

# AREA COVERAGE PLANNING THAT ACCOUNTS FOR POSE UNCERTAINTY WITH AN AUV SEABED SURVEYING APPLICATION

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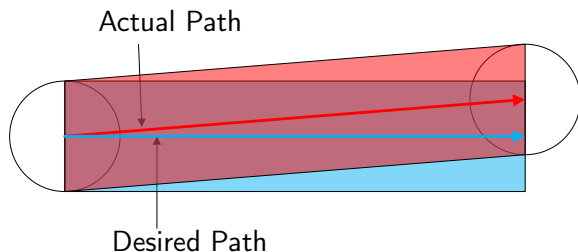
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<sup>2</sup>Defense R&D Canada - Atlantic

<sup>3</sup>COBRA Lab, University of New Brunswick

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# OVERVIEW



- (Most) Coverage literature assumes robot state known <sup>1</sup>

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<sup>1</sup>Examples that don't include Das et al. IROS 2011, Bosse et al ICRA 2007, and others

# MOTIVATION

## 1 PROBABILISTIC COVERAGE FRAMEWORK

# OUTLINE

- 1** PROBABILISTIC COVERAGE FRAMEWORK
- 2** APPLICATION TO AUV SEABED SURVEYING

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- 3** COVERAGE PATH PLANNING WITH UNCERTAIN COVERAGE

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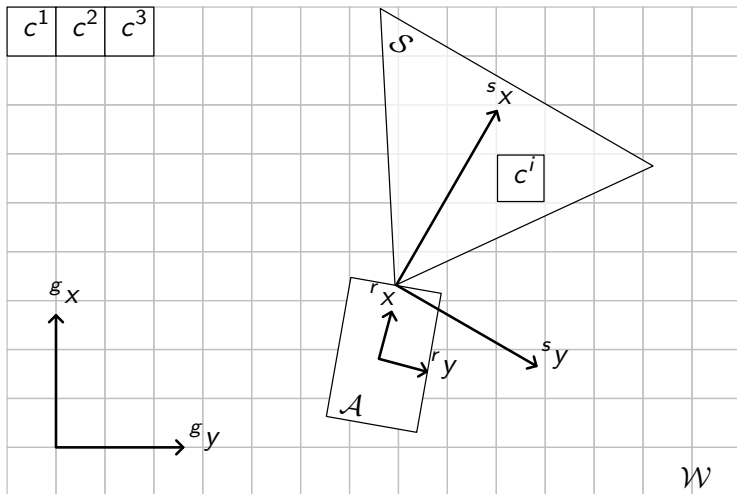
- 1 PROBABILISTIC COVERAGE FRAMEWORK
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- 4 EXPERIMENTAL RESULTS

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# PROBLEM SETUP



# ALGORITHM OVERVIEW

## STEP 1: POSE ESTIMATION

### ■ Filtering

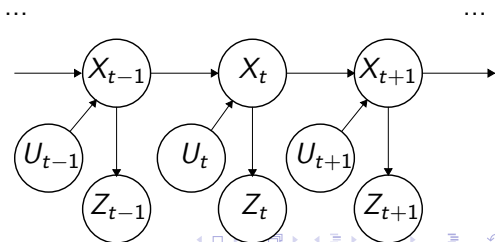
$$bel(x_t) \triangleq$$

$$p(x_t | u_{1:t}, z_{1:t}, x_0)$$

### ■ Smoothing

$$bel(x_{1:t}) \triangleq$$

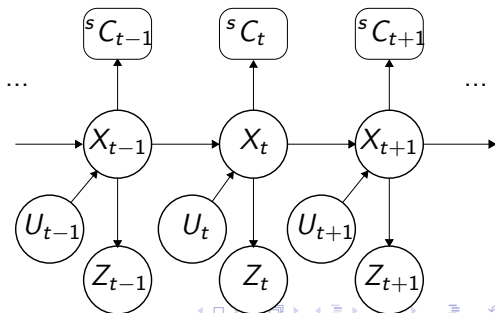
$$p(x_{1:t} | u_{1:t}, z_{1:t}, x_0)$$



# ALGORITHM OVERVIEW

## STEP 2: UNCERTAIN RELATIVE CELL LOCATION

- ${}^s C_t^i$  Location of cell  $i$  at time  $t$  in the coverage sensor frame



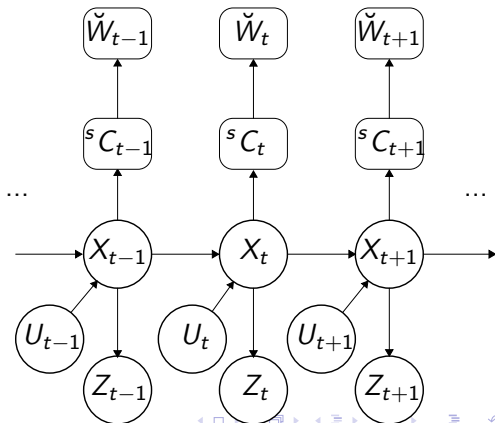
# ALGORITHM OVERVIEW

## STEP 3: PROJECT CELL LOCATION THROUGH COVERAGE SENSOR MODEL

$$\check{W}_t^i = \mathcal{H}(^s C_t^i)$$

$\mathcal{H}$ : Coverage sensor

model

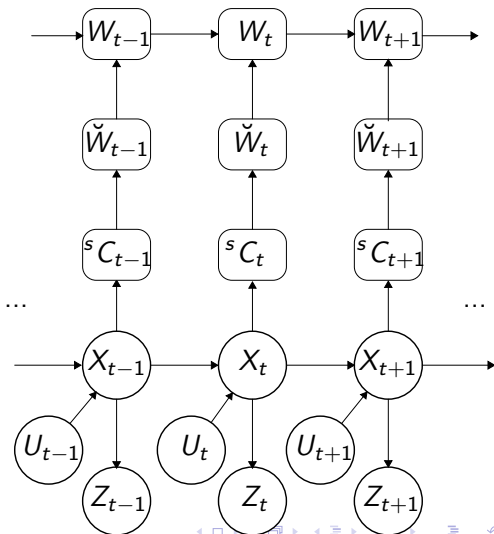


# ALGORITHM OVERVIEW

## STEP 4: RECURSIVE COVERAGE UPDATE

$$W_t^i = \max(\check{W}_t^i, W_{t-1}^i)$$

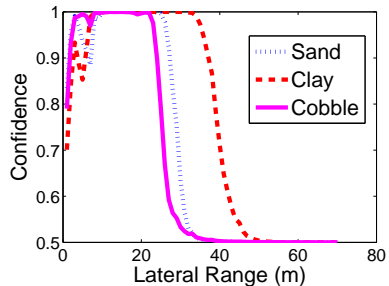
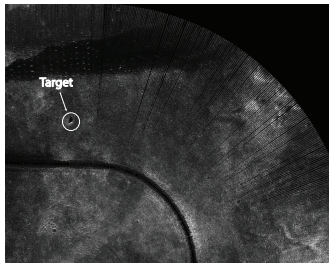
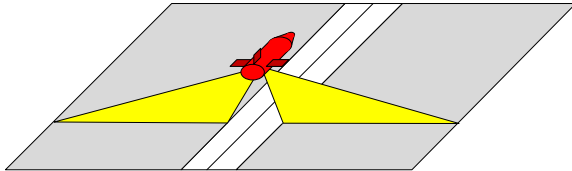
Note: This is an operation  
on RVs



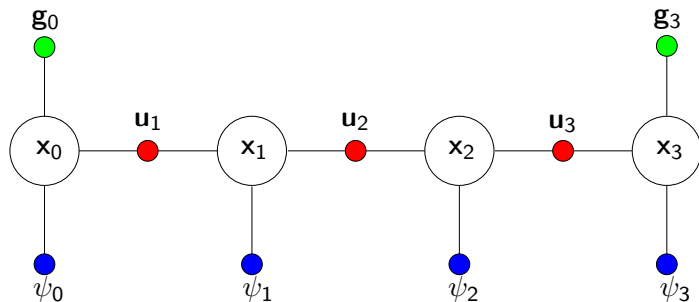
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# SEABED SURVEYING WITH A SIDESCAN SONAR SENSOR



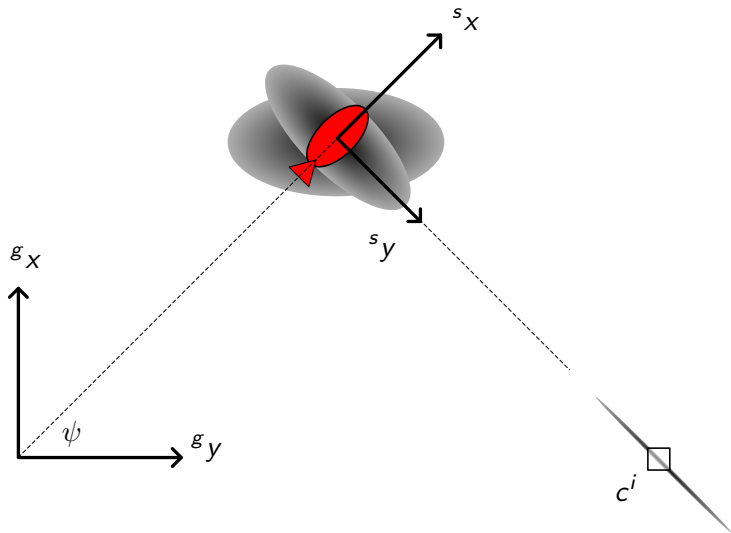
# STEP 1: POSE ESTIMATION



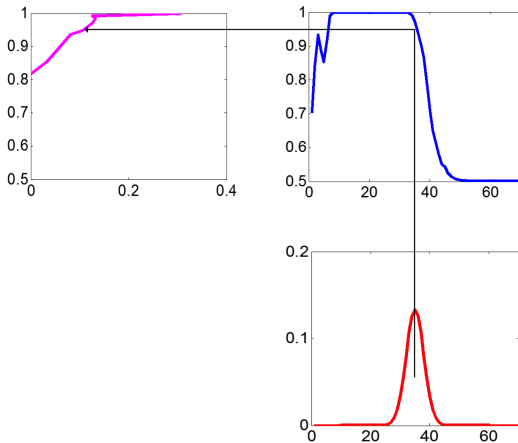
-  GPS Measurements
-  DVL Measurements
-  Compass Measurements



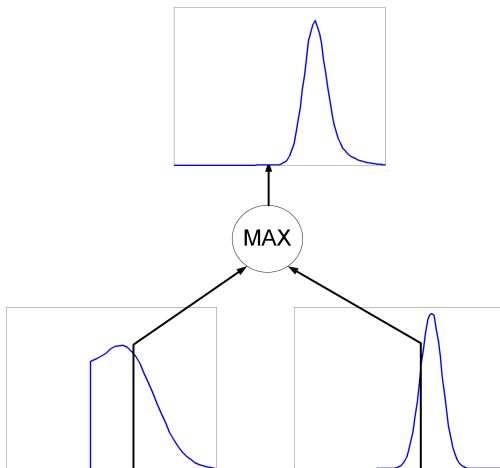
## STEP 2: UNCERTAINTY PROJECTION



# STEP 3: LOCATION UNCERTAINTY $\rightarrow$ COVERAGE UNCERTAINTY



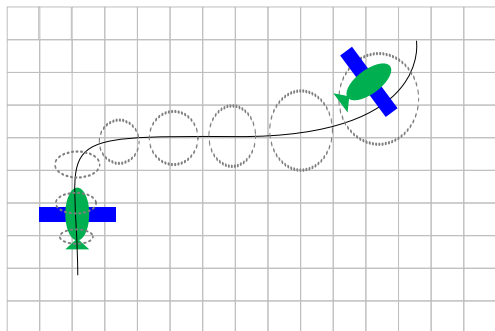
# STEP 4: COMBINING MEASUREMENTS



# OUTLINE

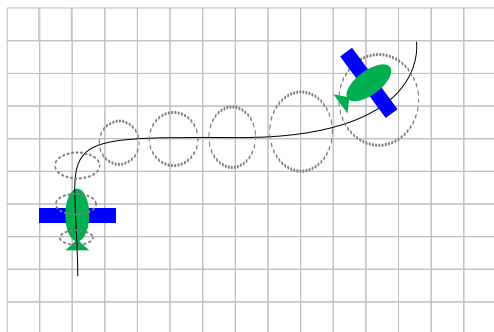
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## COVERAGE AS ENTROPY REDUCTION <sup>2</sup>



$$p(T_t^i = 1) = E[W_t^i]$$

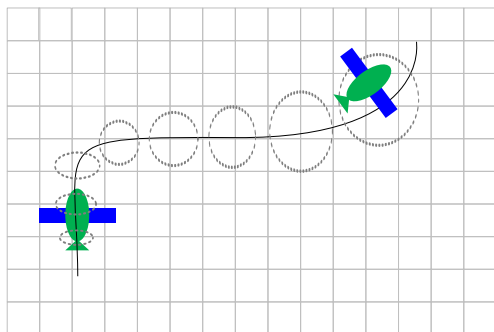
## COVERAGE AS ENTROPY REDUCTION <sup>2</sup>



$$p(T_t^i = 1) = E[W_t^i]$$

$$\Delta H(T_t^i | X_t) = H(T_t^i) - E_{X_t}[H(T_t^i | X_t)]$$

# COVERAGE AS ENTROPY REDUCTION <sup>2</sup>

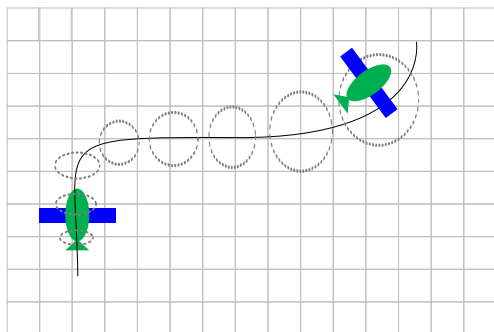


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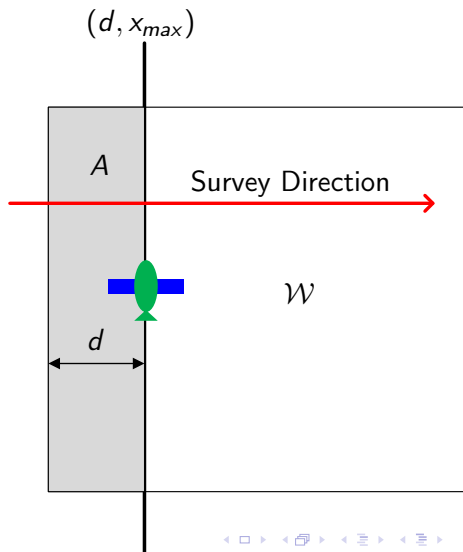
$$\tau : [0, 1] \rightarrow SE(2), s \rightarrow \tau(s)$$

$$\tau^* = \arg \max_{\tau} B(\tau) \triangleq \int_0^1 \sum_i \Delta H(T_t^i | \tau(s)) ds$$



# ADAPTIVE TRACK

$$\tau_d(0) = (d, x_{min})$$
$$\tau_d(1) = (d, x_{max})$$

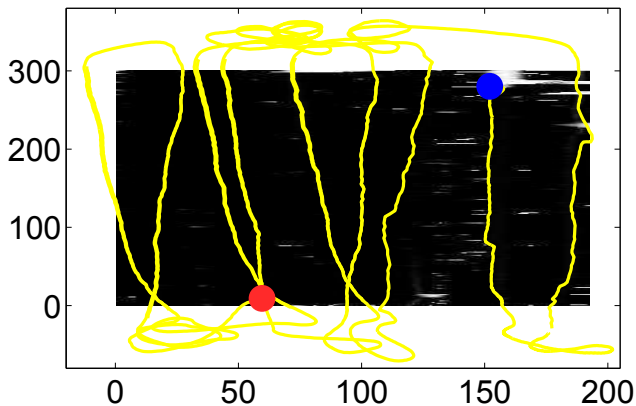


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# HARDWARE FIELD TRIALS

# FINAL RESULT



# CONCLUSIONS AND FUTURE WORK



## SUMMARY

- Probabilistic coverage
- AUV application
- Robust coverage planning

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- Probabilistic coverage
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## FUTURE WORK

- More general path planning
- Presence of obstacles
- Cooperative