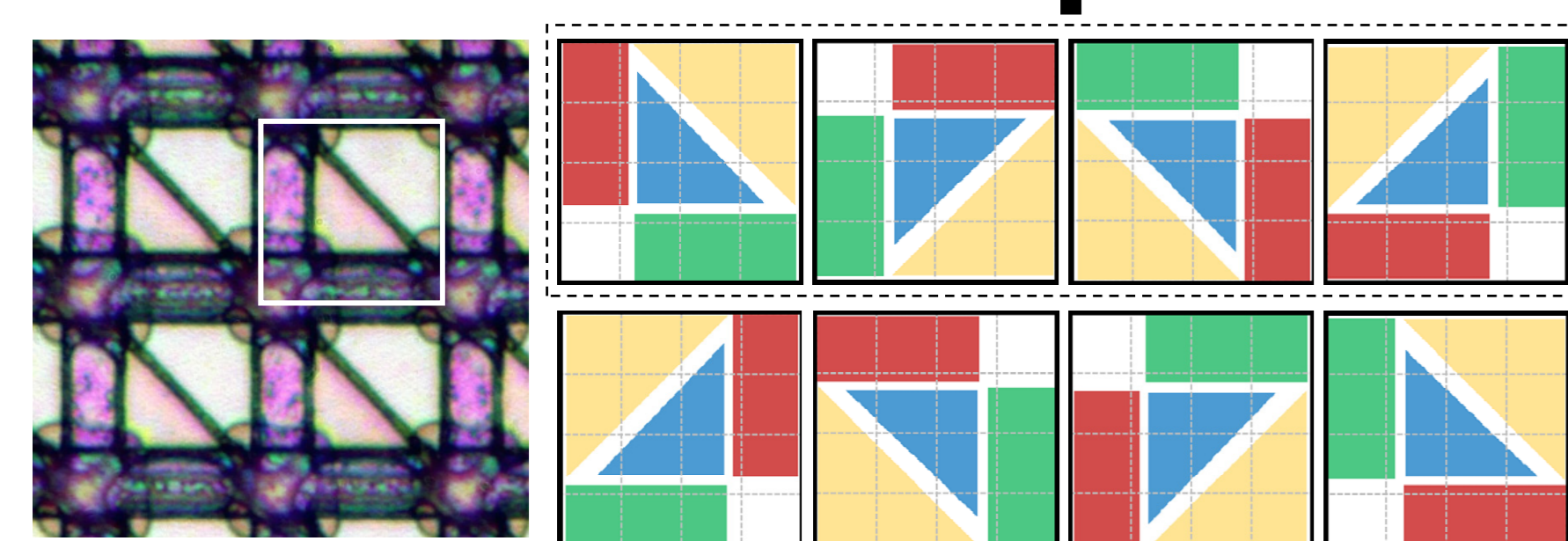
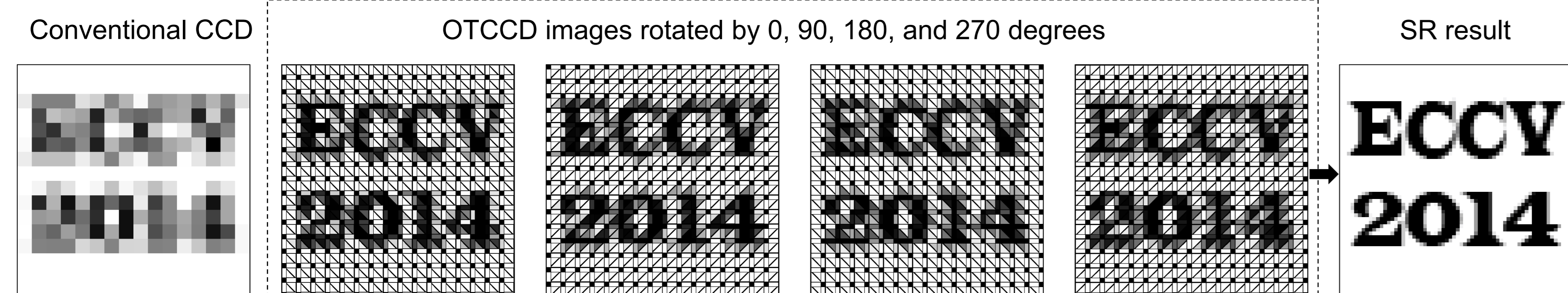


# Sub-Pixel Layout for Super-Resolution with Images in the Octic Group

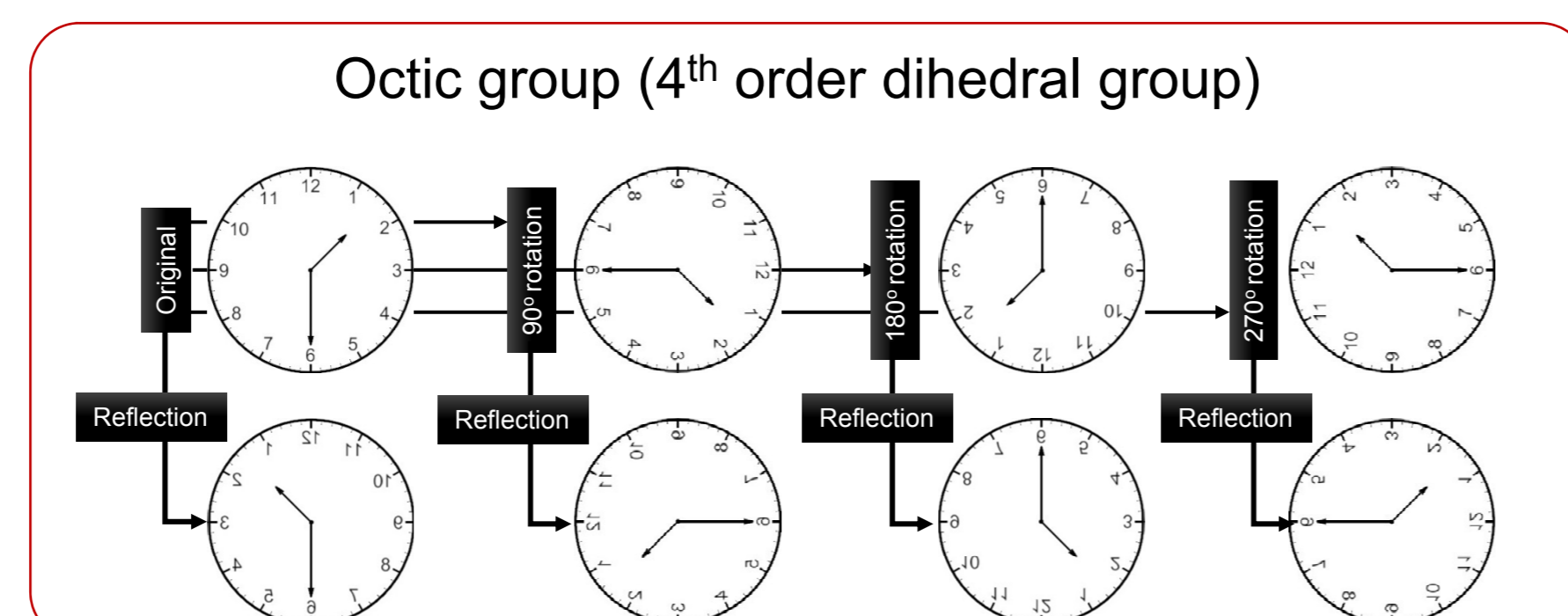
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## Idea illustration



An OTCCD pixel (with 4 sub-pixels) in the octic group



This paper presents a novel super-resolution framework by exploring the properties of non-conventional pixel layouts and shapes. We show that recording multiple images, transformed in the octic group, with a sensor of asymmetric sub-pixel layout increases the spatial sampling compared to a conventional sensor with a rectilinear grid of pixels and hence increases the image resolution. The example above shows OTCCD (Orthogonal-Transfer CCD, MIT Lincoln Lab) images under 4 rotations can perform 4x Super-Resolution (SR).

## Contributions

- o A **novel view** to the SR problem by using an asymmetric sub-pixel layout to form multiple images in the octic group
- o The **theoretical bound** of SR performance w.r.t. the number and distribution of sub-pixels
- o A **sub-pixel layout selection** algorithm to choose good layouts for well-posed SR
- o A simple yet effective **SR reconstruction** algorithm

## Key proposition

Given a group of pixels with  $t$  poses in the octic group  $\mathcal{G}$  with each pixel containing  $r$  sub-pixels, for a designated magnification factor  $\mathcal{M}$ ,  $\text{rank}(\mathbf{P}^T)$  is bounded as

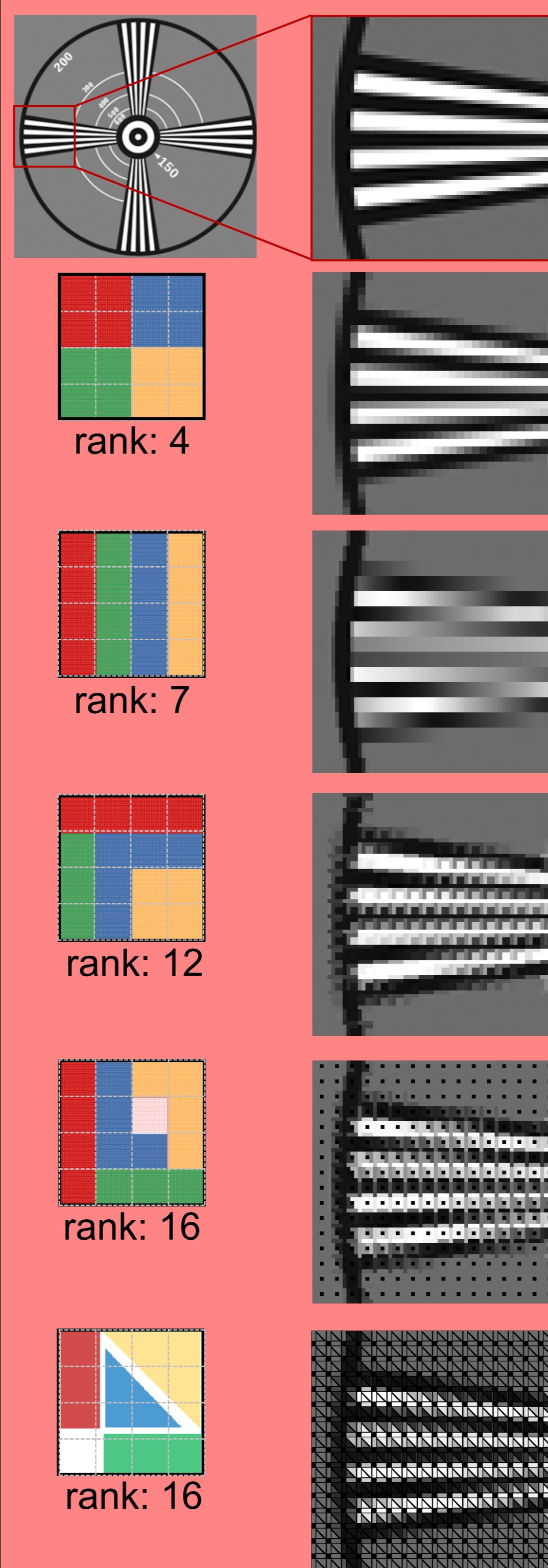
$$\text{rank}(\mathbf{P}^T) \leq \min(\mathcal{M}^2, t(r - 1) + 1)$$

$\text{rank}(\mathbf{P}^T)$  is determined by number and distribution of sub-pixels; It evaluates the well-posedness of SR reconstruction.

## Potential hardware

OTCCD + Dove prism + rotation mount

## Result



Simulated images with various sub-pixel layouts for 4x SR.

**4x SR Result**  
OTCCD layout  
GT | LR | SR

**8x SR Result**  
LR | SR

Note how higher-rank layouts increase the resolution.

Ground truth

Sub-pixel layouts for 8x SR.

rank: 64

4x SR needs 4 images rotated by 90°; 8x SR needs all 8 images in the octic group.

SR results varying with sub-pixel layouts

All full-rank sub-pixel layouts achieve SR reconstruction with designated magnification.

Image observed with a conventional sensor with a rectilinear grid of pixels

This is the gap among sub-pixels (treat as a dumb pixel). It also contributes to SR.

## Real-simulation result for 4x (left) and 8x (right) SR



**Take-home message:** "Rotation-asymmetric sub-pixel layout + rotated images" play an important role in increasing spatial sampling to break the limit of reconstruction-based super-resolution.