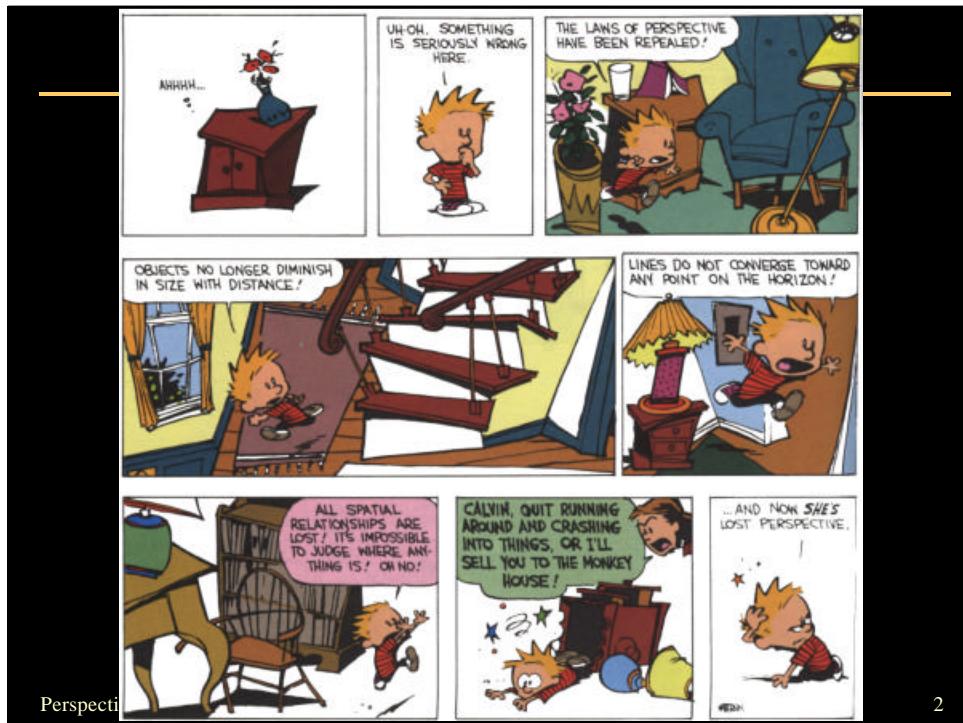


*The Art and Science of Depiction*

# Linear Perspective

Fredo Durand  
MIT- Lab for Computer Science



## *Assignments for Monday 30.*

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- Solso *Cognition and the Visual Arts*
  - Chapter 8 & 9
- Final project
  - Firm subject

## *Plan of the next sessions*

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- Drawing and projection
- Denotation
- Tone & color

## *Plan*

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- Intro to perspective
- History of Renaissance perspective
  - Early attempts
  - Brunelleschi
  - Alberti
  - De la Francesca
  - Leonardo
  - Dürer
- Gadgets
- Distortion issues

Perspective

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## *Perspective*

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- Does linear perspective “occur” in nature
  - E.g. we “experience” foreshortening
- Perspective or perspectives?

Perspective

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## *Pictorial depth cues*

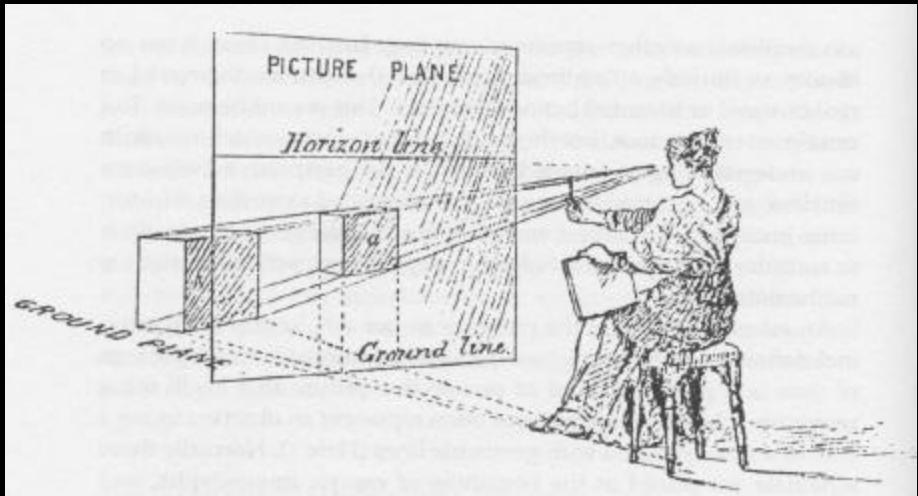
- Occlusion
- Size
- Position relative to the horizon
- Convergence of parallels, linear perspective
- Shading, shadow
- Texture gradient
- Aerial perspective

Perspective

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## *Introduction to Perspective*

- Importance of the single viewpoint

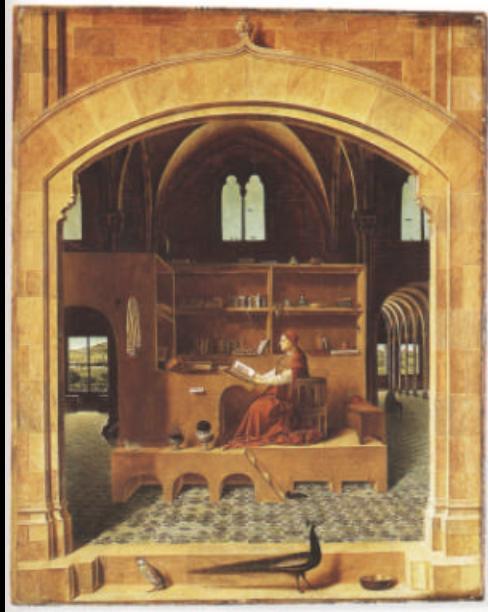


Perspective

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## *Linear Perspective*

- Image as a window
- *St Jerome In His Study*  
Antonello da  
Messina 1475



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Perspective

## *Some accompanying concepts*

- Viewpoint
- Foreshortening
- Vanishing point
- Very linked to architectural spaces

Perspective

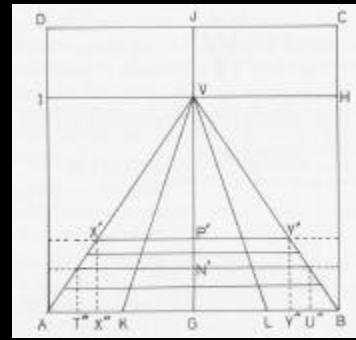
10

## *Primary/secondary geometry*

- Primary geometry
  - Description in 3D object-space
- Secondary geometry
  - Description in 2D image-space



Perspective



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## *Plan*

- Intro to perspective
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Perspective

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## *Early attempts*

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- St John the Baptist Retiring to the Desert  
Giovanni di Paolo 1454



Perspective

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## *Early attempts*

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- Giotto, 1297-1299



Perspective

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## *Early attempts*

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- Lorenzetti 1337-1340



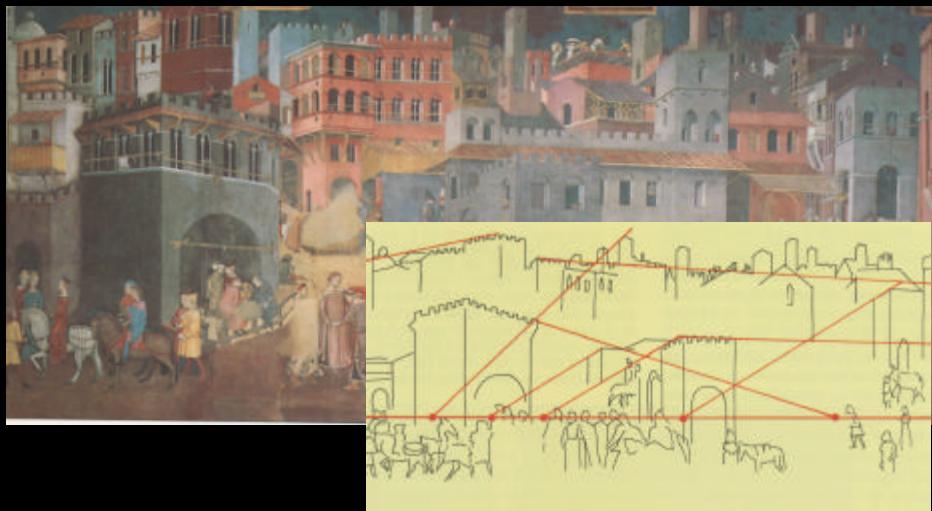
Perspective

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## *Early attempts*

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- Lorenzetti 1337-1340



Perspective

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## *Giotto's rules*

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- Lines and planes above eye level incline downwards when they move away
- Below eye level upwards when they move away
- Lines to the left incline inwards to the right

Perspective

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## *Giotto*

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- Confirmation of the Rule of St Francis 1325

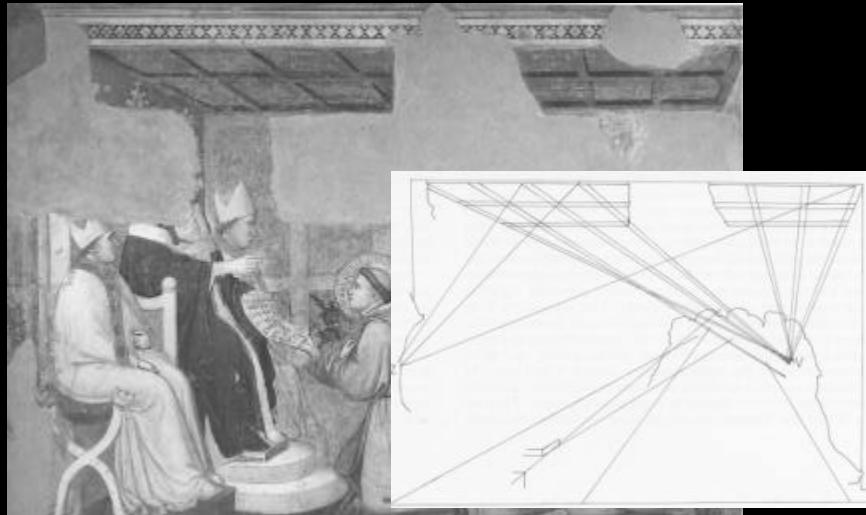


Perspective

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## *Giotto*

- Confirmation of the Rule of St Francis 1325



Perspective

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## *Early attempts*

- Pietro Lorenzetti,  
*Birth of the  
Virgin*  
1342



Perspective

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## *Plan*

---

- Intro to perspective
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- Distortion issues

## *Brunelleschi's experiments, 1413*

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- Existing buildings
- Measurement, surveying
- Single viewpoint
- First scientific mimesis

## *Brunelleschi's experiment, 1413*



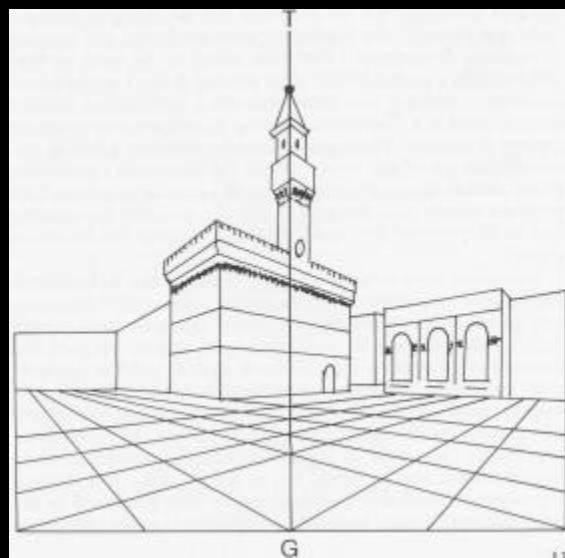
Perspective



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## *Brunelleschi's second experiment*

- Cut out
- Note that this is 2-point perspective



Perspective

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## *Limitations*

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- Existing buildings
- Requires measurement

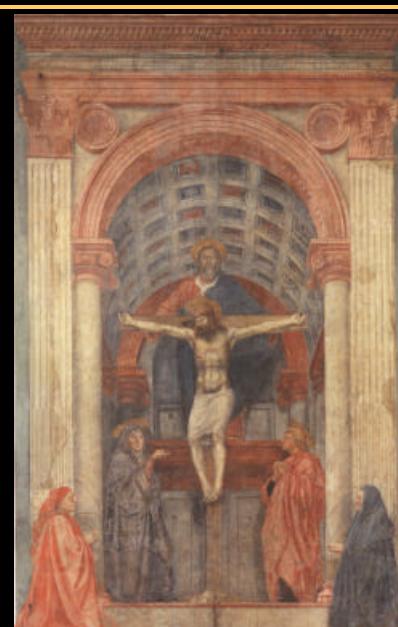
Perspective

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## *Masaccio, The Trinity, 1427*

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- The oldest perspective painting
- Probably measurement
- Maybe helped by Brunelleschi



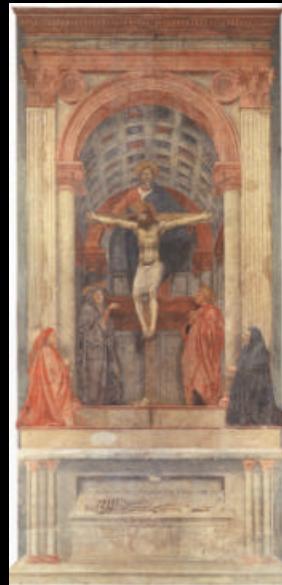
Perspective

## *Masaccio, The Trinity, 1427*

- The oldest perspective painting
  - Santa Maria Novella (Florence)



Perspective



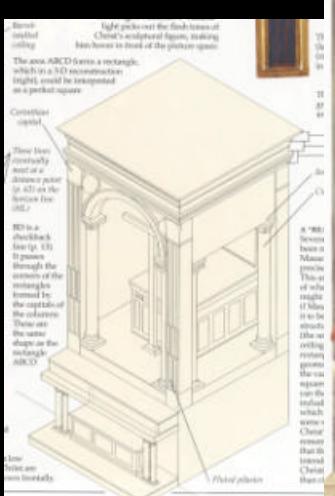
27

## *Masaccio, The Trinity, 1427*

- The oldest perspective painting



Perspective



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## *Plan*

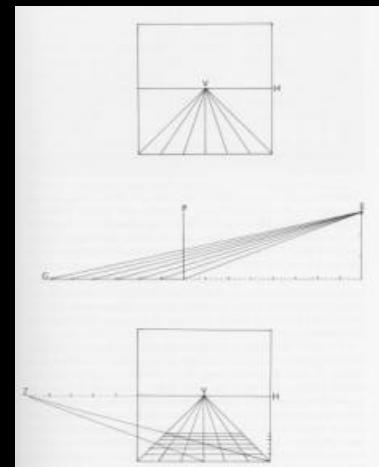
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Perspective

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## *Leon Battista Alberti, On Painting*

- 1435
- Intersections of pyramids with image surface
- Proportional triangles
- Use side view for foreshortening
- Check with diagonal
- Use pavement as reference
- Center = prince of rays



Perspective

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## Leon Battista Alberti, On Painting

- Paolo Uccello, *The Selling of the Host*, 1468



Perspective

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## Legitimate construction

- Carlo Criveli  
*Annunciation* 1486



Perspective

## *Plan*

---

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- Gadgets
- Distortion issues

Perspective

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## *Piero de la Francesca*

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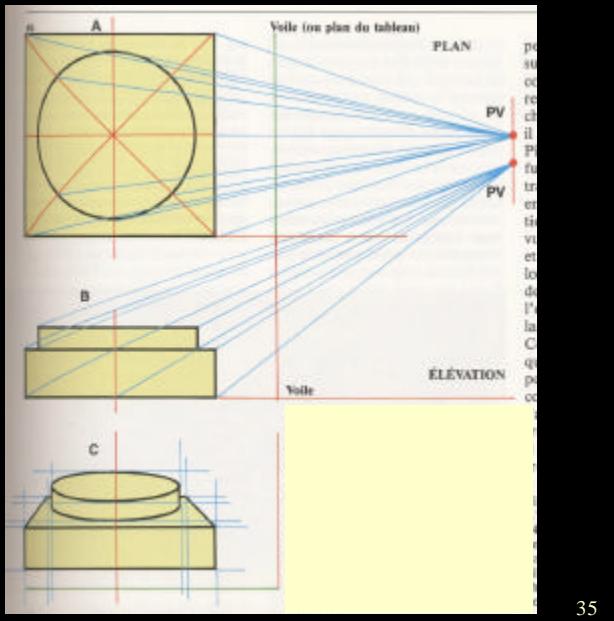
- *De Prospectiva Pingendi*, 1474  
(On the perspective of painting)
- Ratios of distance and size
- Use plan and elevation view

Perspective

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## Piero de la Francesca

- Use plan and elevation view



Perspective

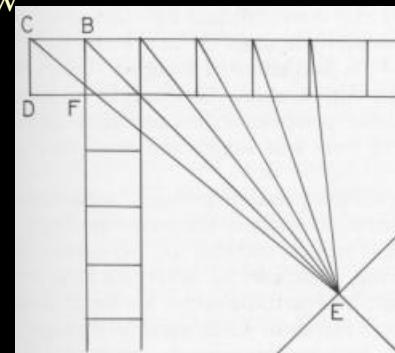
35

## Piero de la Francesca

- *De Prospectiva Pingendi*, 1474  
(On the perspective of painting)
- Ratios of distance and size
- Use plan and elevation view
- Deformation of square
  - Angle of view less than 90°

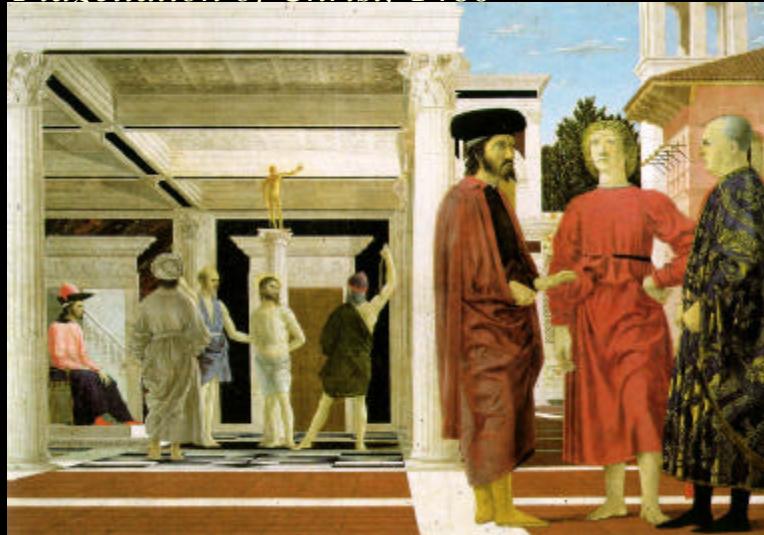
Perspective

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## *Piero de la Francesca*

- *Flagellation of Christ*, 1460



Perspective

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## *Piero de la Francesca*

- Invention of the true cross 1452-59
- “wrong perspective on the left”



Perspective

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## *Piero de la Francesca*

---

- Invention of the true cross 1452-59
- “wrong perspective on the left



Perspective

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## *Plan*

---

- Intro to perspective
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  - Dürer
- Gadgets
- Distortion issues

Perspective

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## *Leonardo & perspective*

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- Techniques of artists' perspective in theory and practice
- Geometry of visual rays
- Devices and instruments
- Optics and the eye
- Curiosities of vision (e.g. anamorphosis)
- Apparent contradictions

Perspective

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## *Leonardo*

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- *Last Supper*, 1497



Perspective

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## *Leonardo*

- *Last Supper*, 1497

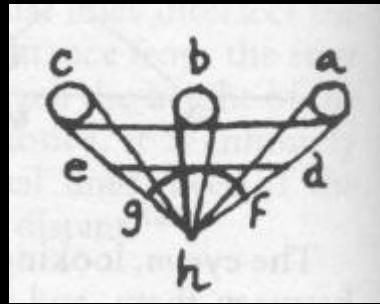
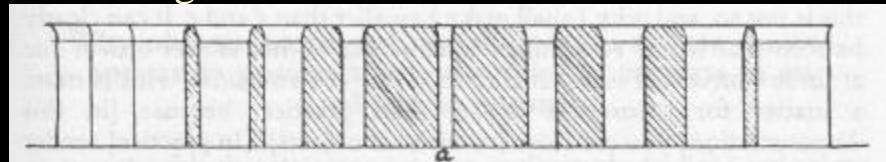


Perspective

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## *Leonardo & contradictions*

- Wide angle vision

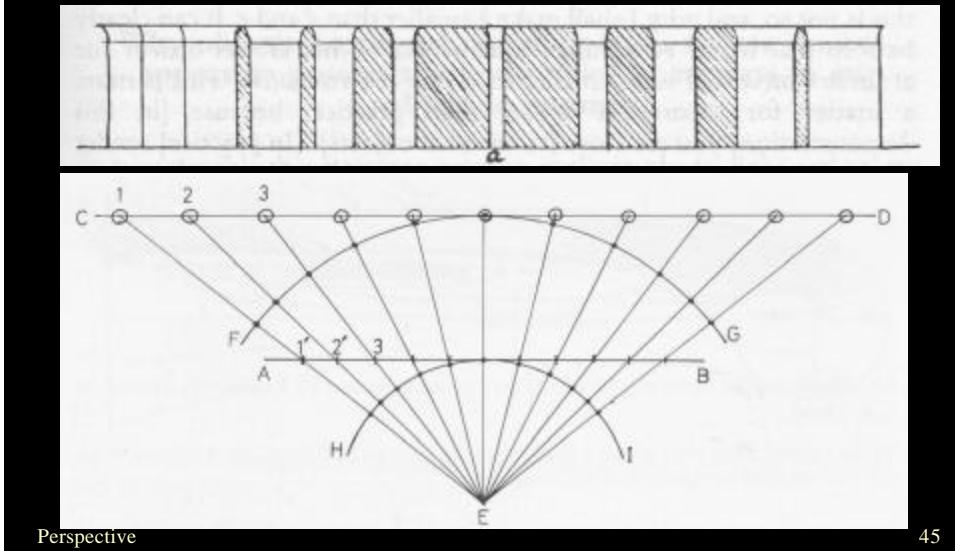


Perspective

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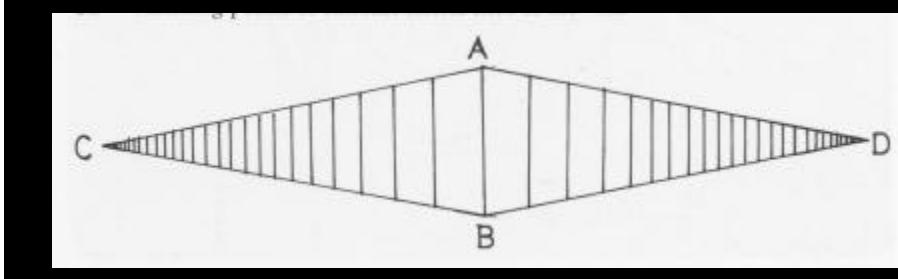
## *Leonardo & contradictions*

- Wide angle vision



## *Leonardo & contradictions*

- Wide angle vision
- Lateral recession



Perspective

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## *Plan*

---

- Intro to perspective
- History of Renaissance perspective
  - Early attempts
  - Brunelleschi
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  - De la Francesca
  - Leonardo
  - Dürer
- Gadgets
- Distortion issues

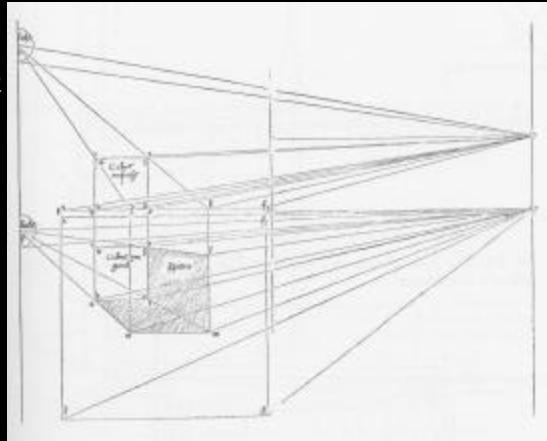
Perspective

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## *Dürer*

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- Traveled to Italy
- Mainly influenced by de la Francesca
- *Instruction in Measurement with Compass and Ruler in Lines, Planes and Solid Bodies*, 1525



Perspective

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## Dürer

- *St Jerome in his Study* 1514
- Very off-center
- Note the verticals



Perspective

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## Dürer

- The artist's glass



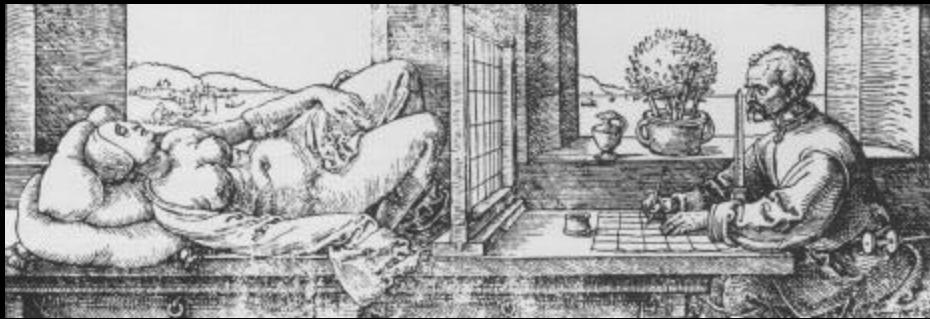
Perspective

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## *Dürer*

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- The draftsman's net



Perspective

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## *Dürer*

---

- Jacob de Keyser's invention



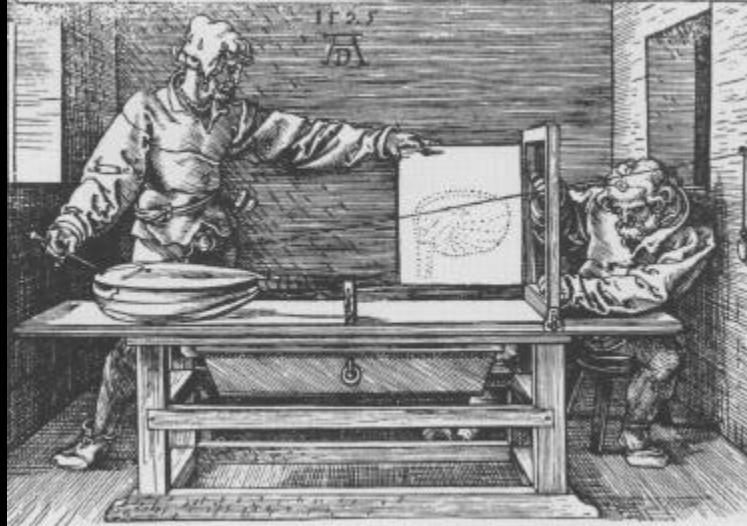
Perspective

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## *Dürer*

---

- Dürer's device



Perspective

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## *Conclusions about Renaissance*

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- Different techniques, refinement
- Measurement
- Mainly central perspective
- No notion of infinity, no vanishing point
- Spiritual notion of mathematical harmony

Perspective

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## After Renaissance

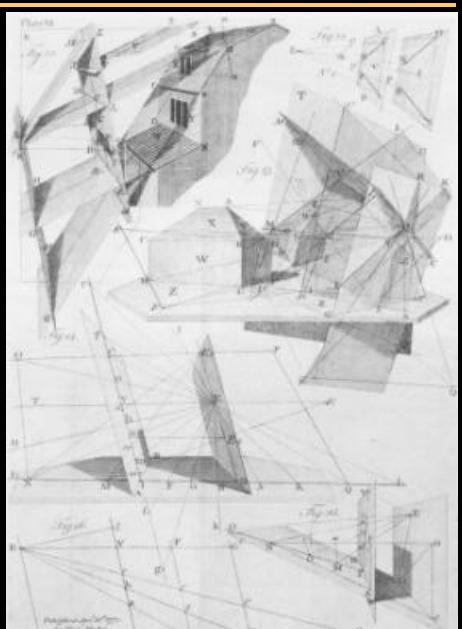
- 17<sup>th</sup>
  - Vanishing point
  - Abstraction
  - Desargues, Descartes
- Flourished until 19<sup>th</sup>
- 20<sup>th</sup> century
  - Come-back for computer graphics and computer vision

Perspective

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## After Renaissance

- Thomas Malton  
*A Complete Treatise on Perspective, 1779*



Perspective

## *Plan*

---

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- Distortion issues

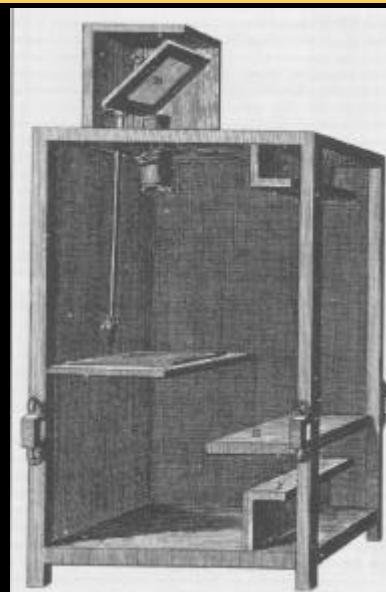
Perspective

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## *Gadgets*

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- Camera obscura



Perspective

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## Vermeer 1660

- Camera obscura



Perspective

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## Gadgets

- Baldassare Lanci's universal instrument for surveying and perspective 1557

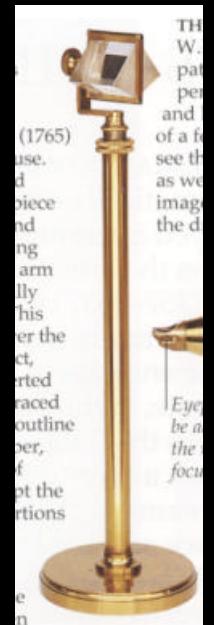
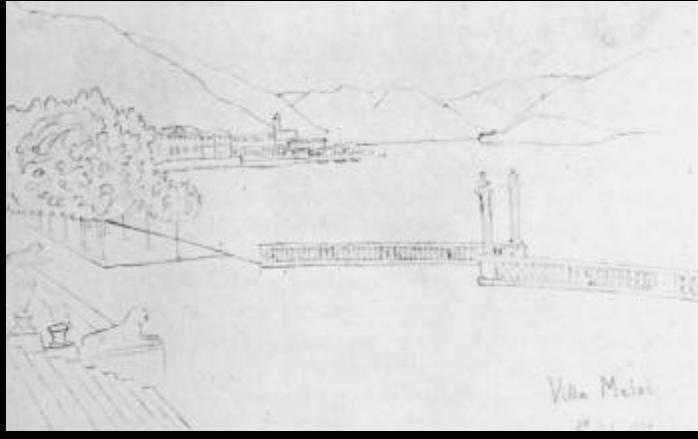


Perspective

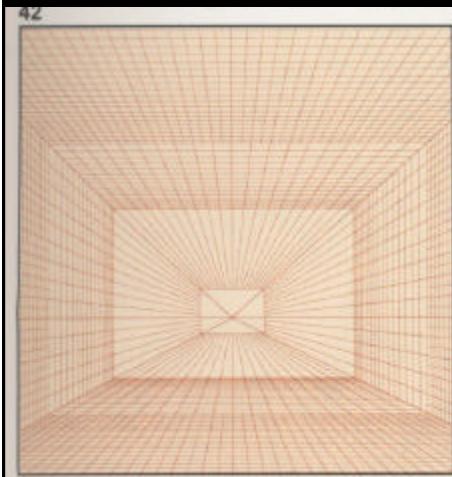
60

## Gadgets

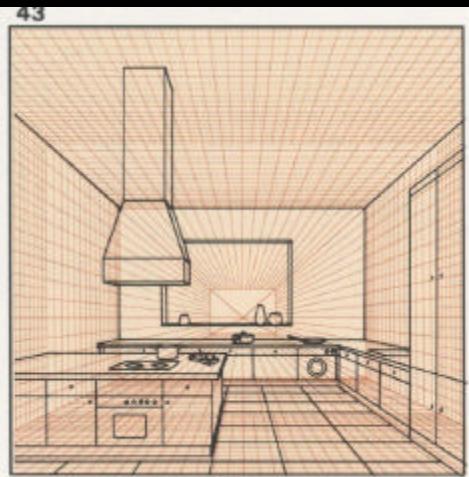
- Camera Lucida
- E.g. Talbot



## Perspective grids



Perspective



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## *Plan*

---

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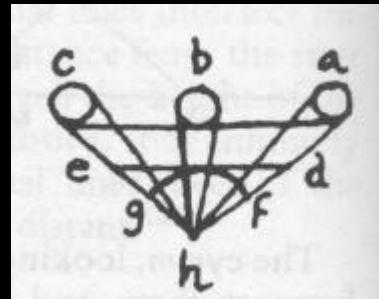
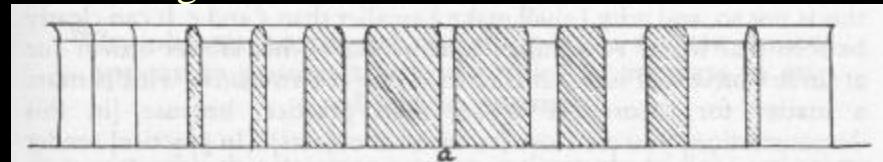
Perspective

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## *Leonardo & contradictions*

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- Wide angle vision

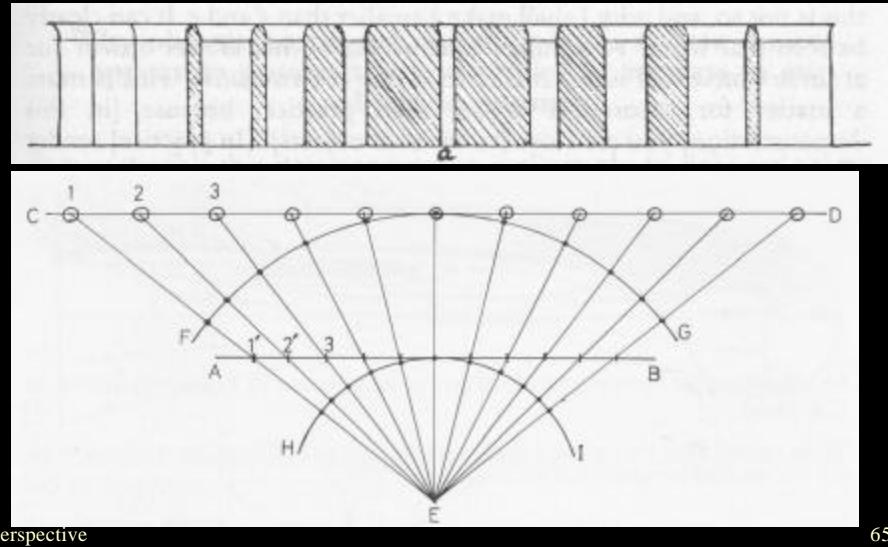


Perspective

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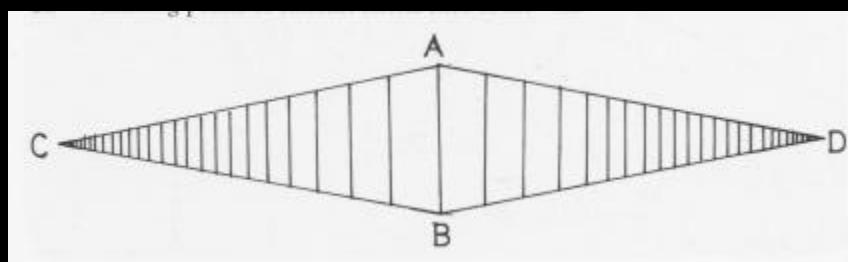
## *Leonardo & contradictions*

- Wide angle vision



## *Leonardo & contradictions*

- Wide angle vision
- Lateral recession



Perspective

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## *Perspective distortion*

- The sphere is projected as an ellipse



Perspective

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## *Perspective distortion*

- The sphere is projected as an ellipse



Perspective

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