

MASSACHUSETTS INSTITUTE OF TECHNOLOGY  
Department of Electrical Engineering and Computer Science  
6.001—Structure and Interpretation of Computer Programs  
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**Recitation 16 — 4/12/2006**  
**More Environment Diagrams**

## Repeat of Rules: Eval

- *name* - Look up *name* in the current environment, if found return value, otherwise lookup in enclosing (parent) environment.
- `(lambda (params) body)` - Create double bubble with code ptr to *params* and *body* and env ptr to current environment.
- `(define name value)` - Evaluate *value* and then create/replace binding for *name* with the result.
- `(set! name value)` - Evaluate *value* and then replace the first binding for *name* in the chain of environments, starting with the current env.
- `(proc args ... )` - Evaluate *proc* and *args* in the current environment, then apply.
- Otherwise – Follow the correct rule (numbers, if, cond, begin, quote, etc.)

## Repeat of Rules: Apply

- Step 1 - Drop a new frame
- Step 2 - Link frame pointer of new frame to environment pointed to by env pointer of double bubble being applied.
- Step 3 - Bind params of double bubble in the new frame.
- Step 4 - Eval the *body* in the new frame.

### Three Counter Attempts

```
1. (define make-count-proc-1
    (lambda (f)
      (lambda (x)
        (let ((count 0))
          (cond ((eq? x 'count) count)
                (else
                 (set! count (+ count 1))
                 (f x)))))))
```

```
(define sqrt-c-1
  (make-count-proc-1 sqrt))
```

```
(sqrt-c-1 4)
(sqrt-c-1 'count)
```

This counter won't work: Each time `sqrt` is called within `make-count-proc-1` the counter value `count` will be reset to 0. So passing the message `'count` will always return 0 regardless of how many times `sqrt-c-1` has been called.

```
2. (define make-count-proc-2
    (lambda (f)
      (let ((count 0))
        (lambda (x)
          (cond ((eq? x 'count) count)
                (else
                 (set! count (+ count 1))
                 (f x))))))))
```

```
(define sqrt-c-2
  (make-count-proc-2 sqrt))
(define sqr-c-2
  (make-count-proc-2 square))
```

```
(sqrt-c-2 4) ==> 2
(sqrt-c-2 'count) ==> 1
```

```
(sqr-c-2 4) ==> 16
(sqr-c-2 'count) ==> 1
```

This version will result in independent counters for `sqrt-c-2` and `sqr-c-2`. Each time `make-count-proc-2` is applied.

```
3. (define make-count-proc-3
    (let ((count 0))
      (lambda (f)
        (lambda (x)
          (cond ((eq? x 'count) count)
                (else
                 (set! count (+ count 1))
                 (f x)))))))

(define sqrt-c-3
  (make-count-proc-3 sqrt))
(define sqr-c-3
  (make-count-proc-3 square))

(sqrt-c-3 4) ==> 2
(sqrt-c-3 'count) ==> 1

(sqr-c-3 4) ==> 16
(sqr-c-3 'count) ==> 2
```

In this version, there is only a single counter for any procedure that's been composed with `make-count-proc-3`. The `'count` message now returns the total number of times that either `sqrt-c-3` or `sqr-c-3` has been applied to a number.

4. The procedure `last-pair` returns the last pair of a list (guaranteed to have `'()` in the `cdr`).

```
(define (list-inserters lst)
  (let ((last (last-pair lst)))
    (list (lambda (x)
            (set-cdr! lst (cons x (cdr lst)))
            lst)
          (lambda (y)
            (set-cdr! last (cons y '()))
            (set! last (cdr last))
            lst))))
```

```
(define the-list (list 1 3 4))
```

```
(let ((ins (list-inserters the-list)))
  ((list-ref ins 0) 2)
  ((list-ref ins 1) 5))
```

Finish the environment diagram.

