

# Diffuse Reflectance Imaging with Astronomical Applications

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## Indirect Imaging with Diffuse Reflection

**Diffuse surfaces** generally blur together incident lighting from many directions

- To what extent can we use **diffuse objects** as “cameras”?
- How much **resolution** can we hope to achieve?



**Goal:** Recover detailed incident illumination (or surface albedo) using photos measuring the reflectance of a diffuse object.

## Theory of Reflection and its Inversion

Single-bounce light transport

$$B(\mathbf{p}, \vec{\omega}_o) = \int_{\Omega} \underbrace{\alpha(\mathbf{p})}_{\text{reflected radiance}} \underbrace{L(\mathbf{p}, \vec{\omega}_i)}_{\text{surface albedo}} \underbrace{\rho(\vec{\omega}_i, \vec{\omega}_o)}_{\text{incoming radiance}} \underbrace{V(\mathbf{p}, \vec{\omega}_i)}_{\text{BRDF}} \underbrace{\max(\vec{\omega}_i \cdot \vec{n}, 0)}_{\text{visibility}} \underbrace{d\vec{\omega}_i}_{\text{clipped cosine}}$$

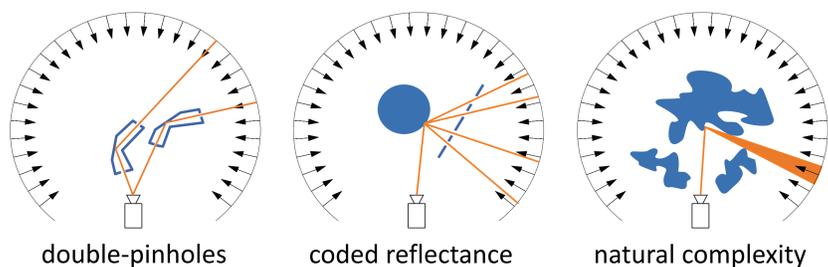
Matrix formulation

$$p(\mathbf{y}|\mathbf{x}) = \mathcal{N}(\mathbf{Ax}, \eta^2\mathbf{I})$$

observed pixels    transfer matrix    distant lighting    noise

- Reflectance  $\approx$  spherical convolution of lighting and BRDF
- Images of convex Lambertian objects with distant lighting lie in a  $\sim 9\text{D}$  subspace [Basri and Jacobs, 2003] [Ramamoorthi and Hanrahan, 2001]

## Key: Occlusion Geometry for Illumination Coding



“Sculpture design” for inverse rendering

- Occlusion creates high frequencies, improves conditioning
- In the extreme, scene geometry isolates individual rays

## Bayesian Reconstruction Method

Standard MAP estimation

- Gaussian prior [Wiener 1949]

$$p(\mathbf{x}) = \mathcal{N}(\mathbf{0}, \Sigma_{\mathbf{x}})$$

$$p(\mathbf{x}|\mathbf{y}) = \mathcal{N}(\Sigma(\frac{1}{\eta^2}\mathbf{A}^T\mathbf{y}), \Sigma)$$

$$\Sigma = (\Sigma_{\mathbf{x}}^{-1} + \frac{1}{\eta^2}\mathbf{A}^T\mathbf{A})^{-1}$$

- Sparse derivative prior [Levin et al. 2007]

$$g(z) = |z|^{0.8}$$

Reconstructing the stable component of **time-varying lighting**

- Marginalize out temporal variations

$$p(\mathbf{y}|\mathbf{x}, \mathbf{t}_1, \dots, \mathbf{t}_D) = \mathcal{N}\left(\begin{bmatrix} \mathbf{A}_1(\mathbf{x} + \mathbf{t}_1) \\ \vdots \\ \mathbf{A}_D(\mathbf{x} + \mathbf{t}_D) \end{bmatrix}, \eta^2\mathbf{I}\right)$$

temporal binning with Gaussian prior

$$p(\mathbf{y}|\mathbf{x}) = \mathcal{N}\left(\begin{bmatrix} \mathbf{A}_1 \\ \vdots \\ \mathbf{A}_D \end{bmatrix} \mathbf{x}, \begin{bmatrix} \mathbf{A}_1 \Sigma_{\mathbf{t}} \mathbf{A}_1^T & & 0 \\ & \ddots & \\ 0 & & \mathbf{A}_D \Sigma_{\mathbf{t}} \mathbf{A}_D^T \end{bmatrix} + \eta^2\mathbf{I}\right)$$

temporal variations as correlated noise

## (1) Rim Reflectance Imaging

Exploit visibility differences very close to **occlusion boundary**

- Single shot** is enough
- Requires high resolution, compact lighting
- Novel approach (to our knowledge)

## (2) Time-Varying Imaging

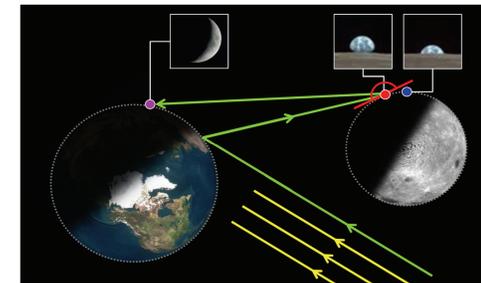
Exploit variation over time in the occlusion geometry

- Single pixel** is enough
- Requires many shots, natural variation
- Classical astronomy (“light curves”)

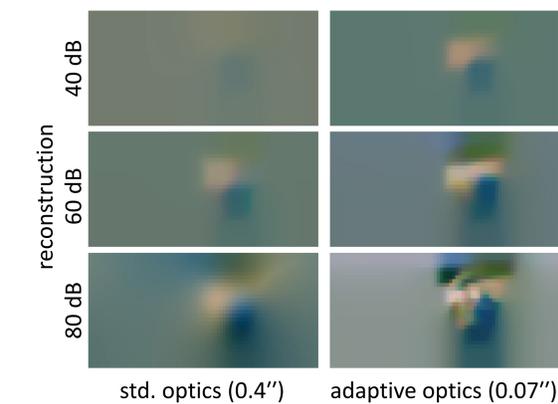
## Moon as a Mirror - Feasibility Study

Observing Earth via its reflection in the moon

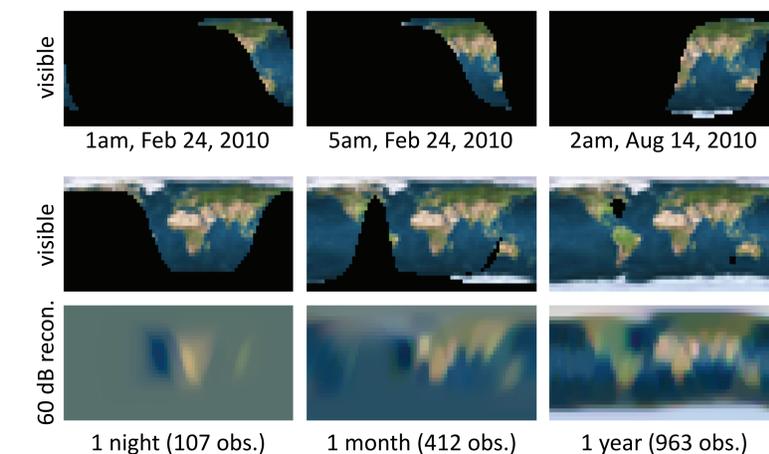
- BBSO **earthshine** project measures albedo over time [Qiu et al. 2003] [Pallé et al. 2003]
- Can we resolve more than a single pixel?



### Simulation: Rim reflectance imaging



### Simulation: Time-varying imaging



### Simulation: Time-varying imaging with clouds



## Martian Surface from Single-Pixel Data

**Real data:** 234 historical photometry measurements [Irvine et al. 1968ab]

