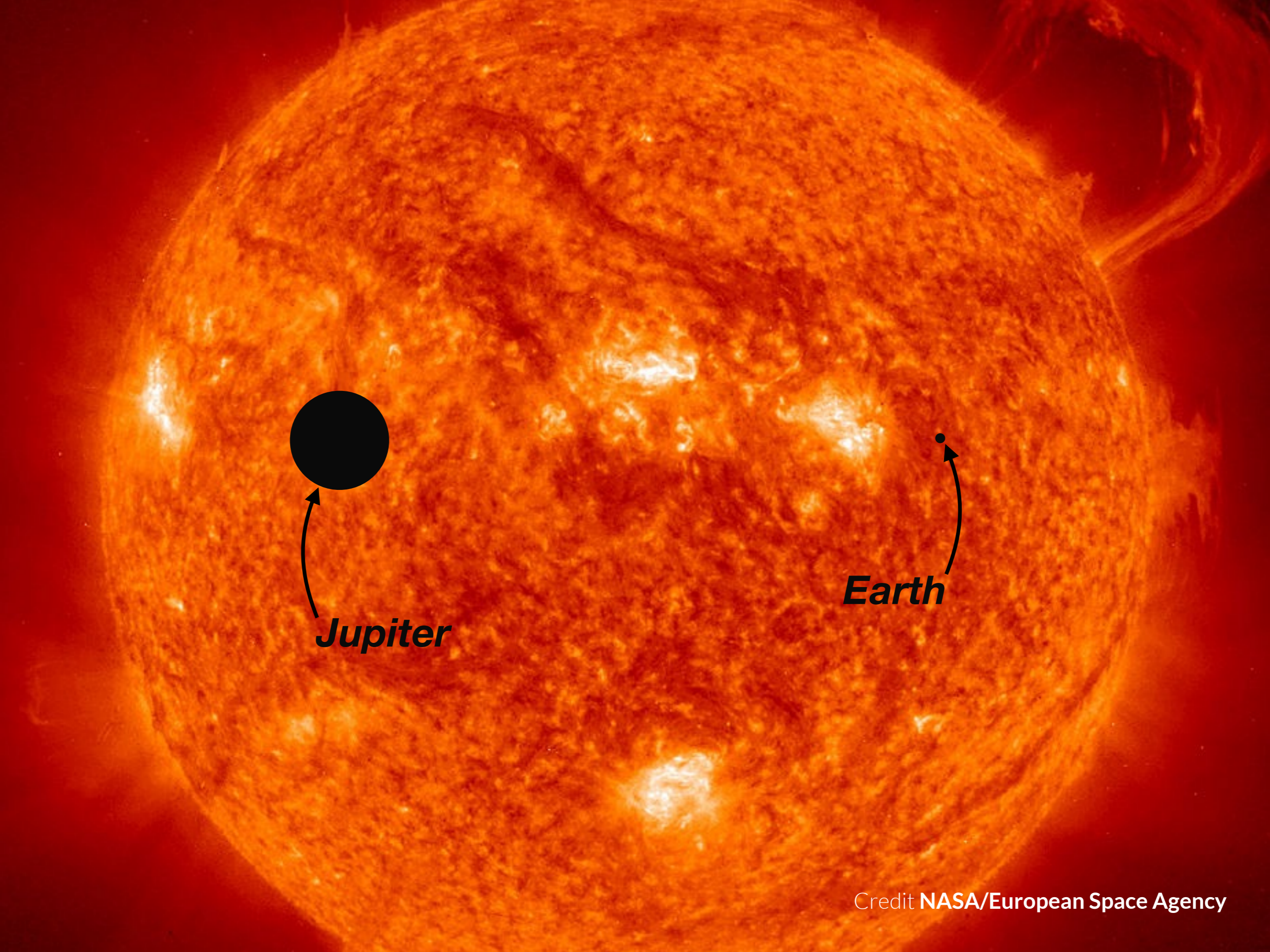
the **transit** method



Credit **NASA/European Space Agency**



Jupiter

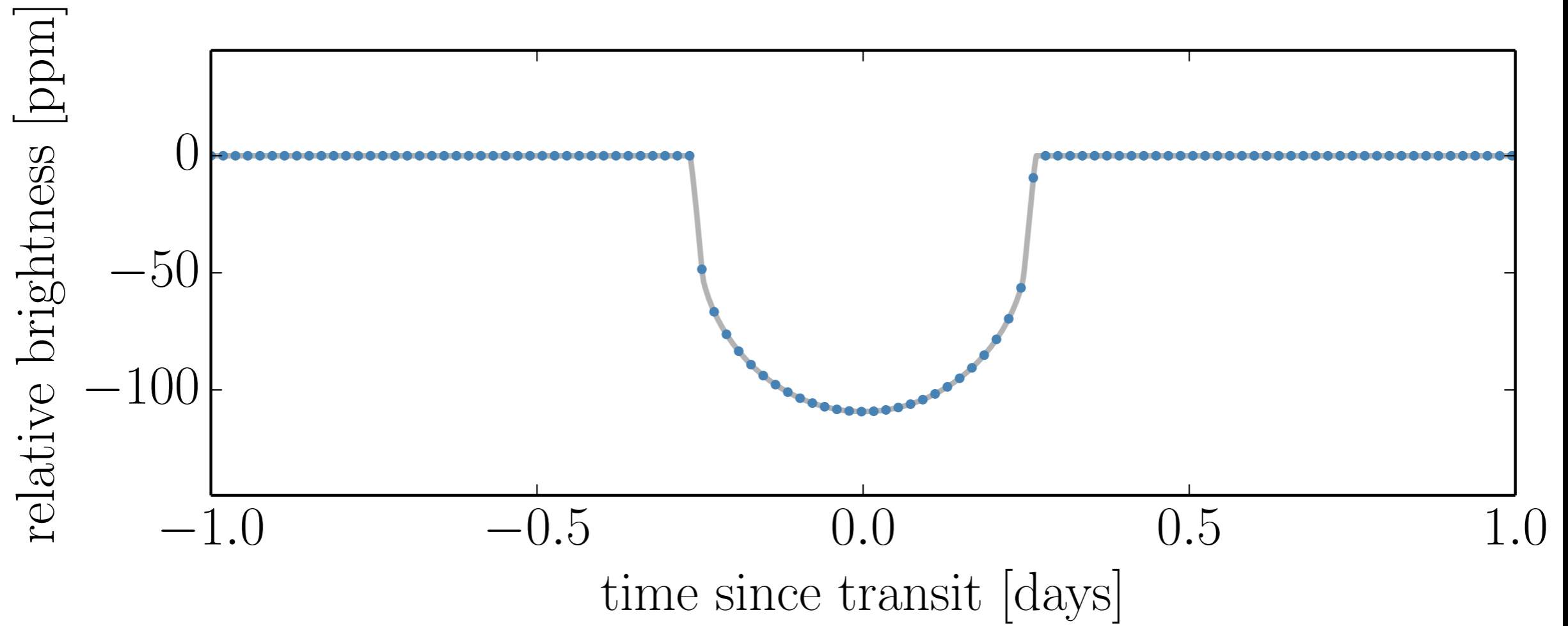
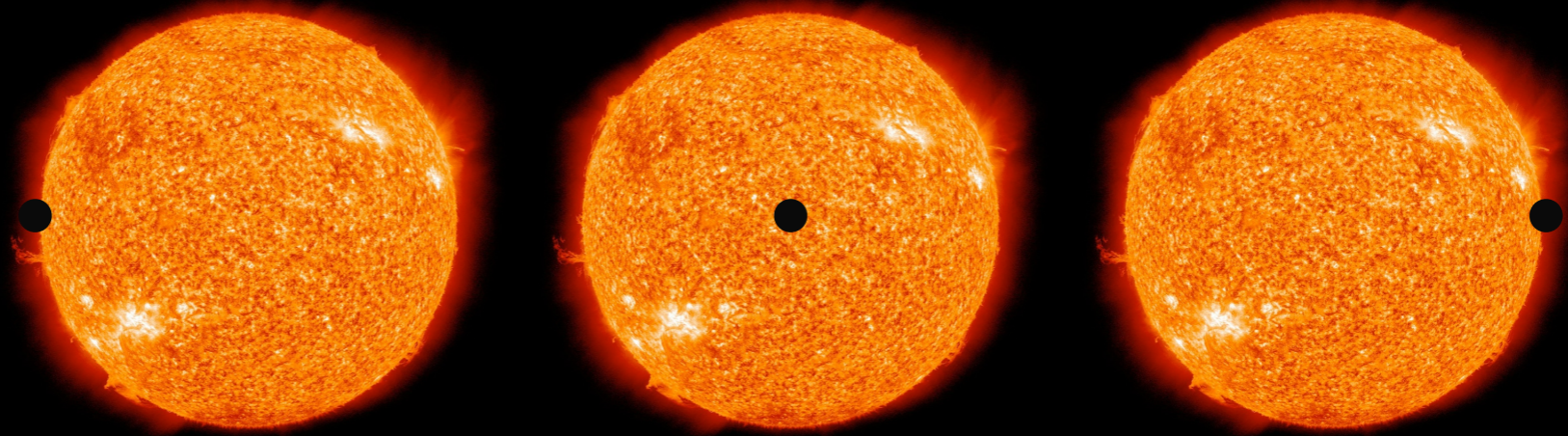


Jupiter

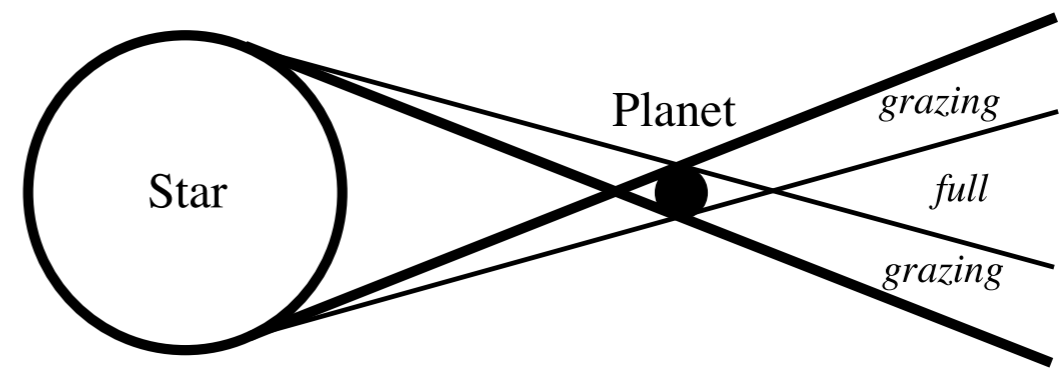
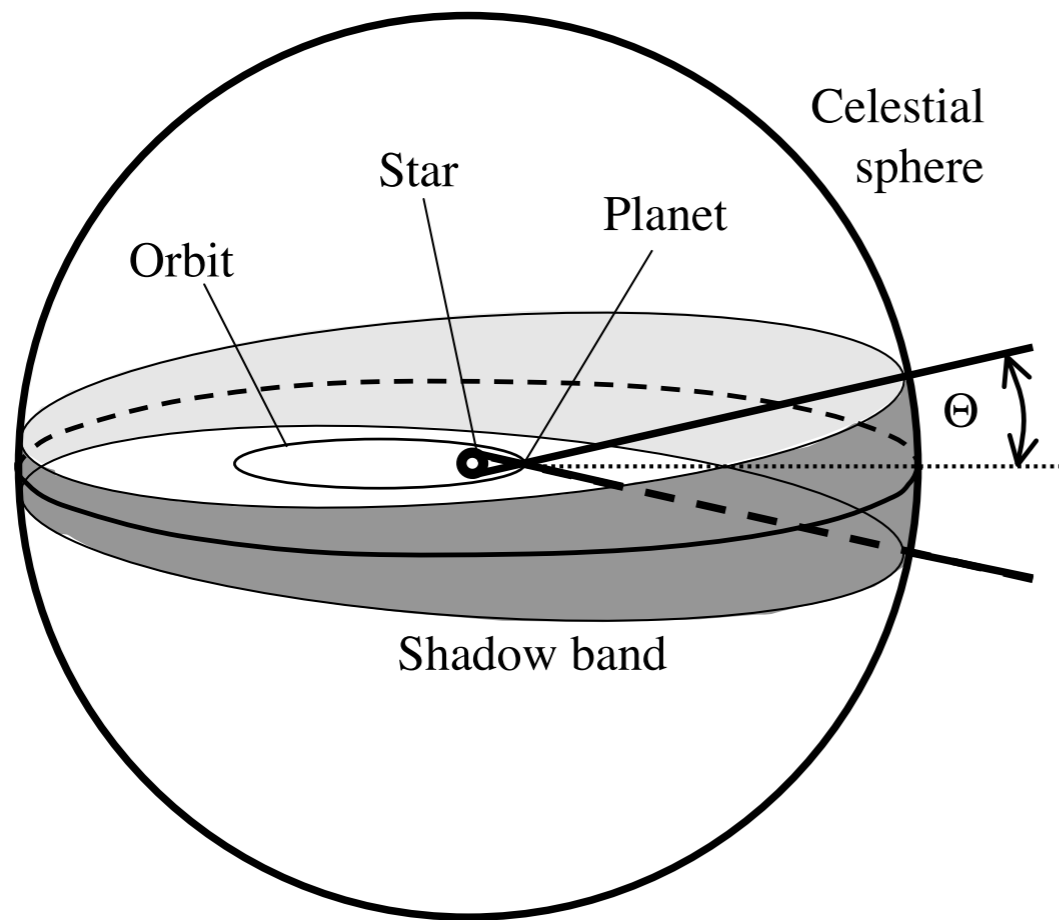


Earth

that's not what most stars look like!



everything is against us!



Close-up

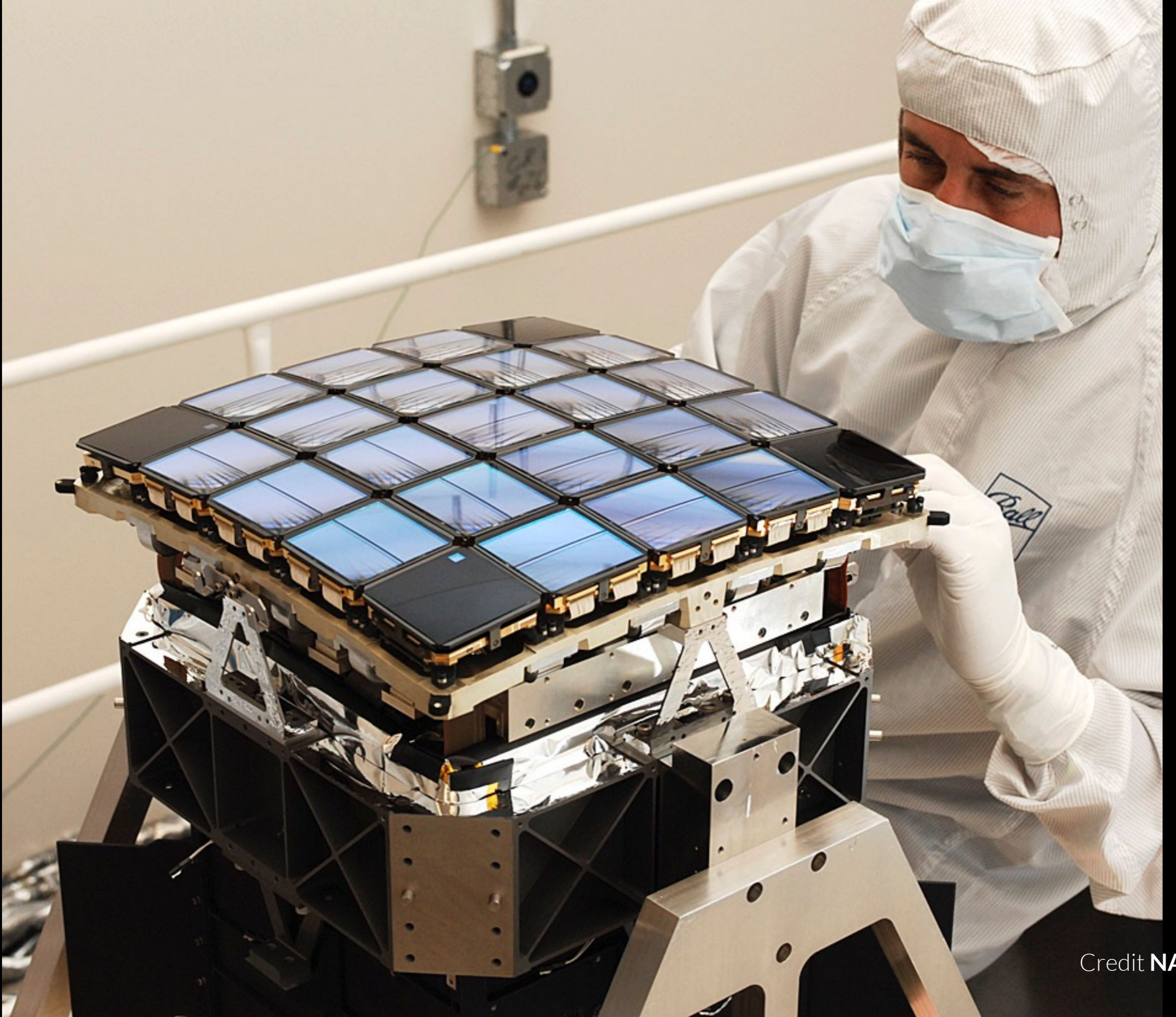
need to look at **the right place**
at **the right time**

and measure
extremely precise
photometry

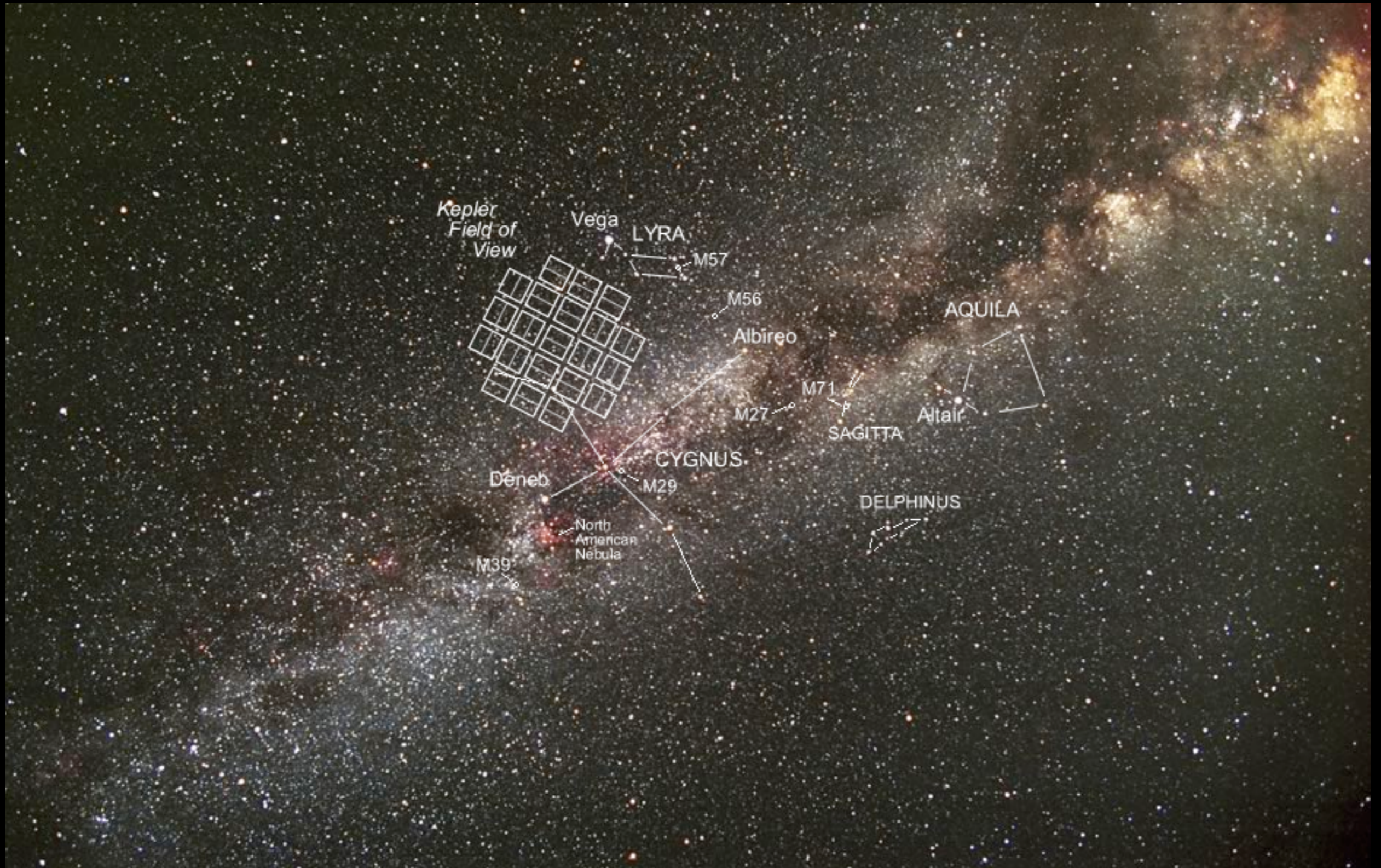
Kepler

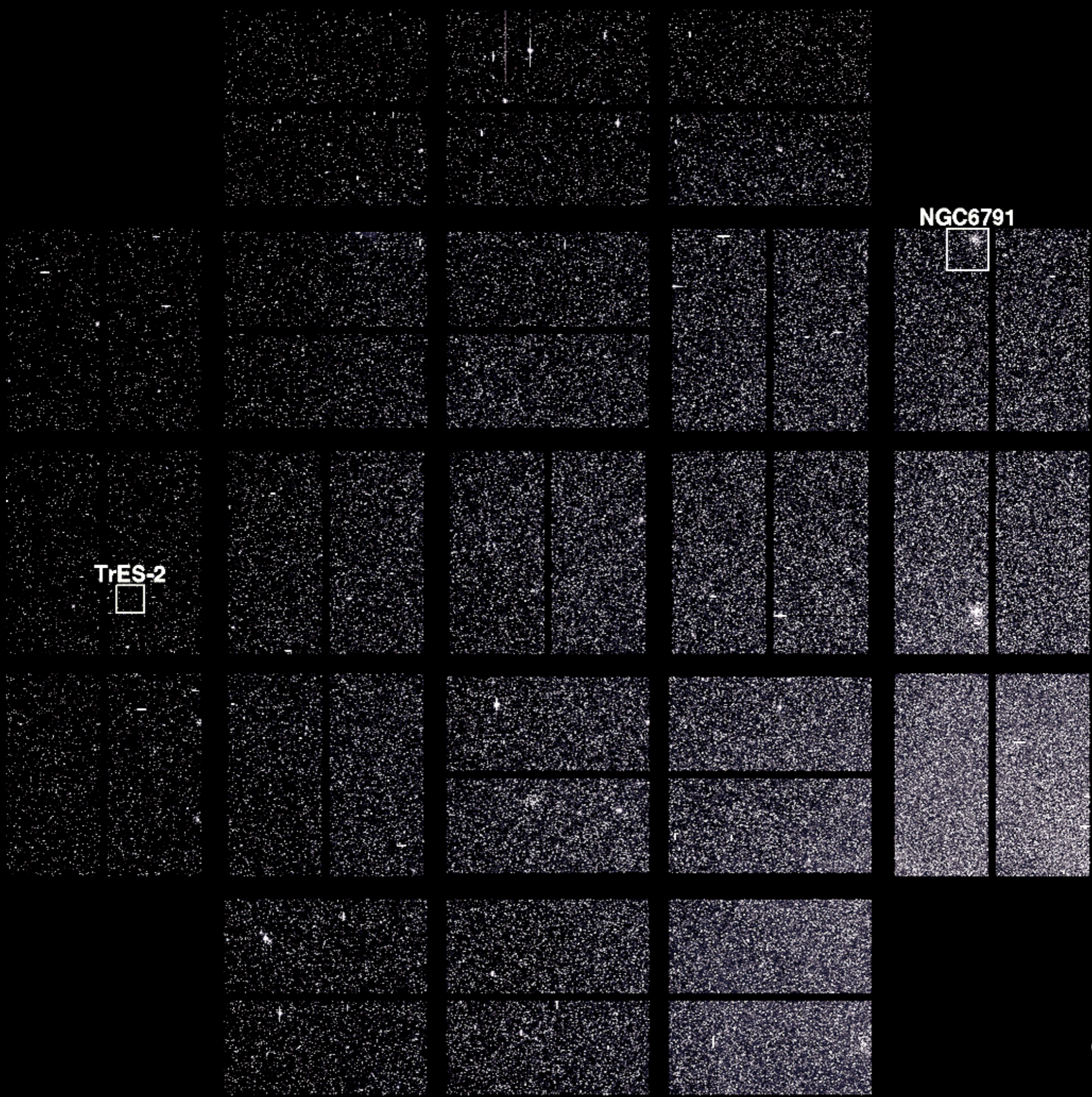


Credit NASA



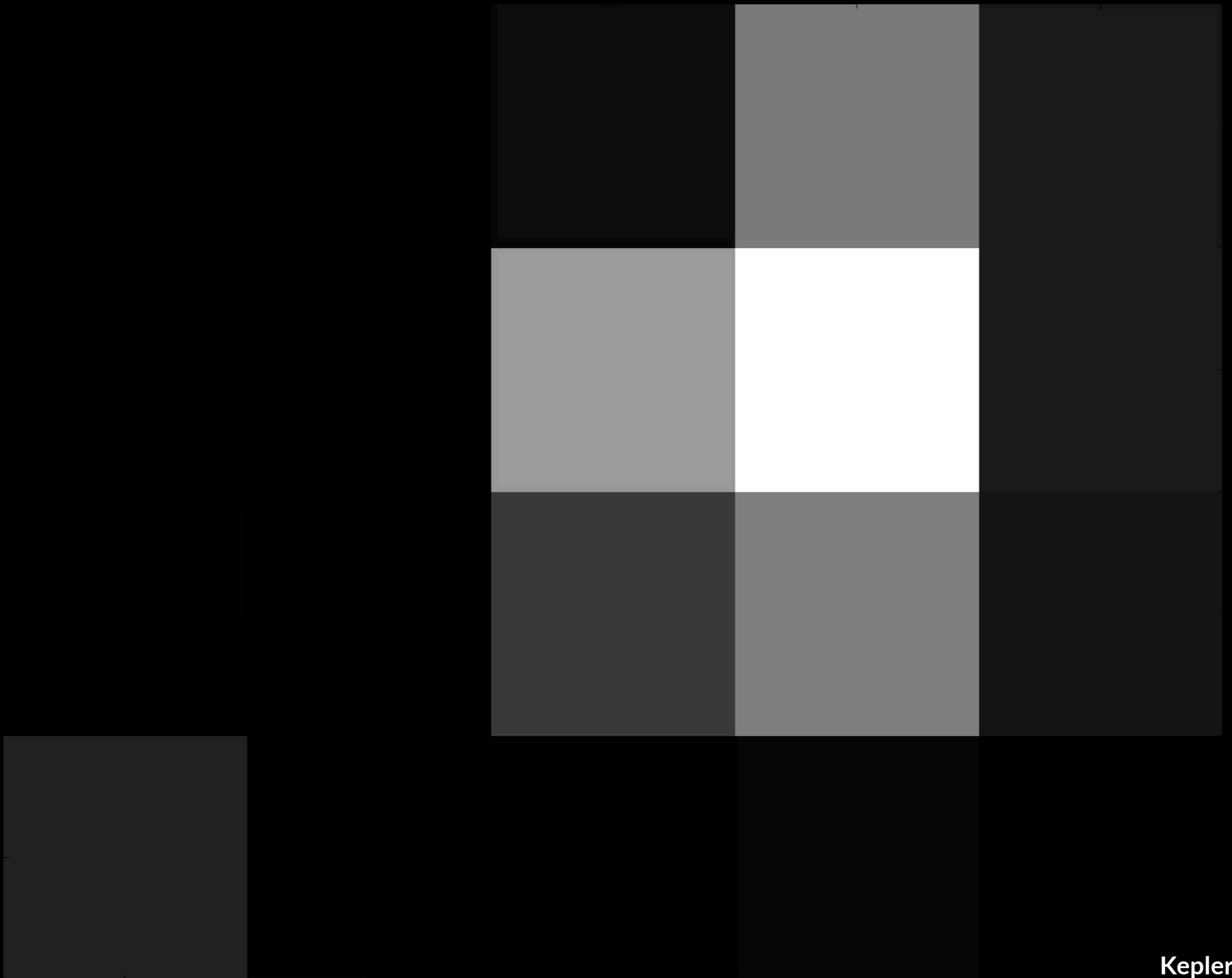
Credit NASA



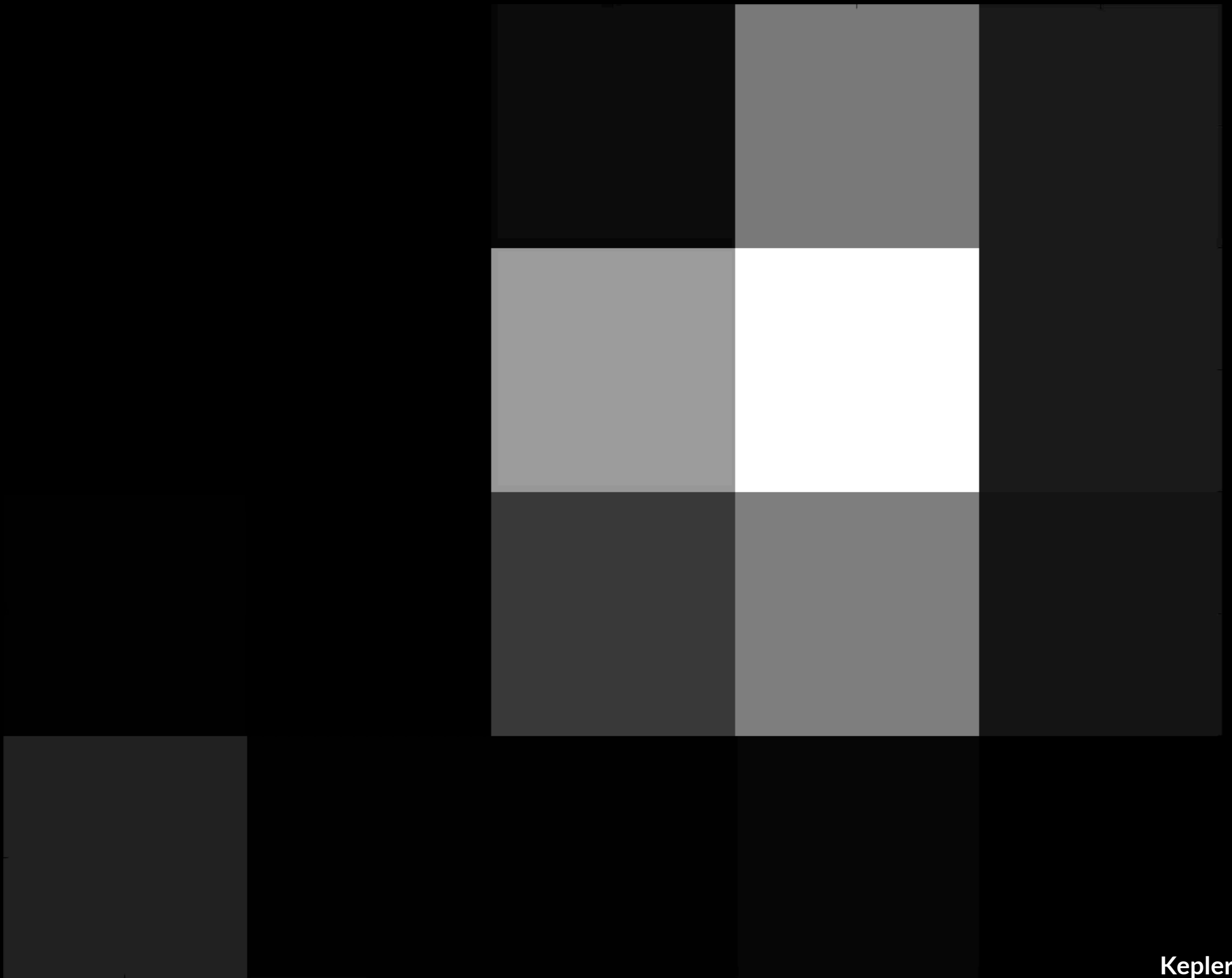


TrES-2

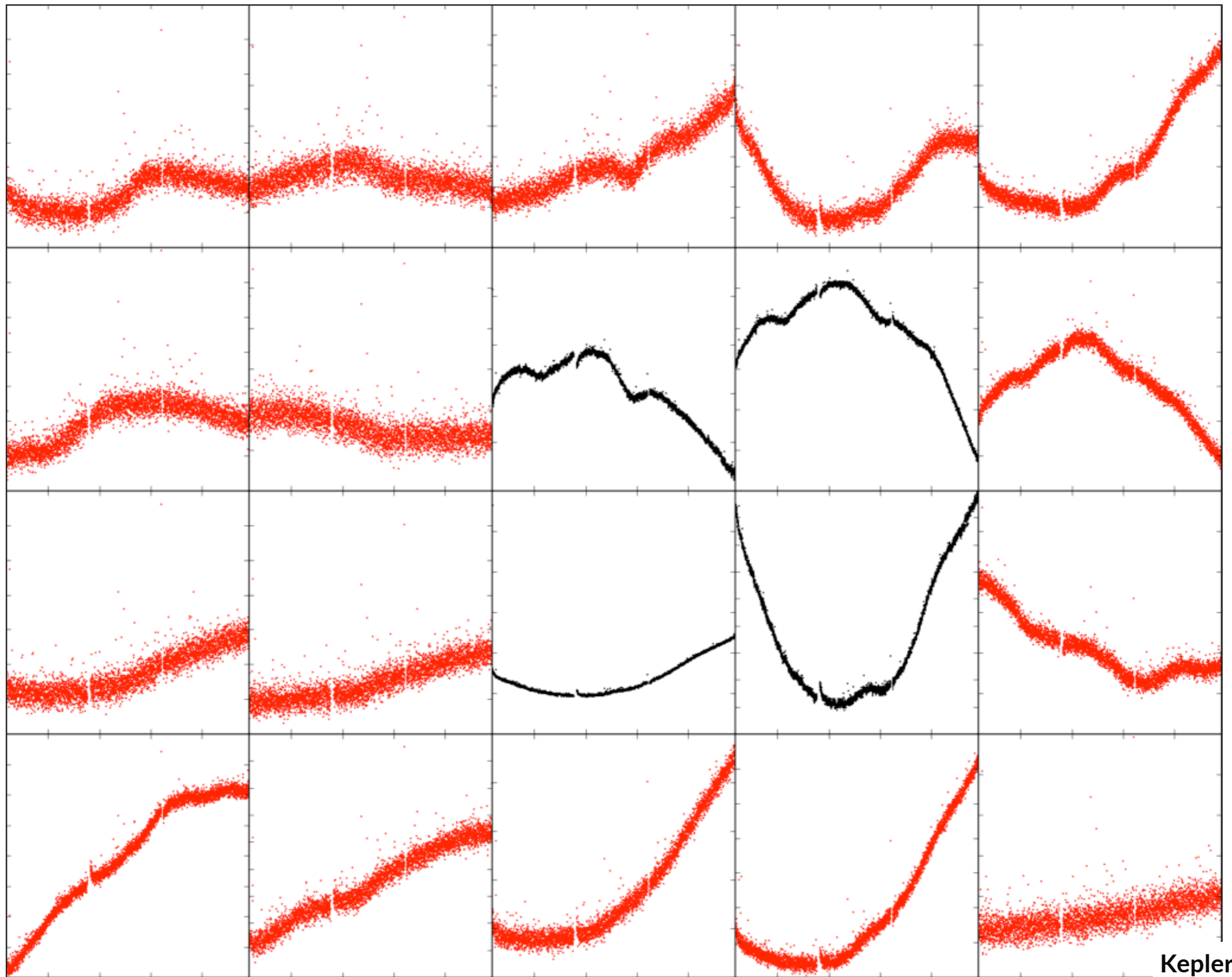
NGC 6791



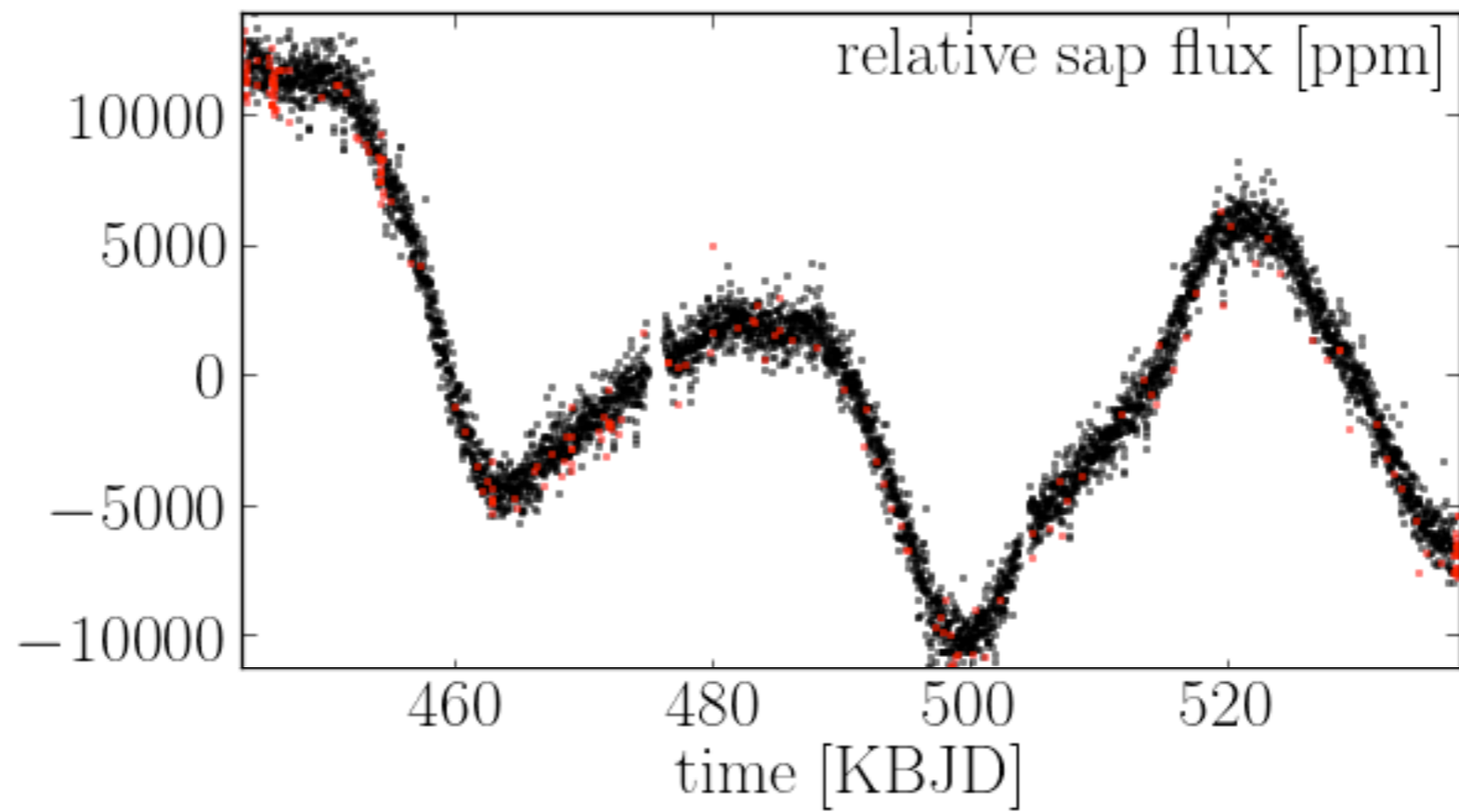
Kepler-32

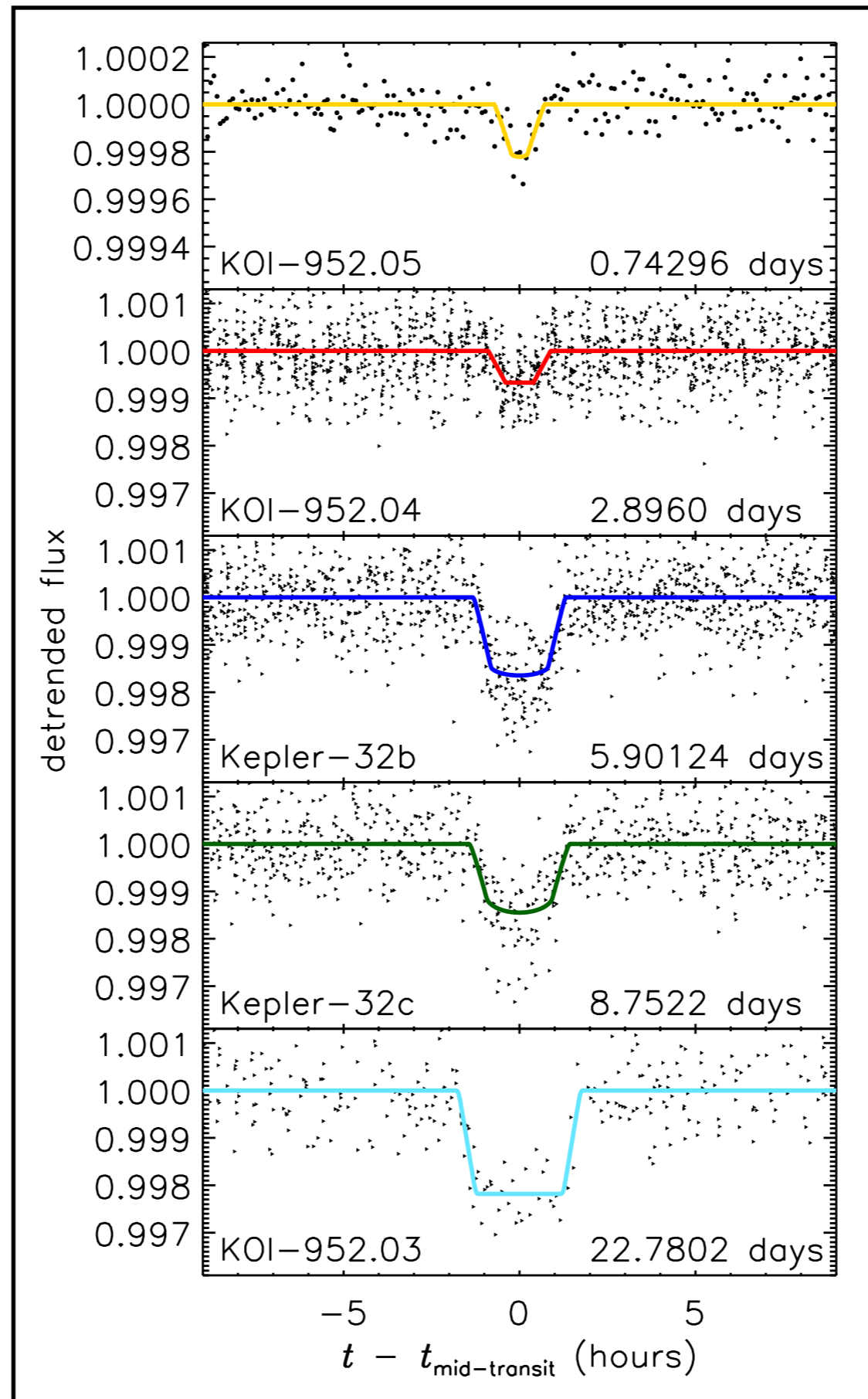


Kepler-32

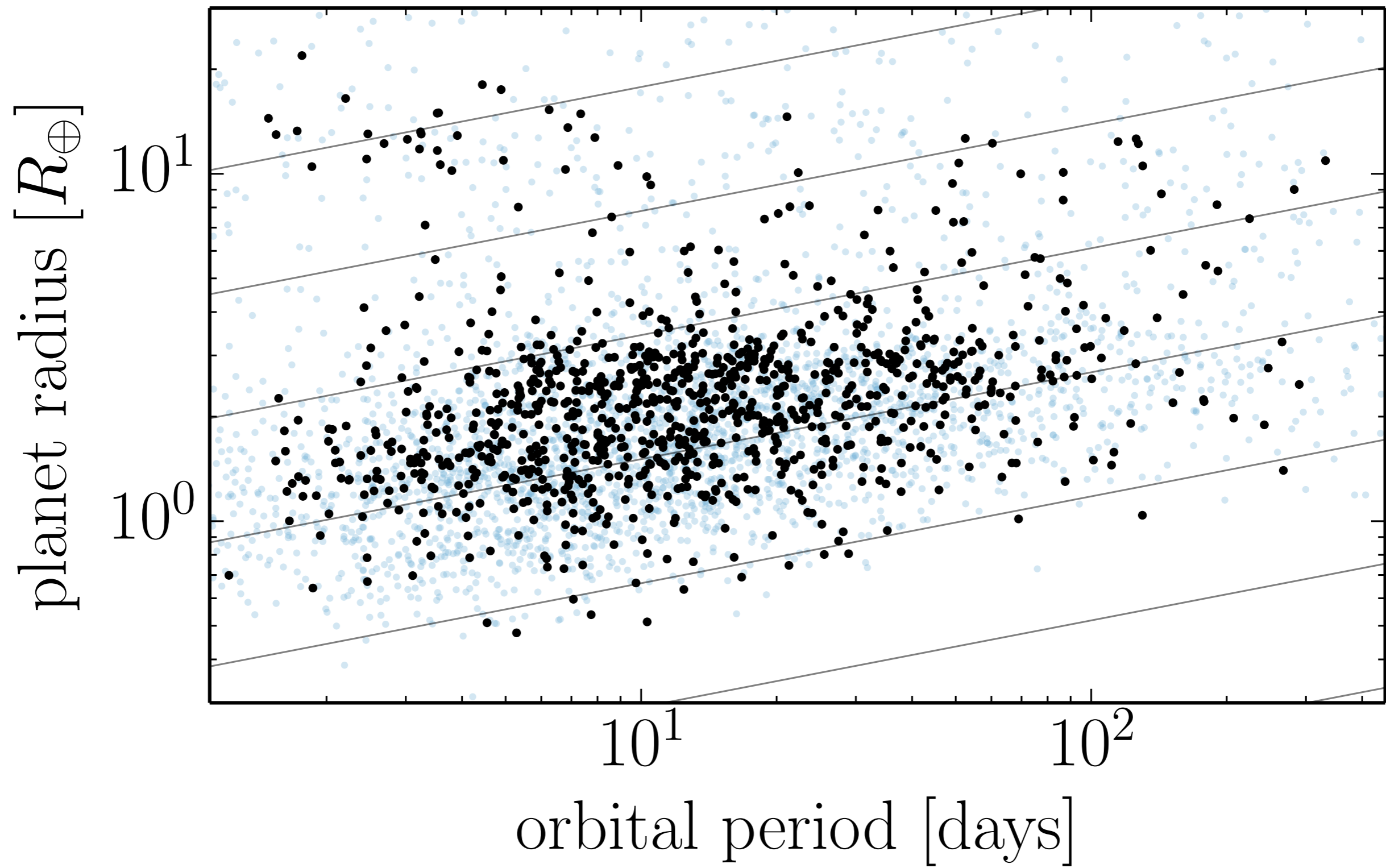


Kepler-32

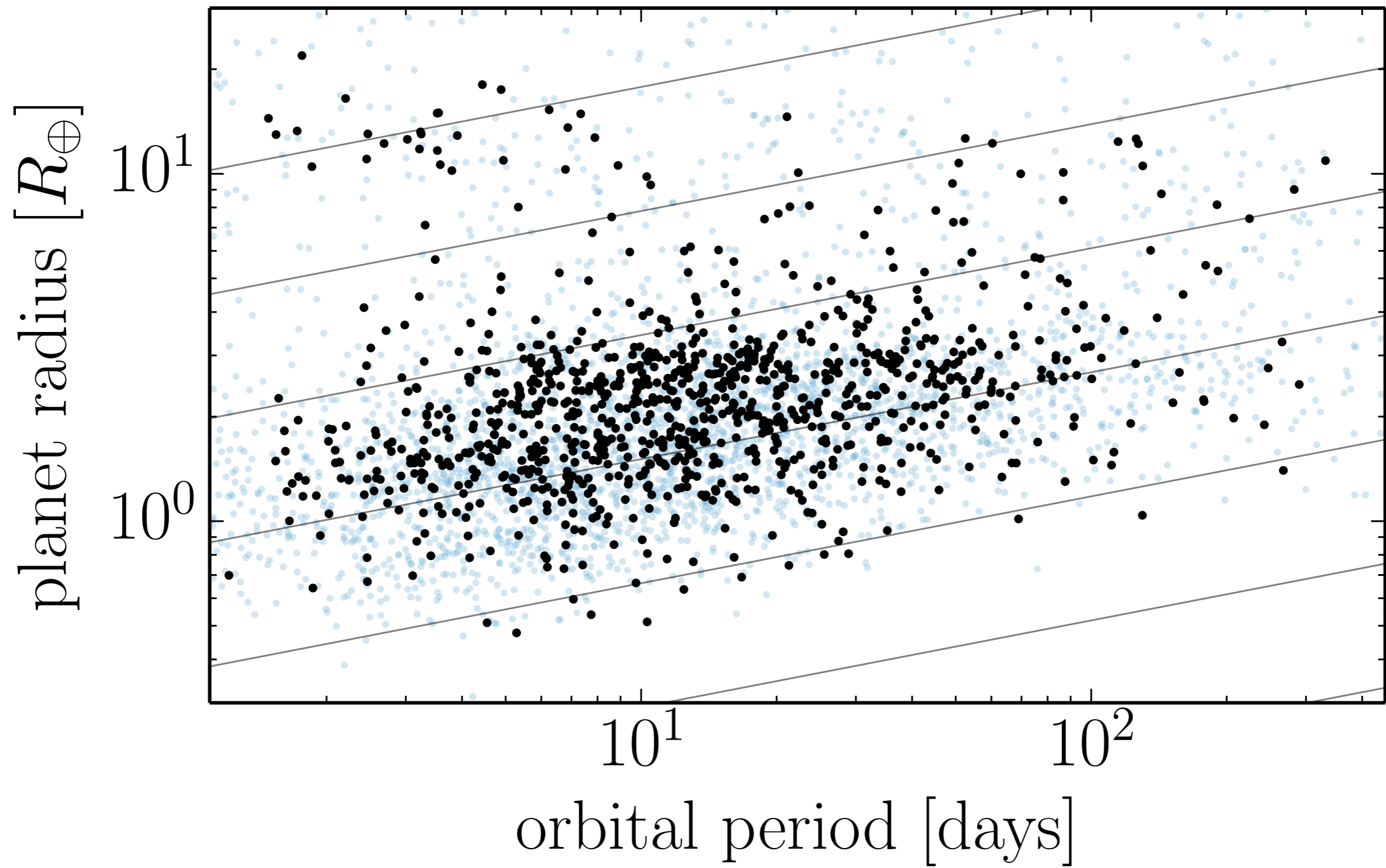


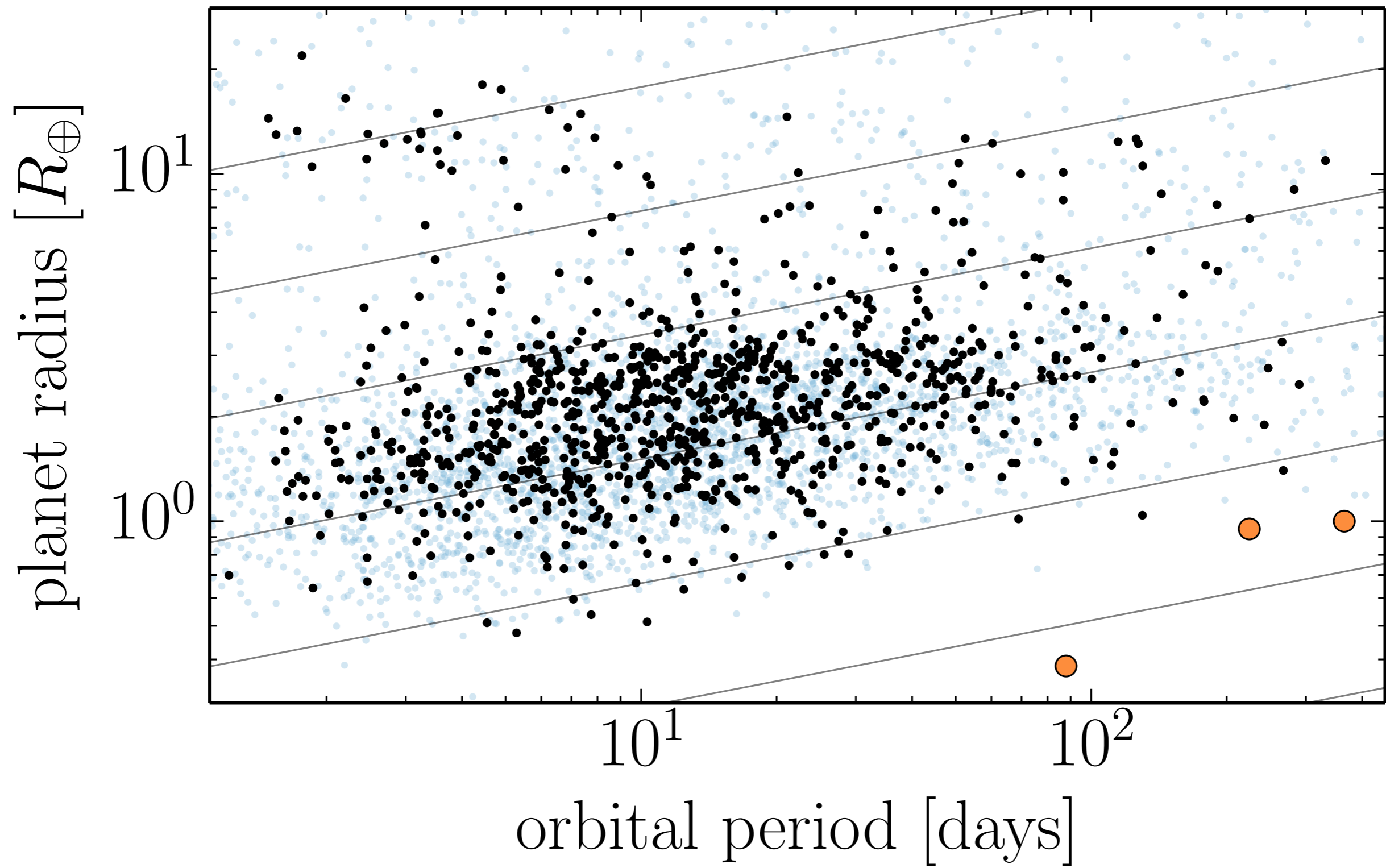


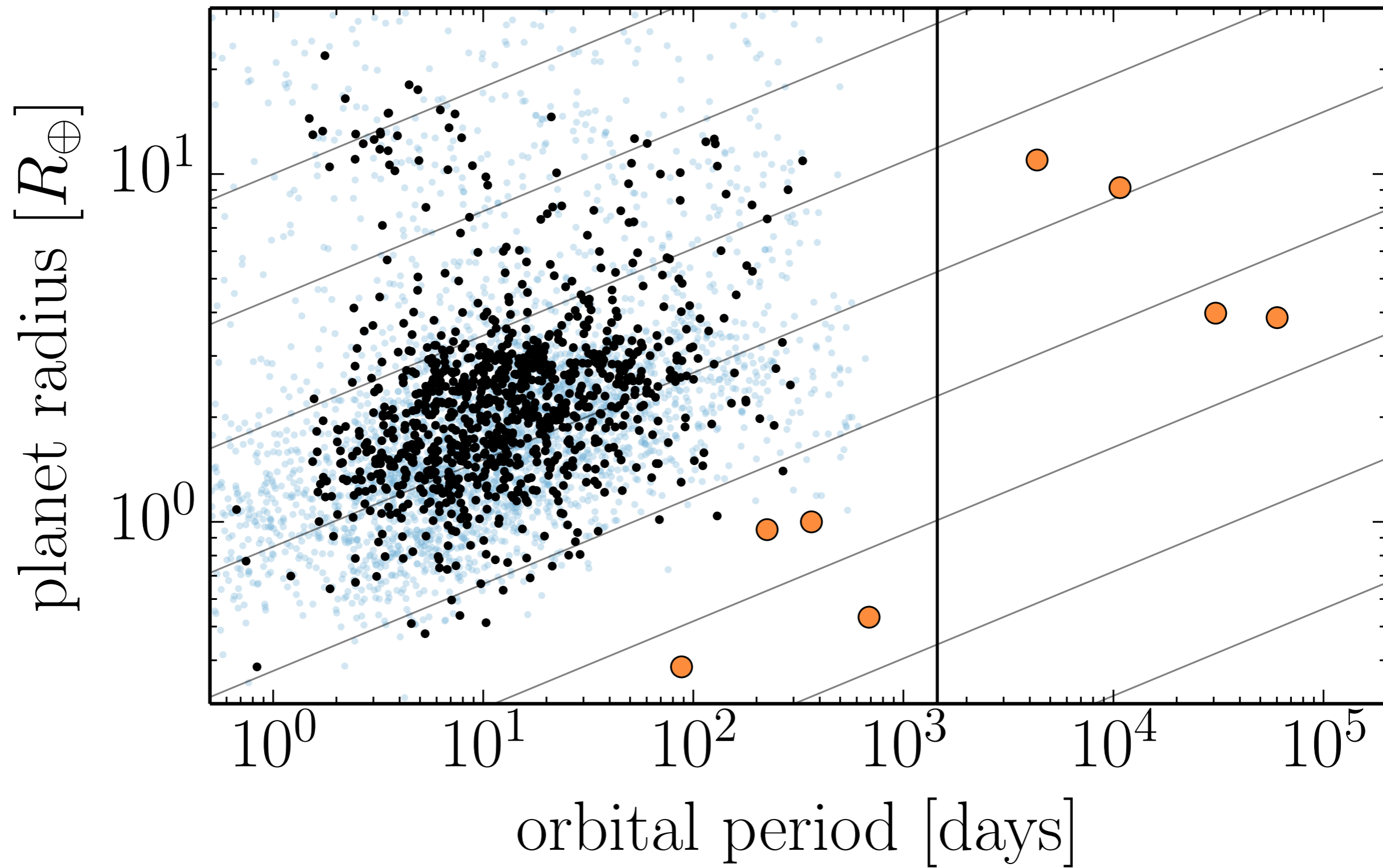
Credit **Fabrycky et al. (2012)**



that looks pretty good...







May 2013

The Kepler Mission
goes up in flames

* not exactly

Kepler



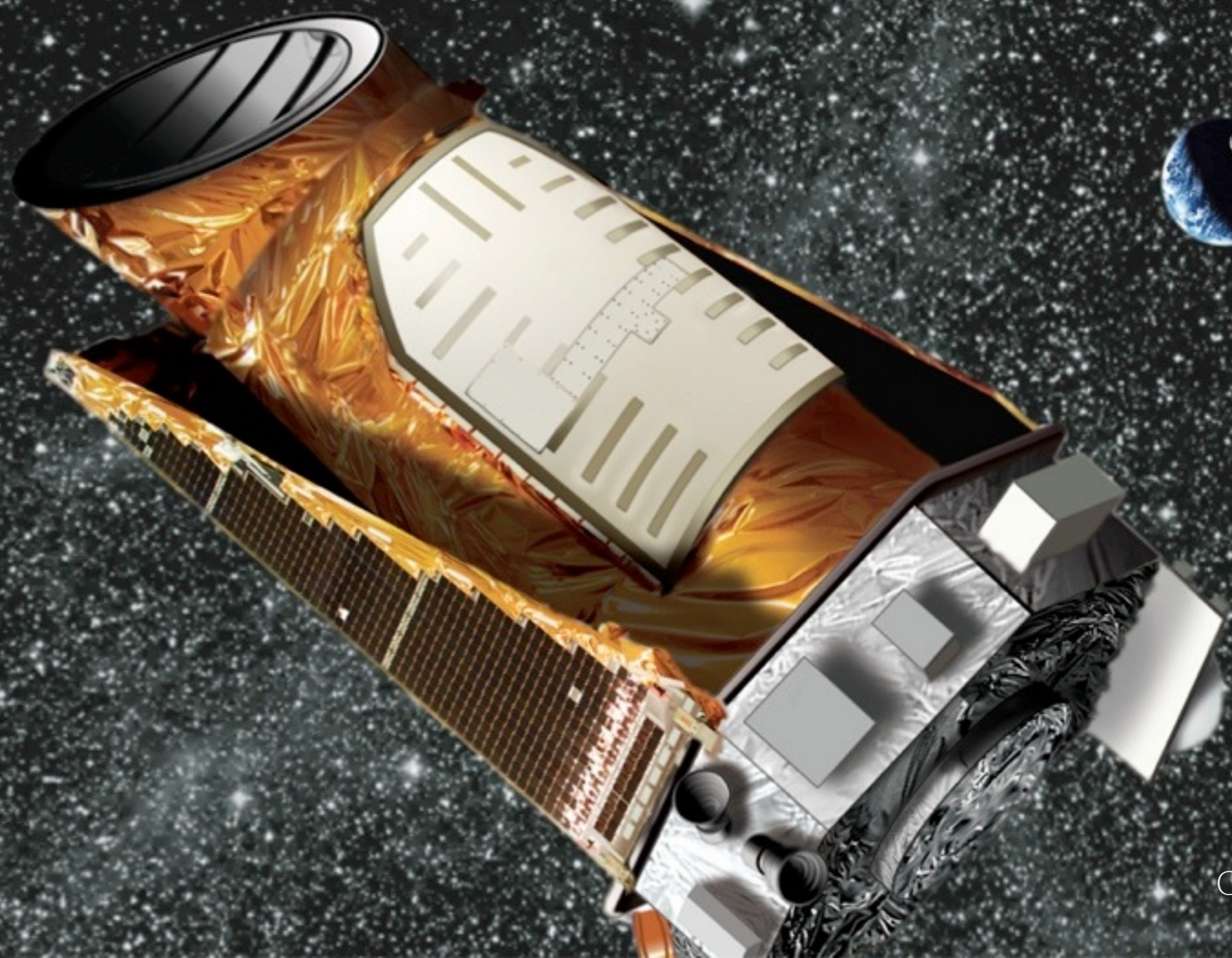


introducing: **K2**

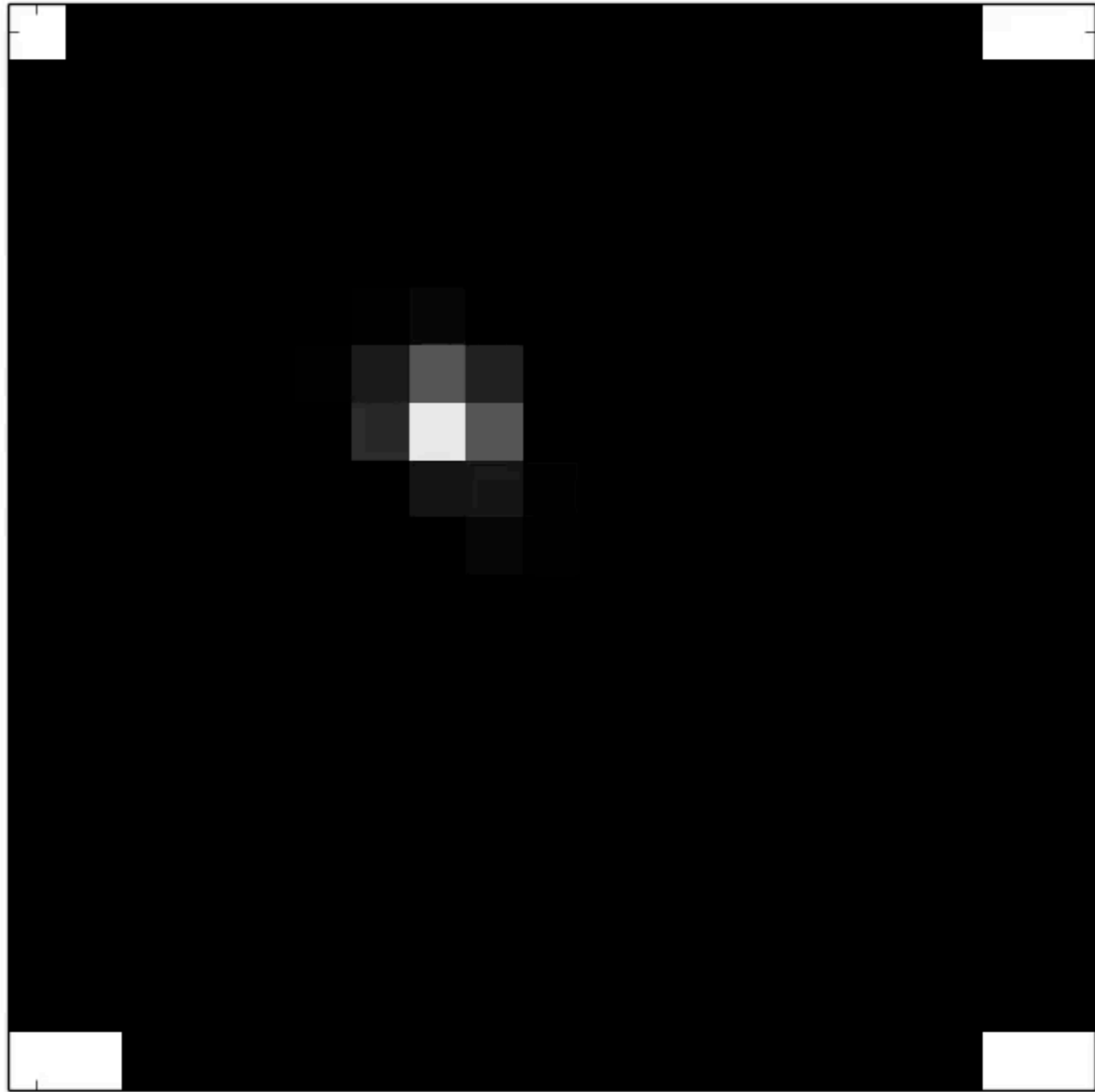


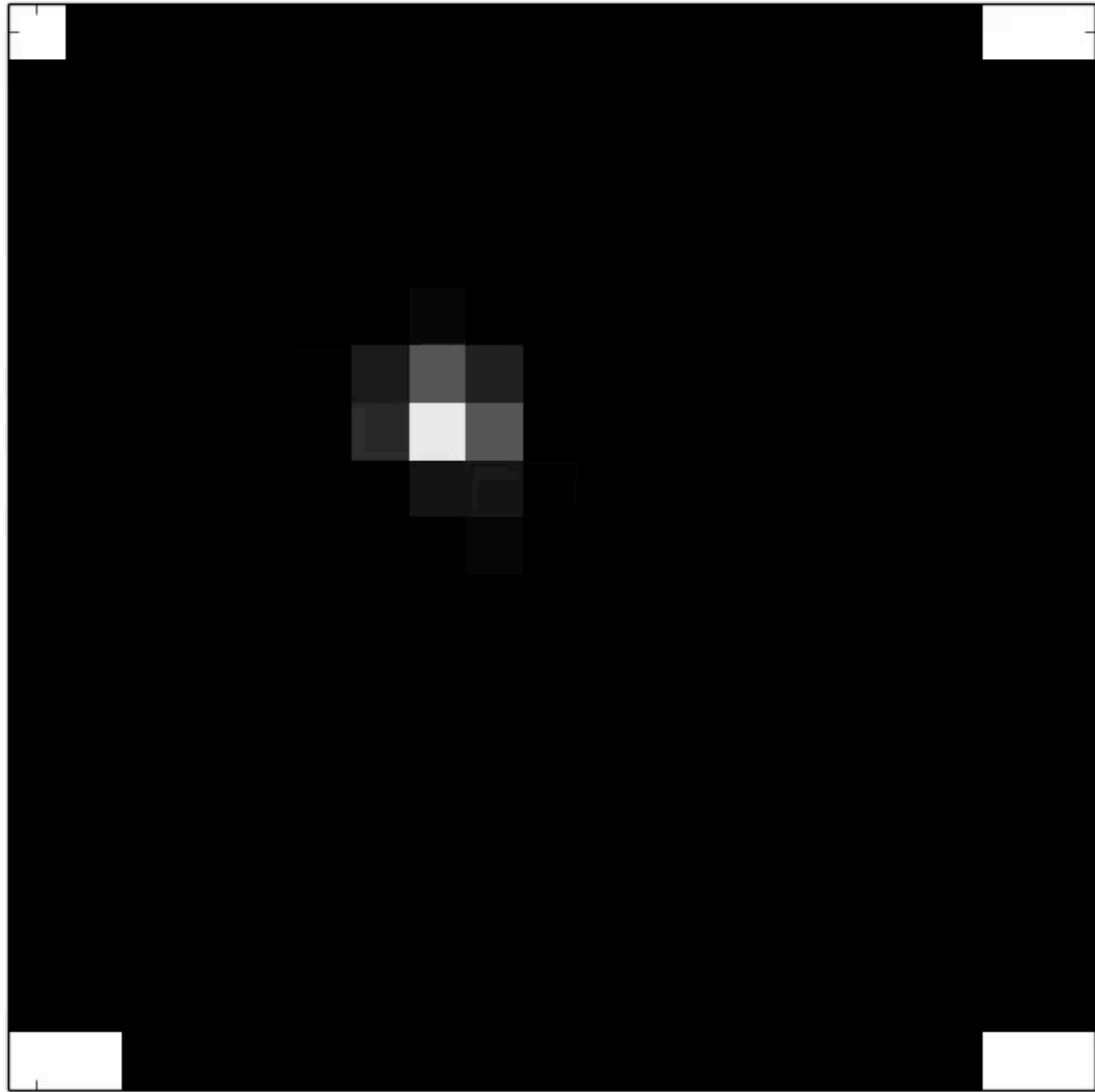
Flickr user [Aamir Choudhry](#)

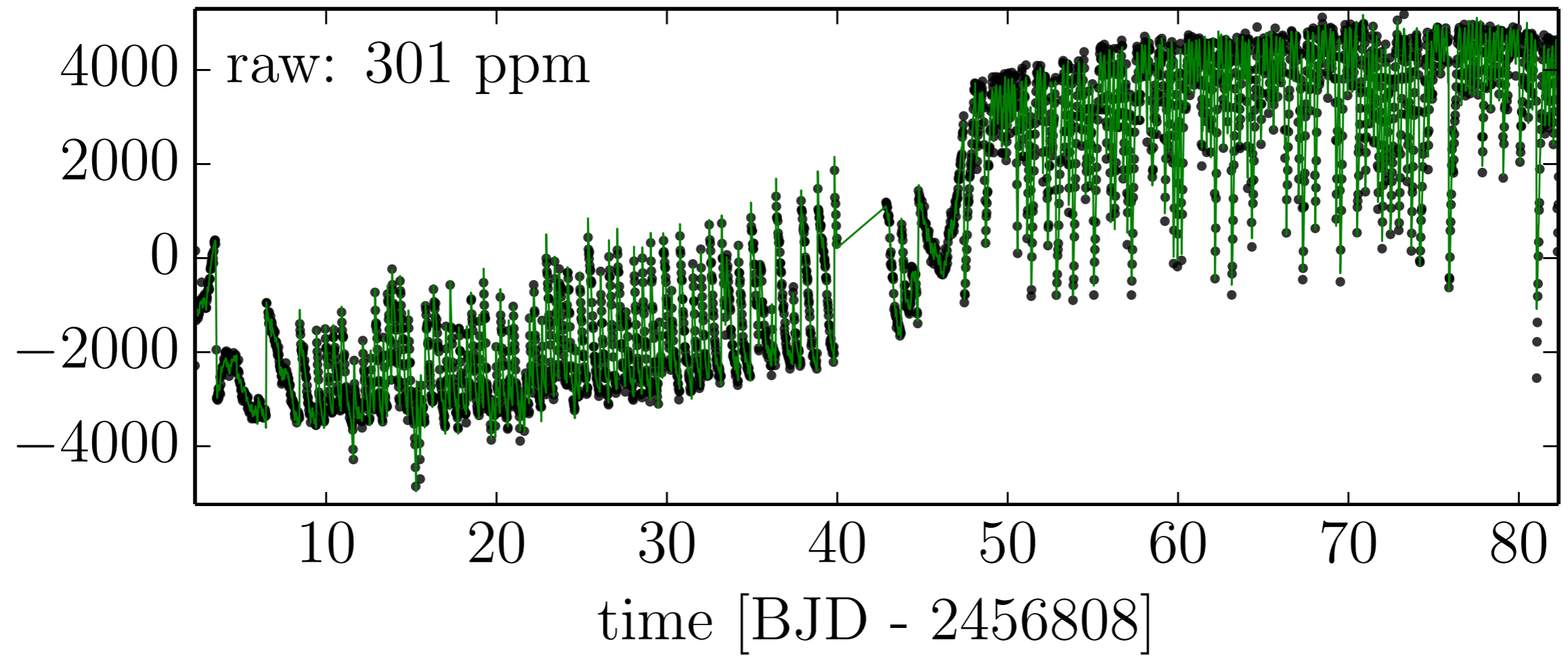
K2

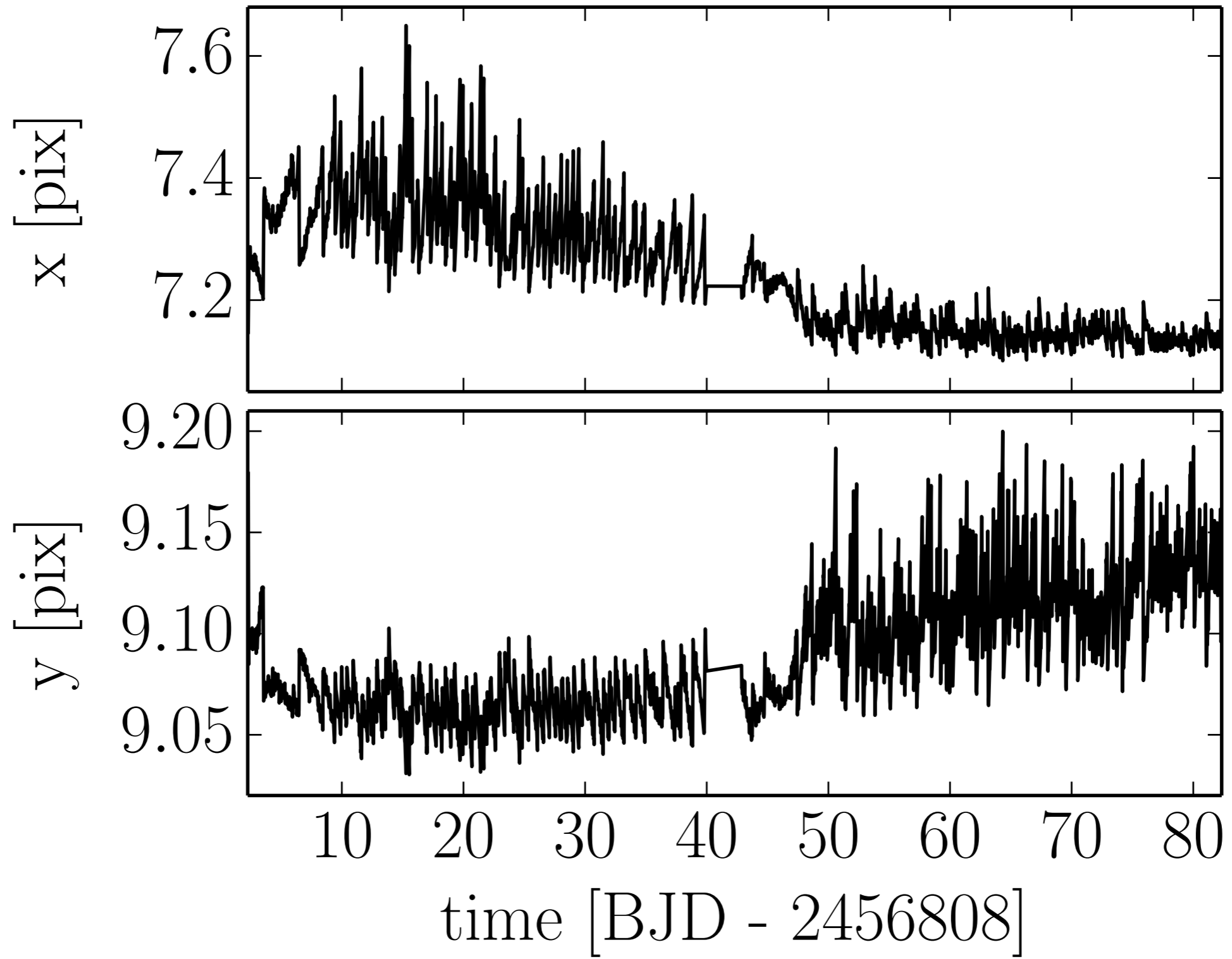


Credit NASA



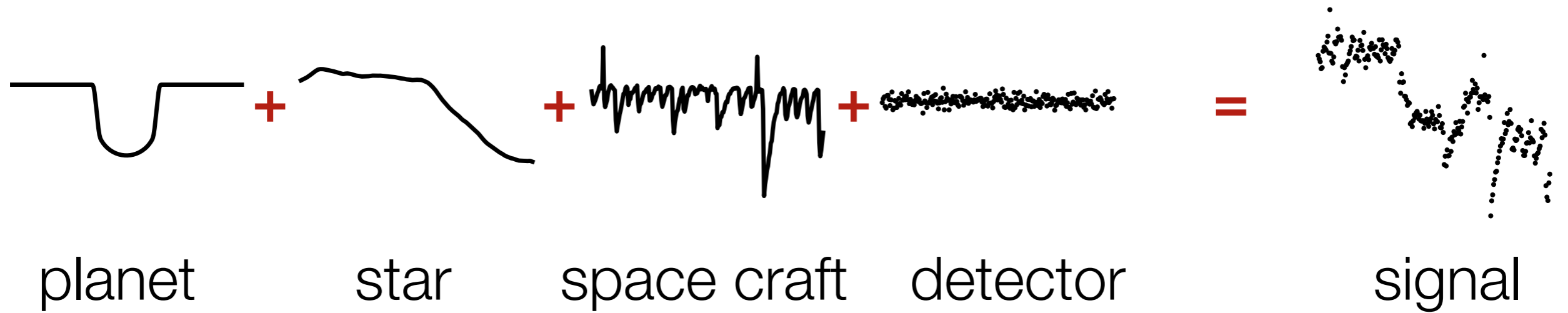




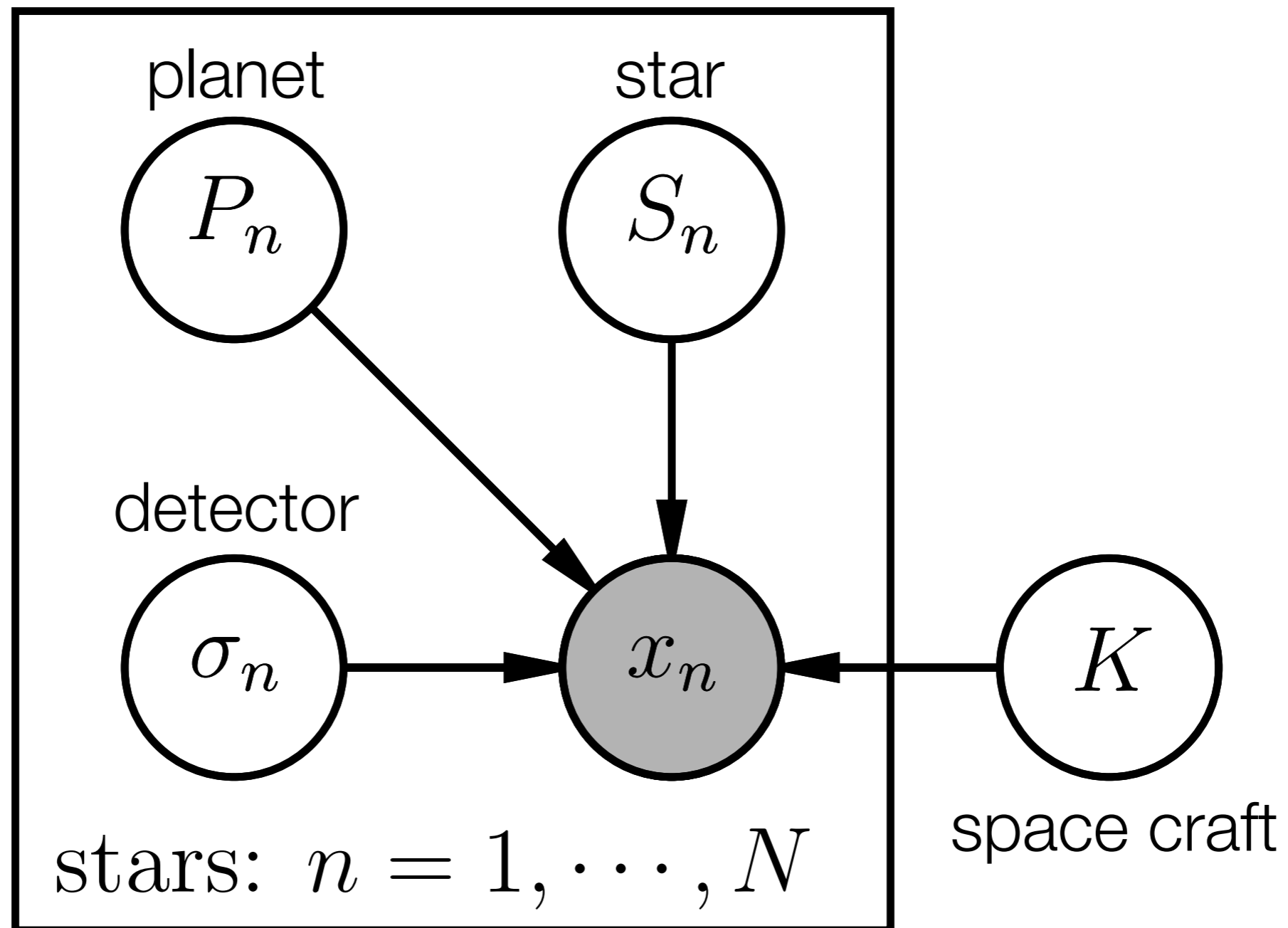


Can we find planets using *K2*?

Anatomy of a transit signal



Designing the probabilistic model

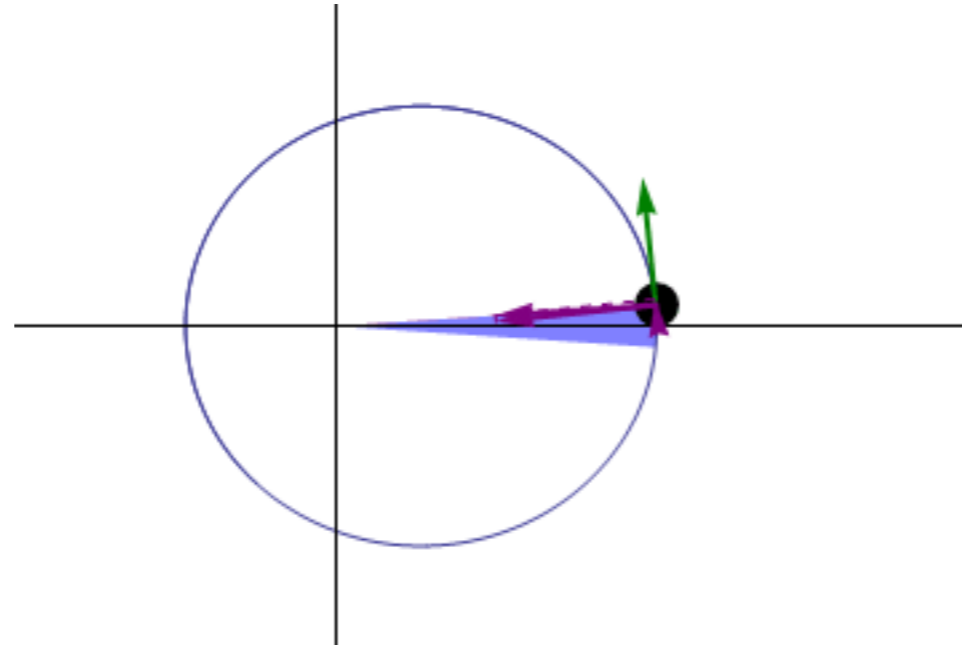


Designing the probabilistic model

representation:

planet: physics and geometry
star: continuous in time → GP
noise: CCD, photon noise → Poisson
space craft: ??

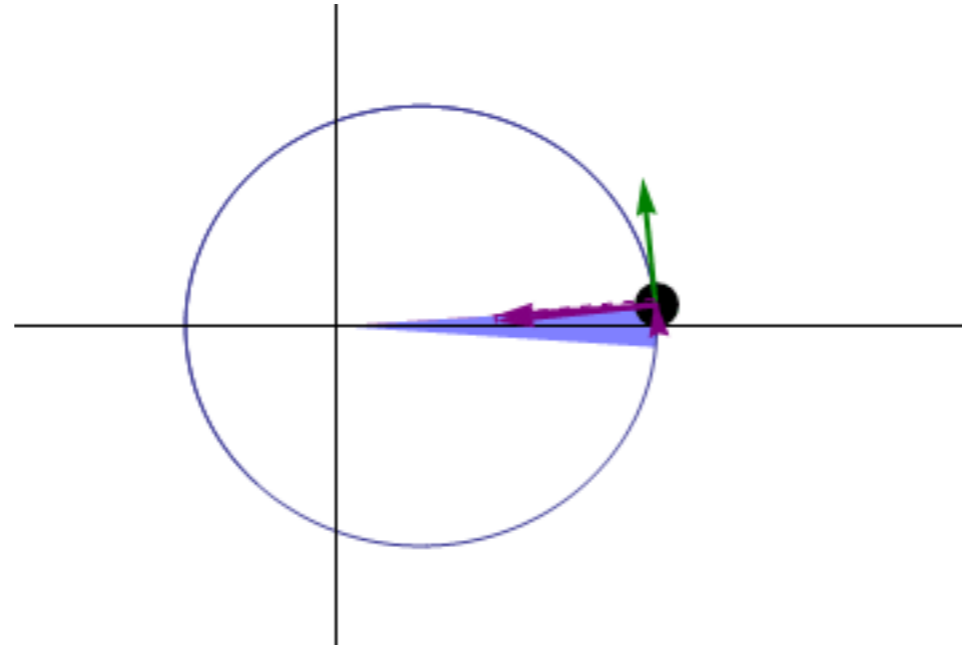
The **planet orbit** model



Kepler's Laws of Planetary Motion



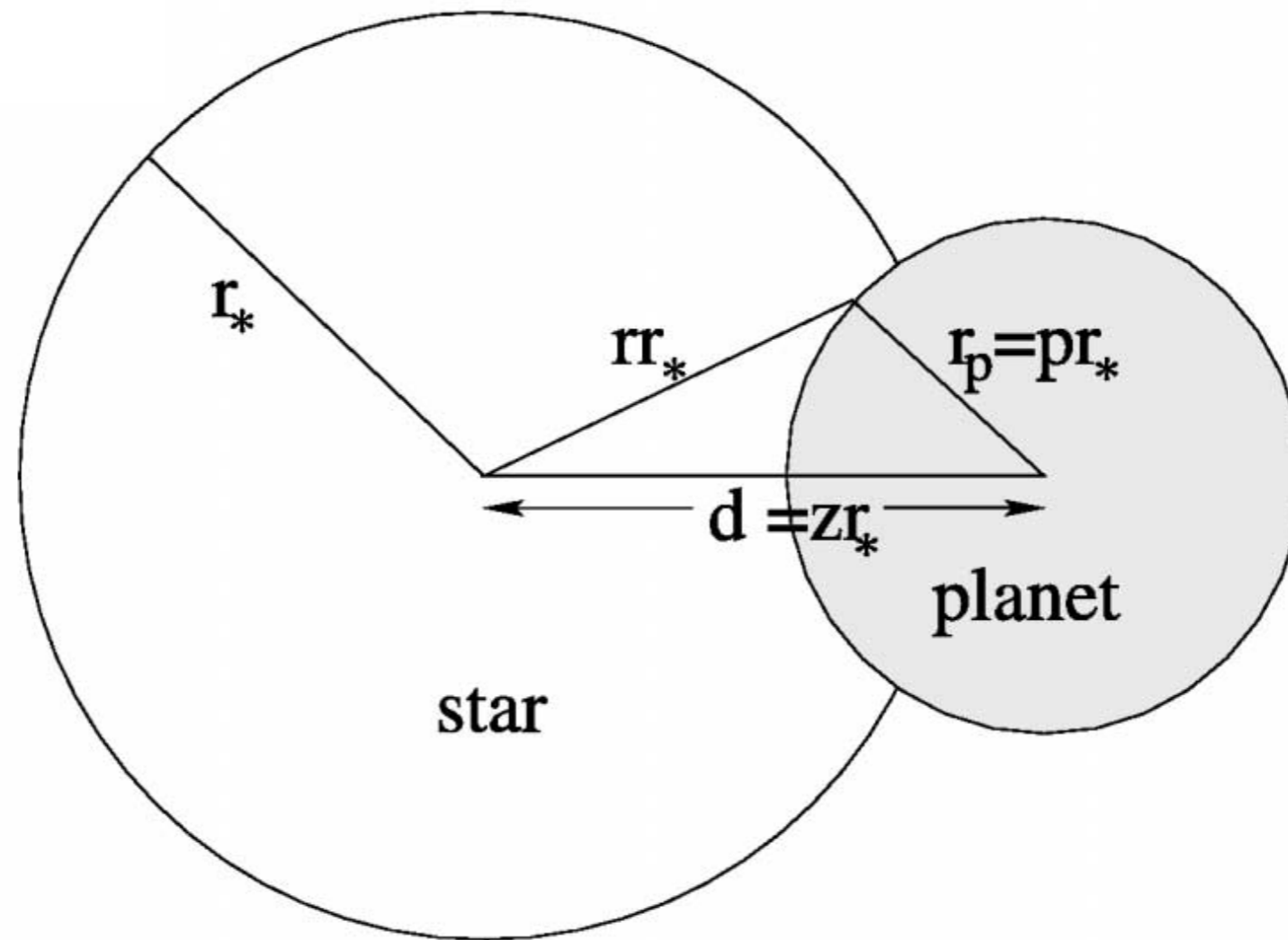
The **planet orbit** model



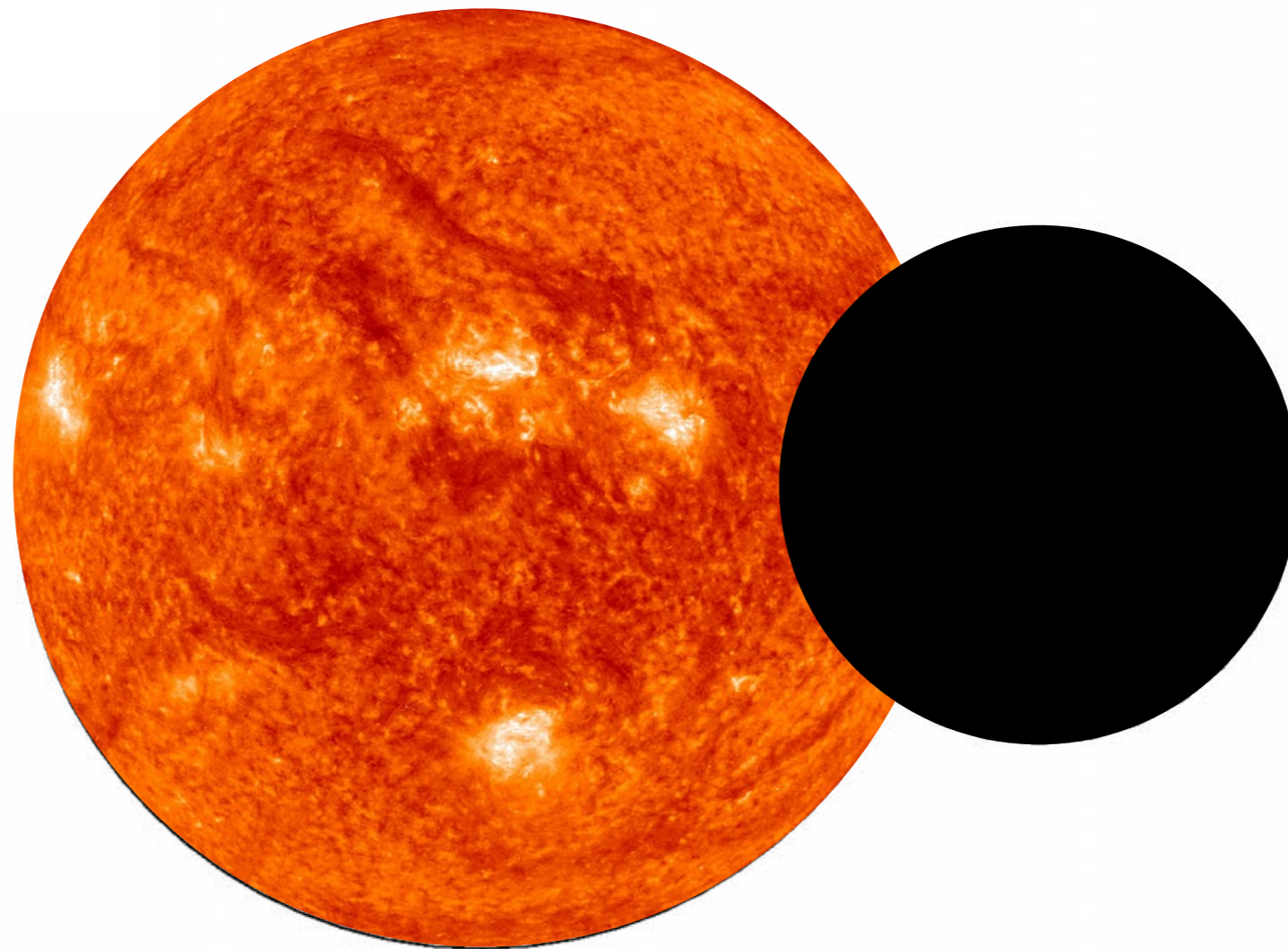
Kepler's Laws of Planetary Motion



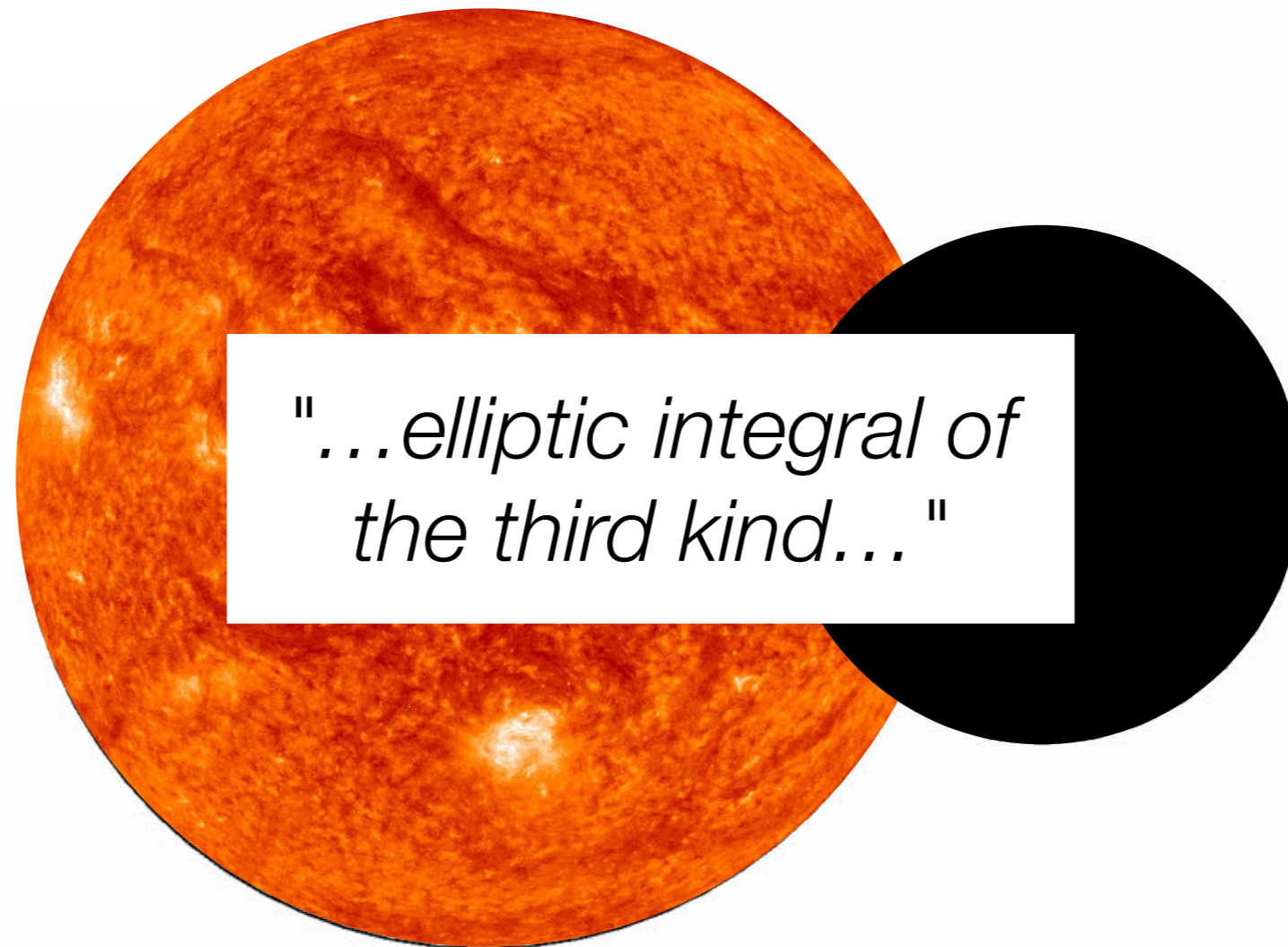
The planet transit model



The planet transit model

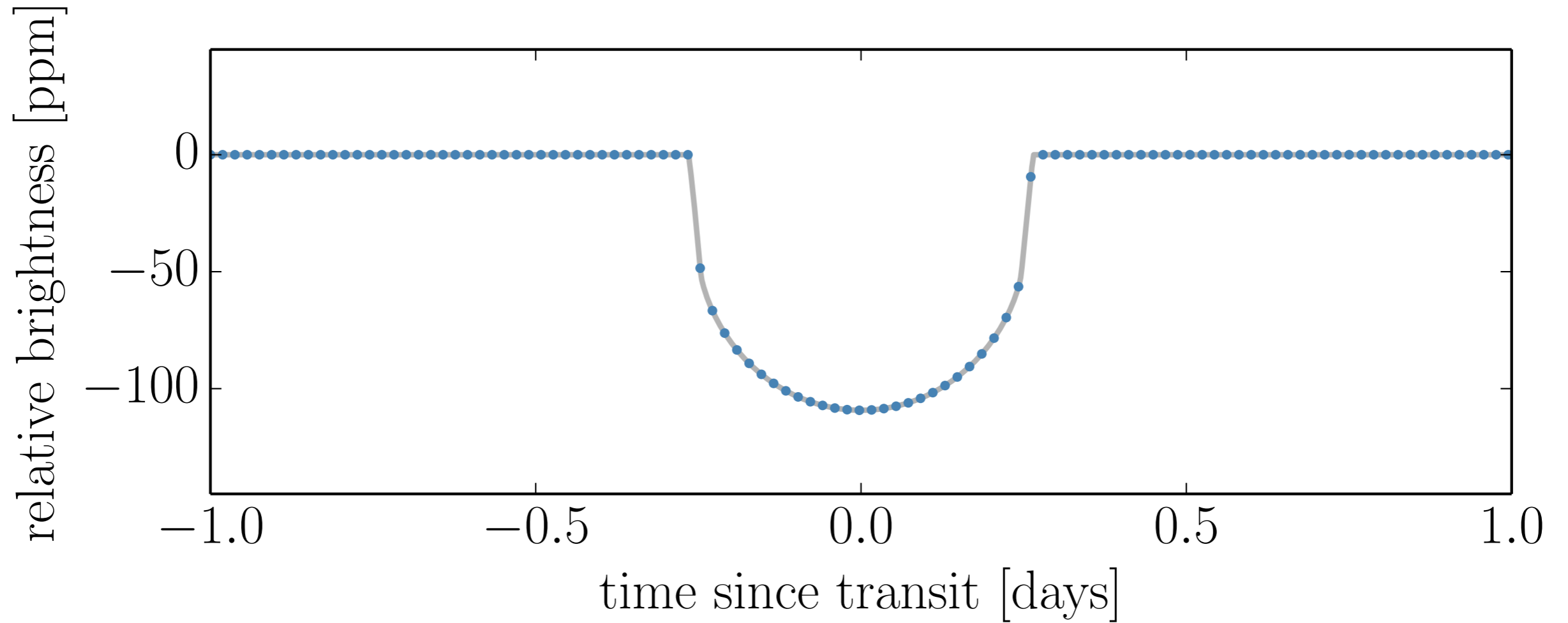


The planet transit model



*"...elliptic integral of
the third kind..."*

The planet transit model

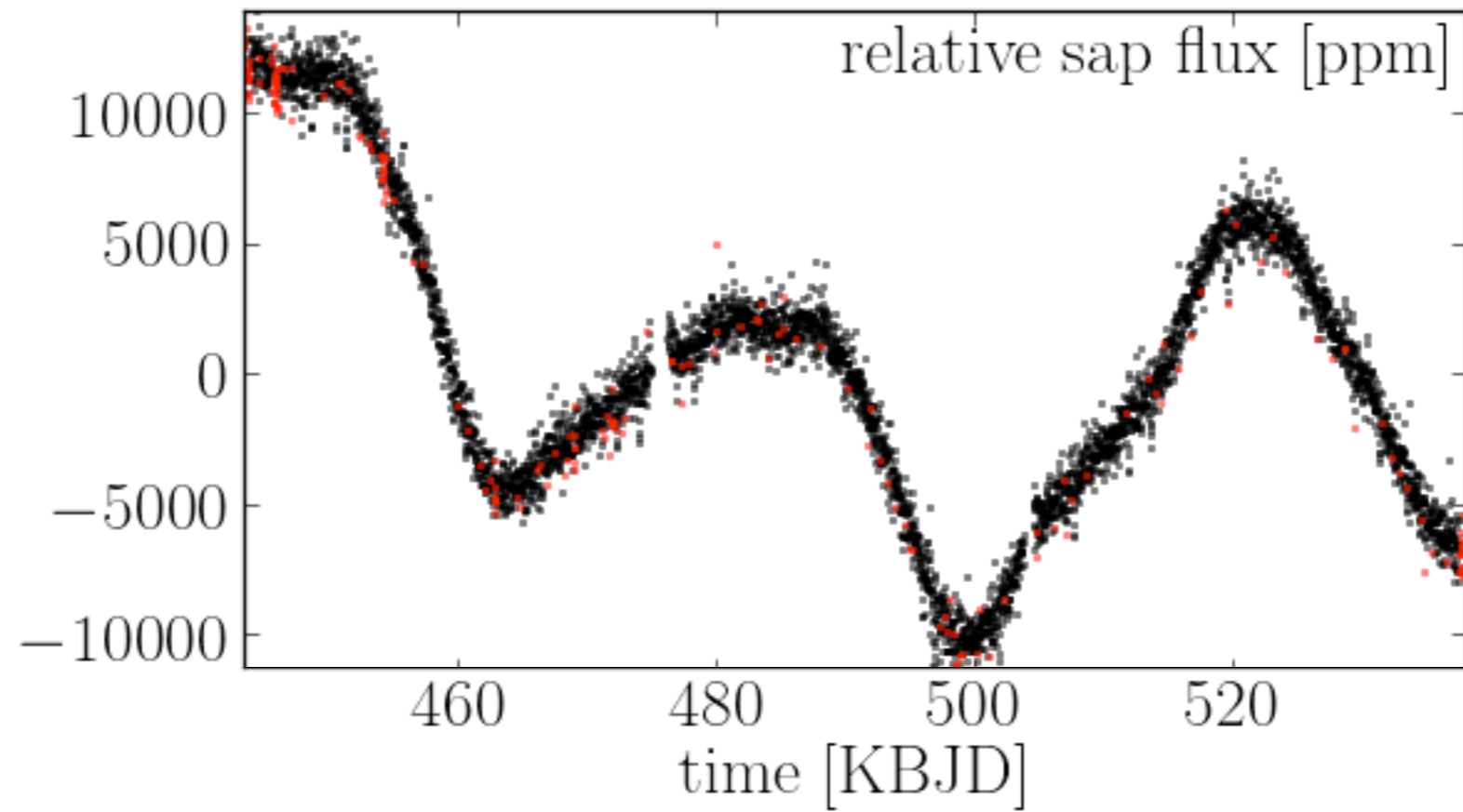


Designing the probabilistic model

representation:

planet: physics and geometry
star: continuous in time → GP
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space craft: ??

The **stellar variability** model



The **stellar variability** model

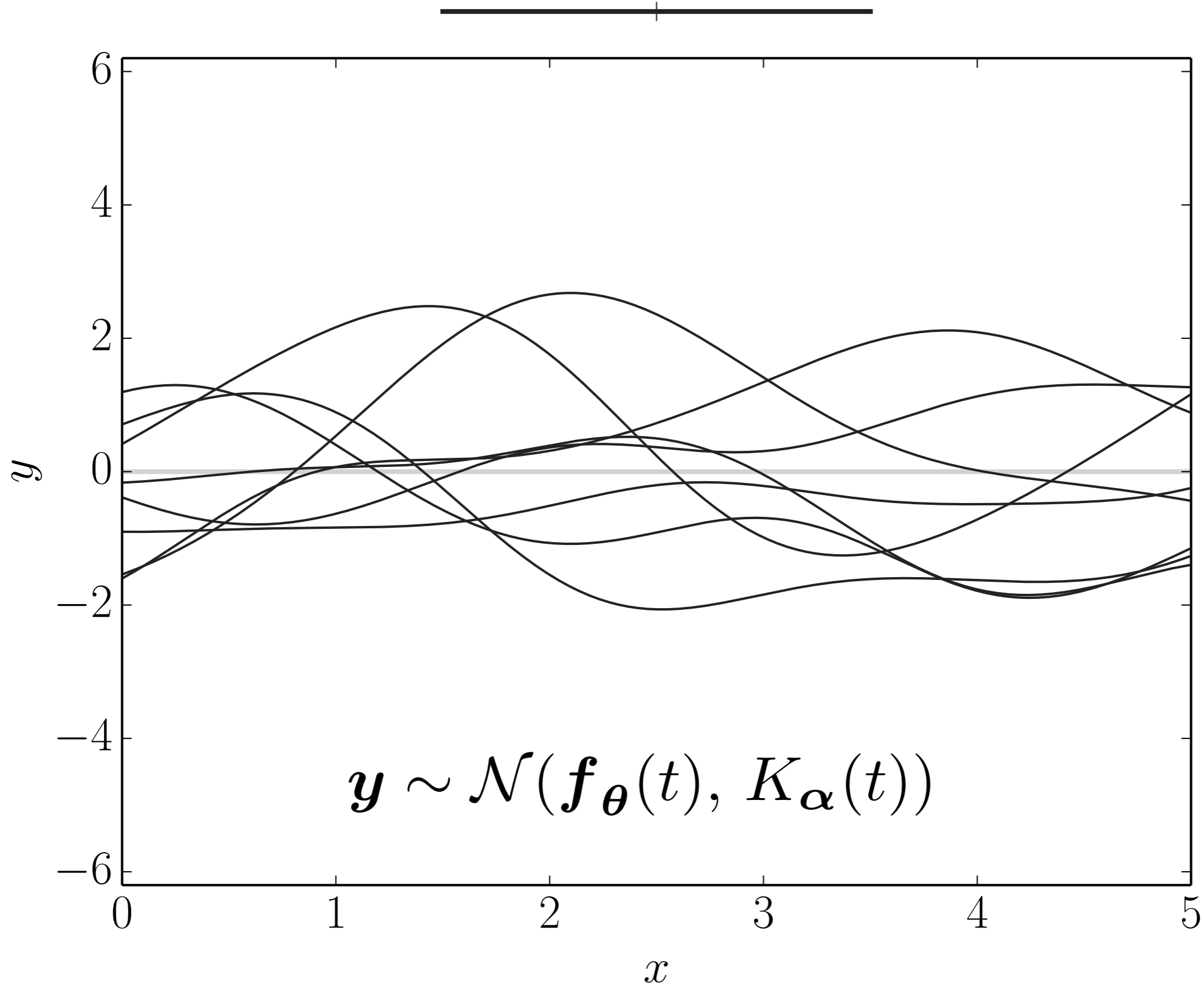
Gaussian Covariance

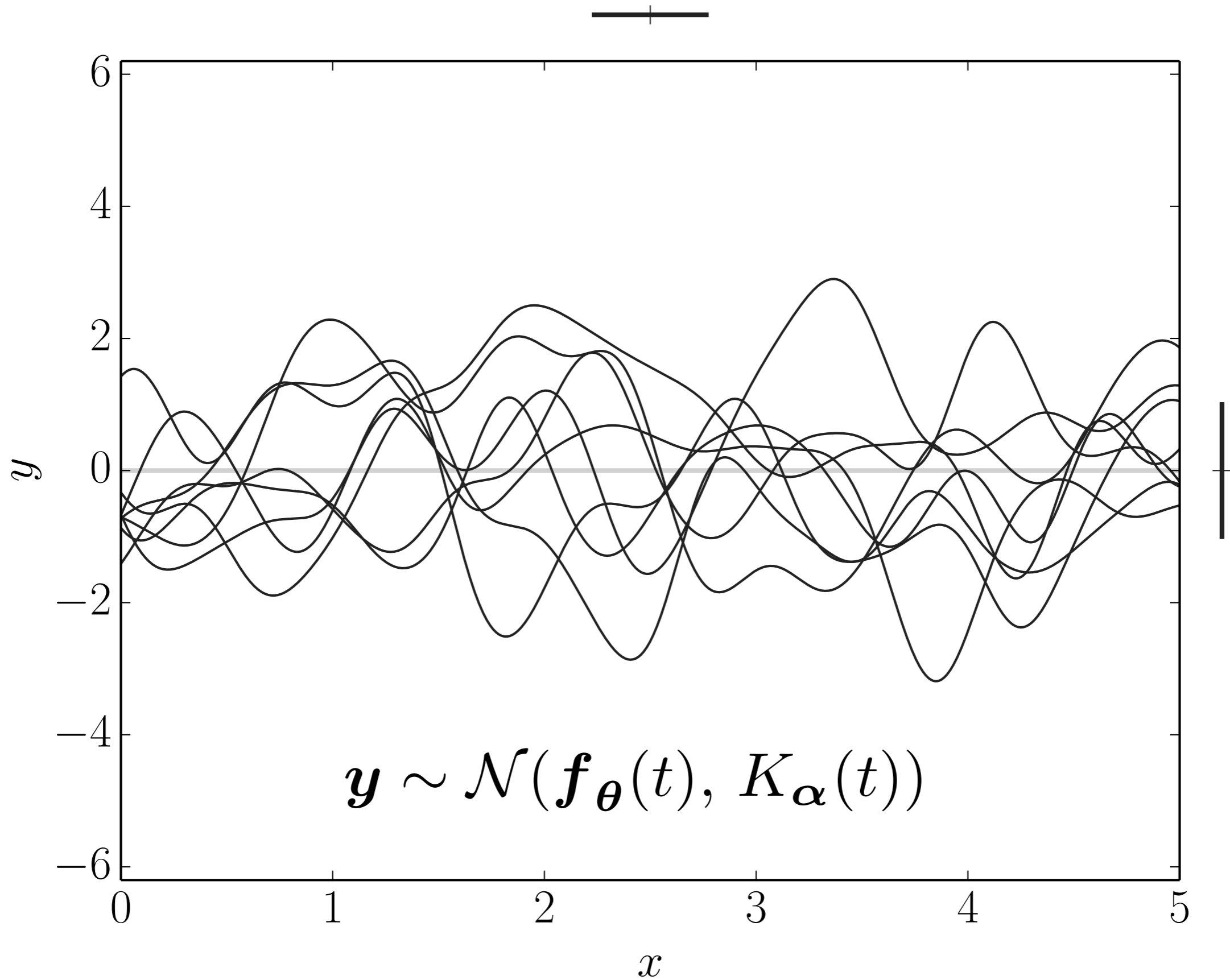
↓ ↓

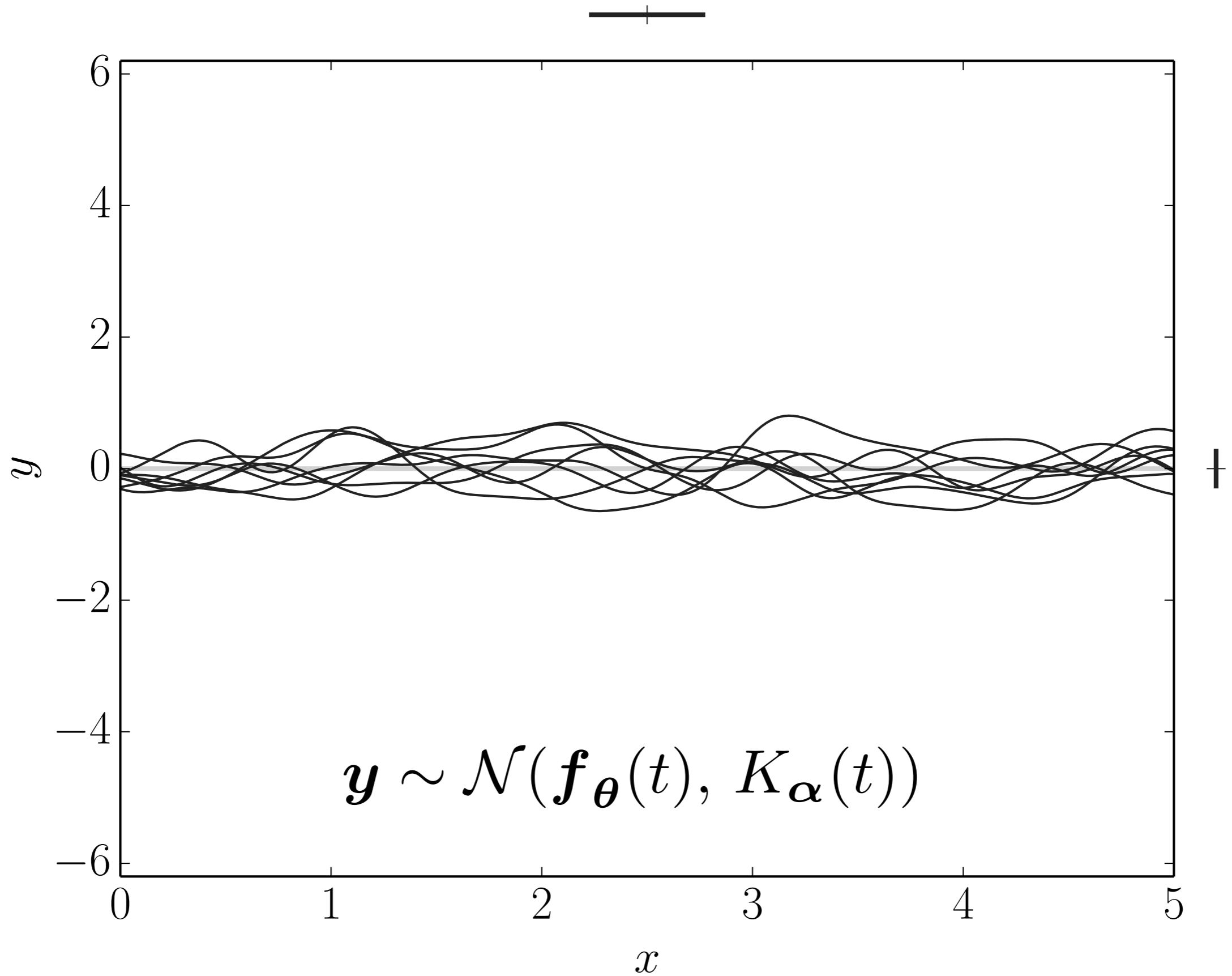
$$\mathbf{y} \sim \mathcal{N}(\mathbf{f}_{\boldsymbol{\theta}}(t), K_{\boldsymbol{\alpha}}(t))$$

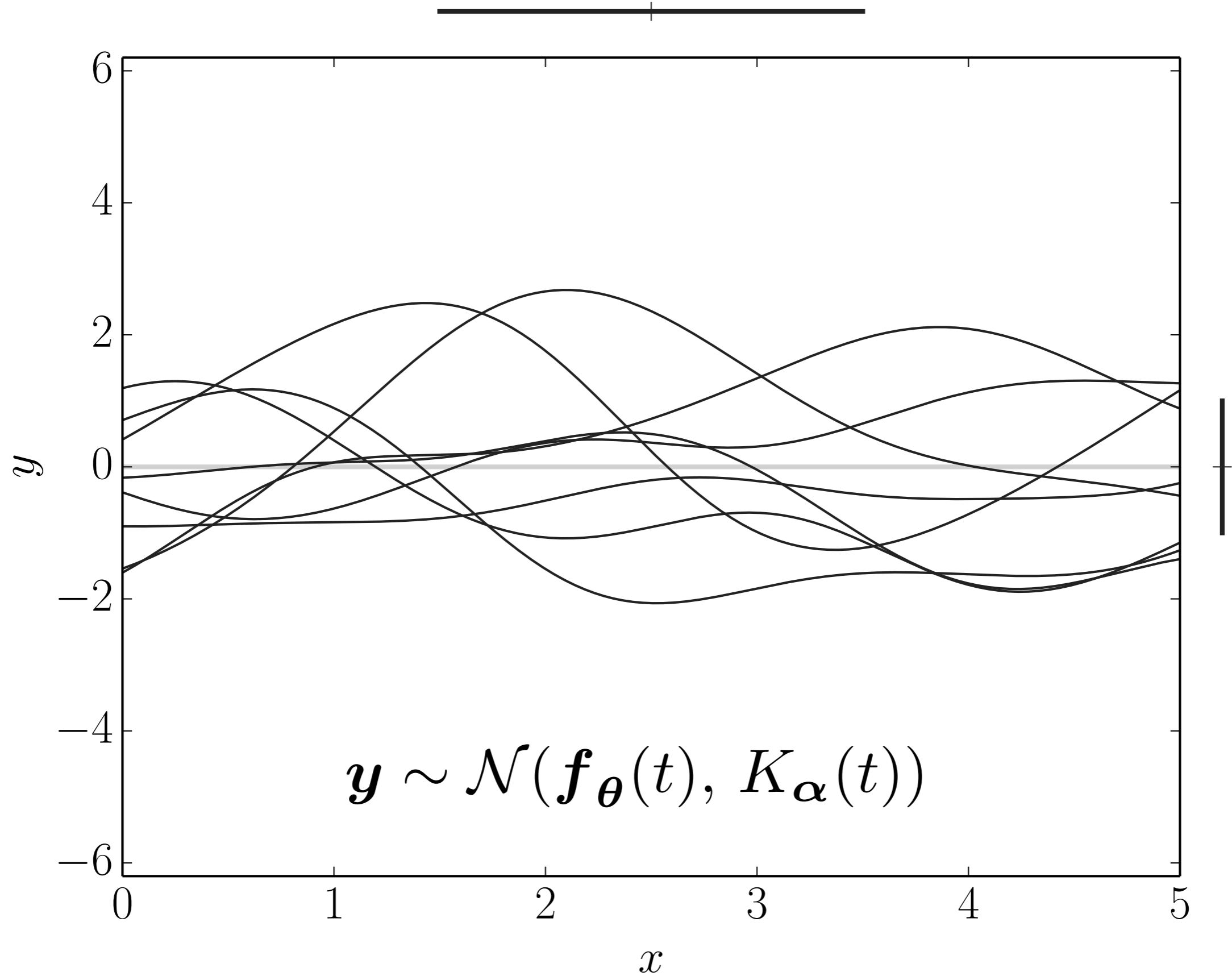
 ↑

Mean

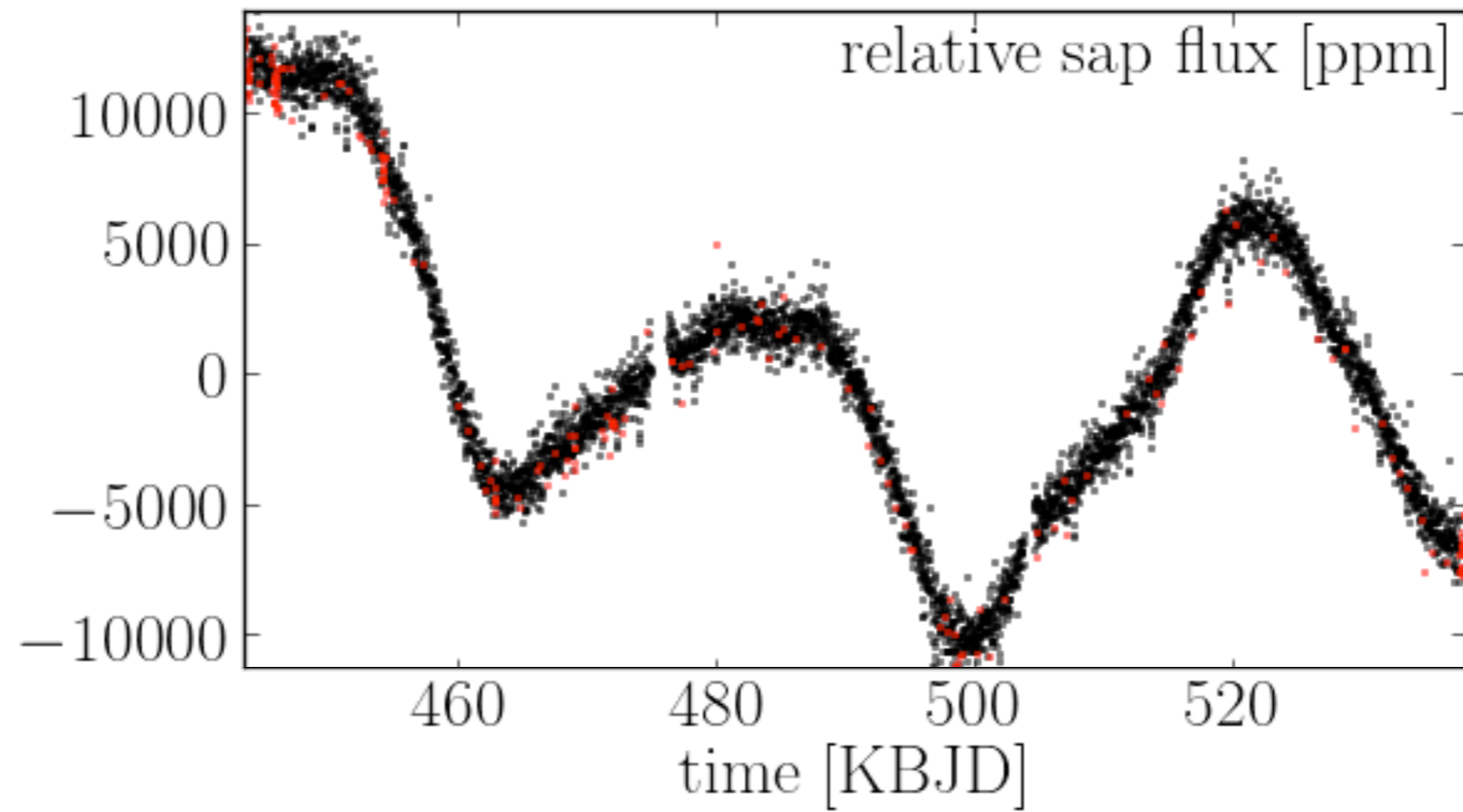








The **stellar variability** model



Designing the probabilistic model

representation:

planet: physics and geometry
star: continuous in time → GP
noise: CCD, photon noise → Poisson
space craft: ??

The noise model



Designing the probabilistic model

representation:

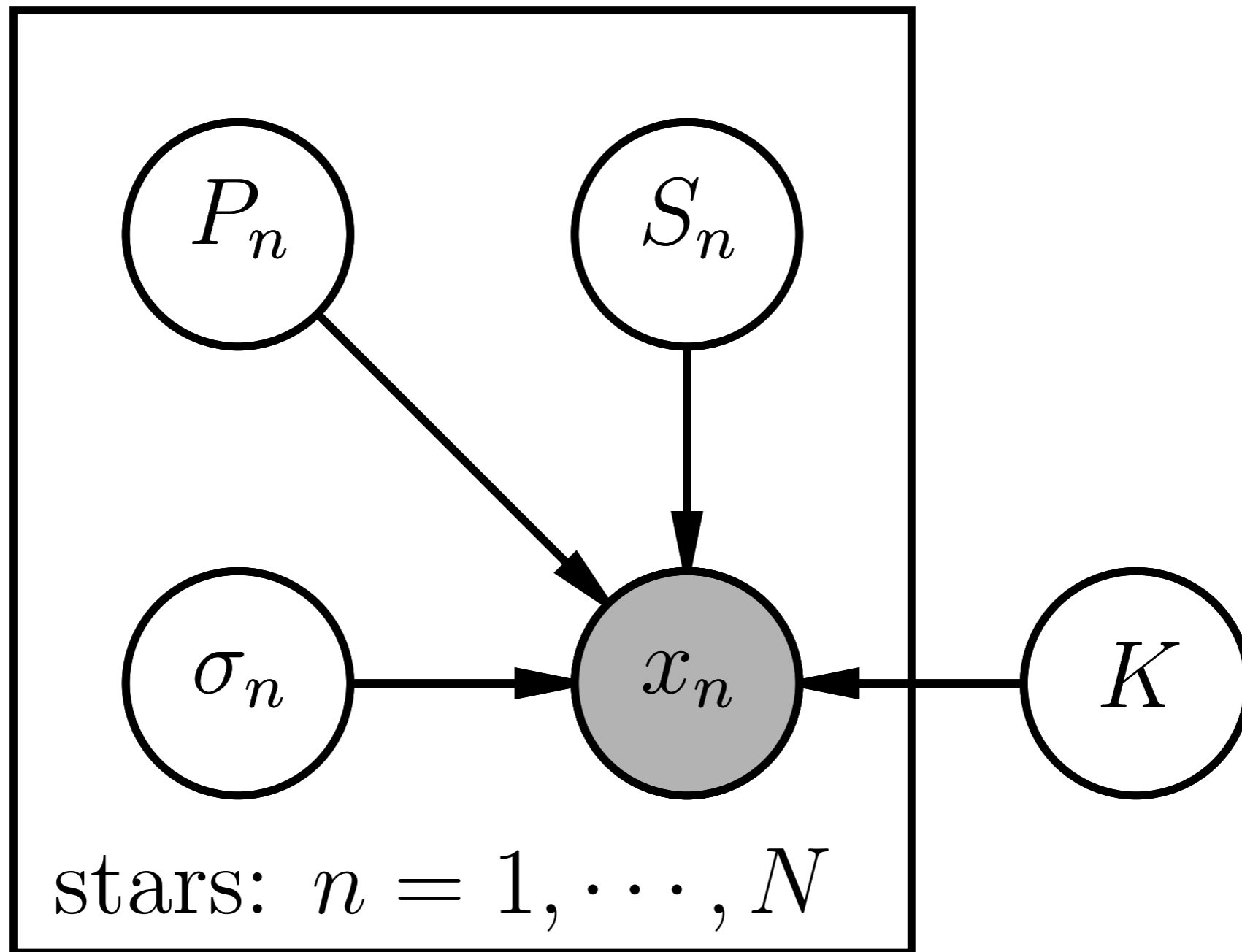
planet: physics and geometry

star: continuous in time → GP

noise: CCD, photon noise → Poisson

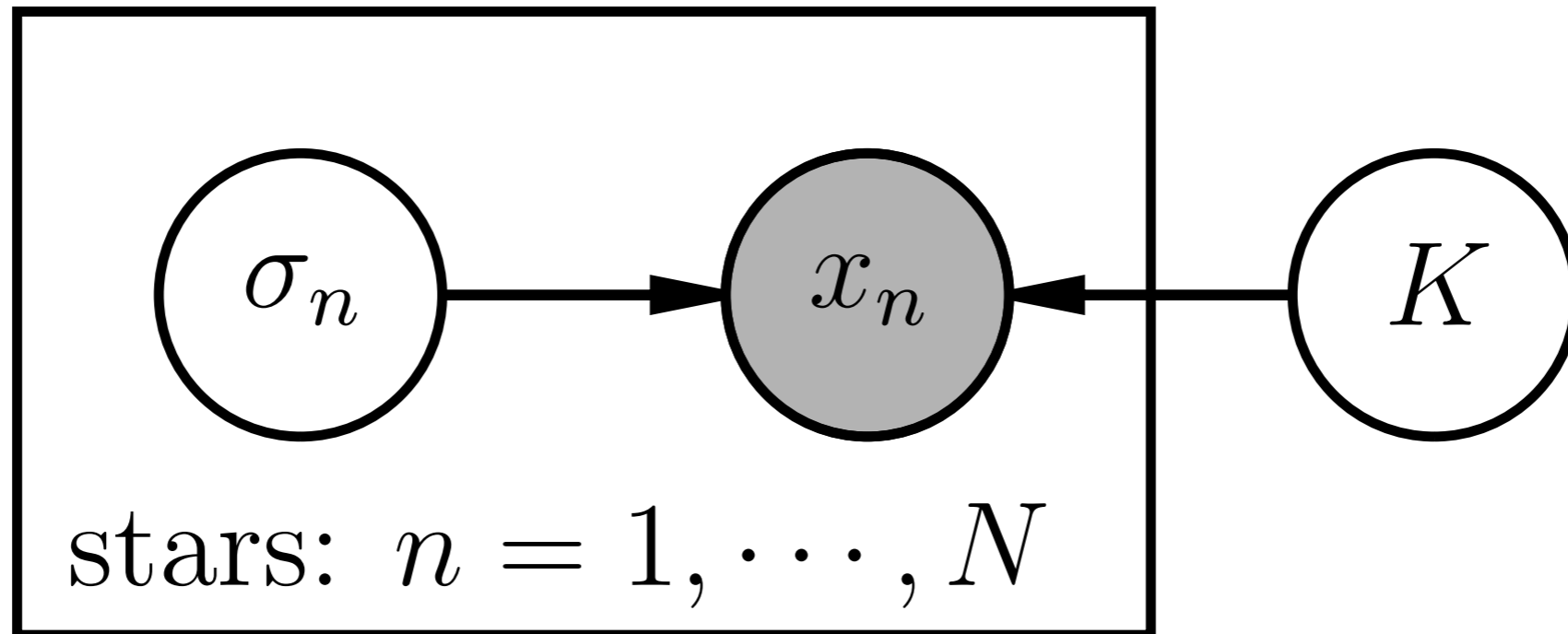
space craft: ??

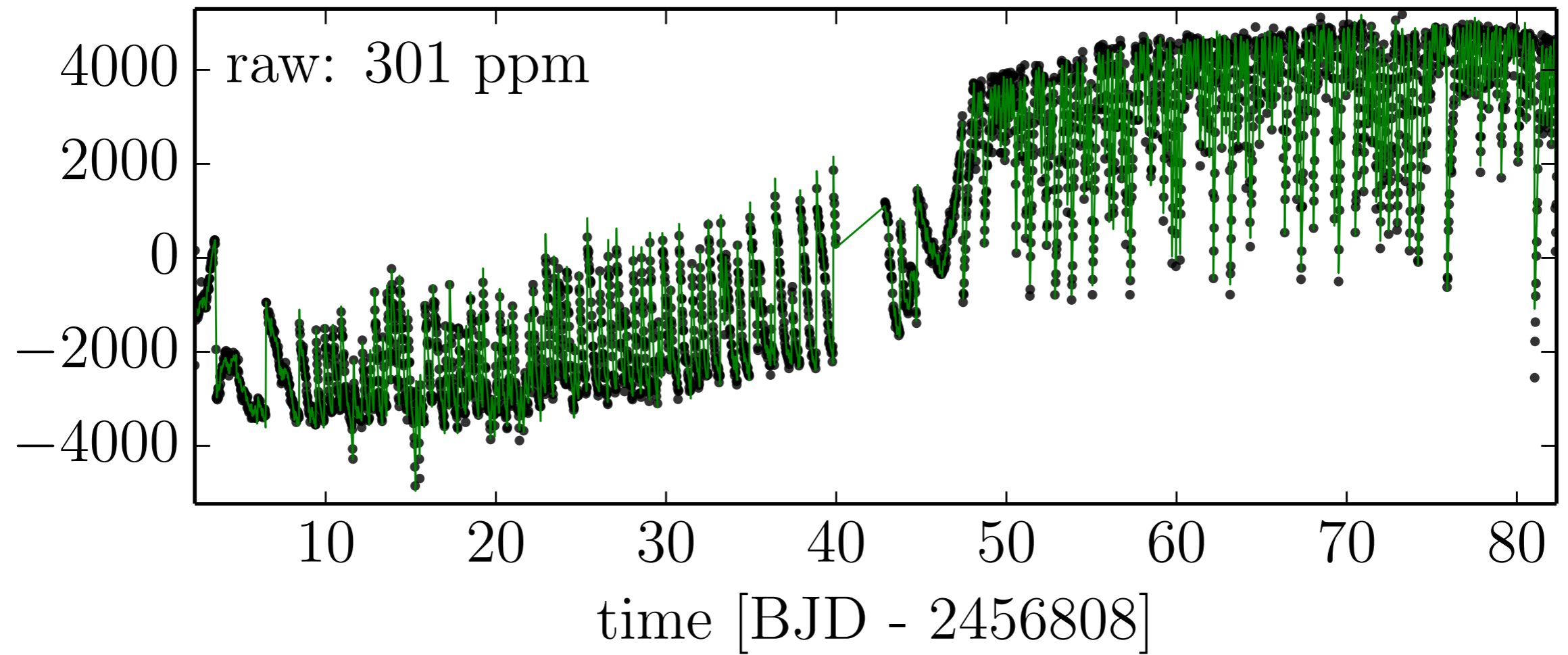
Designing the probabilistic model

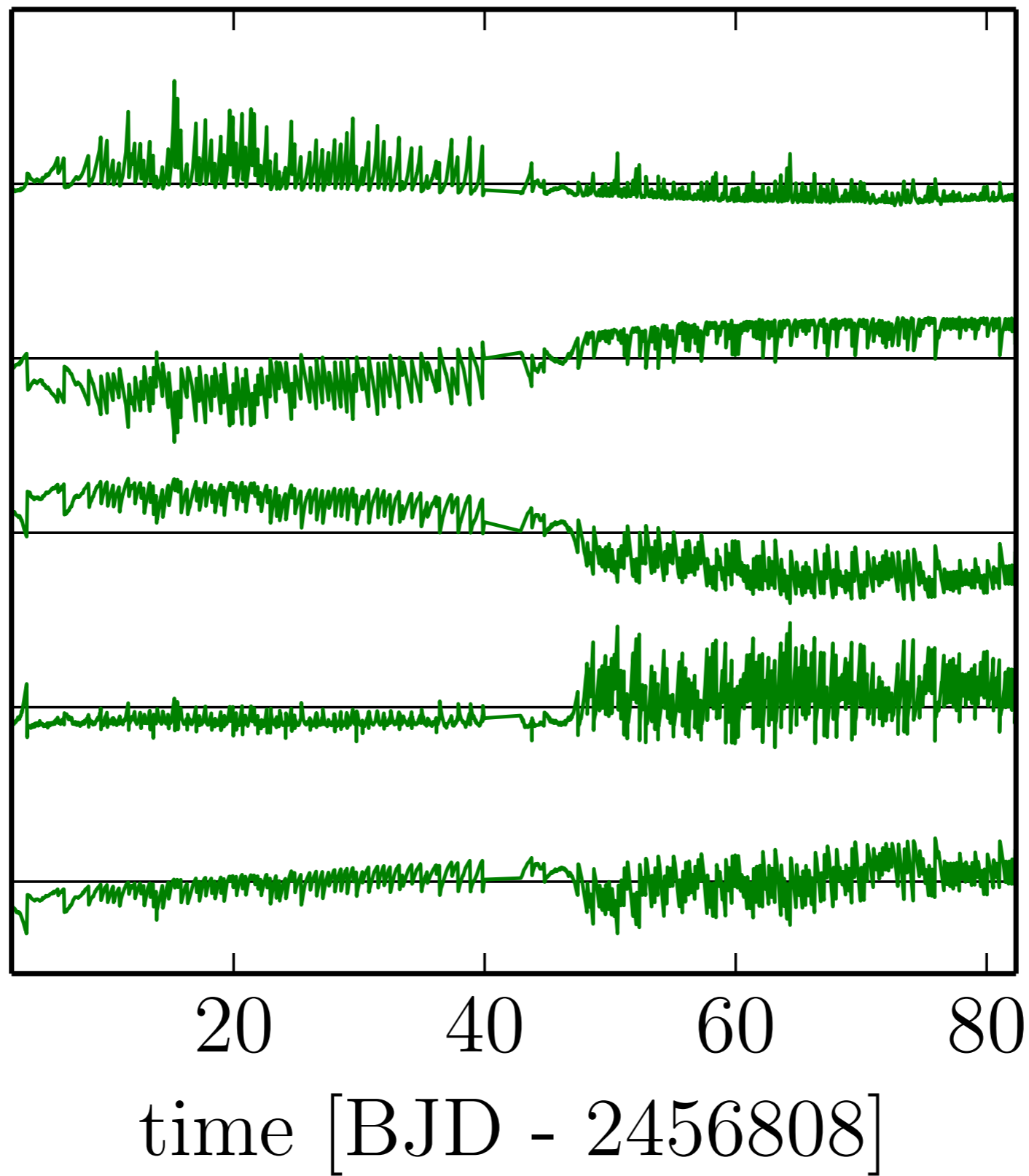


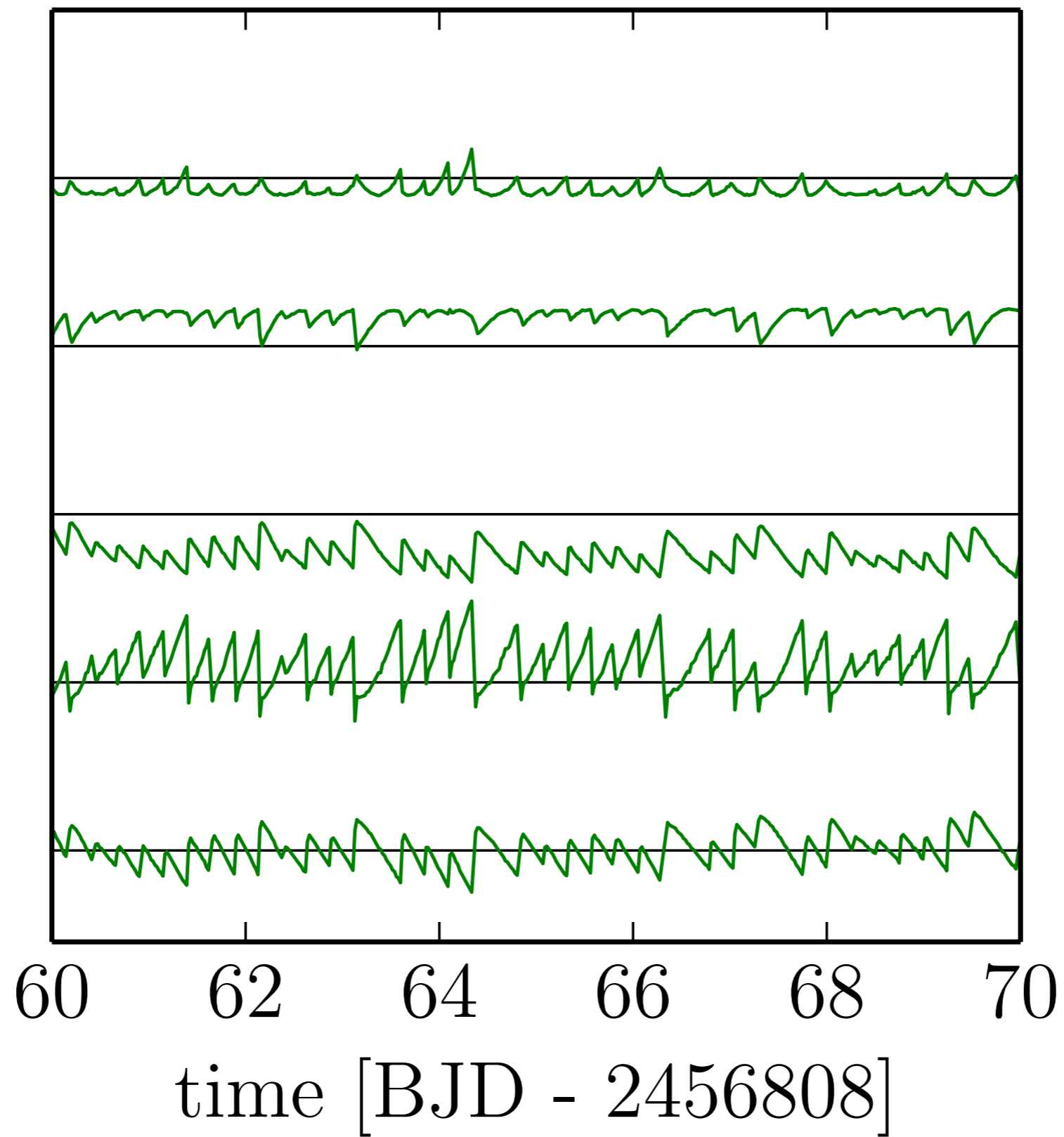
Designing the probabilistic model

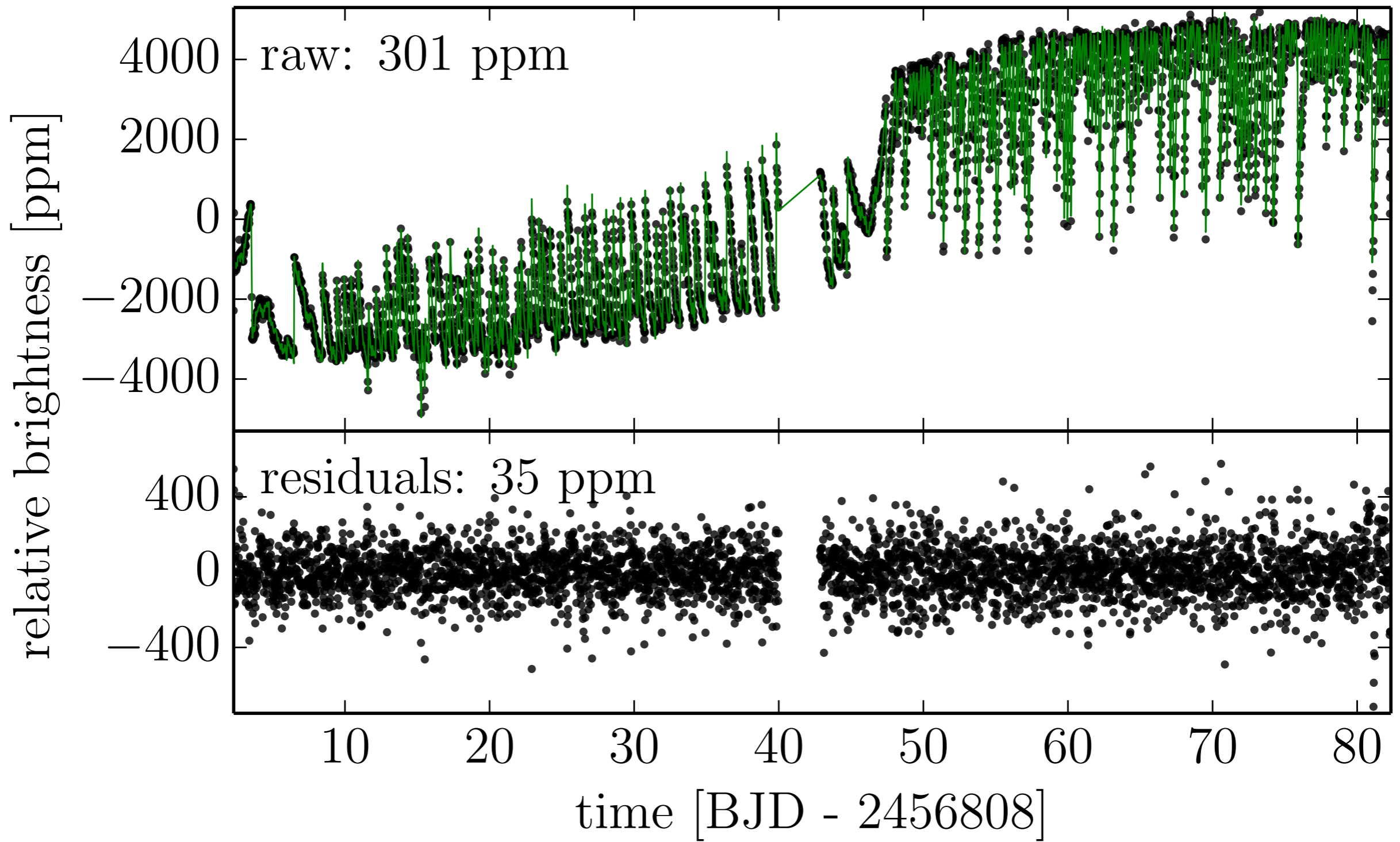
simple space craft assumption:









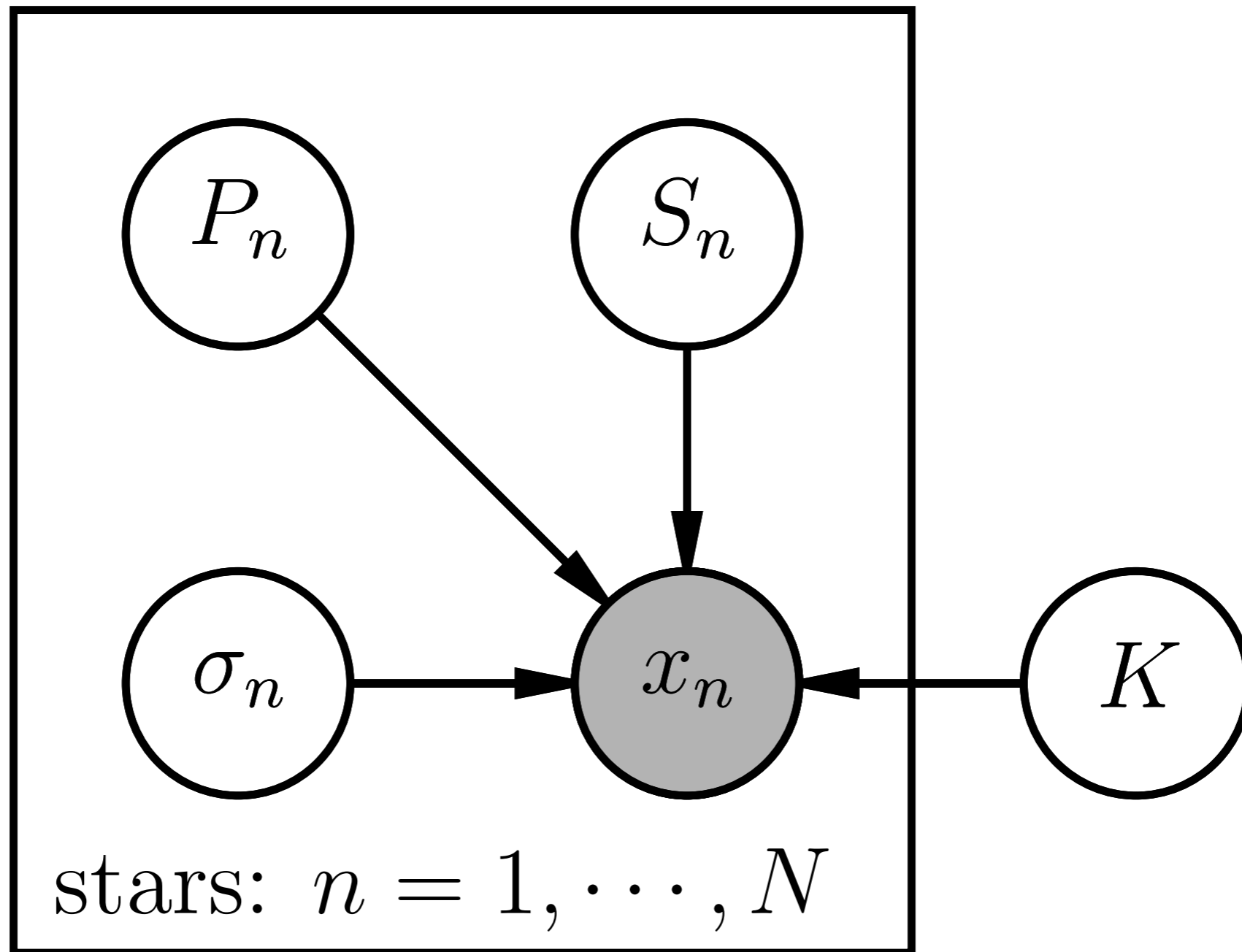


Designing the probabilistic model

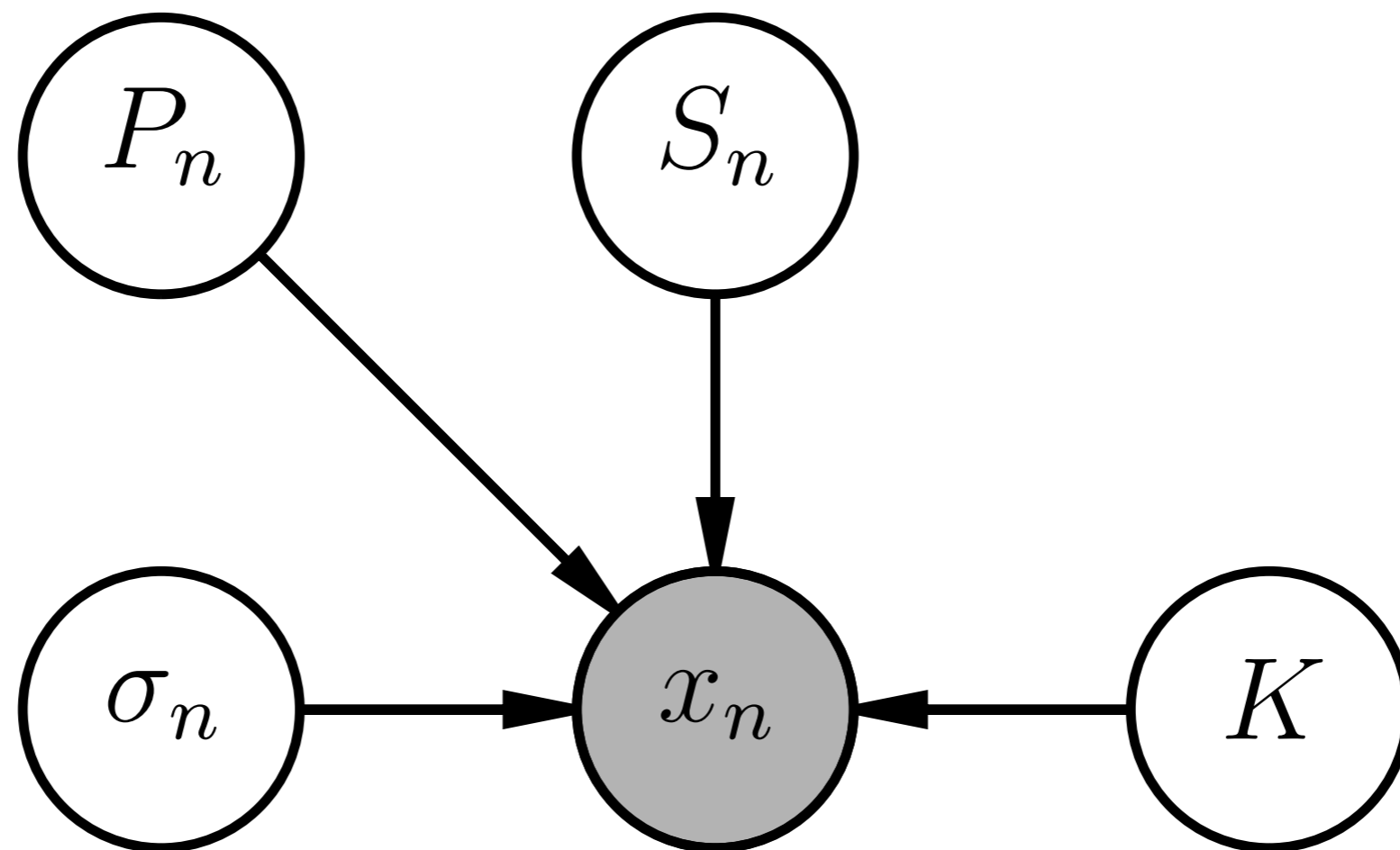
representation:

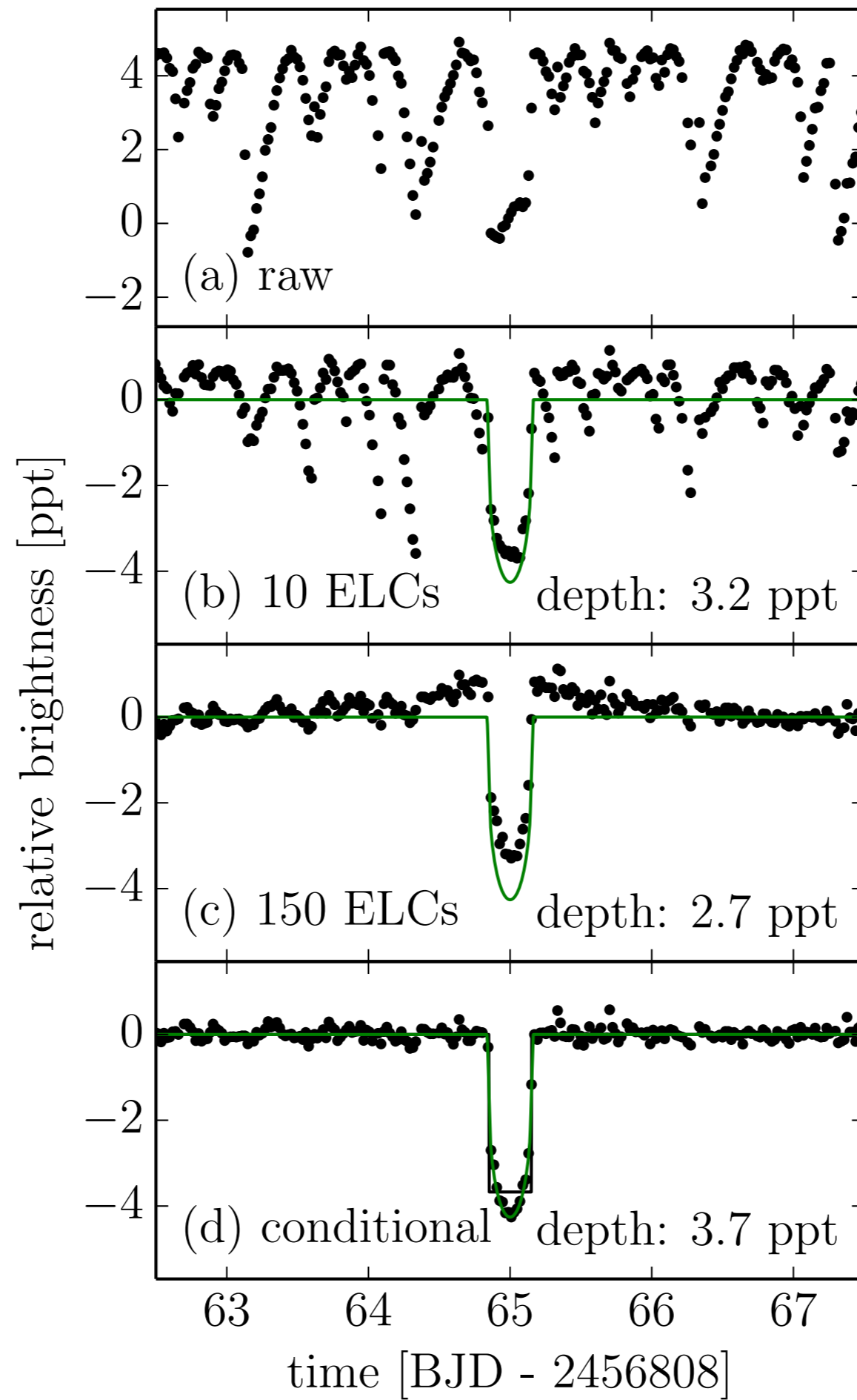
- planet:** physics and geometry
- star:** continuous in time → GP
- noise:** CCD, photon noise → Poisson
- space craft:** data-driven linear model

Designing the probabilistic model



Designing the probabilistic model





Can we find planets using *K2*?

Yes.

K2 Campaign 1 exoplanet discoveries

21,703 stars

80 days of data

36 planet candidates

18 confirmed planets

Published:

Foreman-Mackey, Montet, Hogg, *et al.* (arXiv:1502.04715)

Montet, Morton, Foreman-Mackey, *et al.* (arXiv:1503.07866)

Schölkopf, Hogg, Wang, Foreman-Mackey, *et al.* (arXiv:1505.03036)



KEPLER-452b



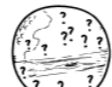
NASA HAS ANNOUNCED THE DISCOVERY OF A (SUPER-)EARTH-SIZED PLANET IN THE HABITABLE ZONE OF A SUN-LIKE STAR.

I SUGGEST WE NAME THIS PLANET "PLUTO" BOTH TO CELEBRATE THE GREAT WORK BY THE NEW HORIZONS TEAM, AND TO MAKE THE STUPID "IS PLUTO A PLANET" DEBATE A LITTLE MORE CONFUSING.

WHILE WE WAIT TO HEAR FROM THE IAU, HERE'S A REVISED AND UPDATED LIST OF PLANET NAME SUGGESTIONS (SEE XKCD.COM/1253)

NEW OR UPDATED ENTRIES IN RED

STAR	PLANET	SUGGESTED NAME
GUESE 667C	b	SPACE PLANET
	c	PILF
	d	A STAR
	e	e'); DROP TABLE PLANETS;--
	f	BLOGOSPHERE
	g	BLOGODROME
	h	EARTH
	TAU CETI	b
c		GIANT DOG PLANET
d		TINY DOG PLANET
e		PHIL PLANET
f		UNICODE SNOWMAN
GLIESE 832		b
	c	WATERWORLD STARRING KEVIN COSTNER
GLIESE 581	b	WAIST-DEEP CATS
	c	PLANET #14
	d	BALLDERAAN
	e	ETERNIA PRIME
	f	TAUPE MARS
	g	JELLY-FILLED PLANET
EPSILON ERIDANI	b	SKYDOT
	c	LASER NOISES
GLIESE 176	b	PANDORA
	c	PANTERA
KEPLER-61	b	GOLDENPALACE.COM
GROOMBRIDGE 31A	b	HOT MESS
KEPLER-442	b	SEAS OF TOOTHPASTE
GLIESE-422	b	THIS ONE WEIRD PLANET
EPIC-201367065	b	SULAWESI
	c	HUGE SOCCER BALL
	d	GEODUDE
	KEPLER-296	b
c		A\$APLANET
d		JURASSIC WORLD
e		THIS LAND
f		SPRINGFIELD
HR 7722	b	BETELGEUSE
	c	BEELEJUICE
EPIC 201912552	b	NETHERLANDS VII
GLIESE 3293	b	ANTISPIT
	c	GOOGLE EARTH
	d	PLANET OF THE APES (DISAMBIGUATION)
KEPLER-283	b	ʃʊəɹənəs
	c	ʃʊ'reinəs
	UPSILON ANDROMEDAE	b
c		STAMPY
d		MOONCHILD
e		HAM SPHERE
HD 20794		b
	c	LEGOLAND
HD 85512	d	PLANET WITH ARMS
	b	LAX MORALITY
HD 40307	b	GOOD PLANET
	c	PROBLEMLAND
	d	GLICKLE
	e	SPARE PARTS
	f	NEW JERSEY VI
	g	HOW DO I JOIN THE IAU
GLIESE 163	b	NEL TYSON'S MUSTACHE
	c	HELP@GMAIL.COM
	d	HAIR-COVERED PLANET
PI MENGAE	b	MOON HOLDER
HD 189733	b	PERMADEATH
KEPLER-22	b	BLUE IVY
KOI-2474	b	STORE-BRAND EARTH
KEPLER-437	b	UNICORN THRESHER
KOI-2418	b	SPHERICAL DISCWORLD
KEPLER-438	b	EMERGENCY BACKUP EARTH
KOI-3010	b	FEEOOOOOOOOOOP
KEPLER-442	b	LIZ
82 ERIDANI	b	HORSEMEAT SURFACE
	c	THE MOON
	d	CONSTANT SAXOPHONES
HD 102365	b	LITTLE BIG PLANET
GLIESE 180	b	DUNE
	c	ARRAKIS
FORMALHAUT	b	SWARM OF BEES
KEPLER-62	b	SPORTY
	c	BABY
	d	SCARY
	e	GINGER
	f	POSH
	HD 69830	b
c		NOVELLA
d		SEXOPLANET
GLIESE 682	b	VERDANT HELLSCAPE
	c	UNSUBSCRIBE
KEPLER-452	b	PLUTO



KEPLER-452b



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KEPLER-438	b	PI
KOI-2418	b	PI
KEPLER-438	b	PI
KOI-3010	b	PI
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KEPLER-452	c	UNSUBSCRIBE
	b	PLUTO



Probabilistic modeling — combining
physical and **data-driven** models — enables
the **discovery of new planets** using **open**
data and **open source software**

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Montet, Morton, Foreman-Mackey, *et al.* (arXiv:1503.07866)

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