

## Exercise 12

*Lecturer: Mohsen Ghaffari**Teaching Assistant: Sebastian Brandt***1 Lower Bound for the  $k$ -Server Problem**

Argue that every online deterministic algorithm for the  $k$ -server problem has competitive ratio at least  $k$ .

**2 Extending Double Coverage to Trees**

Prove that the natural extension of the double coverage algorithm to trees gives a  $k$ -competitive online algorithm for the  $k$ -server problem.

**3 Lower Bounds for Online Bipartite Matching**

Argue that no deterministic online bipartite matching algorithm can achieve a competitive ratio better than  $1/2$ .