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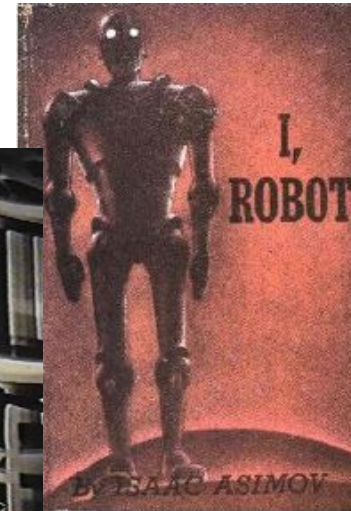
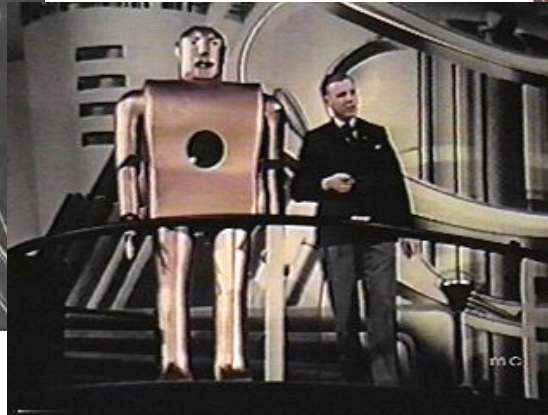
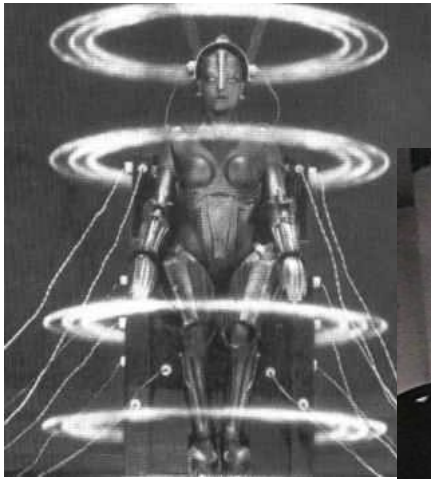
# Robot Intelligence

Leslie Pack Kaelbling  
MIT CSAIL

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# A dream of robots

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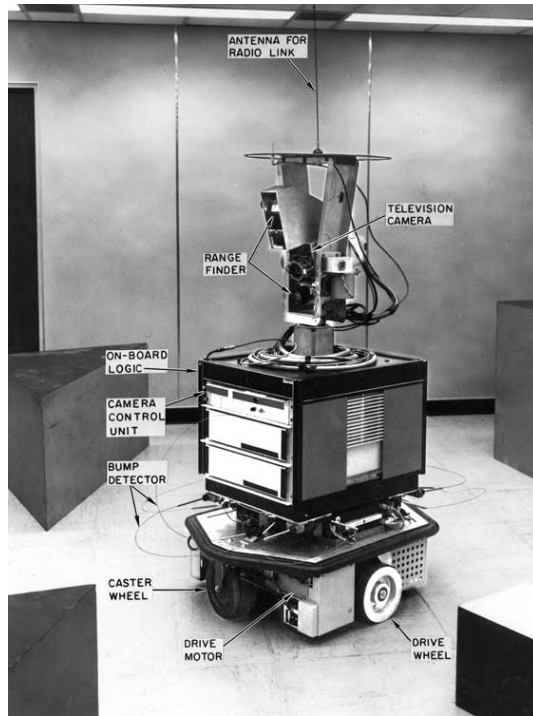
## Commercial reality



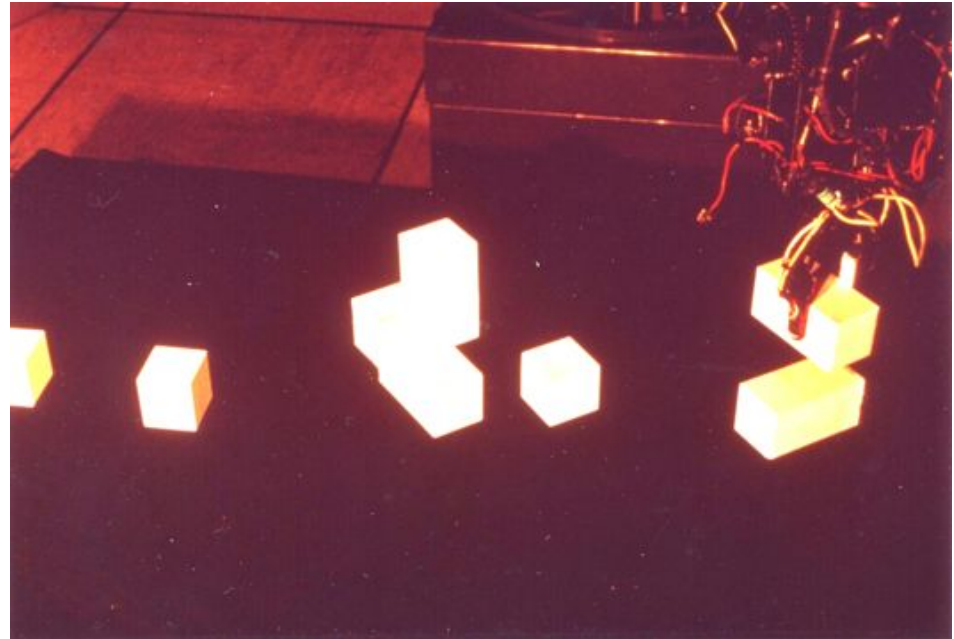
## Research frontier



# Robots and AI were once very close



SRI Shakey



MIT Copy Demo

Robotics drove advances in artificial intelligence:  
planning, learning, reasoning, vision, natural language....



# The best of times

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Good robot hardware

- range sensors, cameras, actuators, ...

Fast computers

Good fundamental algorithms for

- robot motion planning, visual object recognition, ...

Technical advances in

- probabilistic inference, machine learning, knowledge representation

# The worst of times

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Super-human robot fallacy:

- Focus on optimality limits our vision

Fragmented research community

- Subfields with individual standards, vocabulary, benchmarks
- Pieces won't fit together

Many other attractive and important applications

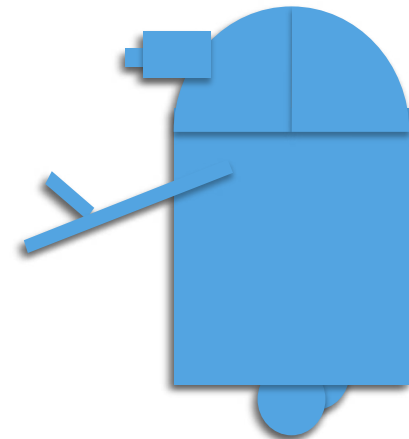
- Web applications, data mining, finance, ...

# The age of wisdom

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How to build the '**central**' **computational mechanisms** for

- **closed-loop control** of a system with
- **sensors and actuators** that has
- **long-term goal-directed** interactions with
- a **complex**
- **imperfectly predictable**  
external environment



# Three technical levers

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Compact description of functions and sets in large spaces

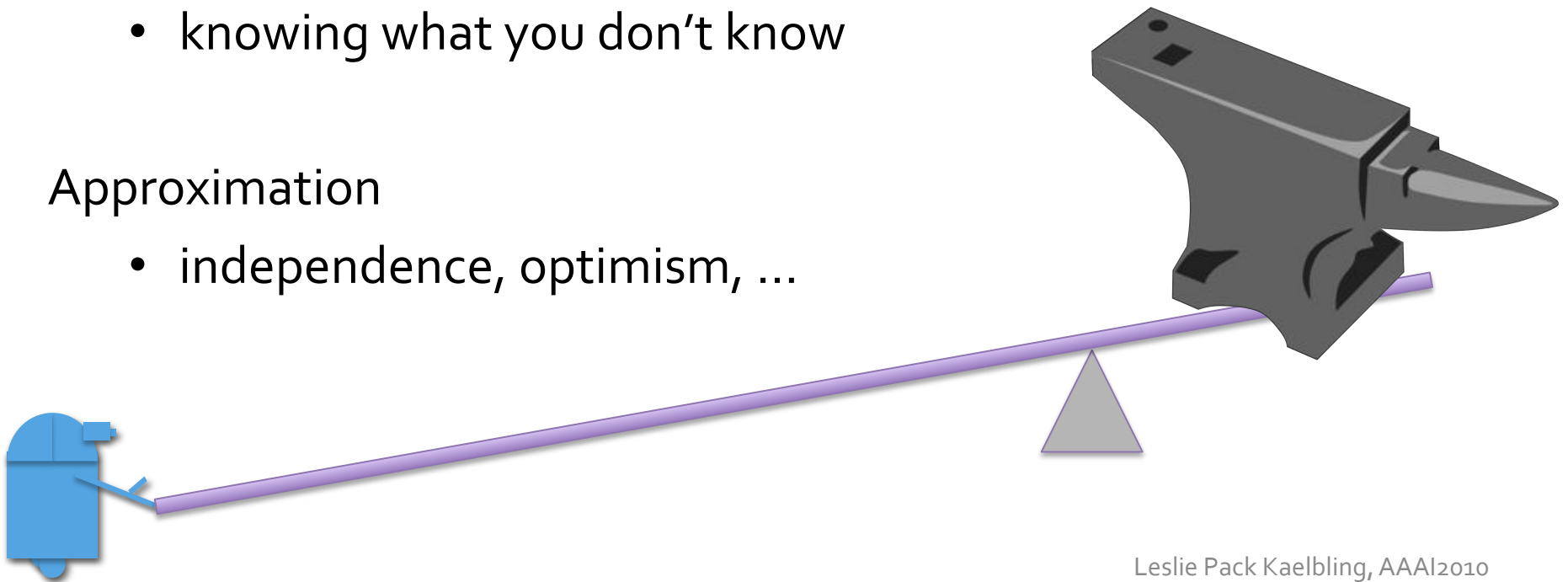
- continuity, geometry
- factoring, logical languages

Explicit representation of uncertainty

- knowing what you don't know

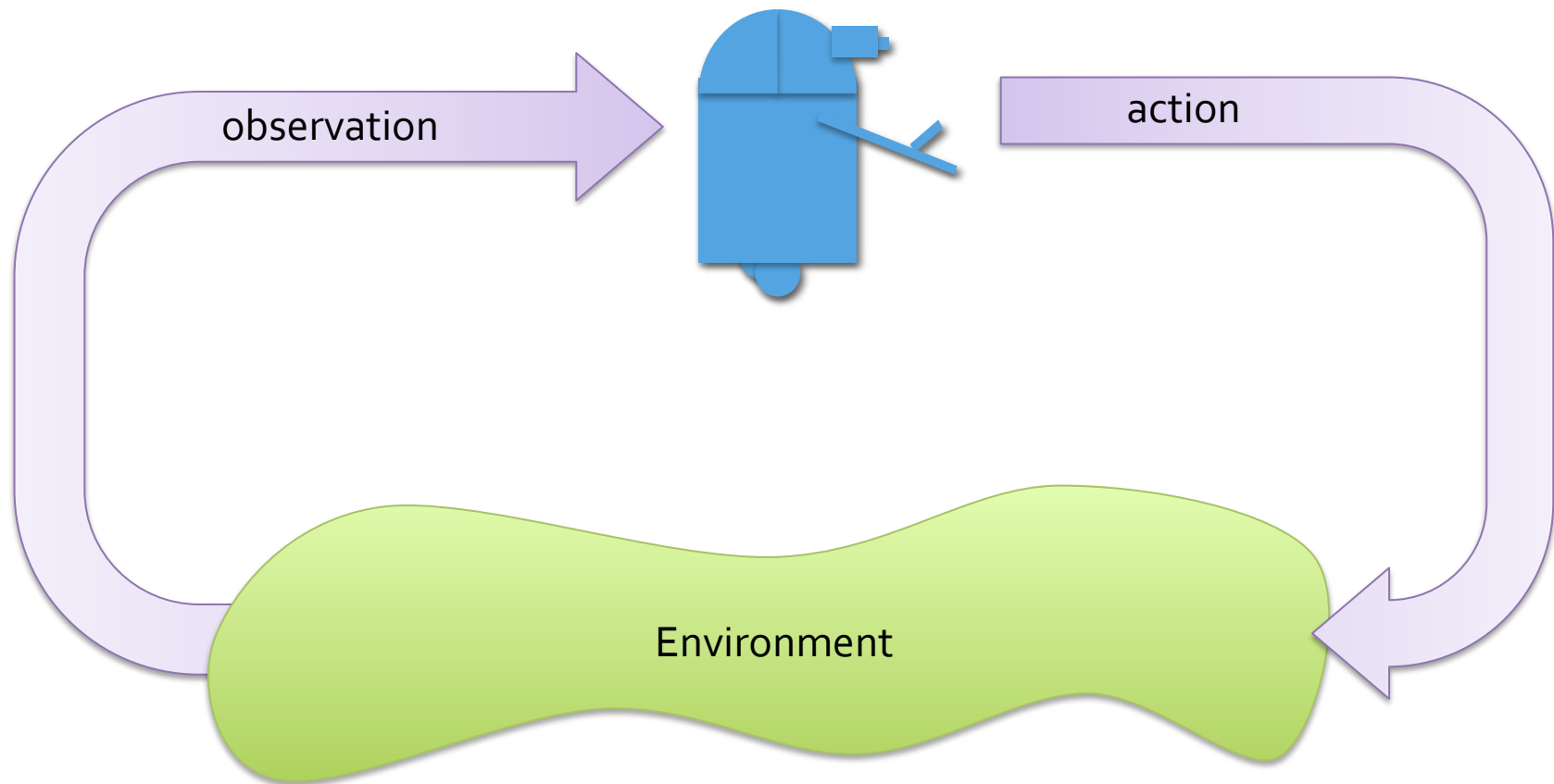
Approximation

- independence, optimism, ...



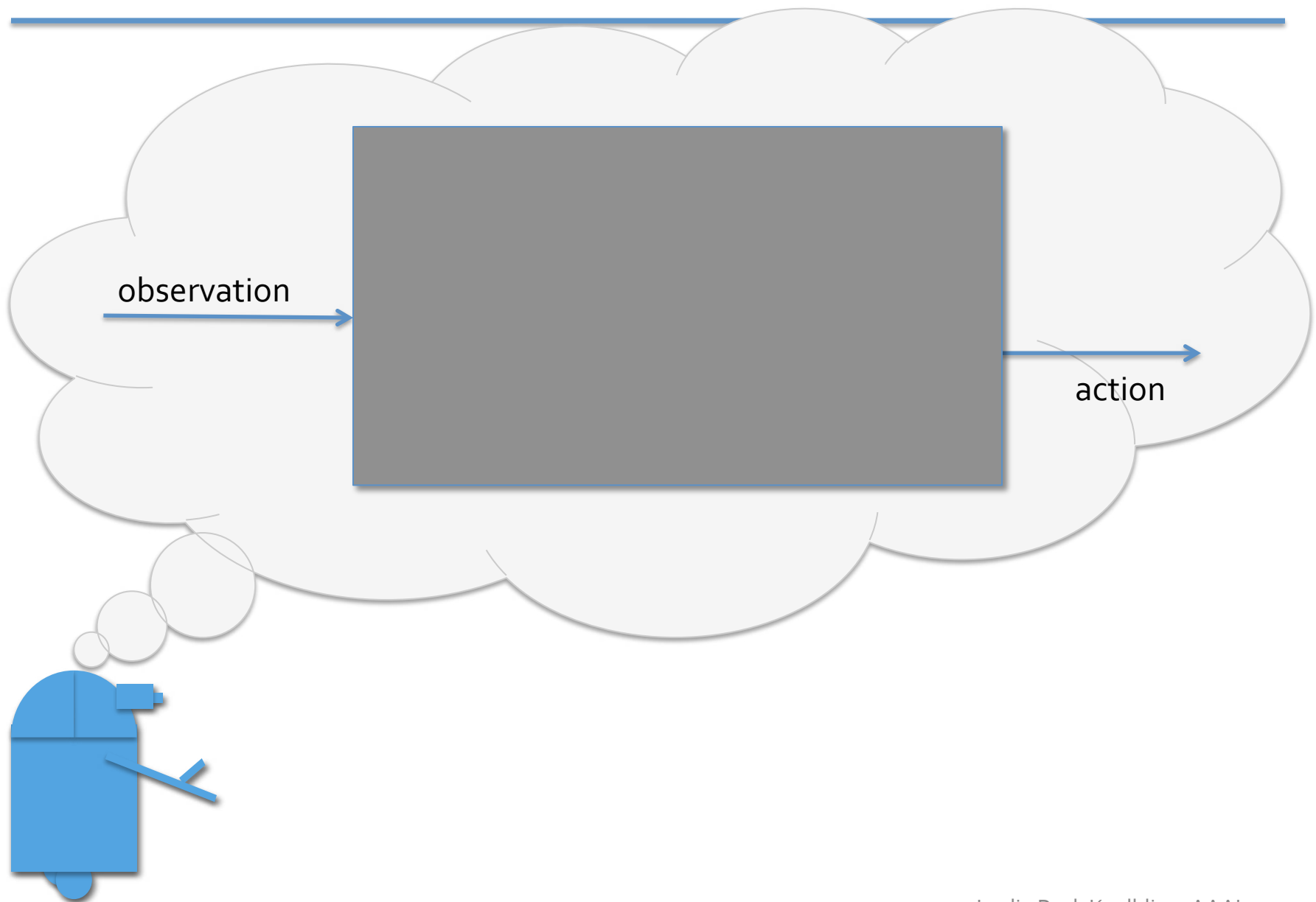
# Interaction with an external environment

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# What to learn? What to build in?

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# Prior + Experience = Learned competence

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How 'big' is the prior? Where does it come from?

Engineers must do for robots what evolution did for us

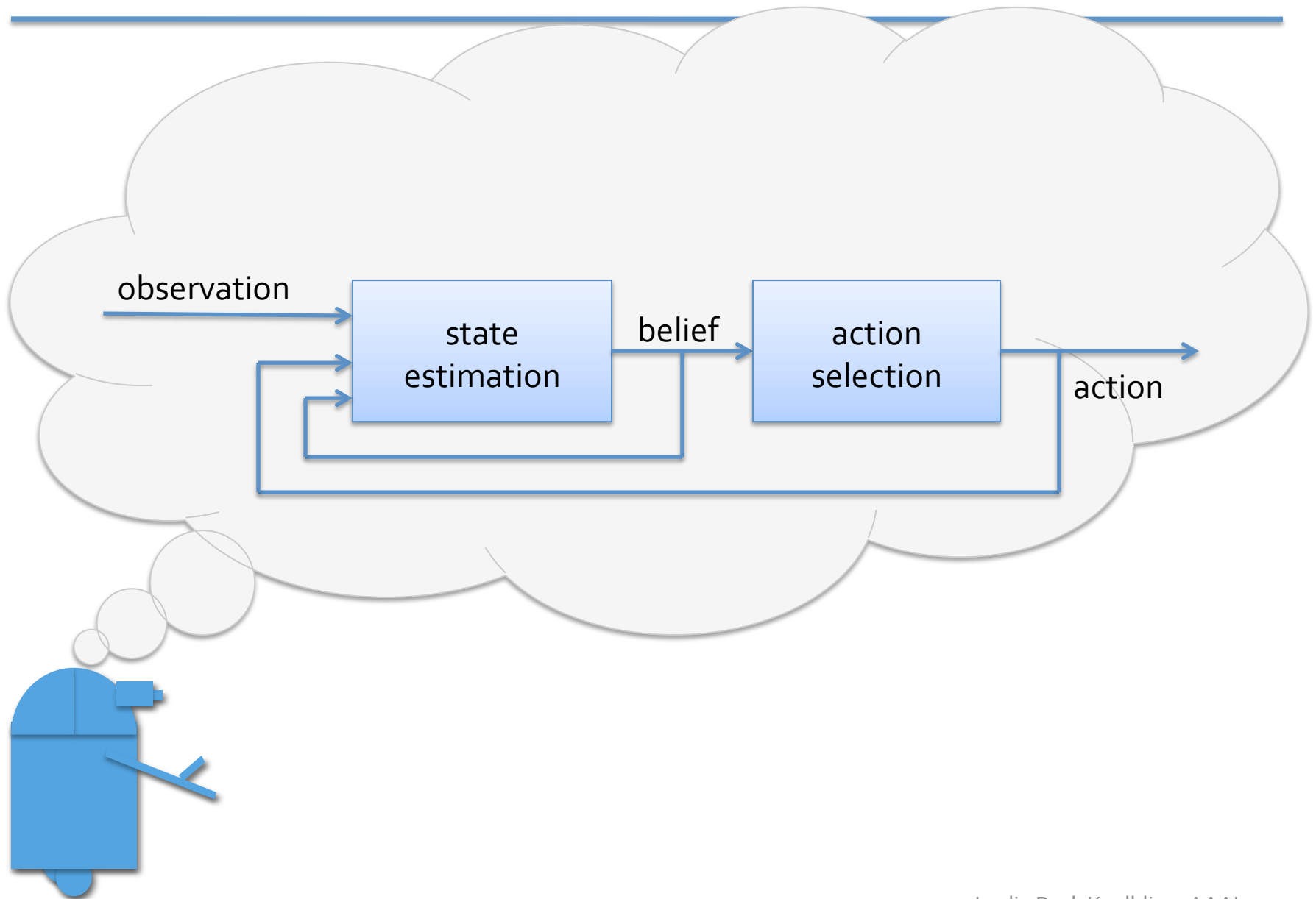
- Build in architectural constraints and fundamental truths (e.g. physical laws)

Agents must learn niche-specific competences  
(and things the engineers can't articulate)

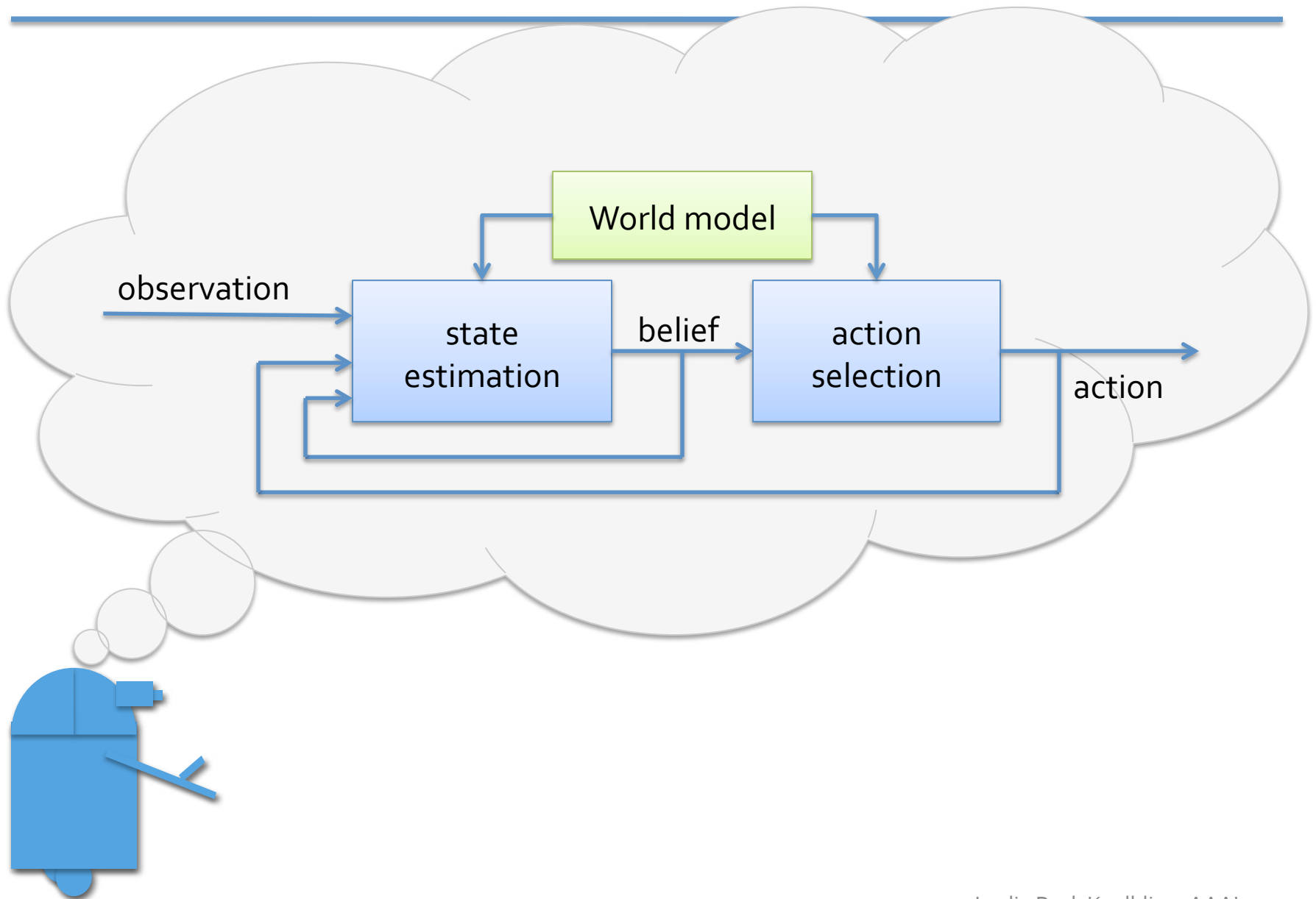
- sensory-motor loops
- world model at several levels of abstraction
- strategies for managing internal computation

# Internal architecture

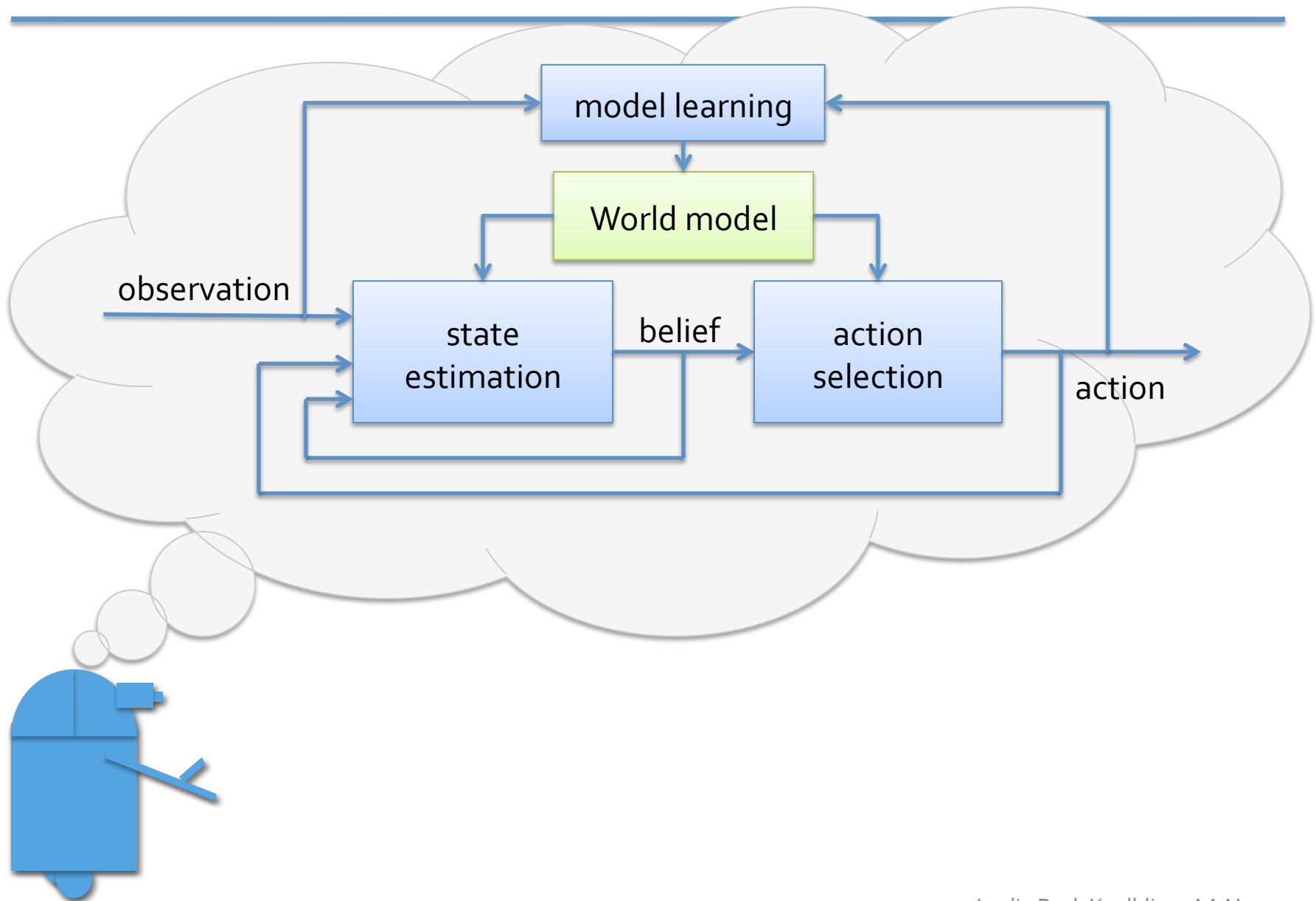
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# Internal architecture



# Internal architecture



# This talk: getting leverage

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Sample points in the technical space

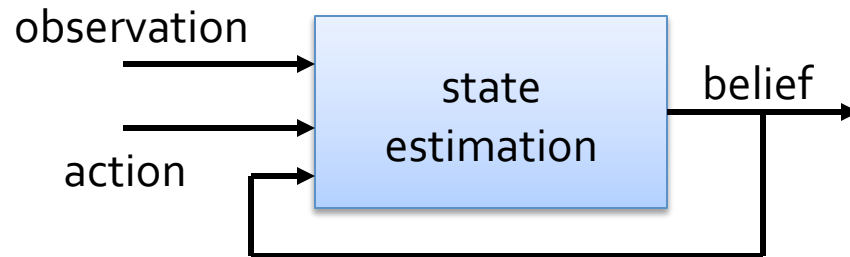
- **state estimation** method
  - combining logic, probability, and approximation
- **3 action selection** examples
  - combining logic or geometry, probability, and approximation
- **model learning** method
  - combining logic, probability, and approximation

Important areas neglected:

- perception, actuation, language and human interaction, multi-agent systems, ...

# The epoch of belief and of incredulity

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**State estimation:** Explicitly represent state of knowledge about external environment using probability

Joint work with Luke Zettlemoyer and Hanna Pasula

# State estimation

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**Problem:** given history of past observations and actions, what do we know about the current state of the world?

**Lazy:** store history of observations, do inference when necessary

**Eager:** maintain an explicit representation of the current distribution over the state of the world (“filtering”)

# Filtering: Bayesian belief state update

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Update after executing an action and receiving an observation

$$\Pr(s_{t+1} \mid \mathbf{a}_t, \mathbf{o}_{t+1}) \propto \Pr(\mathbf{o}_{t+1} \mid s_{t+1}) \sum_{s_t} \Pr(s_{t+1} \mid s_t, \mathbf{a}_t) \Pr(s_t)$$

posterior  
belief

observation  
model

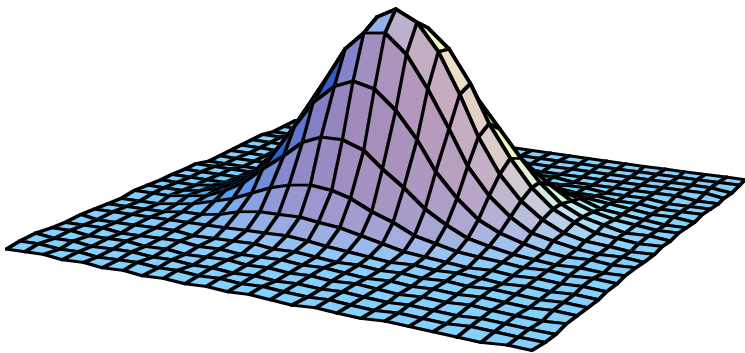
transition  
model

prior  
belief

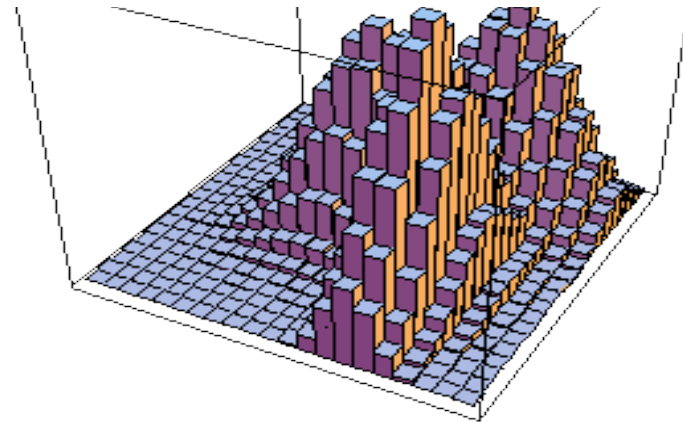
# Representing the belief state

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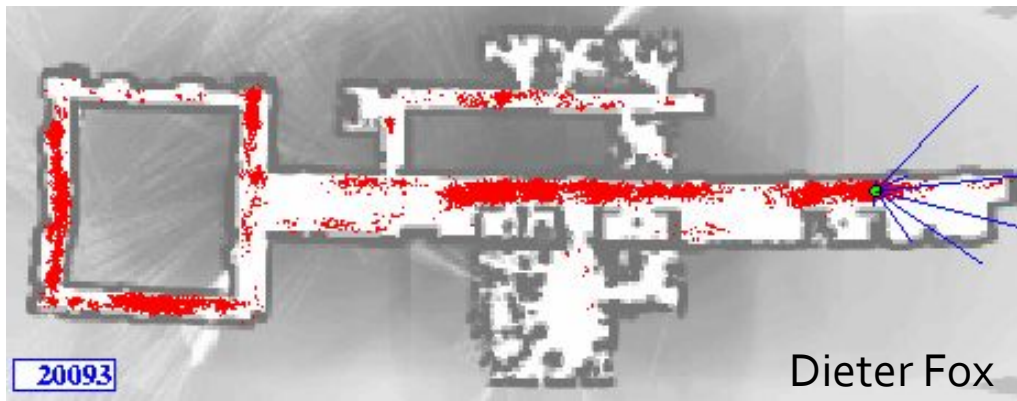
Gaussian



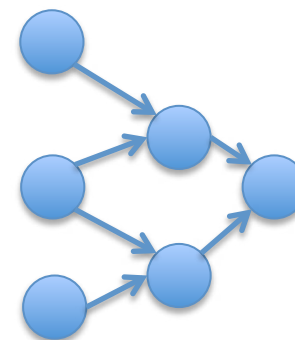
Histogram



Set of particles



Bayesian network

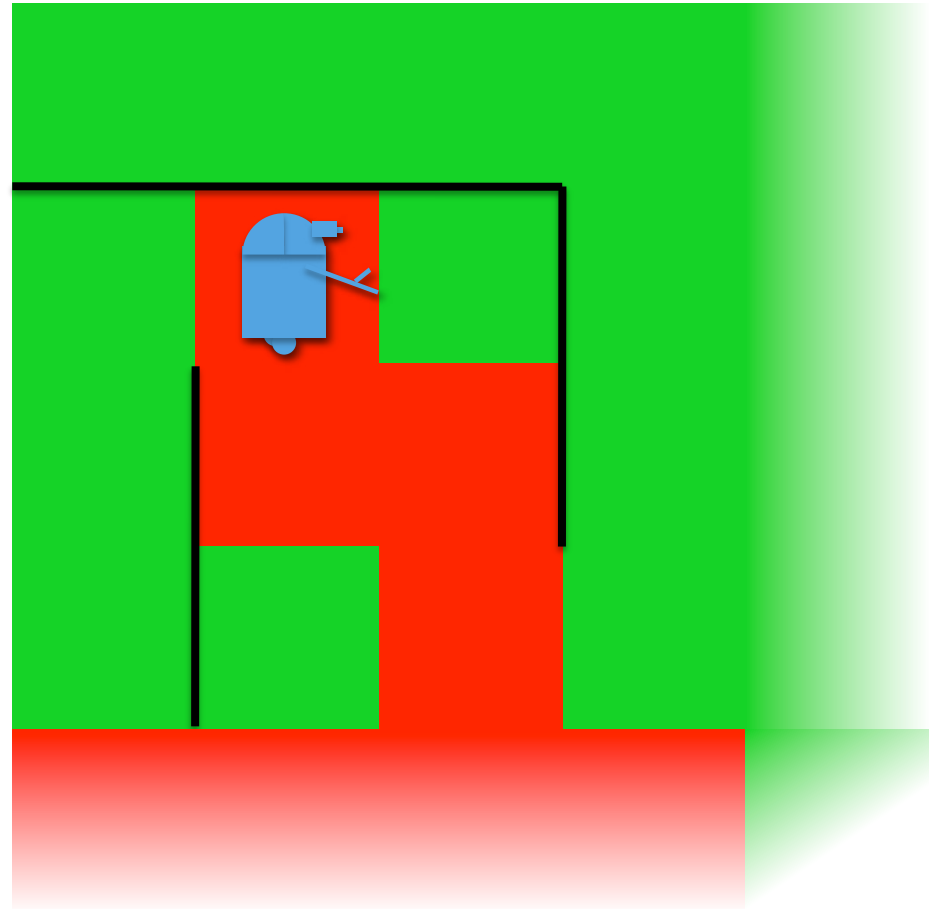


Leslie Pack Kaelbling, AAAI2010

# A big (toy) world

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- dimensions are unknown (possibly infinite)
- walls between some locations
- locations have appearance
- R moves (with error) through the world
- R observes (with error) the color at his location



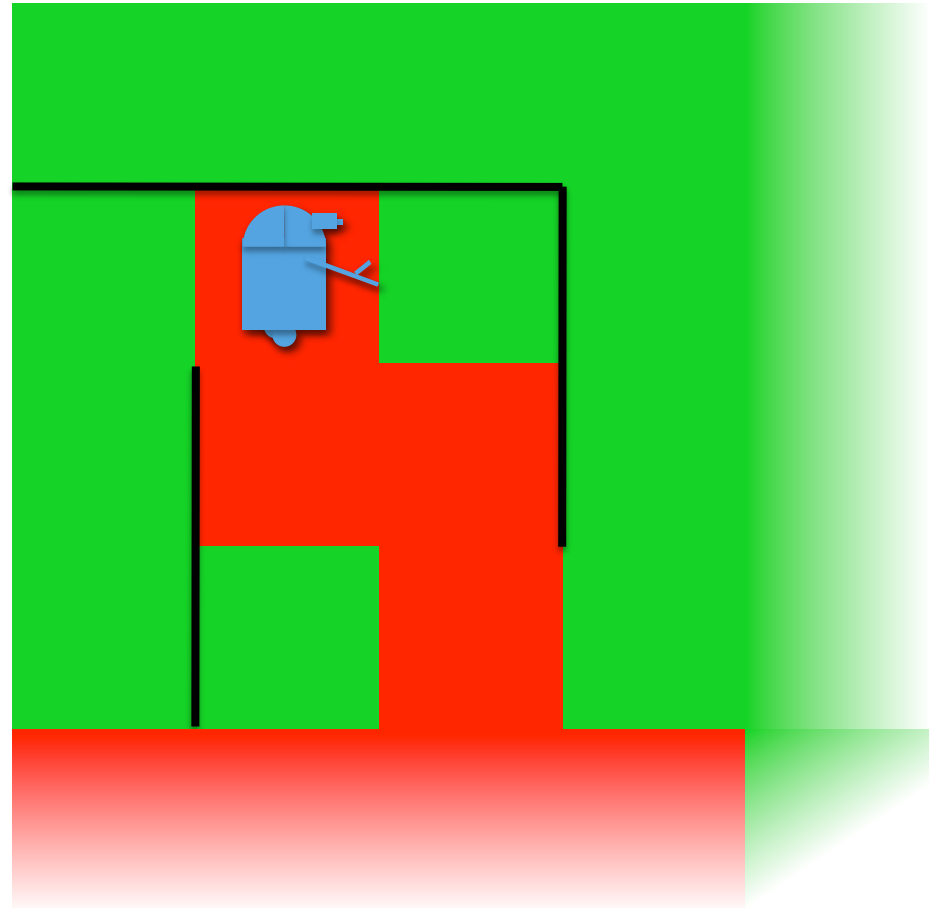
# A day in the life

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R is booted up,

- sees a red square
- tries to move right
- sees a green square

What does R know about the world?



Combine logic and probability to get compact representations of beliefs in complex domains

# First-Order particle filtering

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**Hypothesis:** set of states that are indistinguishable based on the history of observations and actions

$$\Pr(s \mid o_{0:t}, a_{1:t}) \propto \Pr(o_{0:t} \mid s, a_{1:t}) \Pr(s)$$

posterior  
belief

observation and  
transition probability

prior  
belief

Use logic sentences to describe hypotheses

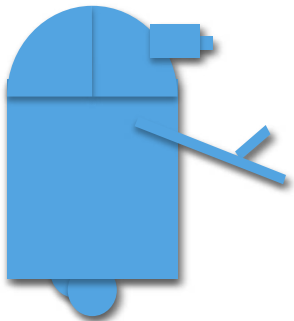
Only represent likely hypotheses

# R wakes up

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- One hypothesis

*True*

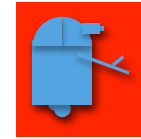


# R sees a red square

---

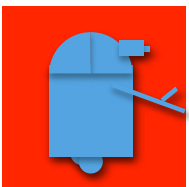
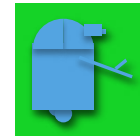
$\exists x.at(R, x) \wedge red(x)$

0.8















$\exists x.at(R, x) \wedge green(x)$

0.2



$P(\text{see red} \mid \text{at red square}) = 0.8$

# R tries to move right

$\exists x, y. at(R, y) \wedge red(x) \wedge rightOf(y, x)$	.504	 
$\exists x, y. at(R, y) \wedge green(x) \wedge rightOf(y, x)$	.126	 
$\exists x, y. at(R, x) \wedge red(x) \wedge rightOf(y, x)$	.056	 
$\exists x, y. at(R, x) \wedge green(x) \wedge rightOf(y, x)$	.014	 
$\exists x. at(R, x) \wedge red(x) \wedge \neg \exists y. rightOf(y, x)$	0.24	 
$\exists x. at(R, x) \wedge green(x) \wedge \neg \exists y. rightOf(y, x)$	0.06	 



Prob wall to right: 0.3  
 Prob fail to move (if no wall): 0.1  
 Prob fail to move (if wall): 1.0

# R tries to move right: sample

---

$\exists x, y. at(R, y) \wedge red(x) \wedge rightOf(y, x)$

$\exists x, y. at(R, y) \wedge green(x) \wedge rightOf(y, x)$

$\exists x, y. at(R, x) \wedge red(x) \wedge rightOf(y, x)$

$\exists x. at(R, x) \wedge red(x) \wedge \neg \exists y. rightOf(y, x)$



Prob wall to right: 0.3  
Prob fail to move (if no wall): 0.1  
Prob fail to move (if wall): 1.0

# R sees a green square

---

$\exists x.at(R, y) \wedge red(x) \wedge rightOf(y, x) \wedge red(y)$

.147



$\exists x.at(R, y) \wedge green(x) \wedge rightOf(y, x) \wedge red(y)$

.036



$\exists x, y.at(R, x) \wedge red(x) \wedge rightOf(y, x)$

.016



$\exists x.at(R, x) \wedge red(x) \wedge \neg \exists y.rightOf(y, x)$

.069



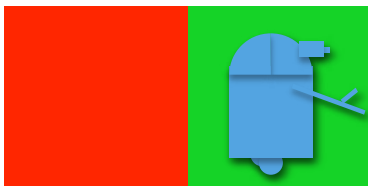
$\exists x.at(R, y) \wedge red(x) \wedge rightOf(y, x) \wedge green(y)$

.585



$\exists x.at(R, y) \wedge green(x) \wedge rightOf(y, x) \wedge green(y)$

.147



# R sees a green square: sample

---

$\exists x.at(R, y) \wedge red(x) \wedge rightOf(y, x) \wedge red(y)$



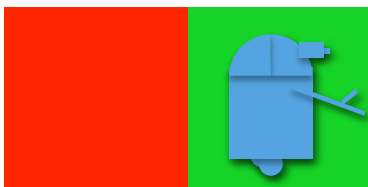
$\exists x.at(R, x) \wedge red(x) \wedge \neg \exists y.rightOf(y, x)$



$\exists x.at(R, y) \wedge red(x) \wedge rightOf(y, x) \wedge green(y)$



$\exists x.at(R, y) \wedge green(x) \wedge rightOf(y, x) \wedge green(y)$



# Technical Story

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Rao-Blackwellization:

$$\begin{aligned} \mathbb{E}_{\text{Pr}(\mathbf{x}_1, \mathbf{x}_2)} f(\mathbf{x}_1, \mathbf{x}_2) &= \mathbb{E}_{\text{Pr}(\mathbf{x}_2)} \mathbb{E}_{\text{Pr}(\mathbf{x}_1 | \mathbf{x}_2)} f(\mathbf{x}_1, \mathbf{x}_2) \\ &\approx \frac{1}{n} \sum_{\text{samples from } \text{Pr}(\mathbf{x}_2)} \mathbb{E}_{\text{Pr}(\mathbf{x}_1 | \mathbf{x}_2)} f(\mathbf{x}_1, \mathbf{x}_2) \end{aligned}$$

For us:

$\mathbf{x}_2$  : logical partition  
 $\mathbf{x}_1$  : state within the partition  
 $f(\mathbf{x}_1, \mathbf{x}_2)$  : Am I in room 6?

created dynamically  
depending on observations

depends only on prior

Many other possible f

# Demand-driven complexity

---

Logical particle filter:

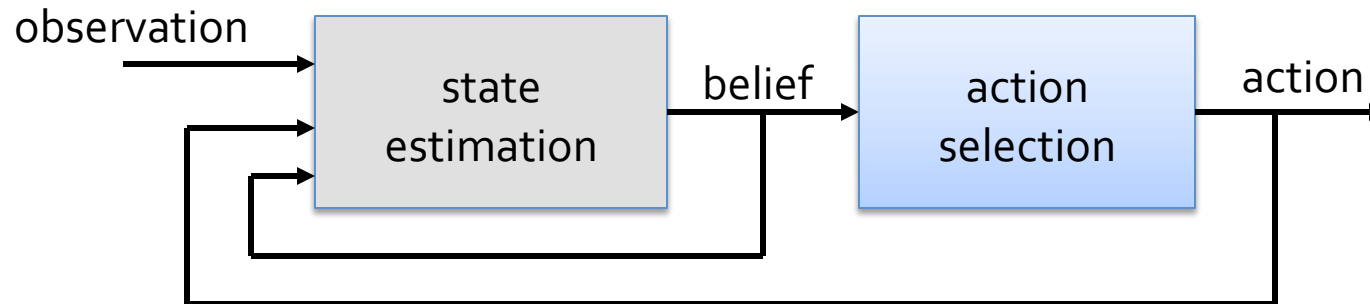
- complexity of **logical form** driven by observations
- concentrates on **most probable** part of the space

Be lazier!

- focus on small set of objects and properties relevant to current goal
- dynamically change focus
- use observation history to initialize new filters

# Action selection

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Plan in belief space:

- every action gains information and changes the world
- changes are reflected in new belief via estimation
- goal is to believe that the environment is in a desired state

# The spring of hope and the winter of despair

---

In domains that lack terrible outcomes:

- plan assuming actions will result in most likely transition and observation
- replan if expectation is violated at runtime

Great success of FF-Replan at ICAPS probabilistic planning competition

Same principle as feedback control using an idealized model

# Optimistic (re)planning in belief space

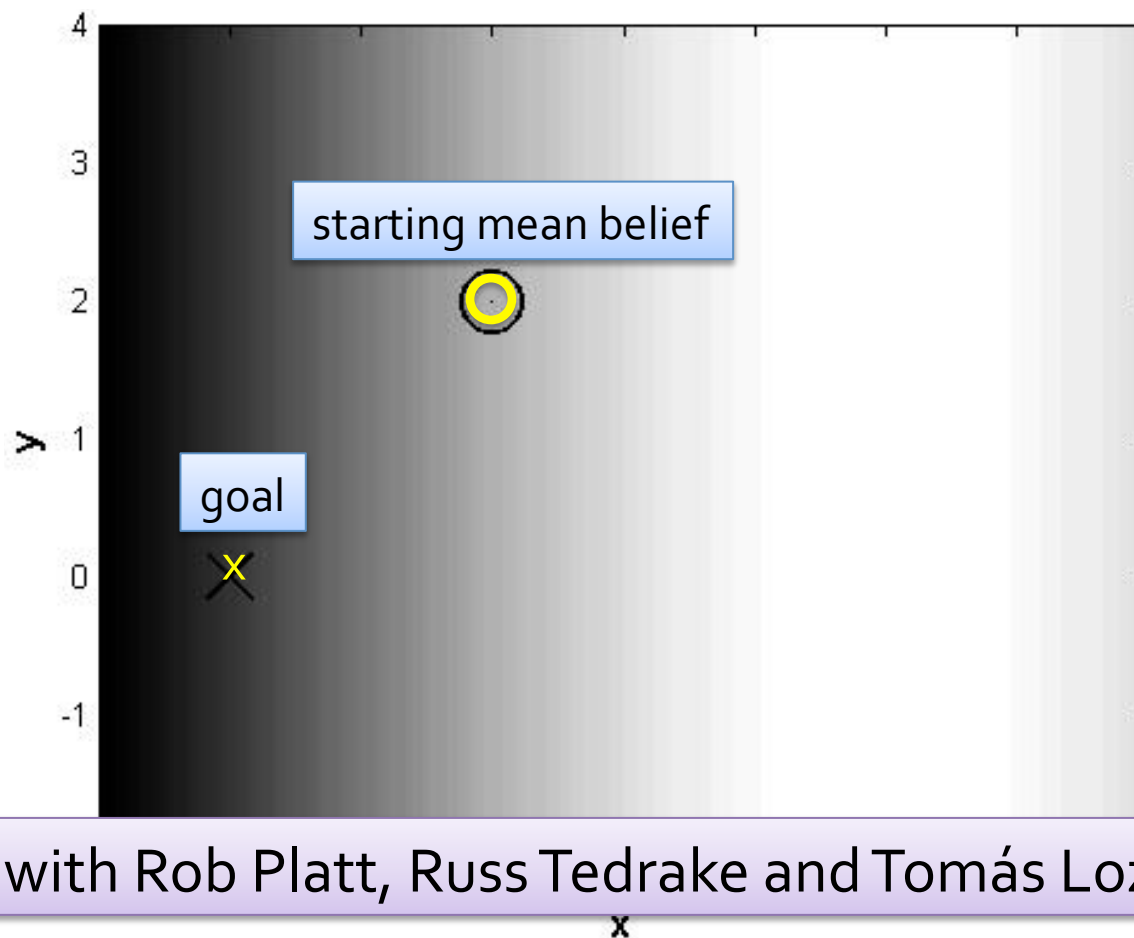
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- **control with state-dependent observation noise:**  
continuous state, action, observation spaces
- **robot grasping with tactile sensing:**  
continuous state, action, observation spaces
- **household robot with local observation:**  
mixed continuous and relational spaces

# The season of light, the season of darkness

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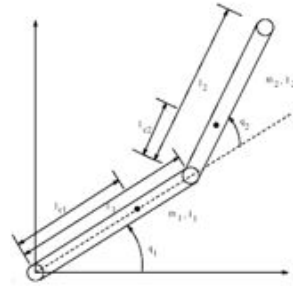
- robot in  $x, y$  space
- good position sensing in light regions; poor in dark



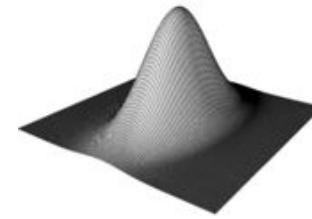
Joint work with Rob Platt, Russ Tedrake and Tomás Lozano-Pérez

# Control in belief space: underactuated

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Acrobot



Gaussian belief:

State space:

$$x = \begin{pmatrix} \theta \\ \dot{\theta} \end{pmatrix}$$

$$b = \begin{pmatrix} m \\ \Sigma \end{pmatrix}$$

Planning objective:

$$x_g = \begin{pmatrix} \pi \\ 0 \end{pmatrix}$$

$$b_g = \begin{pmatrix} x_g \\ 0 \end{pmatrix}$$

Underactuated dynamics:

$$\ddot{\theta} = f(\theta, \dot{\theta}, u)$$

???

# Belief space dynamics

---

Dynamics specify next belief state, as a function of previous belief state and action

- state update: generalized Kalman filter

$$(\mu_{t+1}, \Sigma_{t+1}) = \text{GKF}(o_t, a_t, \mu_t, \Sigma_t)$$

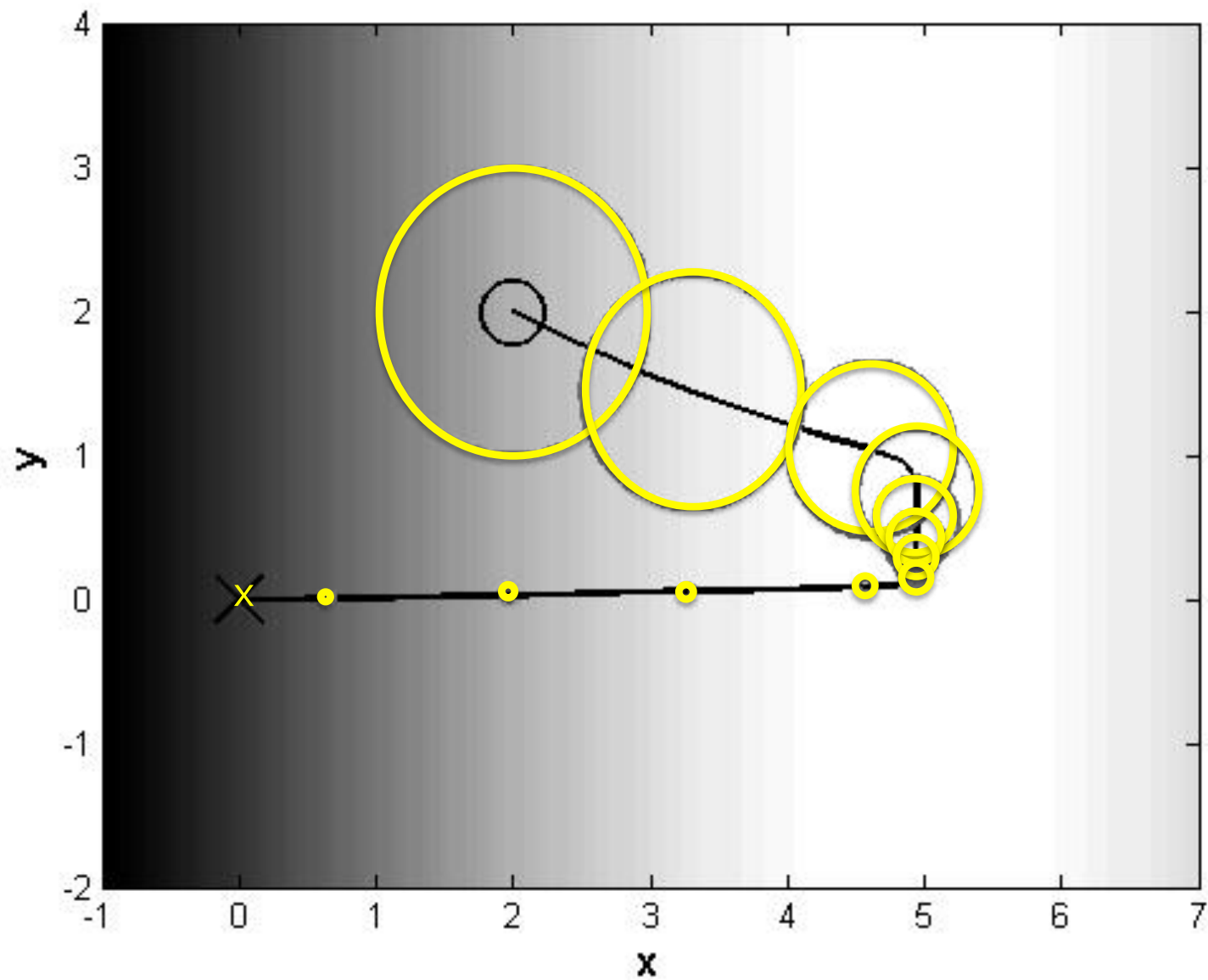
- substitute expected observation in for actual one  
add Gaussian noise

$$\begin{aligned}(\mu_{t+1}, \Sigma_{t+1}) &= F(a_t, \mu_t, \Sigma_t) + N \\ &= \text{GKF}(\bar{o}(\mu_t), a_t, \mu_t, \Sigma_t) + N\end{aligned}$$

- continuous Gaussian non-linear dynamics:  
apply tools from control theory

# Light-dark plan

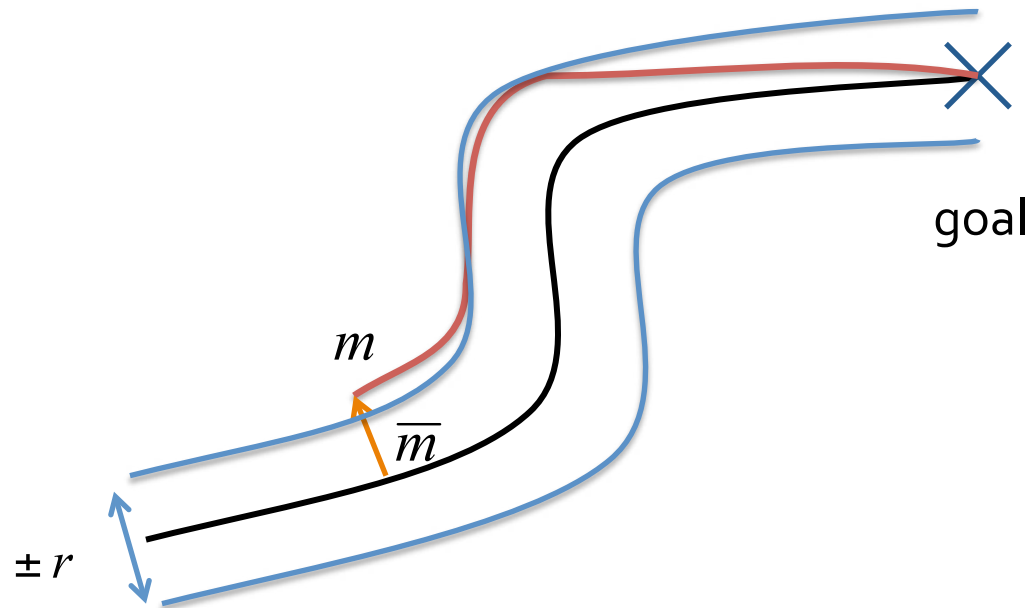
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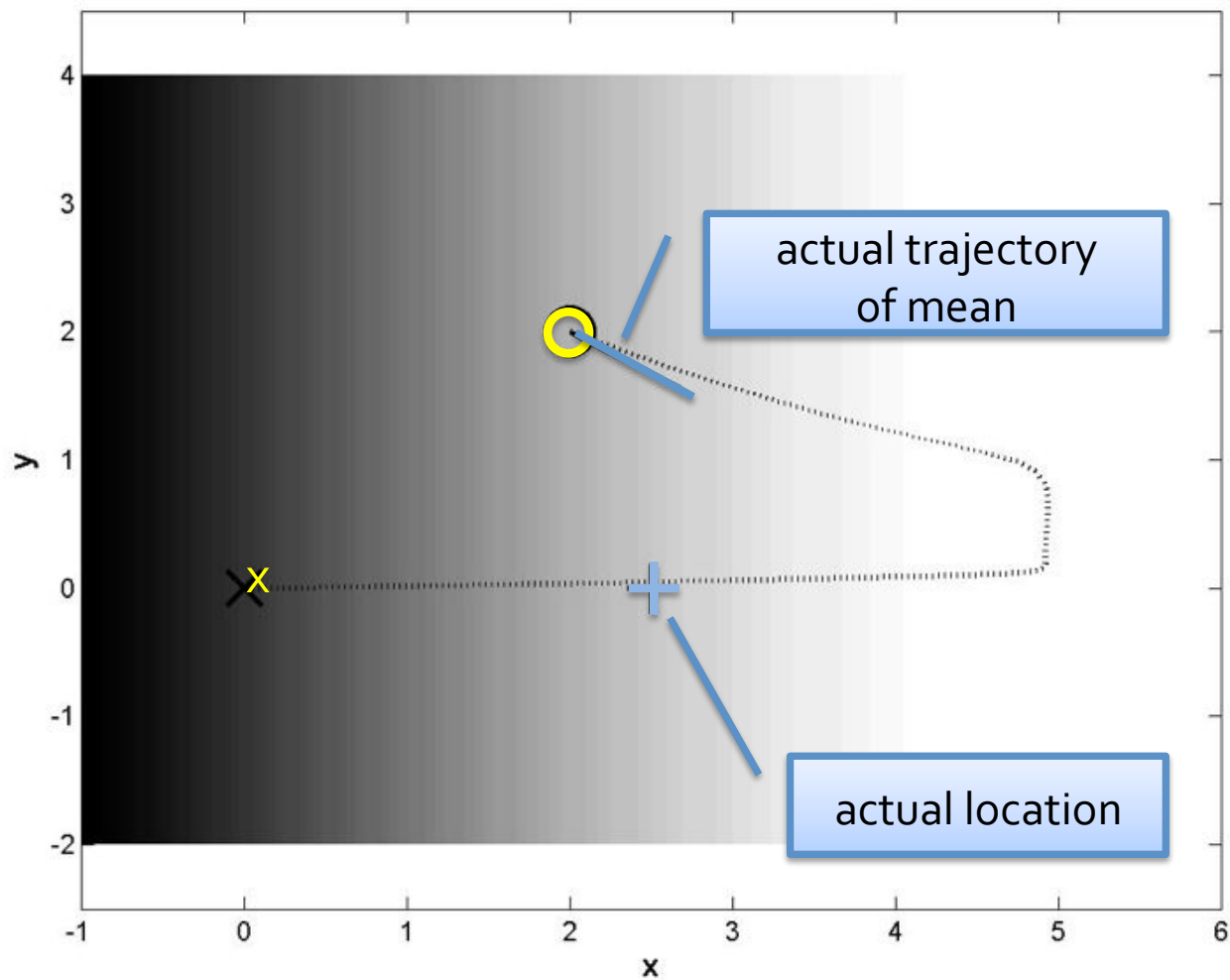
# Replanning

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Replan when new belief state deviates too far from planned trajectory

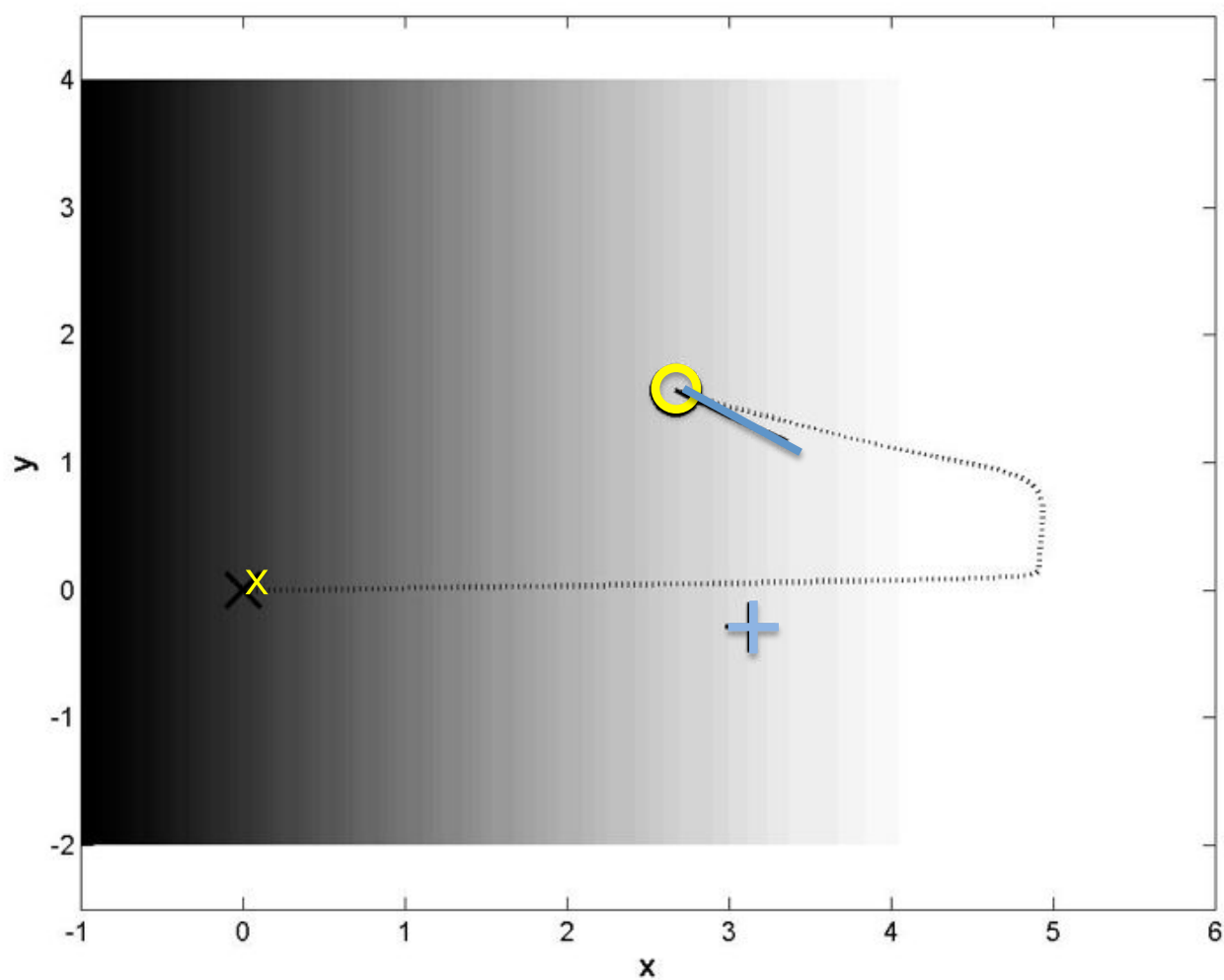


# Replanning: light-dark problem



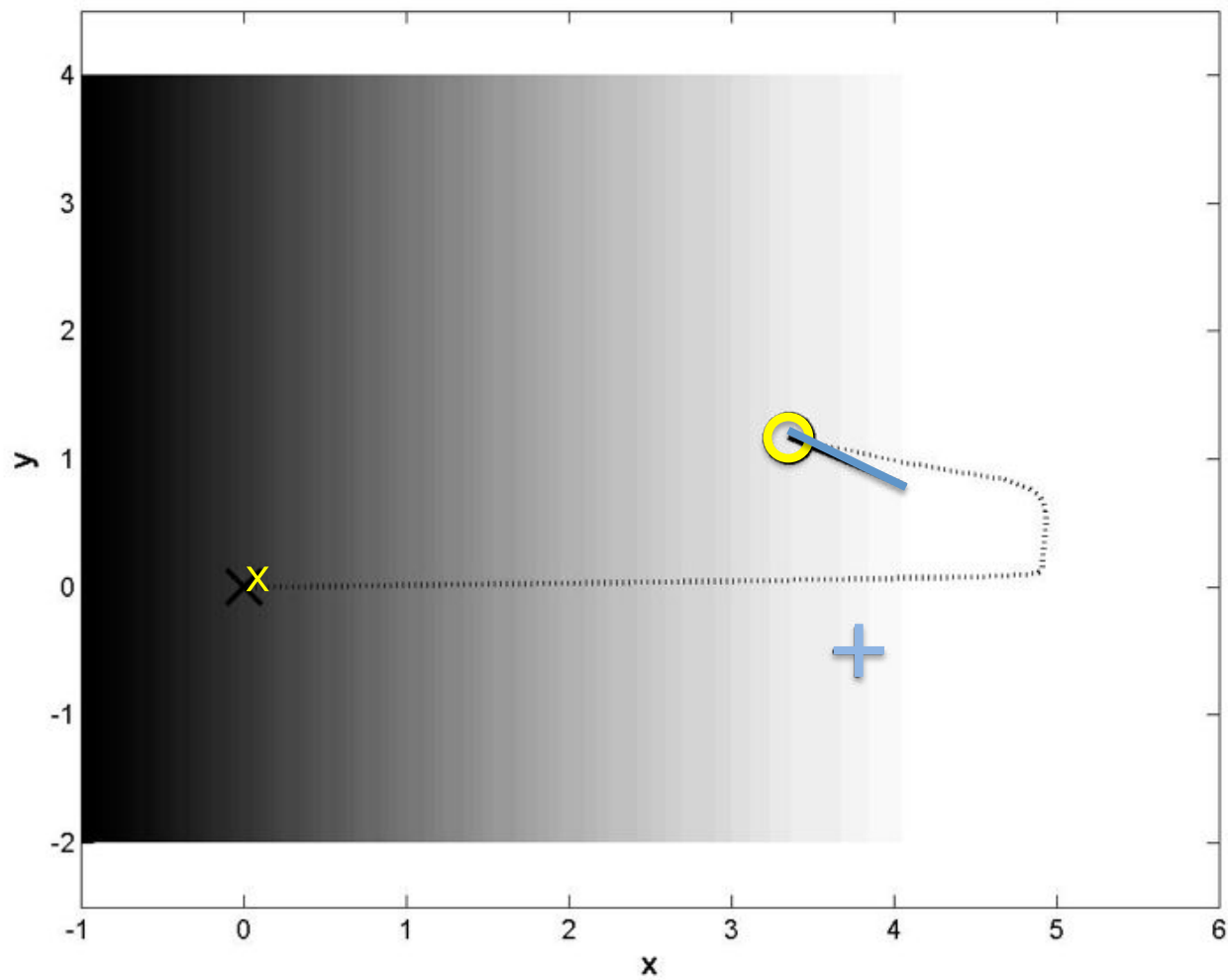
# Replanning: light-dark problem

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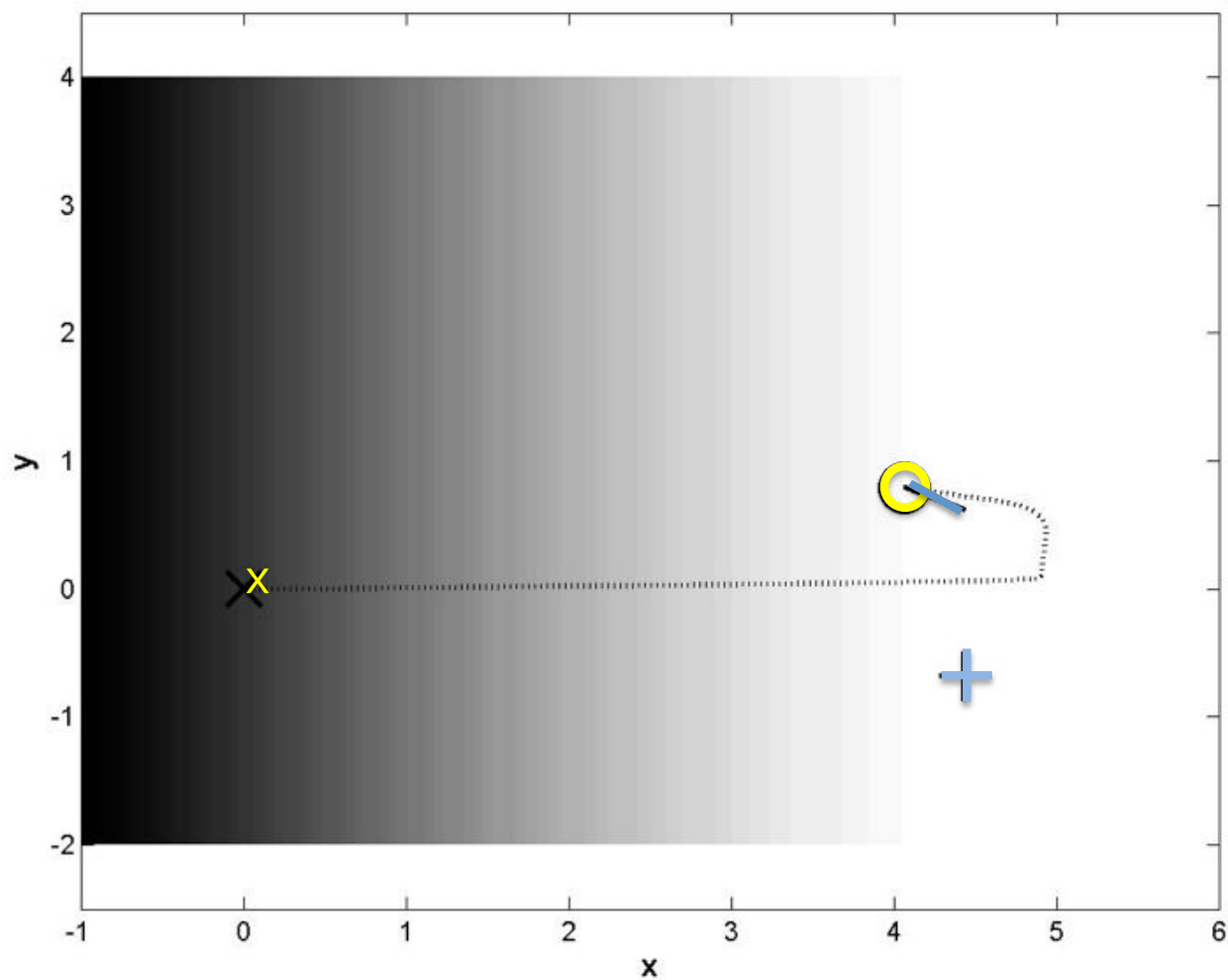
# Replanning: light-dark problem

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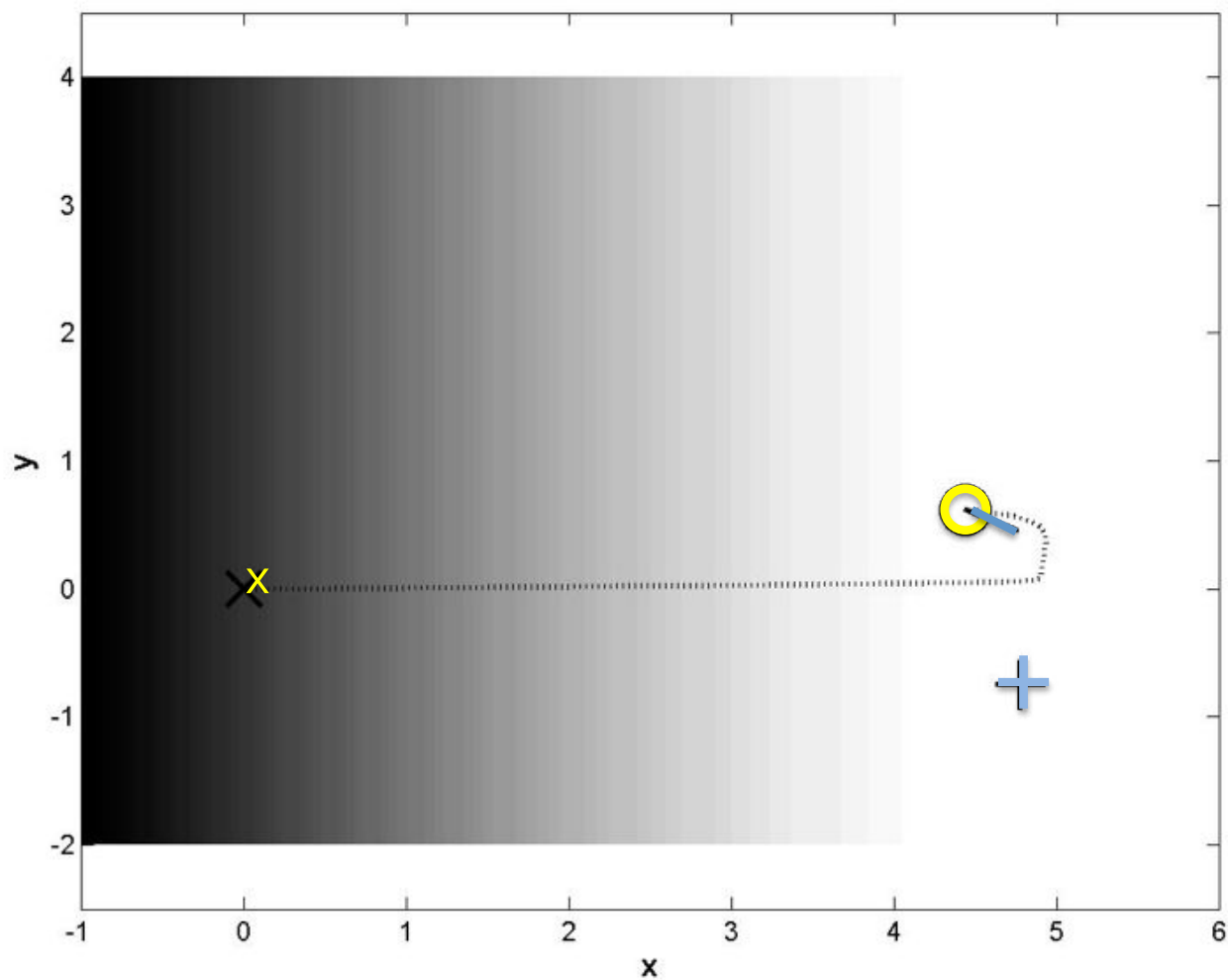
# Replanning: light-dark problem

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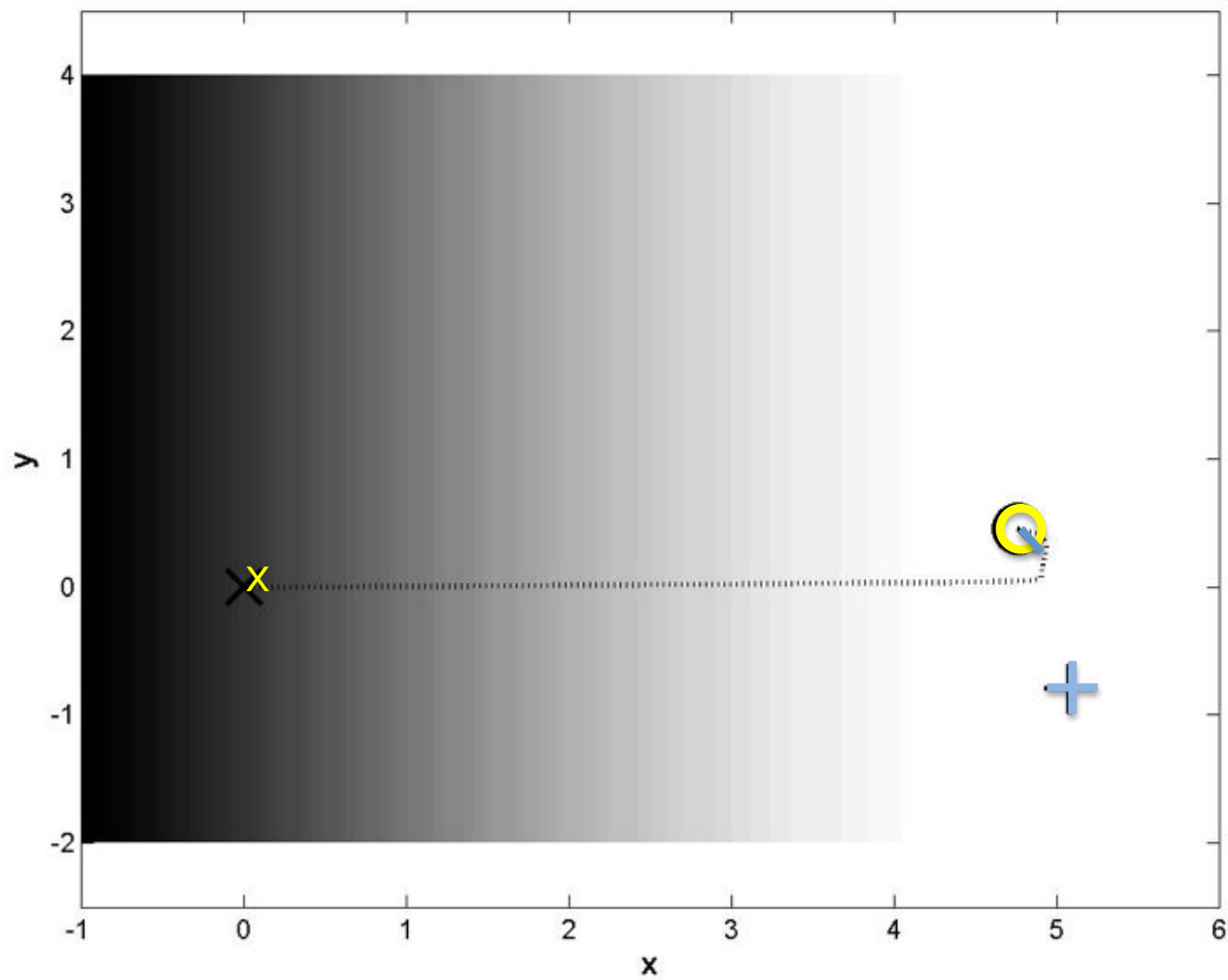
# Replanning: light-dark problem

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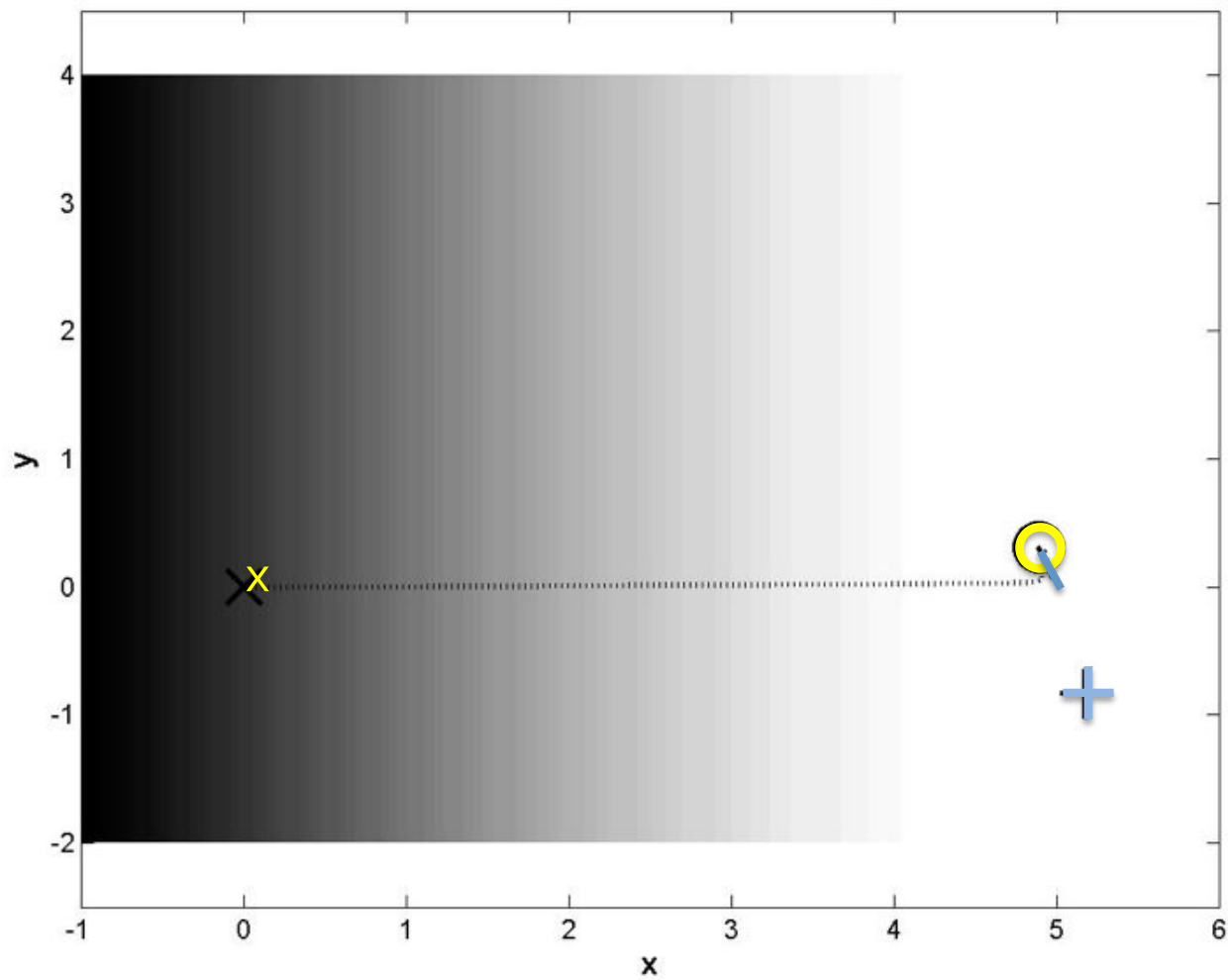
# Replanning: light-dark problem

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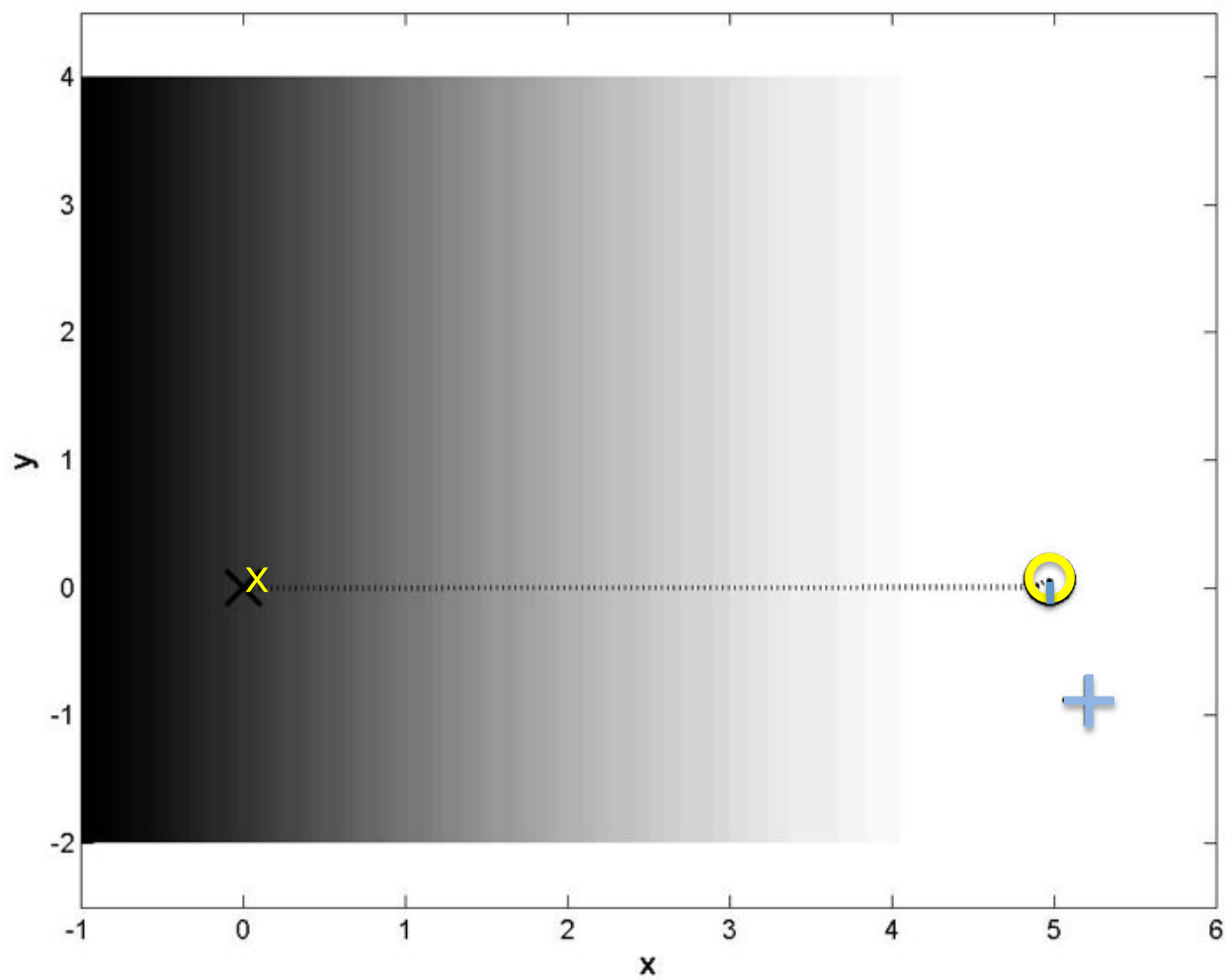
# Replanning: light-dark problem

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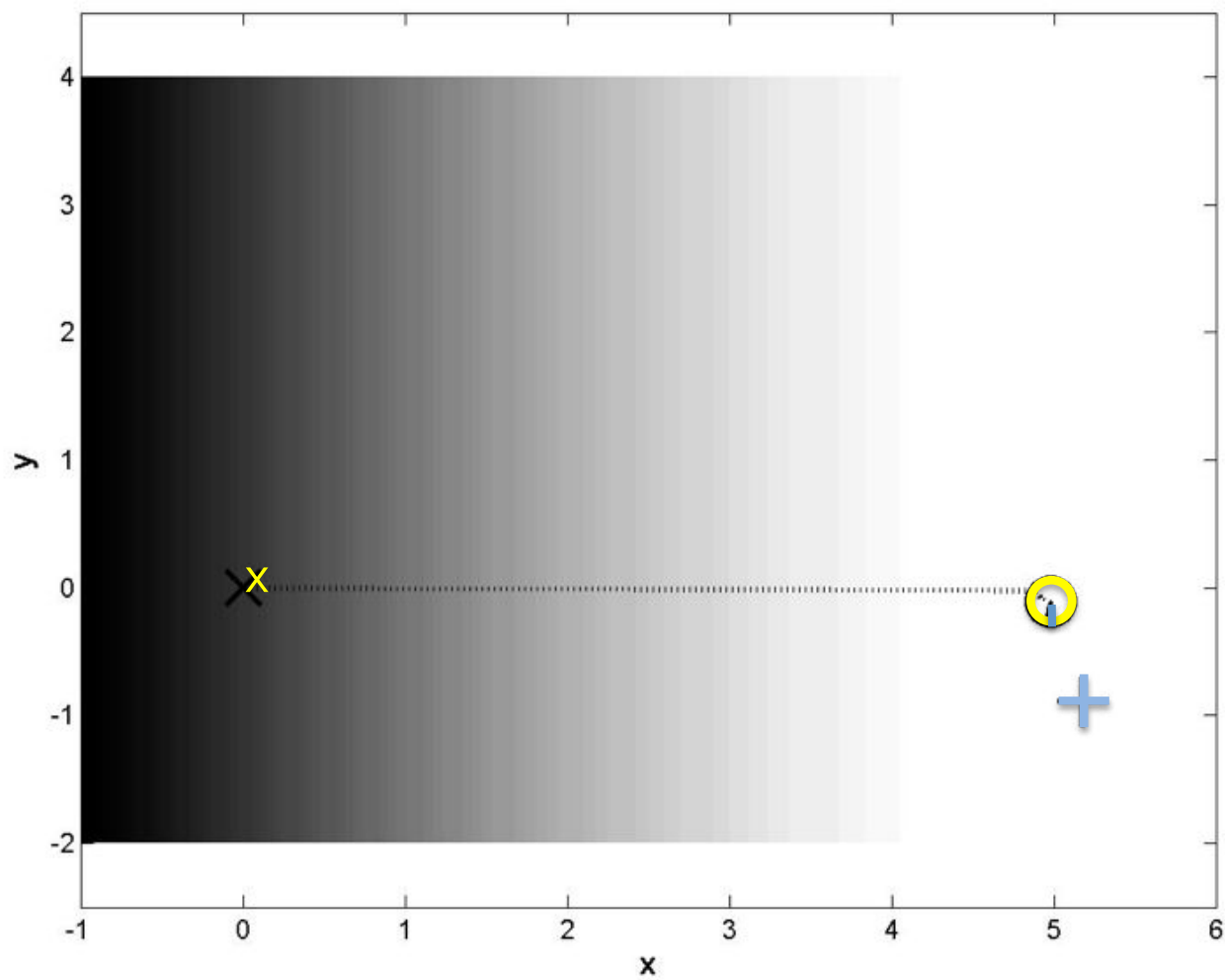
# Replanning: light-dark problem

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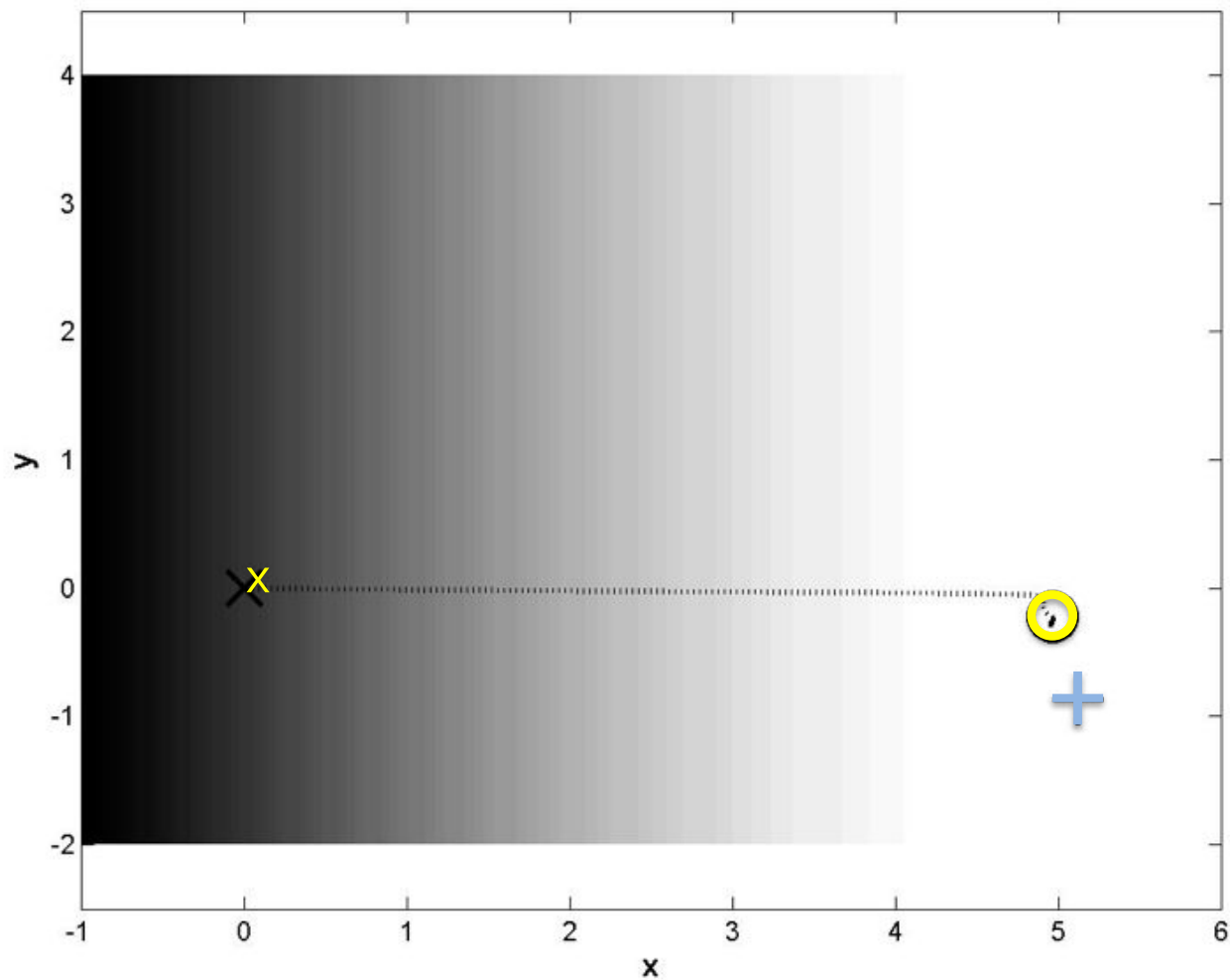
# Replanning: light-dark problem

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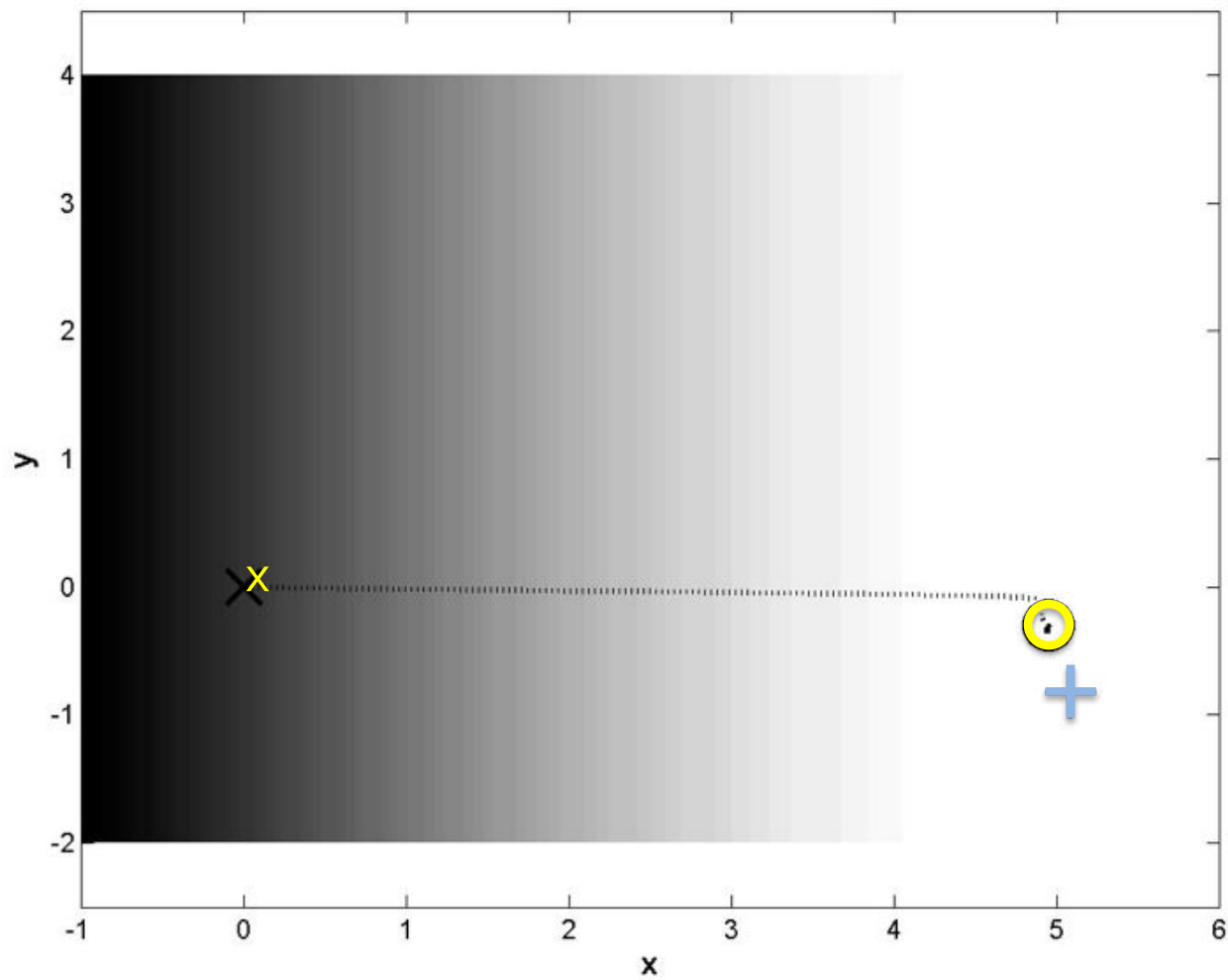
# Replanning: light-dark problem

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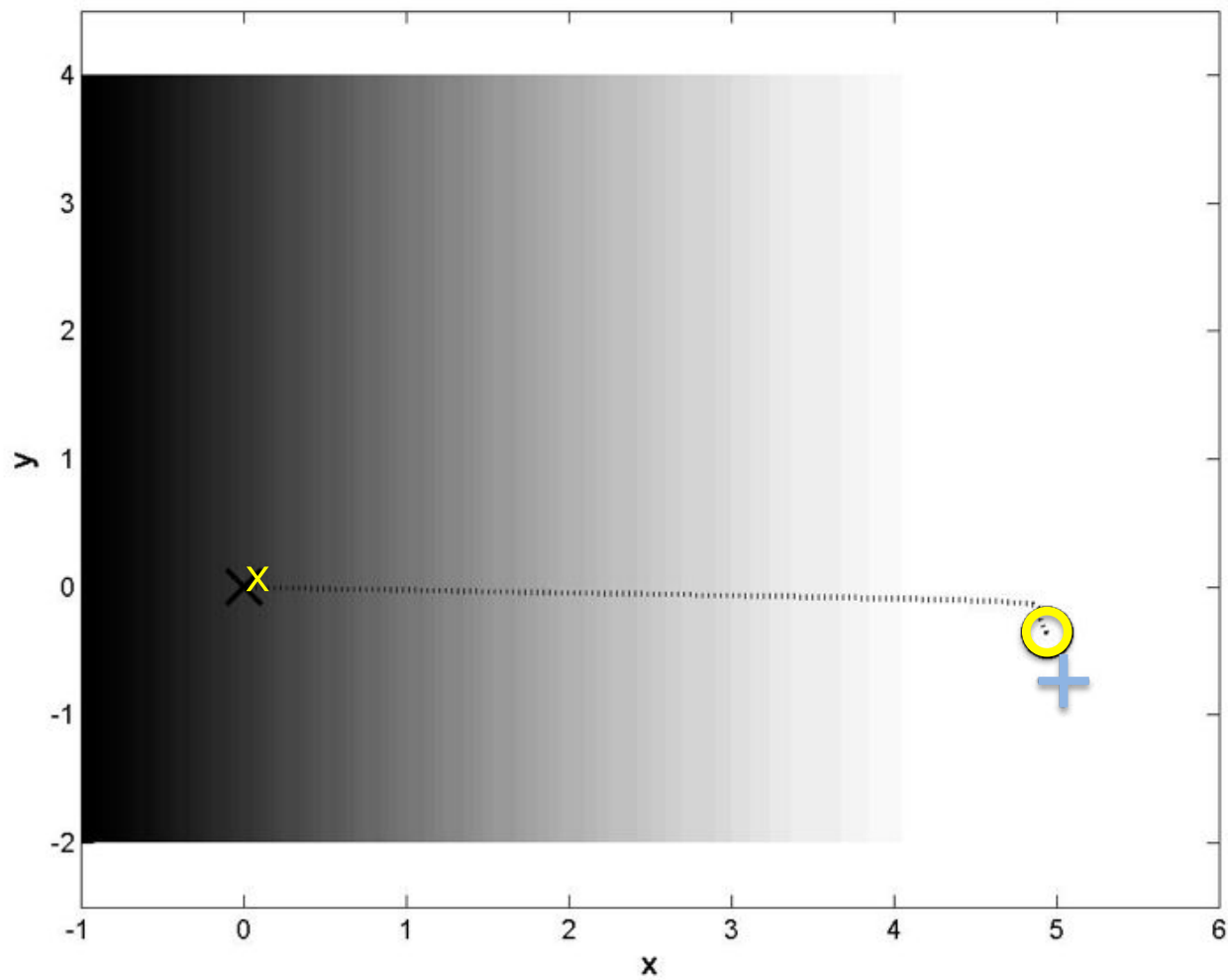
# Replanning: light-dark problem

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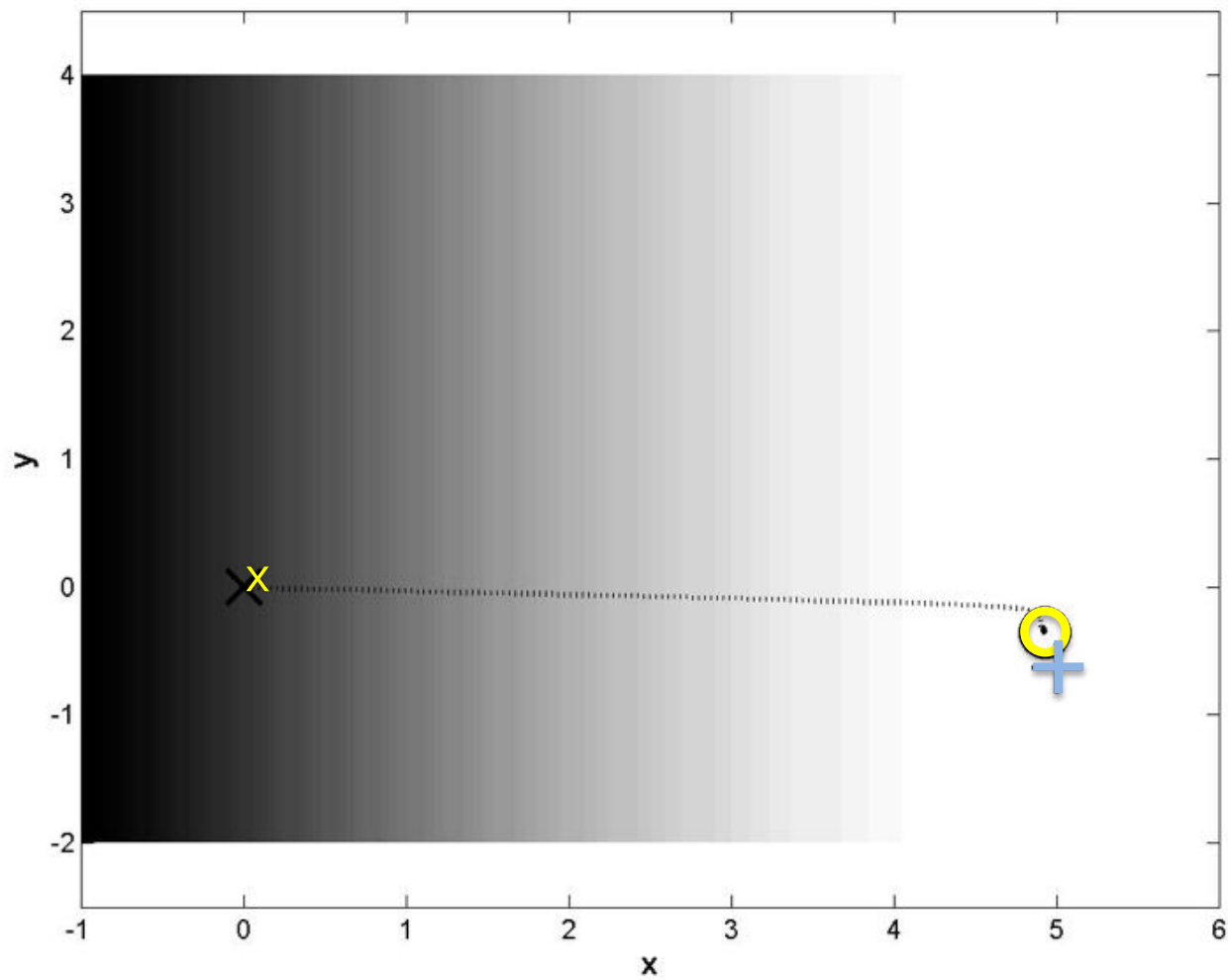
# Replanning: light-dark problem

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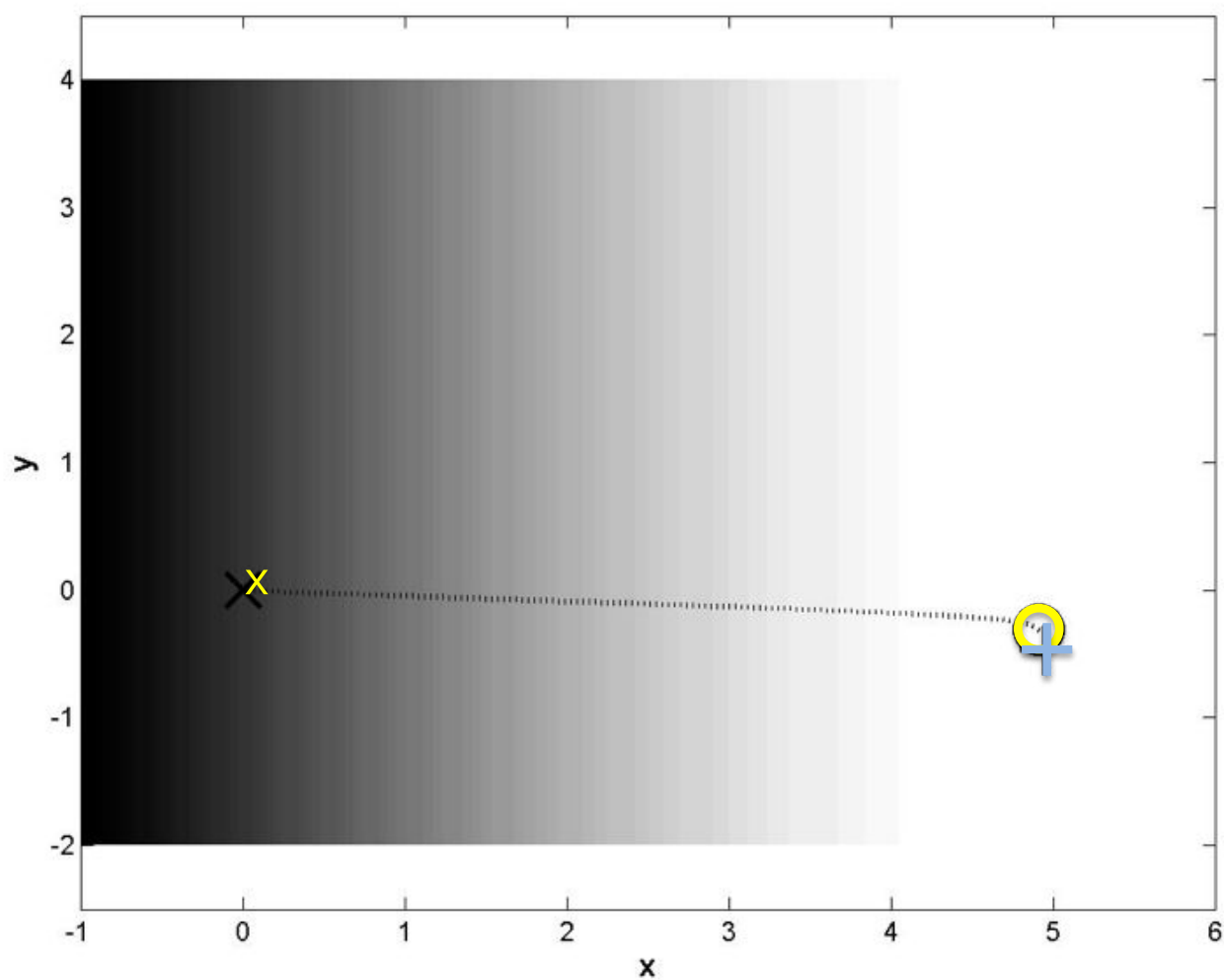
# Replanning: light-dark problem

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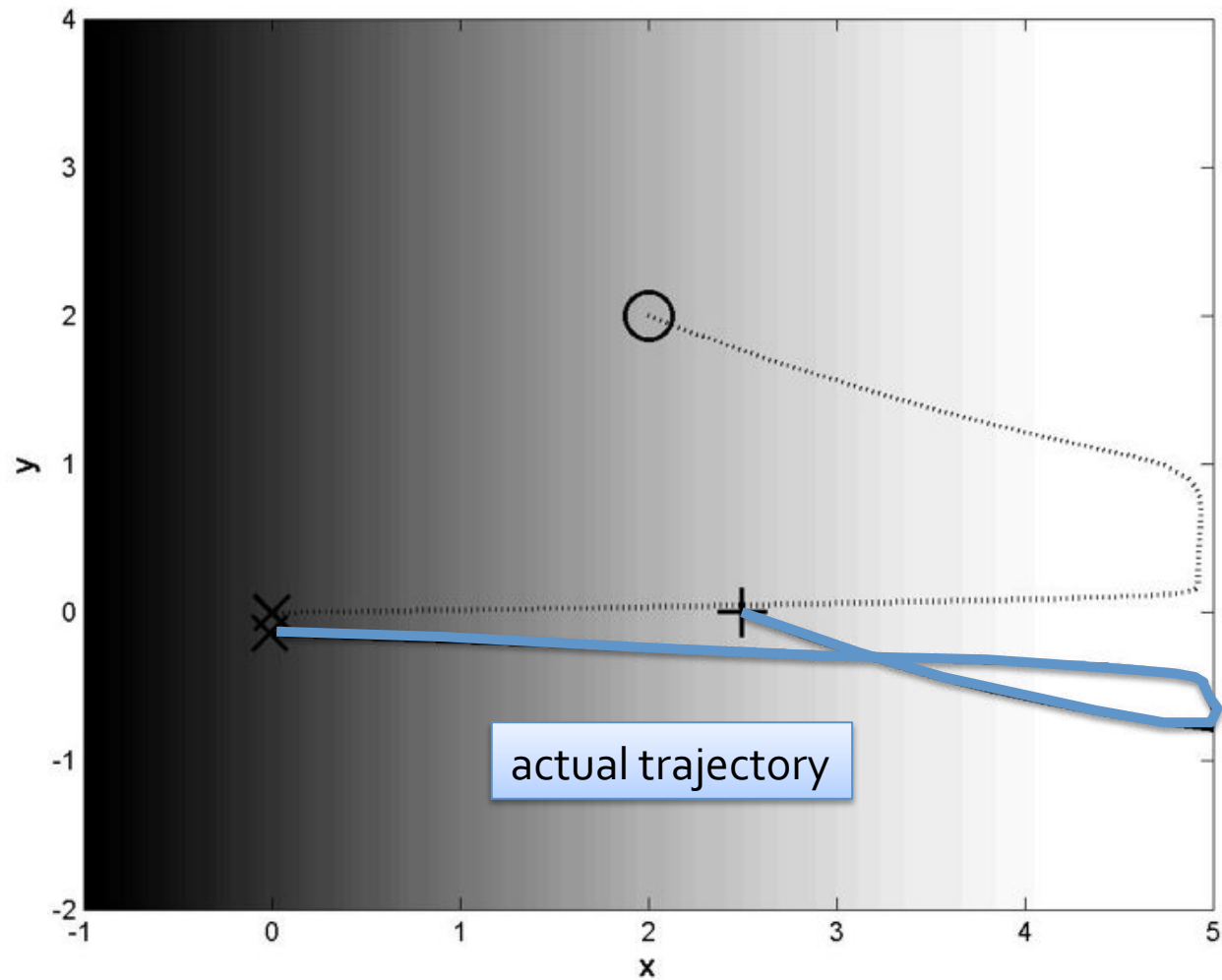


# Replanning: light-dark problem

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# Replanning: light-dark problem



# Optimistic (re)planning in belief space

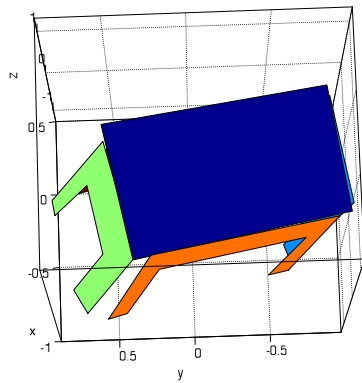
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- **control with state-dependent observation noise:**  
continuous state, action, observation spaces
- **robot grasping with tactile sensing:**  
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- **household robot with local observation:**  
mixed continuous and relational spaces

# Goal: pick up object of known shape with specific grasp

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Visual localization and detection works moderately well...



Joint work with Kaijen Hsiao and Tomás Lozano-Pérez

Leslie Pack Kaelbling, AAAI2010

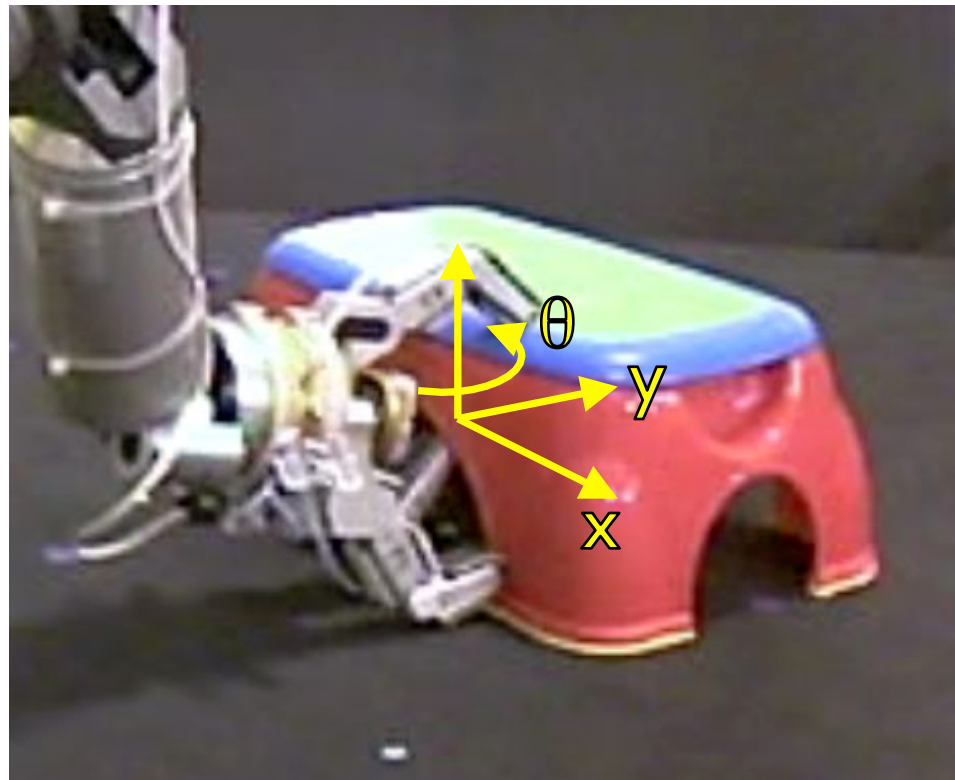
# Hypothesis space

Robot pose:

- 11 DOF
- model as fully observable

Object pose:

- 3 DOF
- model as partially observable



State estimate: probability distribution over object pose

# Macro actions

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Execute a trajectory:

- stop moving arm if any contact is felt
- close each finger until it makes contact

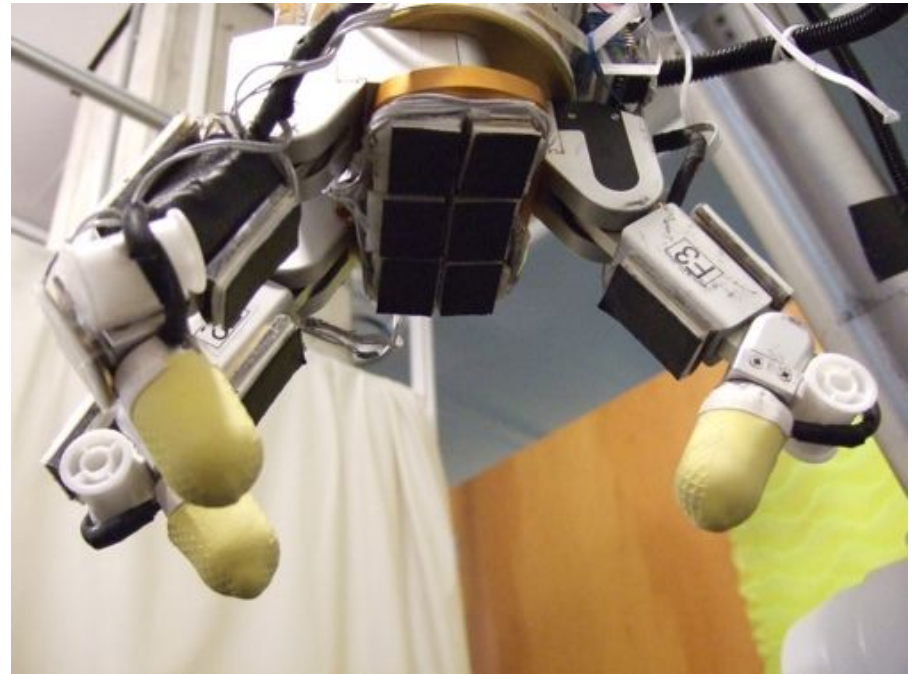


Fixed set of parameterized trajectories, always executed with respect to most likely state

# Observations

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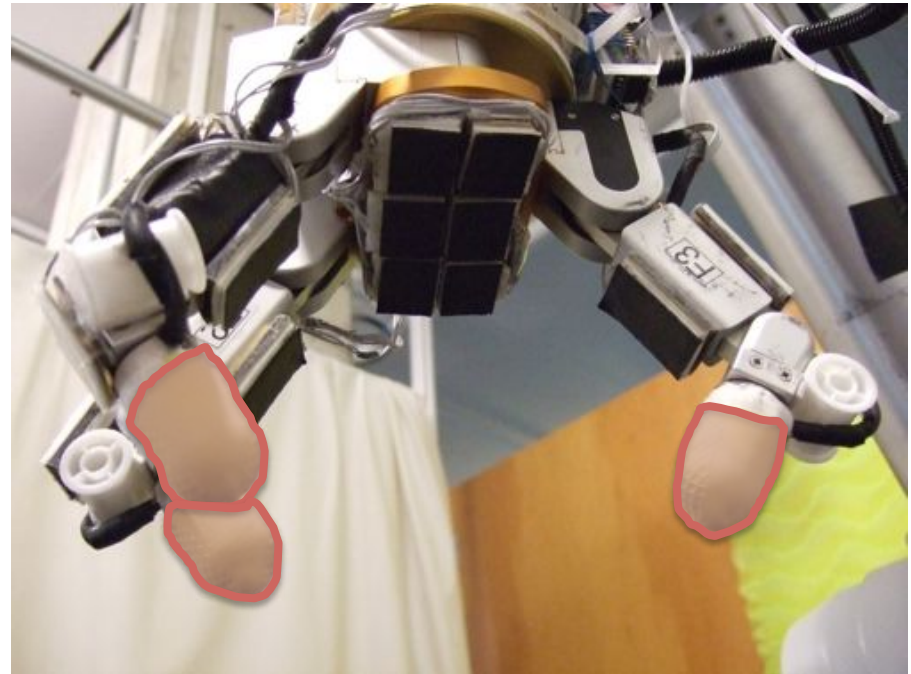
- Arm trajectory according to proprioception



# Observations

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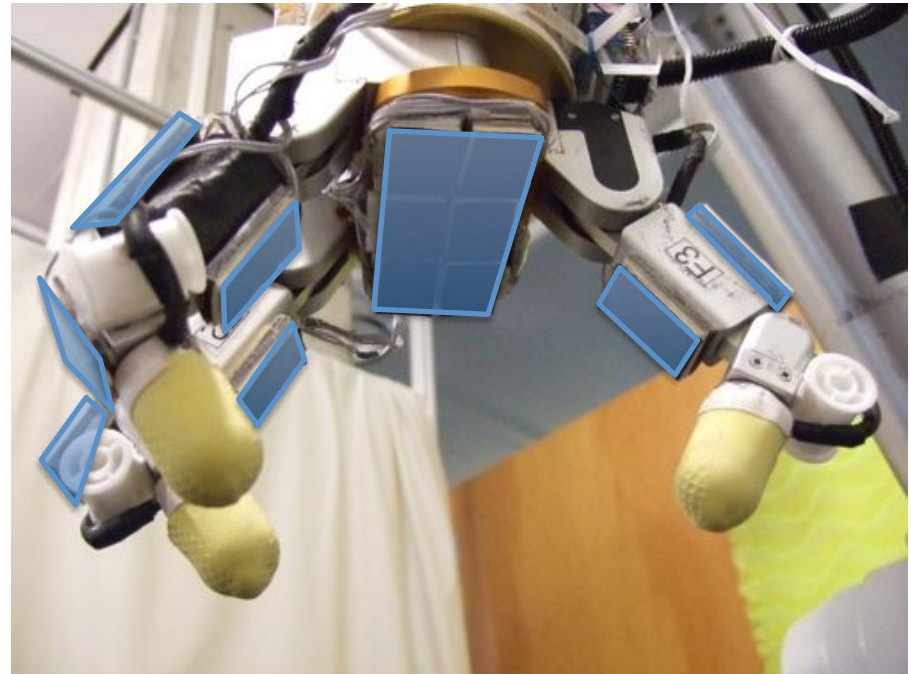
- Arm trajectory according to proprioception
- 6-axis force-torque sensors on fingertips



# Observations

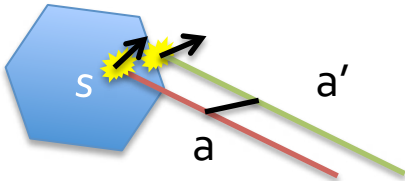
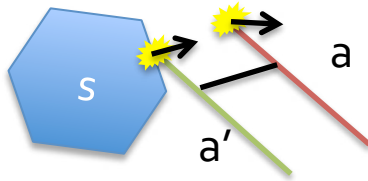
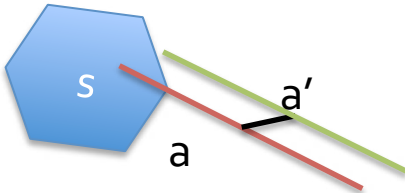
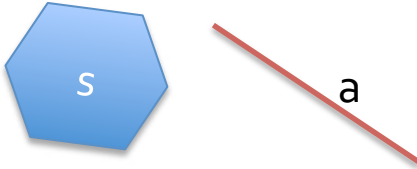
---

- Arm trajectory according to proprioception
- 6-axis force-torque sensors on fingertips
- Binary contact sensors



# Observation model: $\Pr(o \mid s, a)$

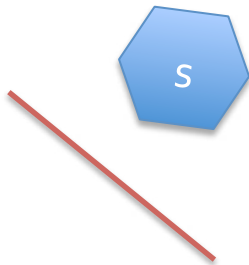
## Nominal observation for $s, a$ : $o^*$

		Contact	no contact
Actual $o$	Contact	<p>Gaussian density on dist to closest <math>a'</math> that would not have caused interpenetration X</p> <p>Gaussian density on dist between contact positions and normals</p> 	<p>Gaussian density on dist to closest <math>a'</math> that would have caused contact X</p> <p>Gaussian density on dist between contact positions and normals</p> 
	no contact	<p>Gaussian density on dist to closest <math>a'</math> that would not have caused contact</p> 	<p>Max value of Gaussian density used for nominal contact case</p> 

# Transition model: $\Pr(s_{t+1} \mid s_t, a_t)$

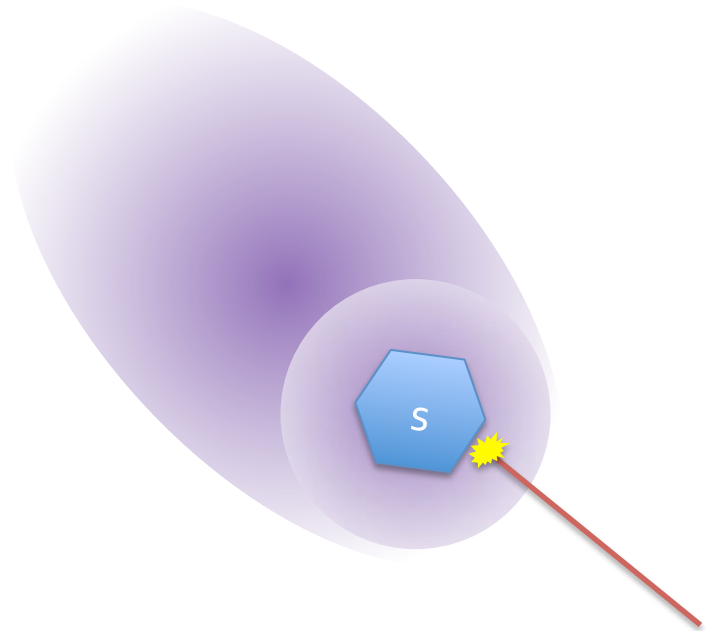
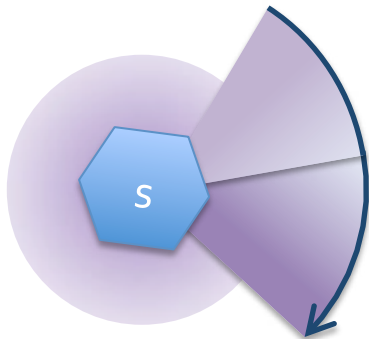
---

**No contact:** no change



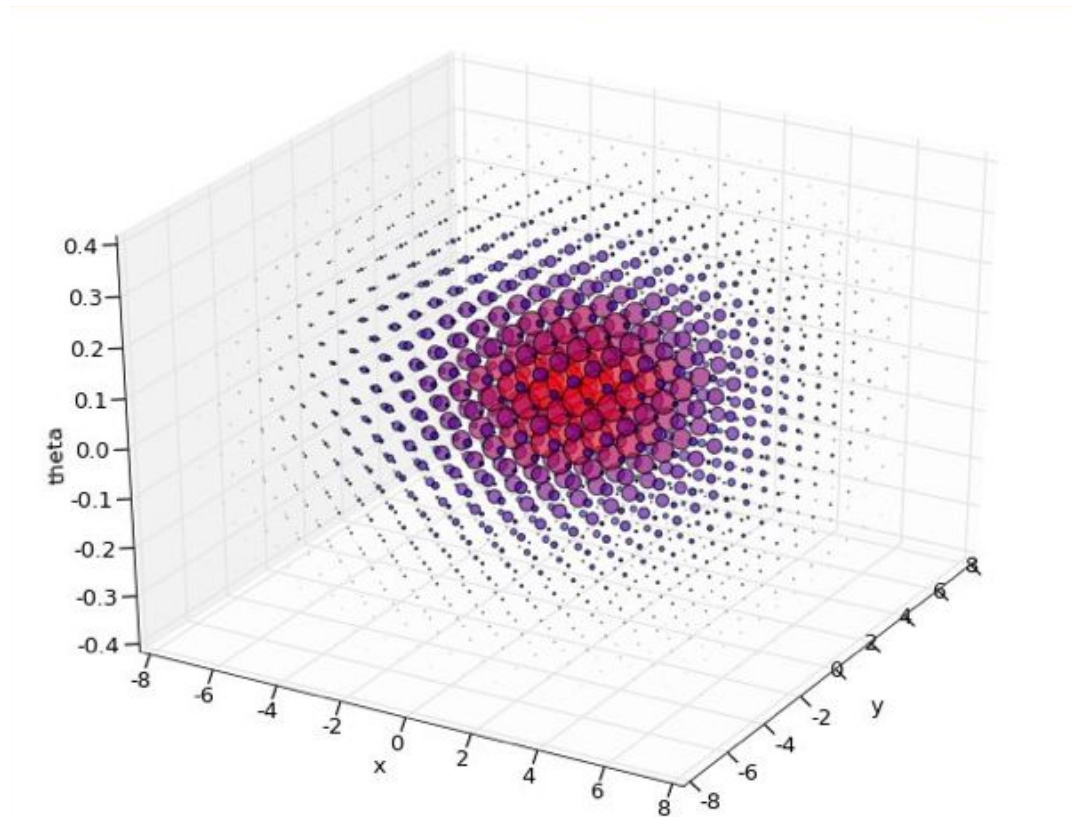
**Contact:** probability of being bumped depends on observation

**Reorientation:** similar to contact with large rotational variances



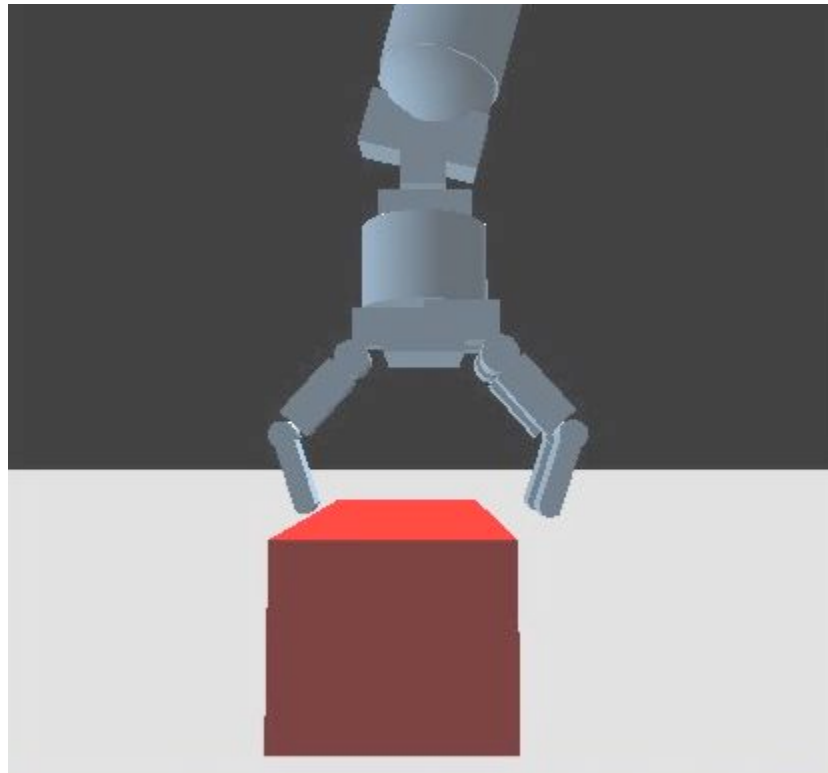
# Initial belief state

---



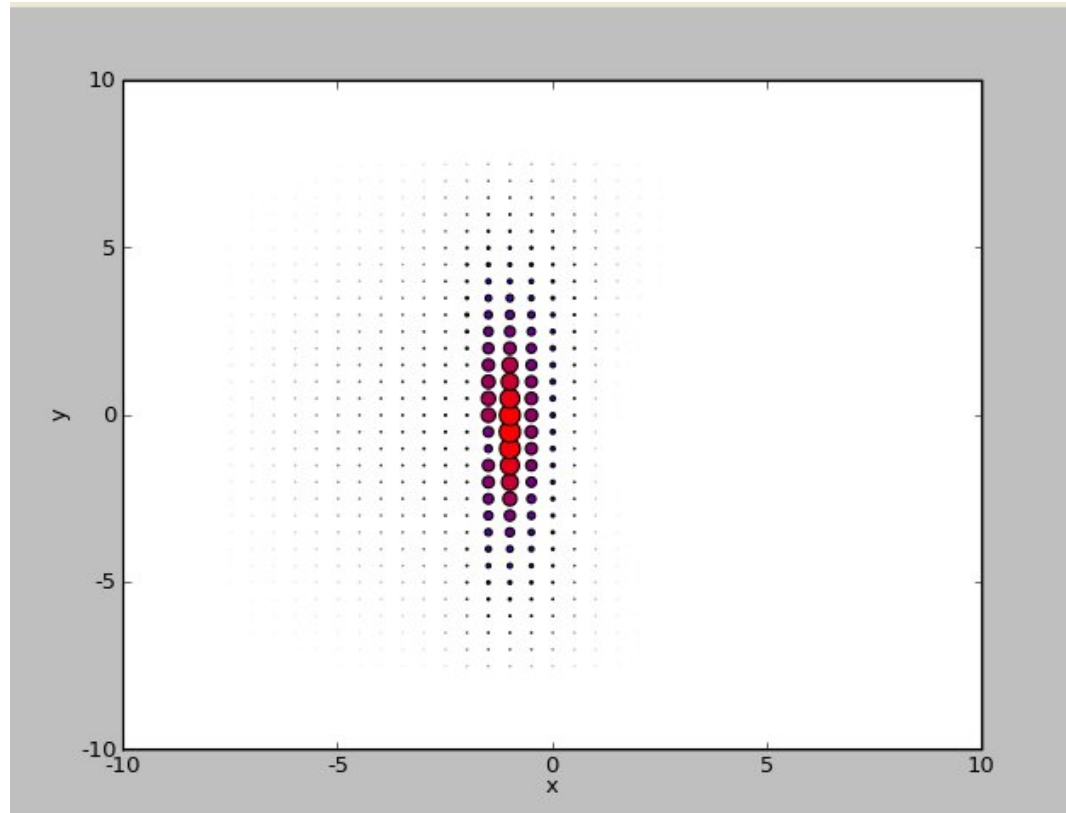
# Tried to move down — finger hit corner

---



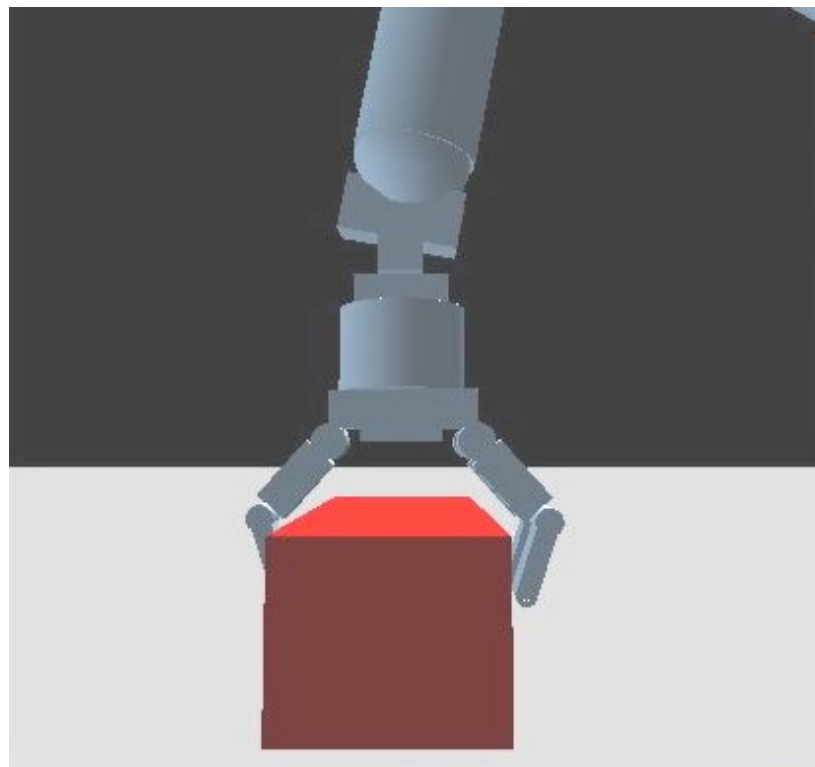
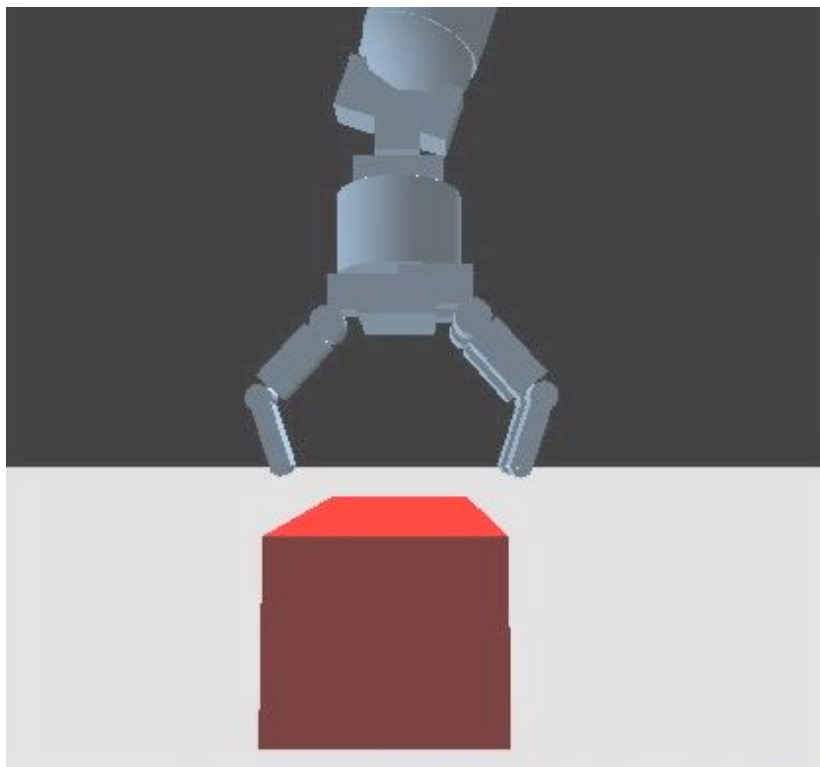
# Updated belief

---



## Another grasp attempt

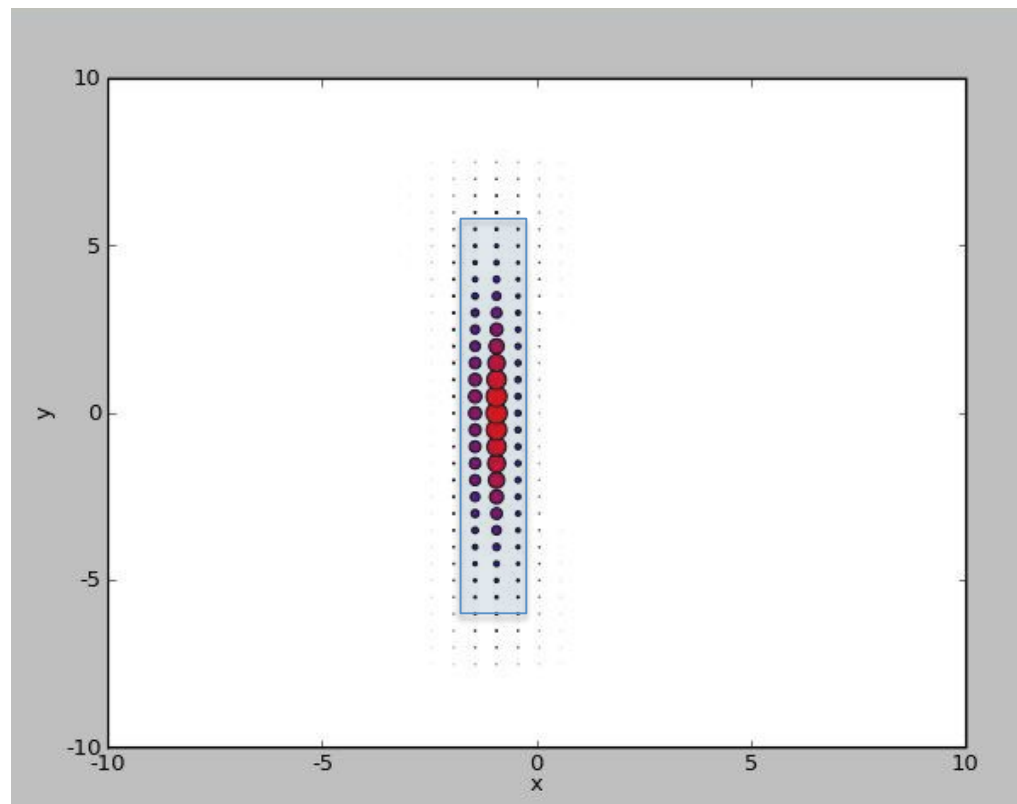
---



# Goals in belief space

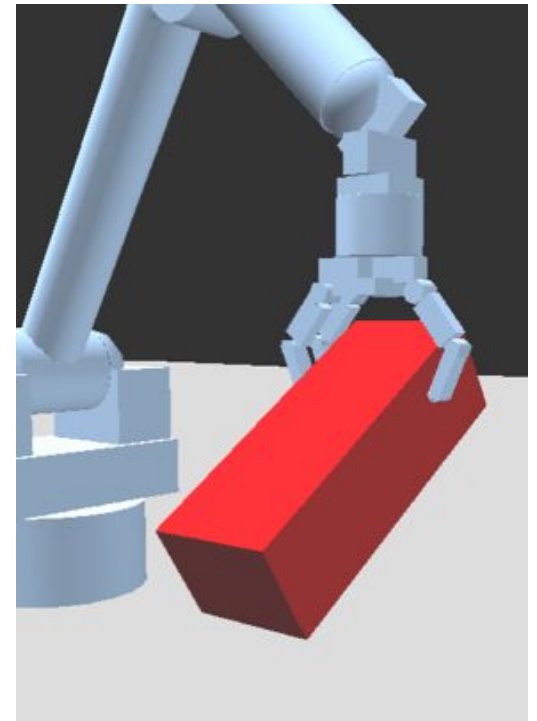
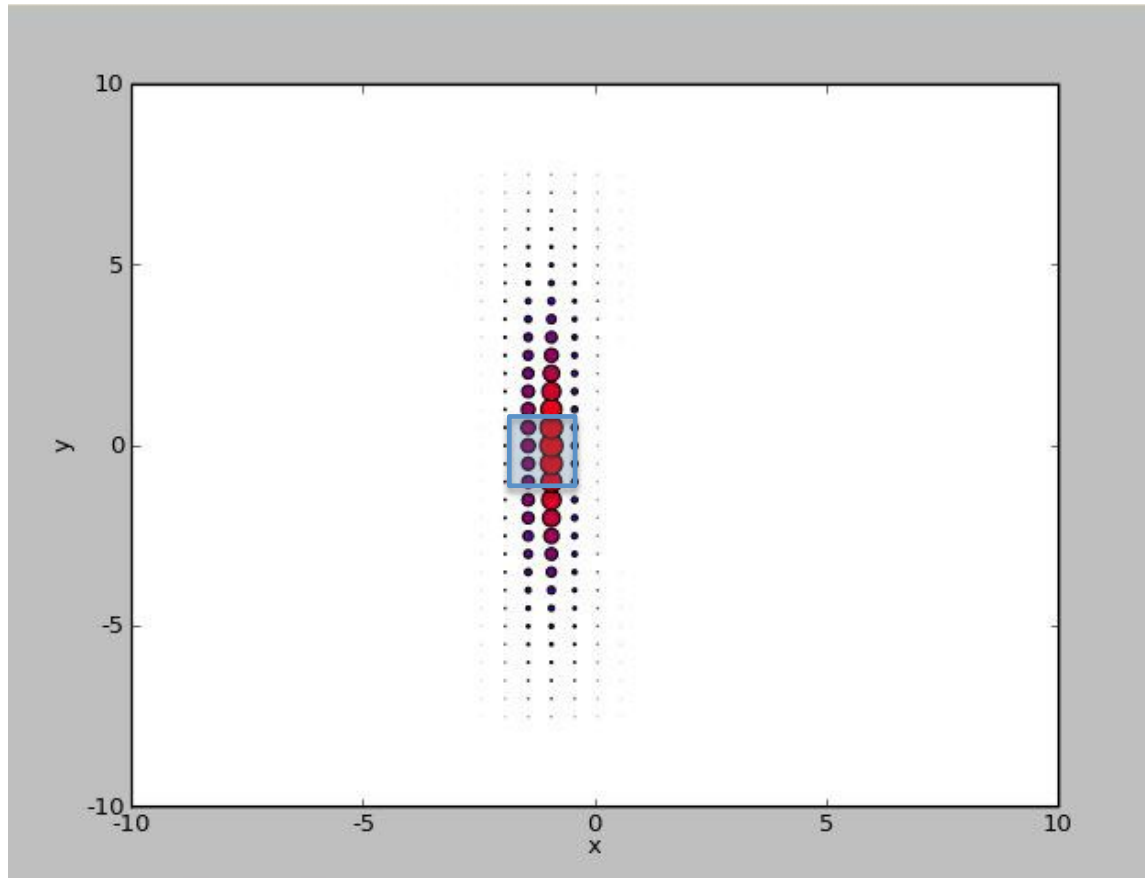
---

- Specify set of desirable ranges in  $X, Y, \Theta$
- Satisfied if probability that the pose is in that set is high



# What if Y coordinate of grasp matters?

---



# Action selection

---

How to select among the actions?

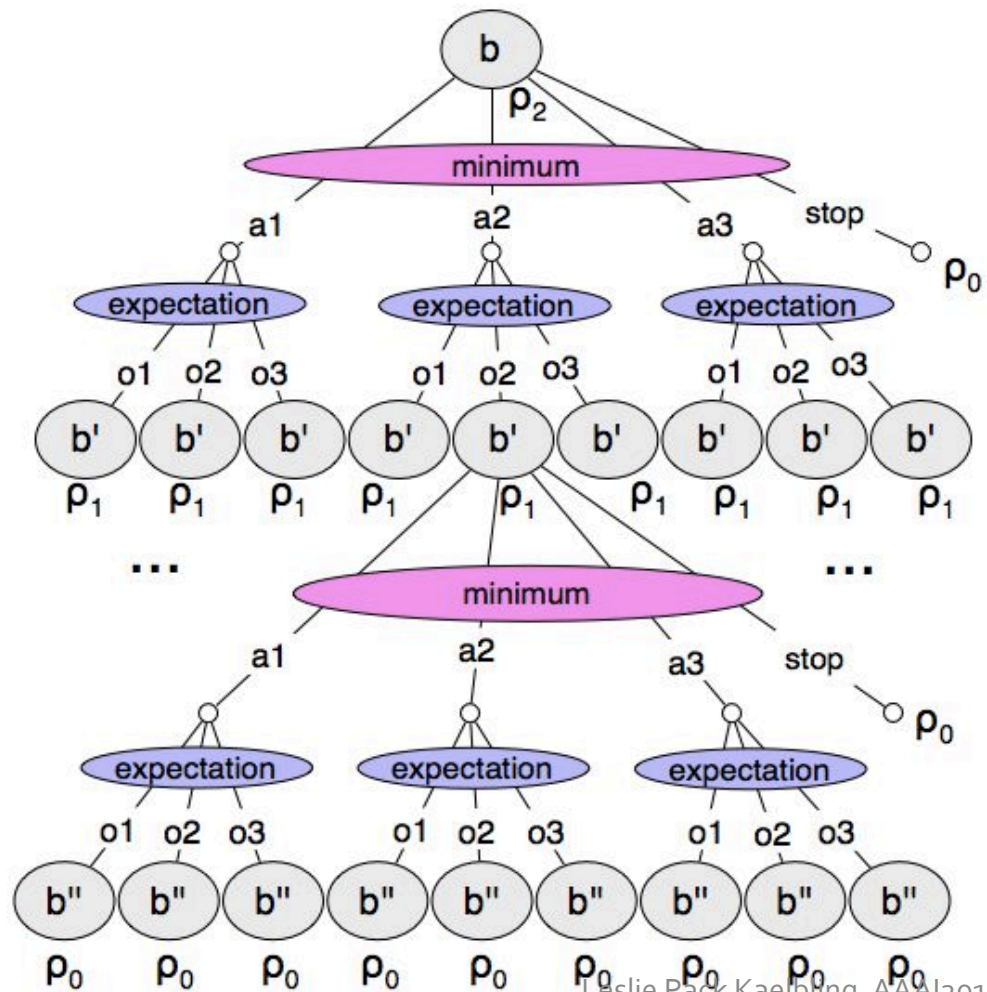
- Until probability of failure given belief is  $< \epsilon$ 
  - Select WRT by searching forward from belief
  - Execute WRT, and get observations  $o$
  - Update belief

WRTs include:

- target grasp
- information-gain trajectories
- re-orientation

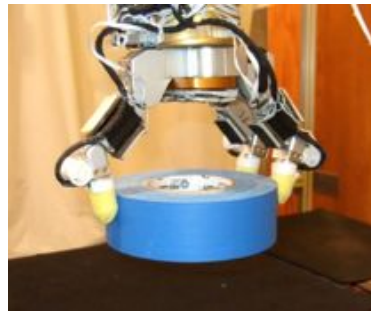
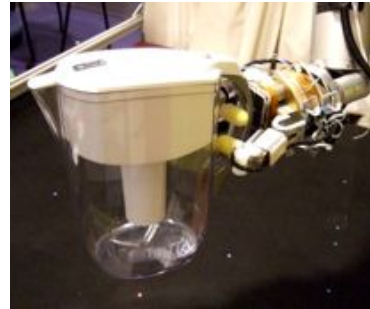
# Forward search

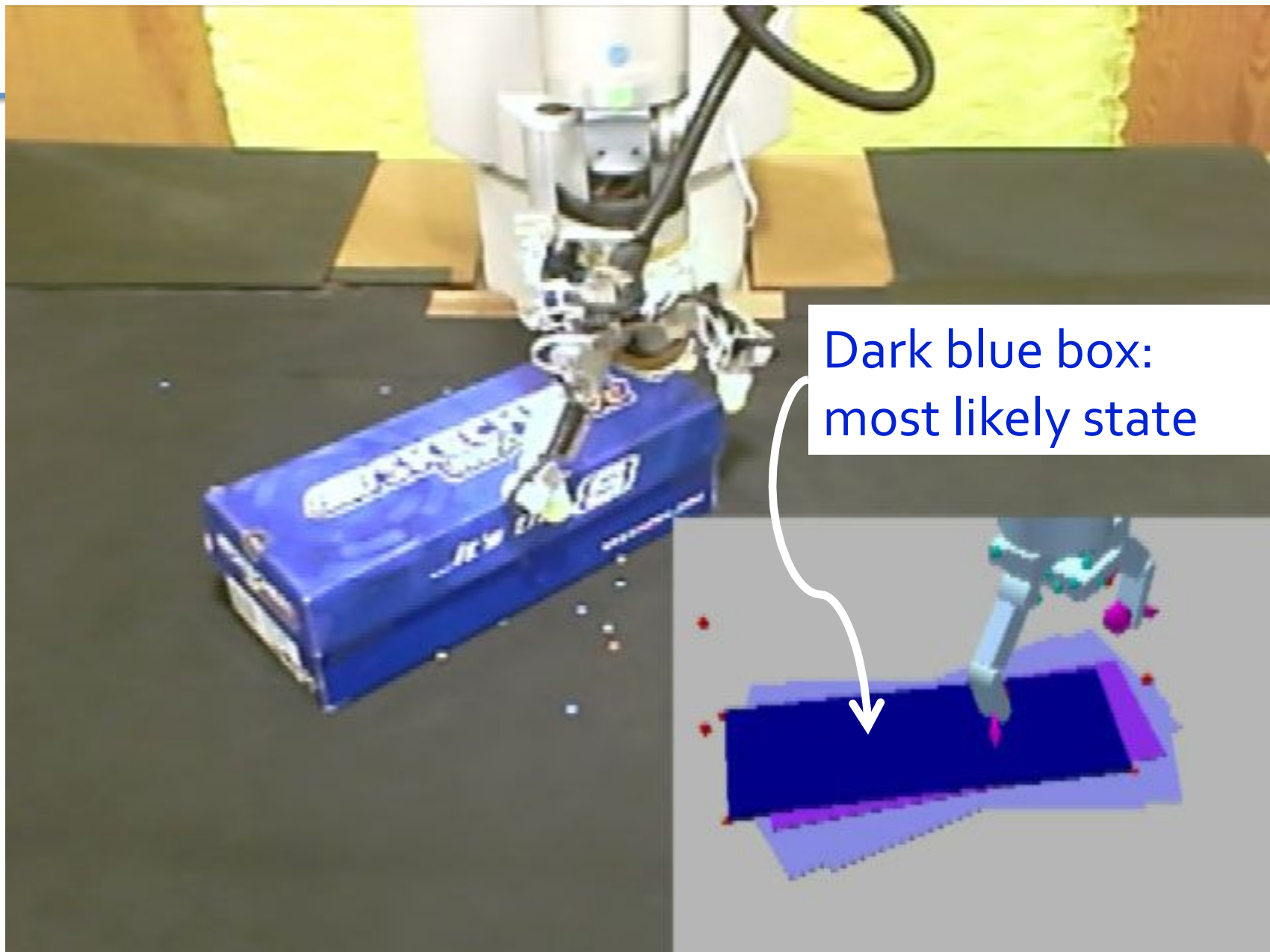
- Compute k-step risk using backward induction
- Prune and cluster to decrease observation branching
- Depth 2 sufficed in our problems
- Risk at leaves is likelihood of failure of target grasp



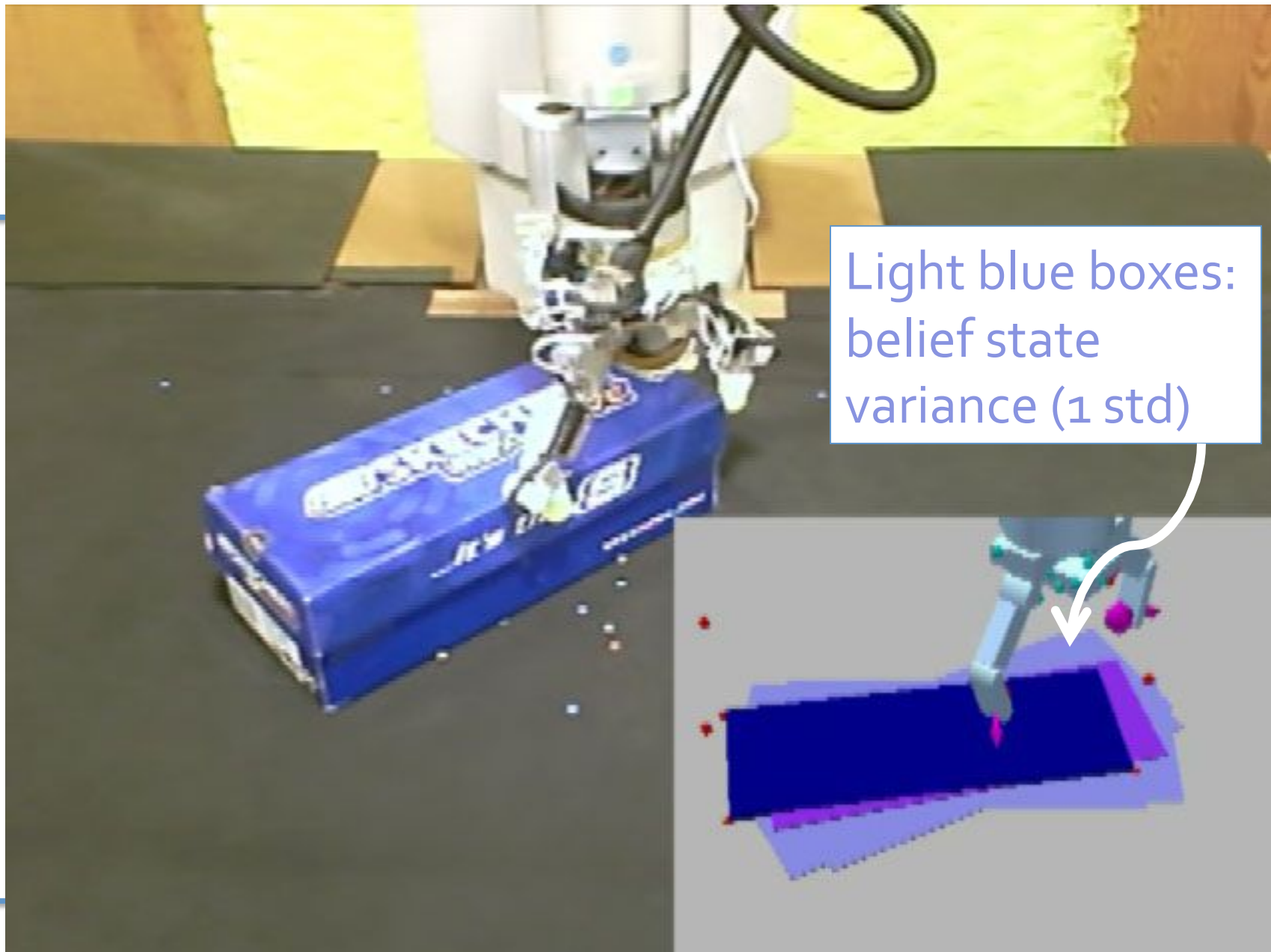
# Objects and desired grasps

---





Dark blue box:  
most likely state



Brita results: 10 / 10 successful grasps

---

Grasping a  
Brita Pitcher  
50x  
Low deviation

# Powerdrill: 10 / 10 successful grasps

---




25x  
speed

# Optimistic (re)planning in belief space

---

- **control with state-dependent observation noise:**  
continuous state, action, observation spaces
- **robot grasping with tactile sensing:**  
continuous state, action, observation spaces
- **household robot with local observation:**  
mixed continuous and relational spaces

## Classes of robotics problems in which:

- Problems are huge:
    - long horizon
    - many continuous dimensions
    - combinatoric discrete aspects
  - No terrible outcomes
  - Geometry is not intricate
  - Partial observability:  
local but fairly reliable
- 
- A wooden spice rack filled with various jars of spices, illustrating the complexity of the problem space. The rack is made of light-colored wood and has several circular compartments, each holding a small jar with a label. The jars are of different sizes and colors, and some are open, showing the spices inside. The background is dark, making the wooden rack and the jars stand out.



Joint work with Tomás Lozano-Pérez

# Symbols to Angles

Initial state known in geometric detail



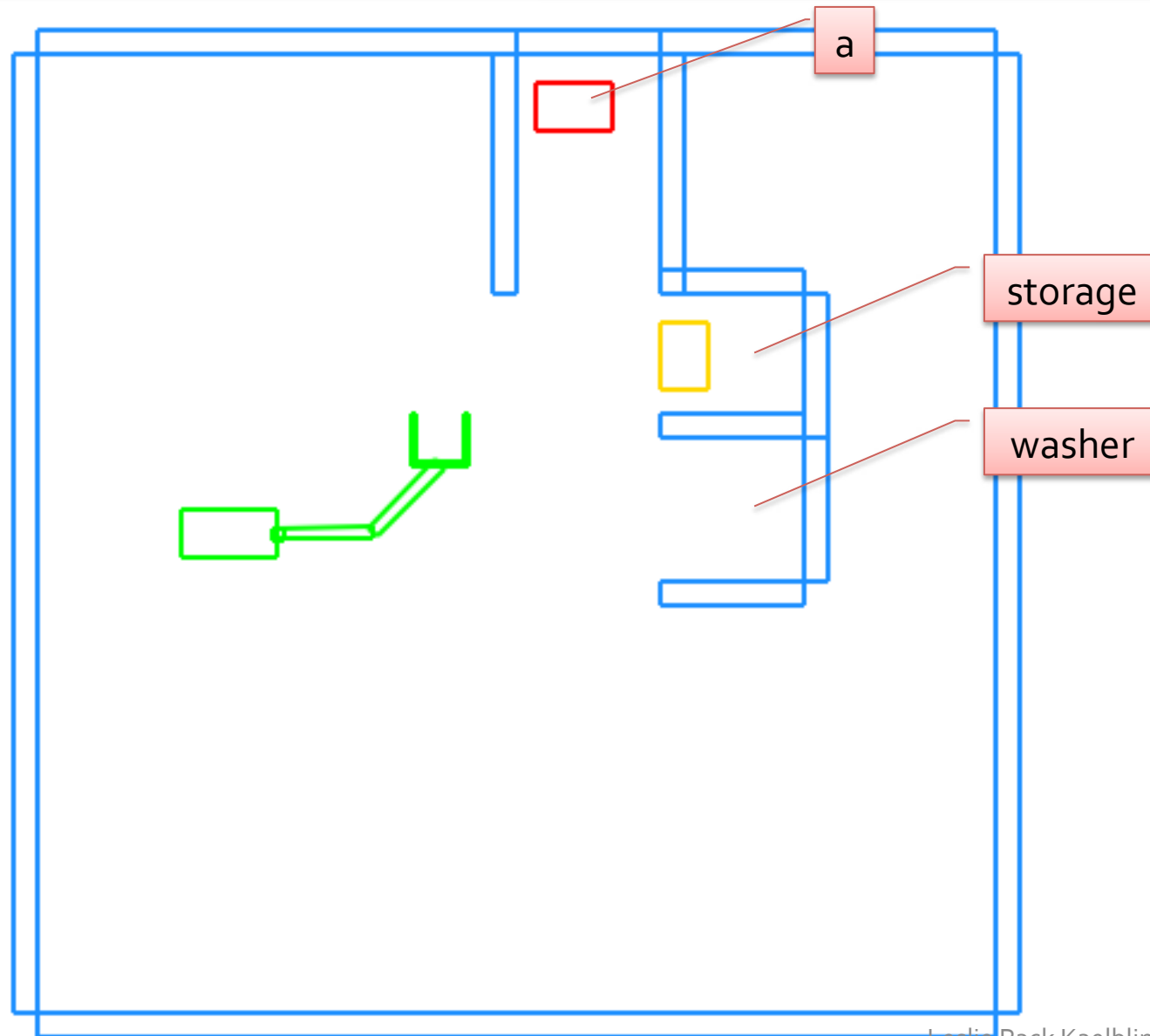
Goal set is abstract, symbolic

$tidy(house) \wedge charged(robot)$

Operator descriptions:

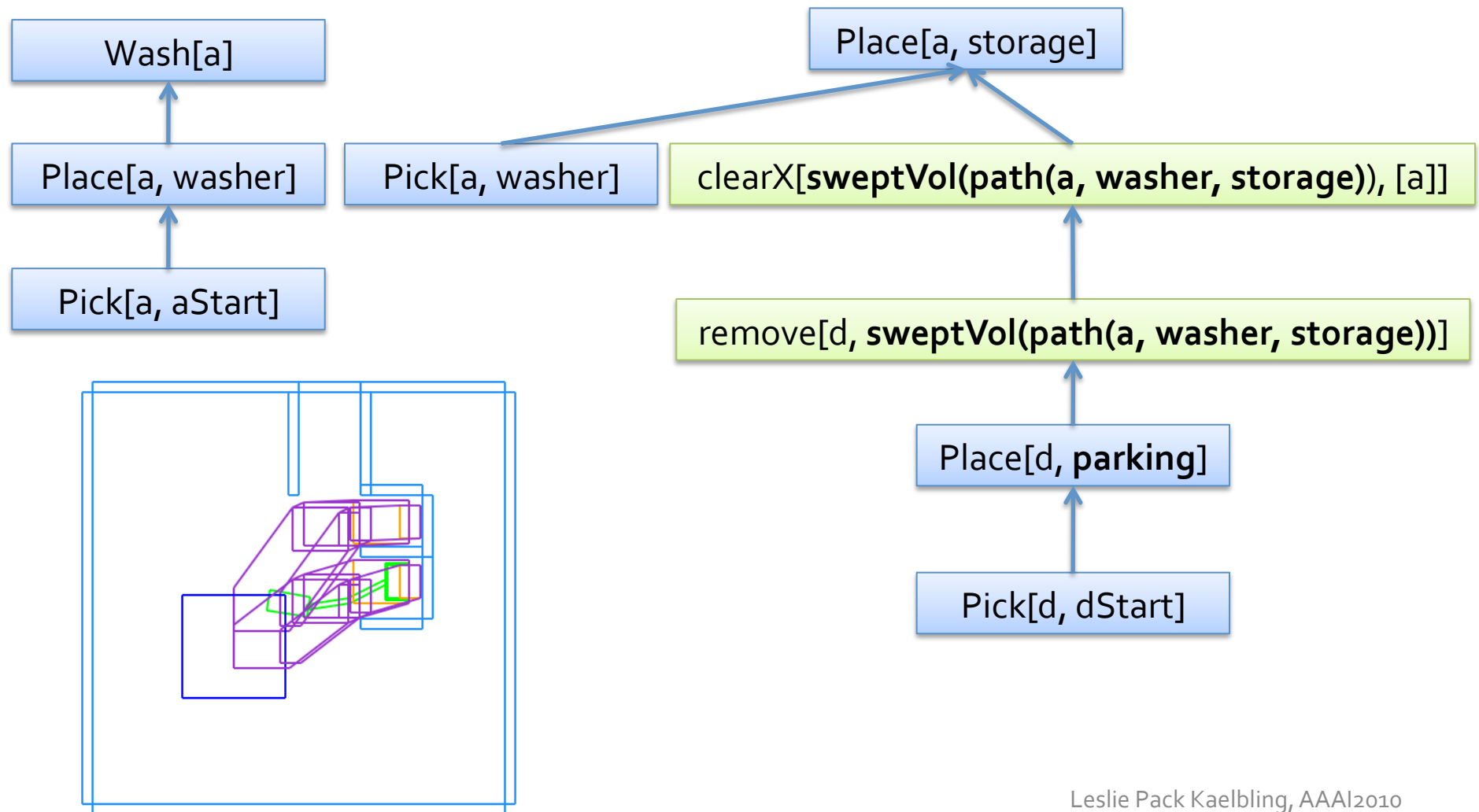
- STRIPS-like, with continuous values
- procedures suggest values for existential vars
- geometric reasoning

# Wash a block and put it away



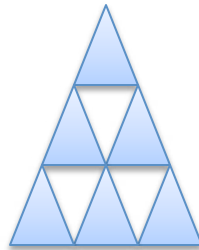
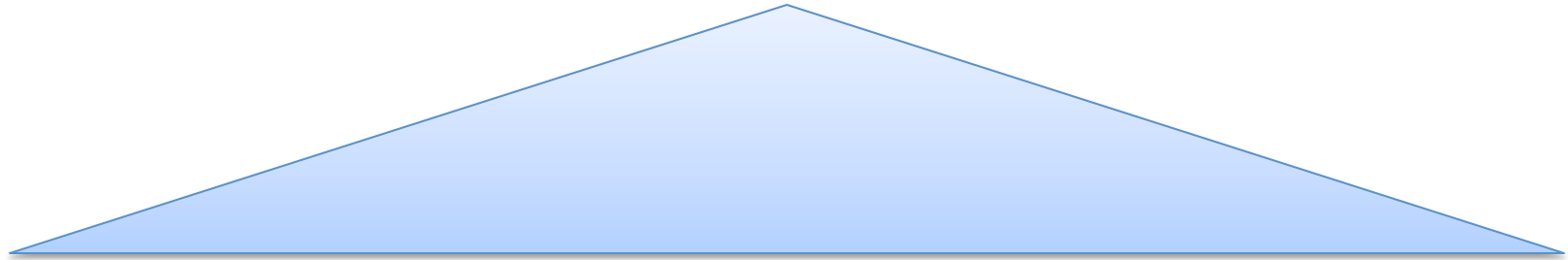
# Clean(a) and In(a, storage): Regression structure

7 primitive steps; 3000 search nodes



# Hierarchy crucial for large problems

---



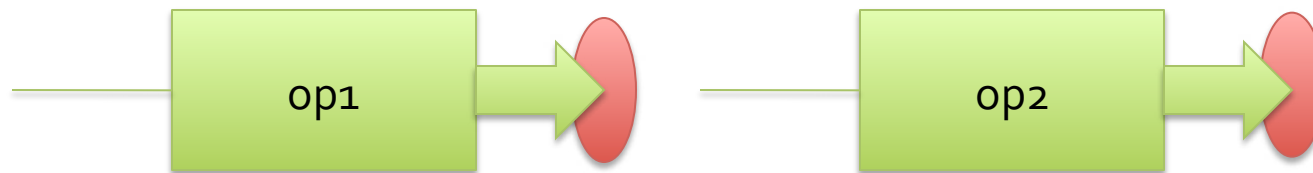
Subtrees represent **serialized subtasks**

# Hierarchical semantics

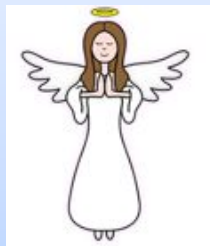
Subgoal is an abstract operator:



What does it mean to sequence two subgoals?



Depends on who gets to choose the outcome:



us



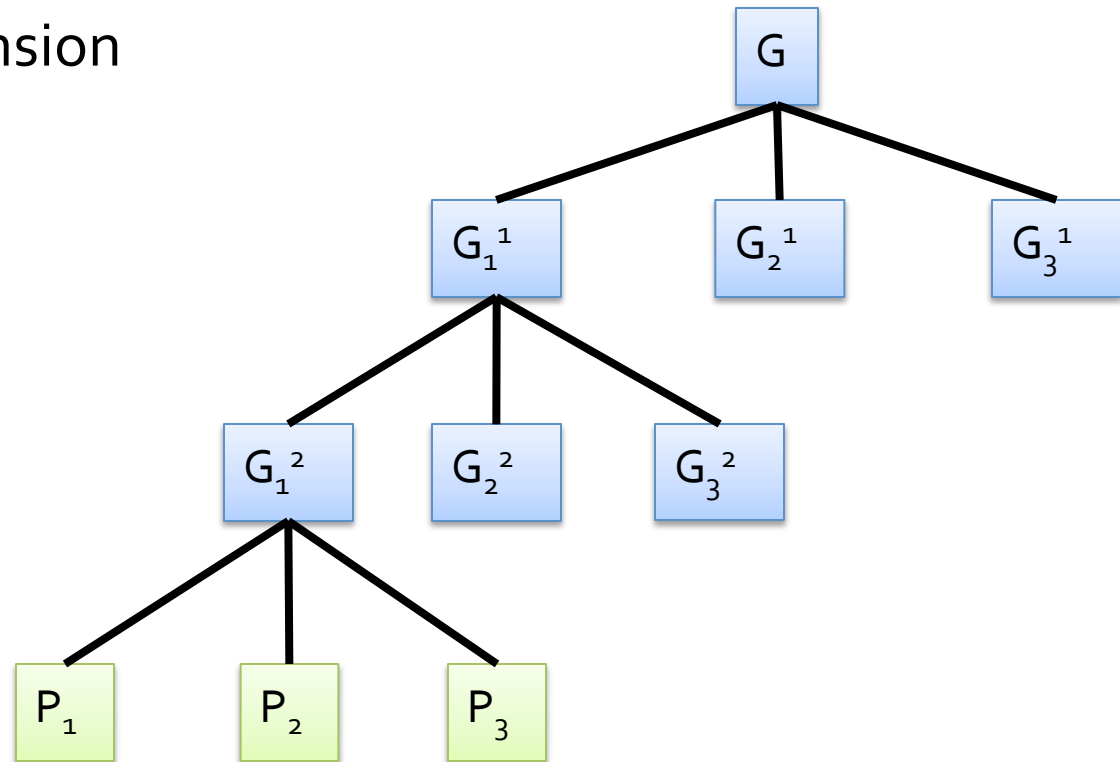
nature

Wolfe, Marthi, Russell

# Planning in the now

---

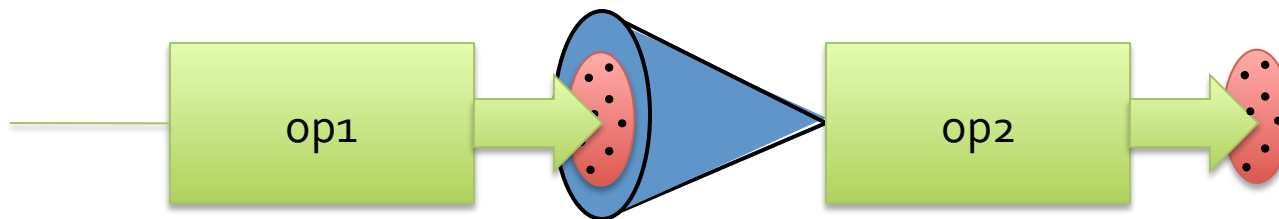
- maintain left expansion of plan tree
- execute primitives
- plan as necessary



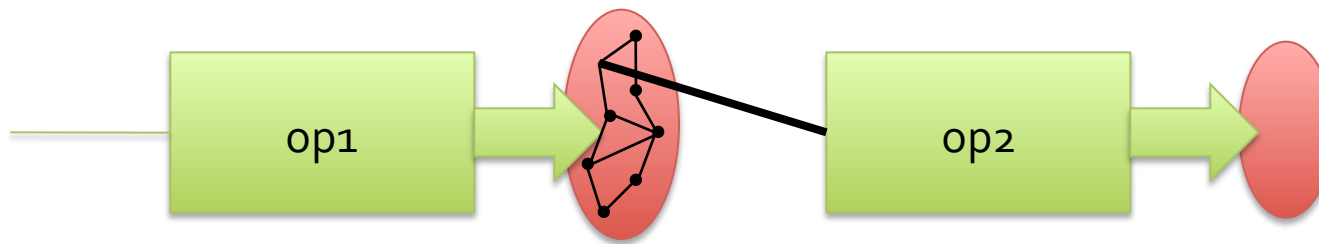
# Satanic semantics



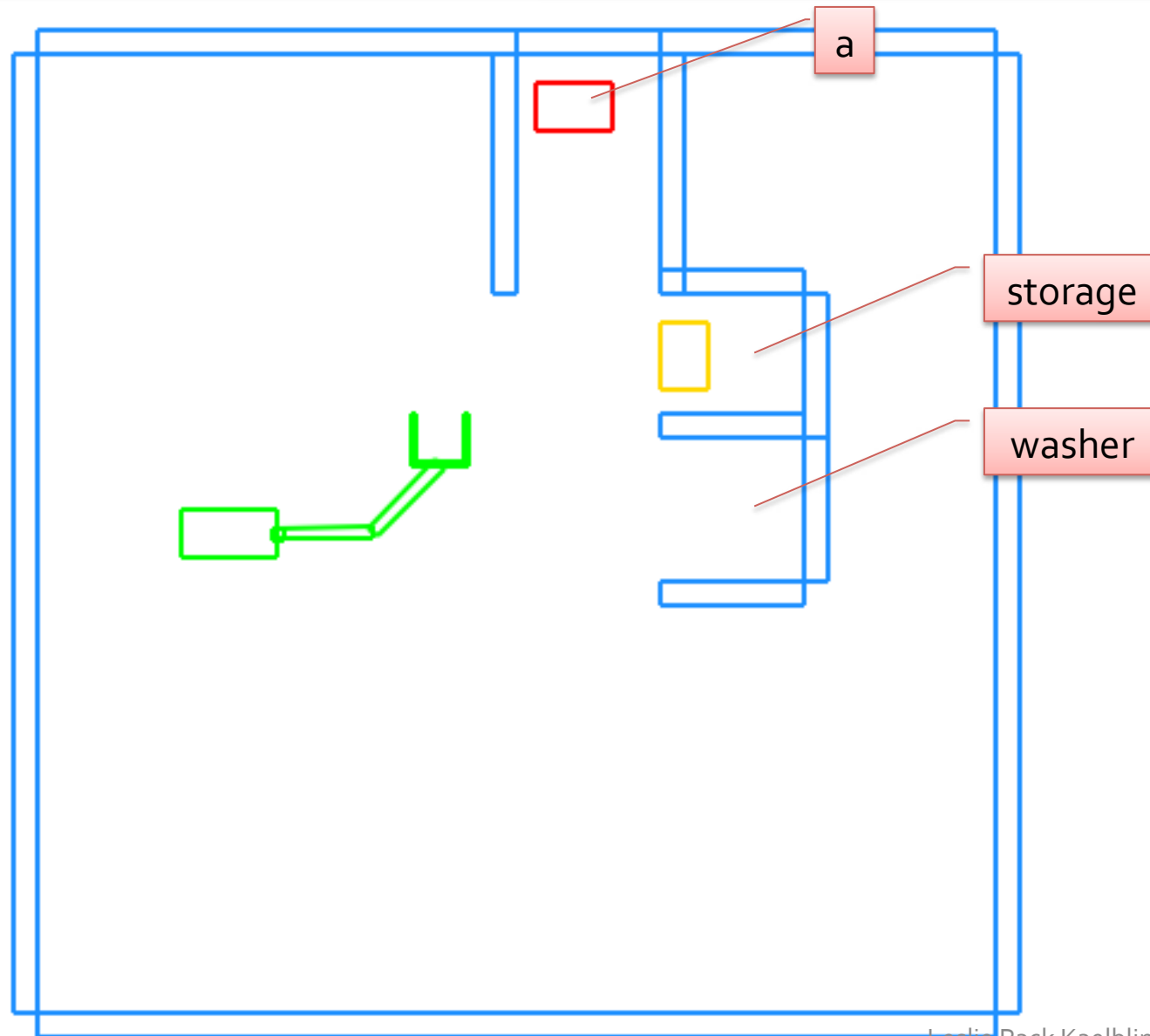
We have to handle any outcome the devil picks

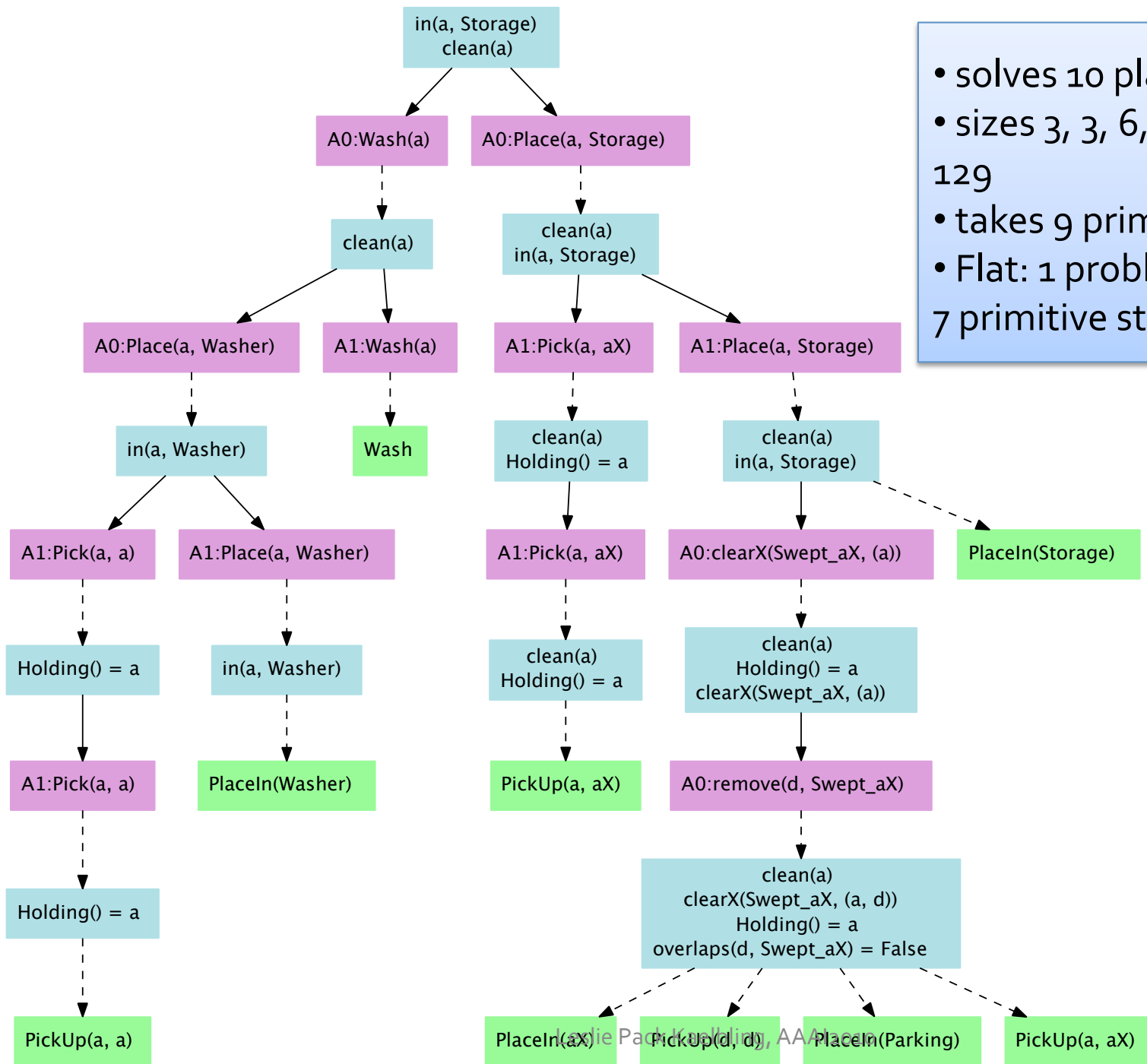


Okay if: Preconditions of op2 can be achieved from any state resulting from op1



# Wash a block and put it away





- solves 10 planning problems
- sizes 3, 3, 6, 5, 2, 7, 6, 8, 13, 129
- takes 9 primitive steps
- Flat: 1 problem, 3000 nodes, 7 primitive steps

# Planning in the Know

---

Plan in the **now in belief space**:

- Make a single plan that will succeed with high probability
- Replan on unexpected observations

Plan at the “**knowledge level**”

Moore;  
Petrack, Bacchus

- Traditional to plan in the powerset of the state space
- We have infinite state space
- Use explicit logical representation of knowledge and lack of knowledge

Plan at **level of abstraction** supported by current belief state

# Going on a tiger hunt

---

**move(Room):**

res: robotLoc = Room

**listen:**

pre: robotLoc = hall

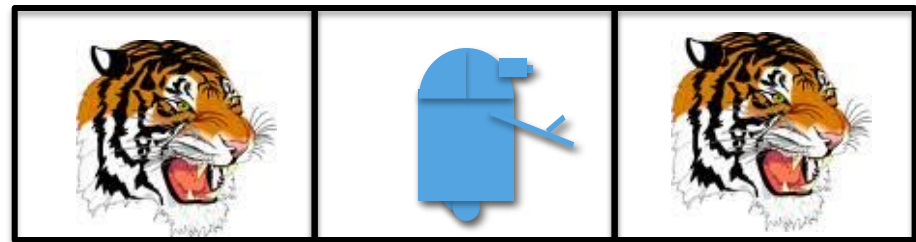
result: KV(tigerLoc)

**shoot:**

pre: robotLoc = tigerLoc

result: deadTiger

$P(\text{tigerLoc} = \text{leftRoom}) = 0.8$



# Going on a tiger hunt: regression search tree

**move(Room):**

res: robotLoc = Room

**listen:**

pre: robotLoc = hall

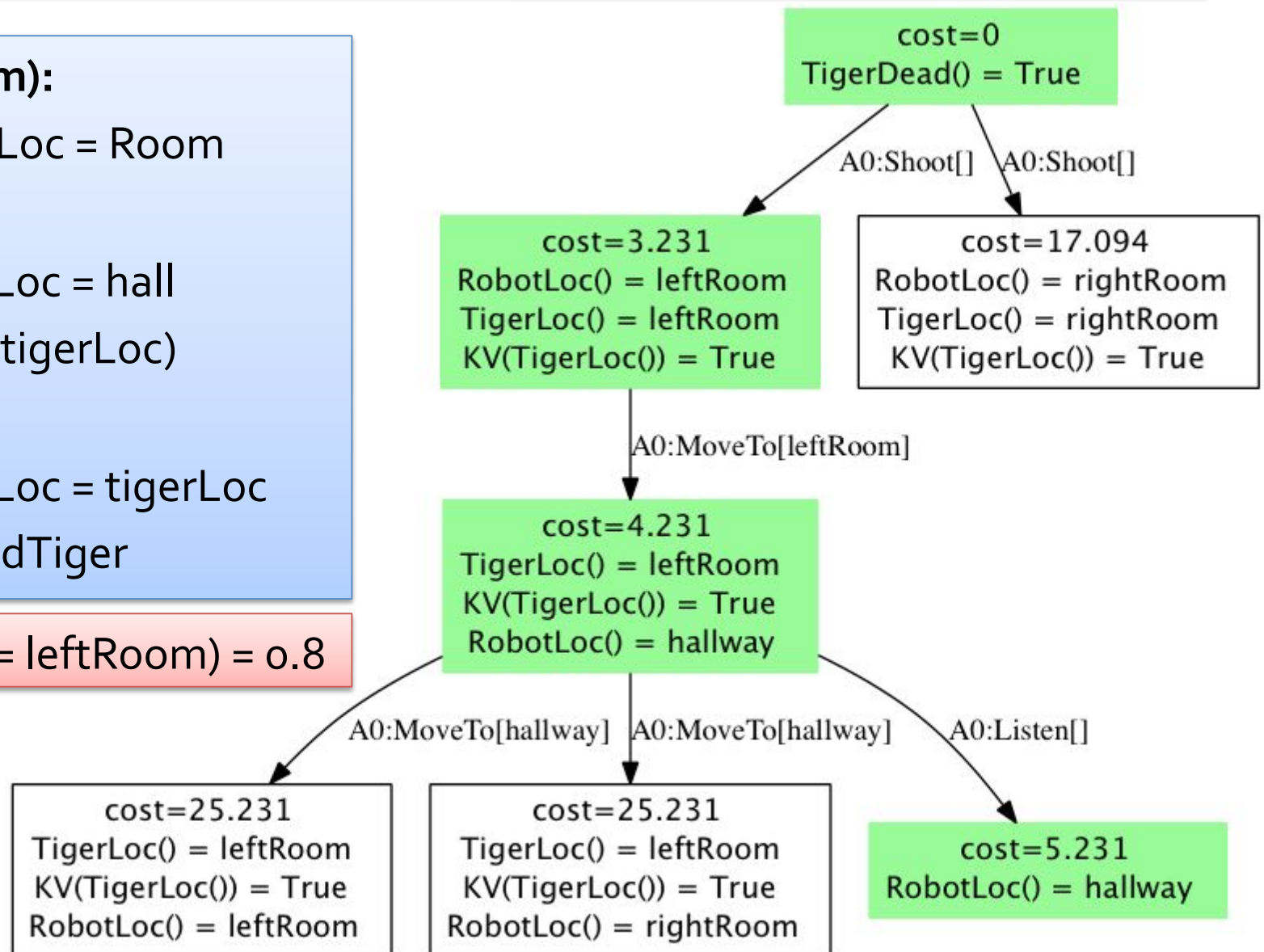
result: KV(tigerLoc)

**shoot:**

pre: robotLoc = tigerLoc

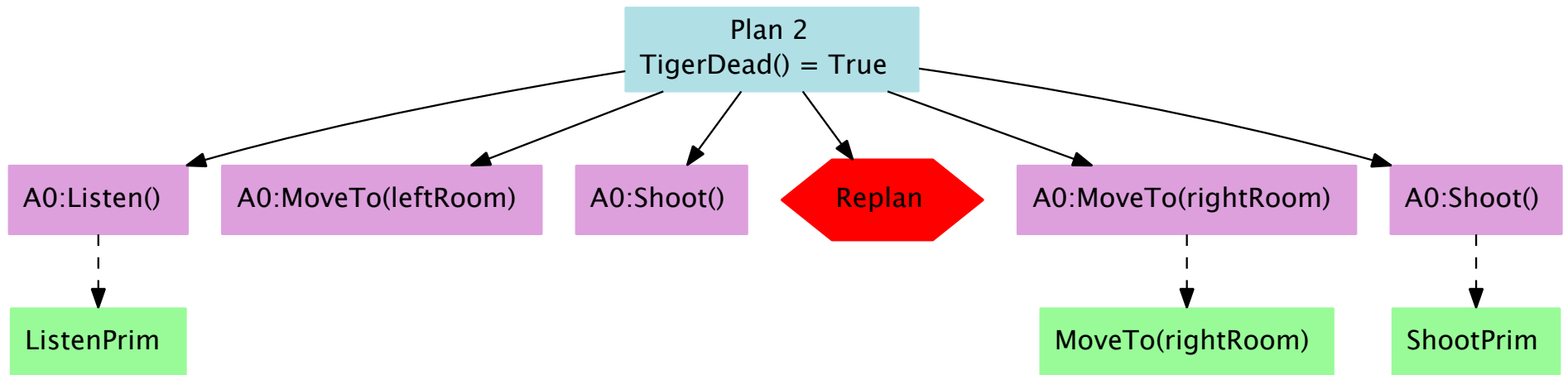
result: deadTiger

$P(\text{tigerLoc} = \text{leftRoom}) = 0.8$



# Monitor execution and replan

---

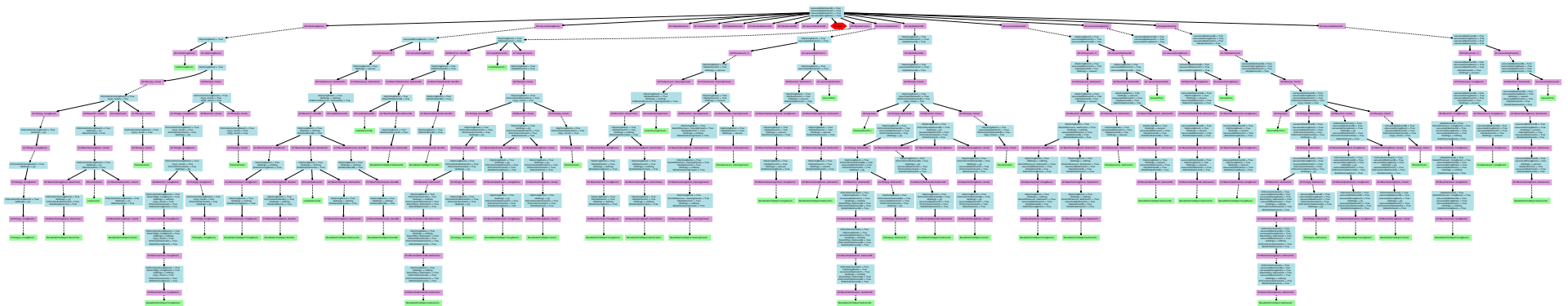


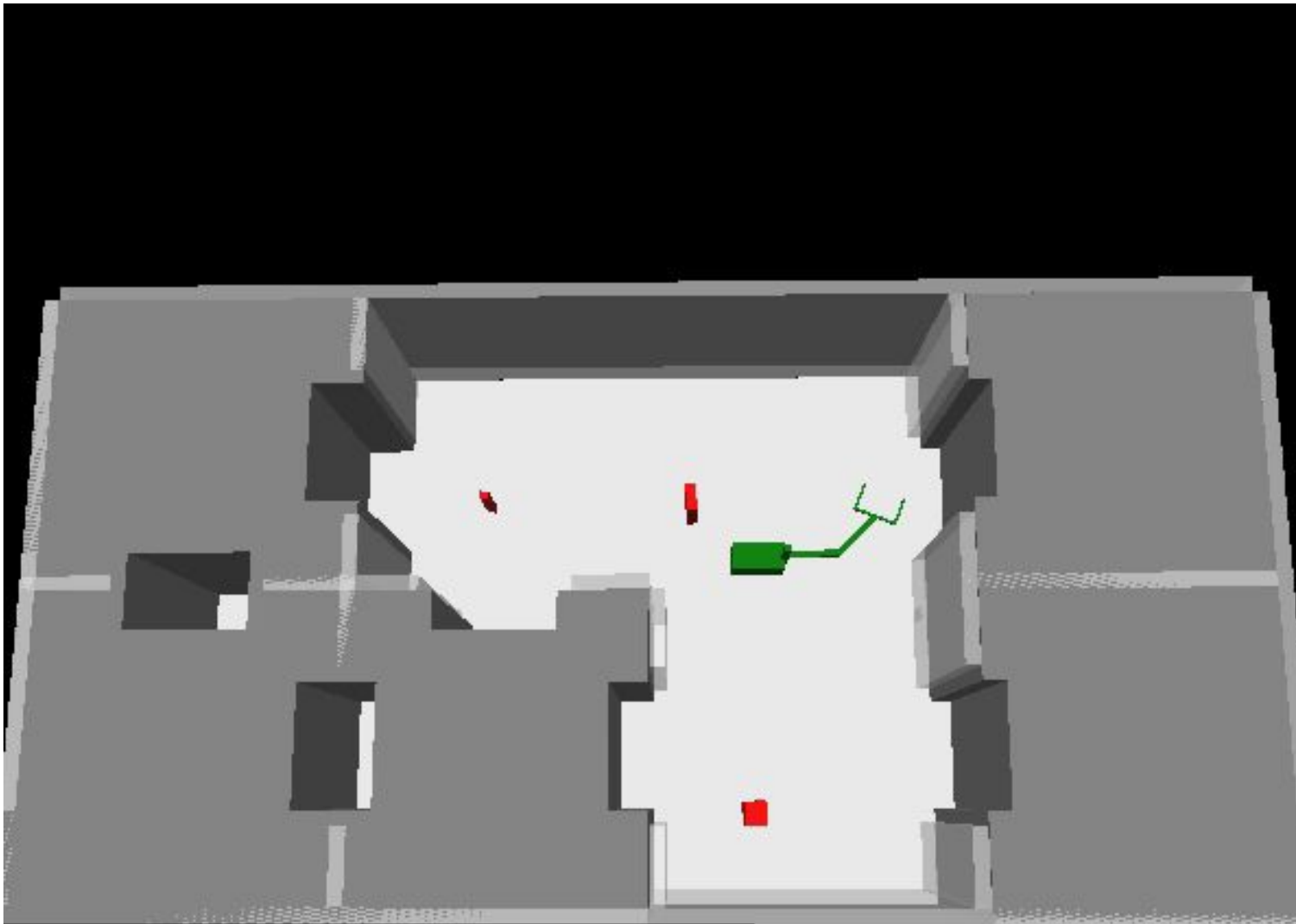
# Cleaning house

---

Goal: vacuum four of the rooms in the house

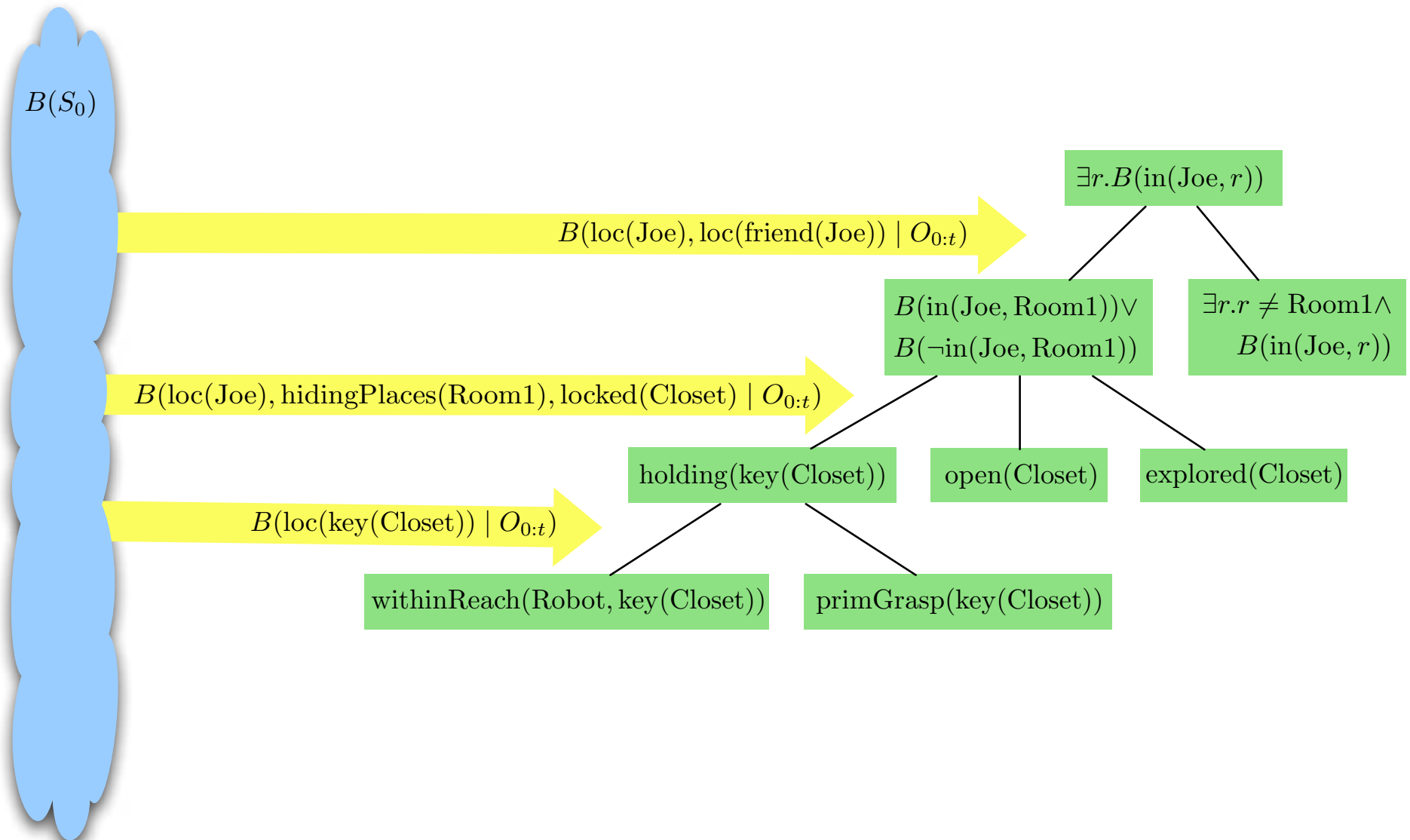
- have to put away junk items before vacuuming
- location of junk is unknown
- location of vacuum is unknown





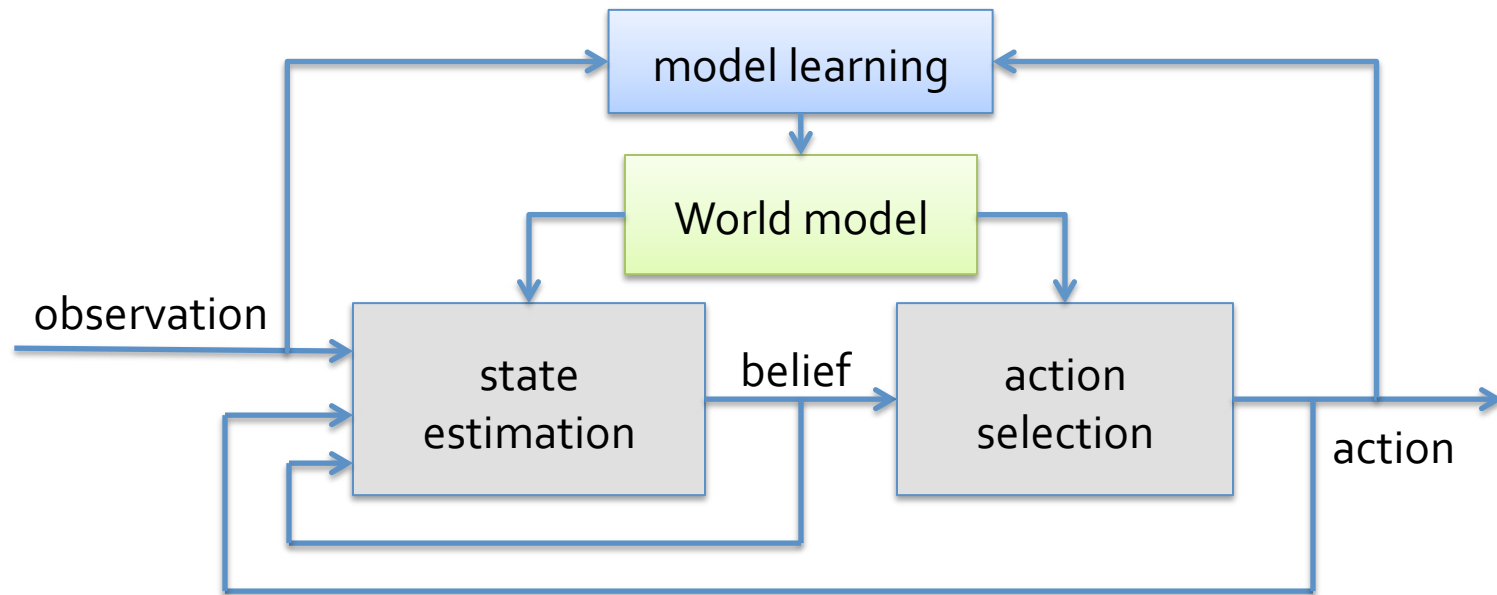
Leslie Pack Kaelbling, AAAI2010

# Plan hierarchy can pose small filtering problems



# Learning a model

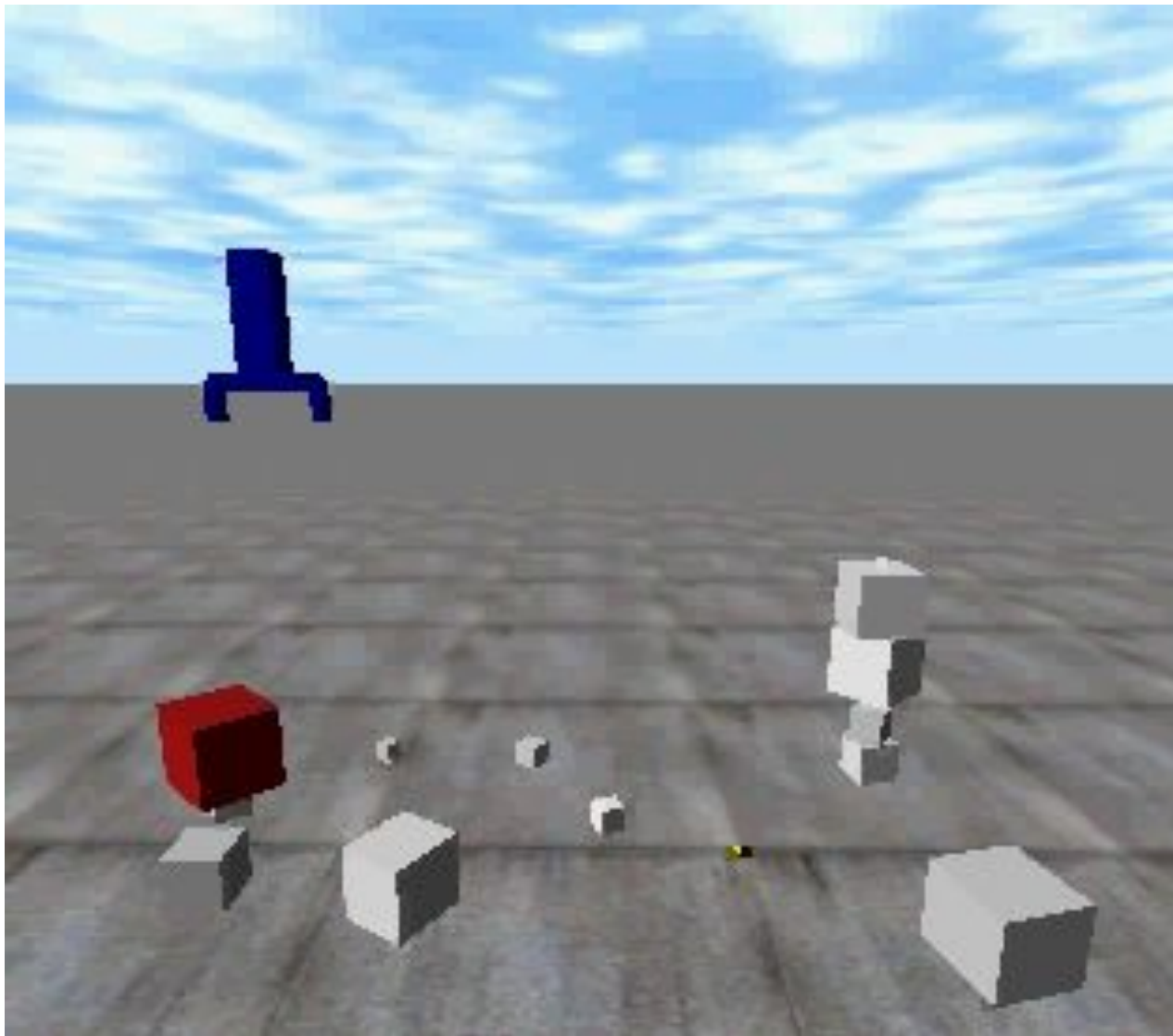
---



Joint work with Hanna Pasula and Luke Zettlemoyer

# Blocks with physics

---



# Representing a world model

---

Probabilistic state transition dynamics:

$$\Pr(s_t \mid s_{t-1}, a)$$

Representation should:

- allow effective generalization
- be useful for planning
- be efficiently learnable

# Probabilistic dynamic rules

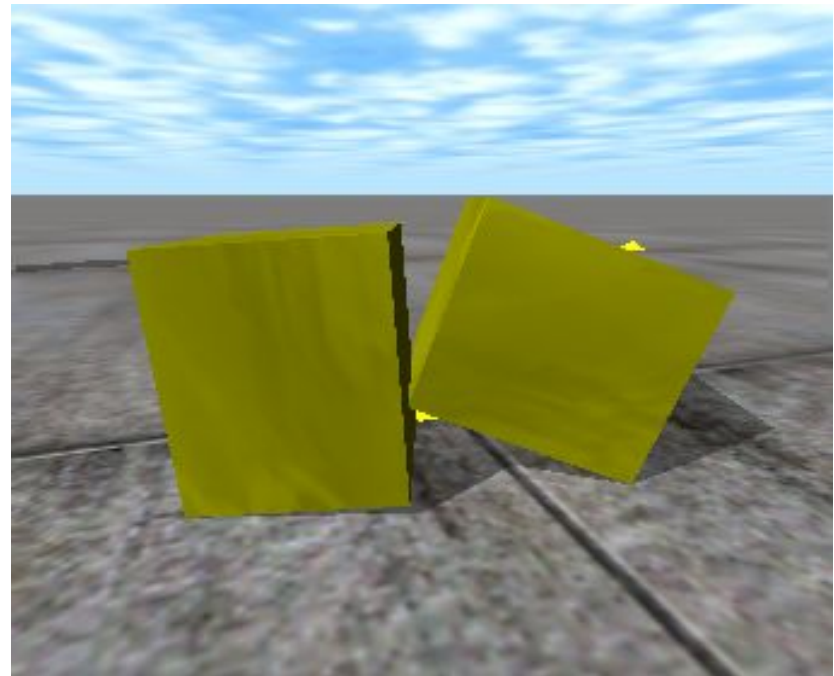
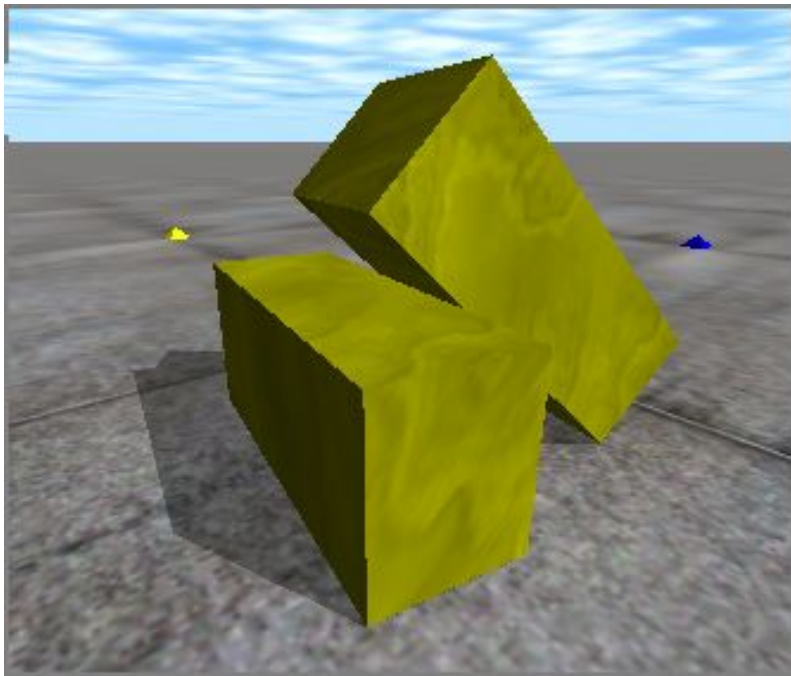
---

Combine logic and probability to model effects of actions in complex, uncertain domains

```
pickup(X): {Y: on(X,Y)}  
  clear(X), inhand-nil, size(X)>2, size(X)<7 →  
    0.803 : ¬on(X,Y)  
    0.093 : no change
```

# Is $X$ on $Y$ ?

---



Useful symbolic vocabulary should be learned

# Neoclassical learning

---

Given experience,  $\{\langle s_t, a_t, s_{t+1} \rangle\}$

Find rule set that optimizes

$$\text{score}(\mathbf{R}) = \sum_t \log \Pr(s_{t+1} \mid s_t, a_t, \mathbf{R}) - \alpha |\mathbf{R}|$$

Start with one default rule: “stuff happens”

- **Symbolic**: add, delete rule; change rule conditions
  - **Greedy**: choose set of outcomes
    - **Convex optimization**: find maximum likelihood probabilities



# Concept invention

New concepts allow predictive theory to be expressed more compactly and learned from less data

$p1(X) :- \neg \exists Y. \text{on}(X, Y)$

X is in the hand

$p2() :- \neg \exists Z. p1(Z)$

nothing is in the hand

$p3(X) :- \neg \exists Y. \text{on}(Y, X)$

X is clear

$p4(X, Y) :- \text{on}(X, Y)^*$

X is above Y

$p5(X, Y) :- p3(X) \wedge p4(X, Y)$

X is on the top of the stack  
containing Y

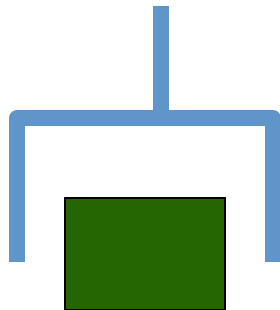
$f6(X) :- \#Y. p4(X, Y)$

the height of X

# Rules learned from data

---

```
pickup(X): {Y: on(X,Y)}  
  clear(X), inhand-nil, size(X)>2, size(X)<7→  
    0.803 :¬on(X,Y)  
    0.093 : no change
```

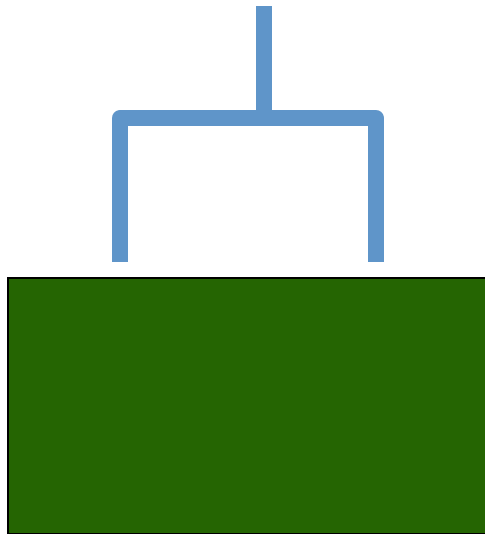


picking up middle-  
sized blocks usually  
works

# Rules learned from data

---

```
pickup(X):  
  clear(X), inhand-nil, ¬size(X)<7 →  
  0.906 : no change
```

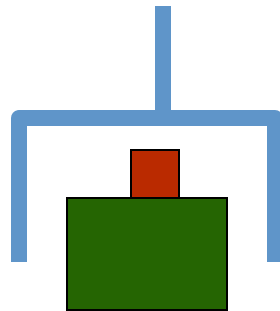


it's impossible to  
pick up very big  
blocks

# Rules learned from data

---

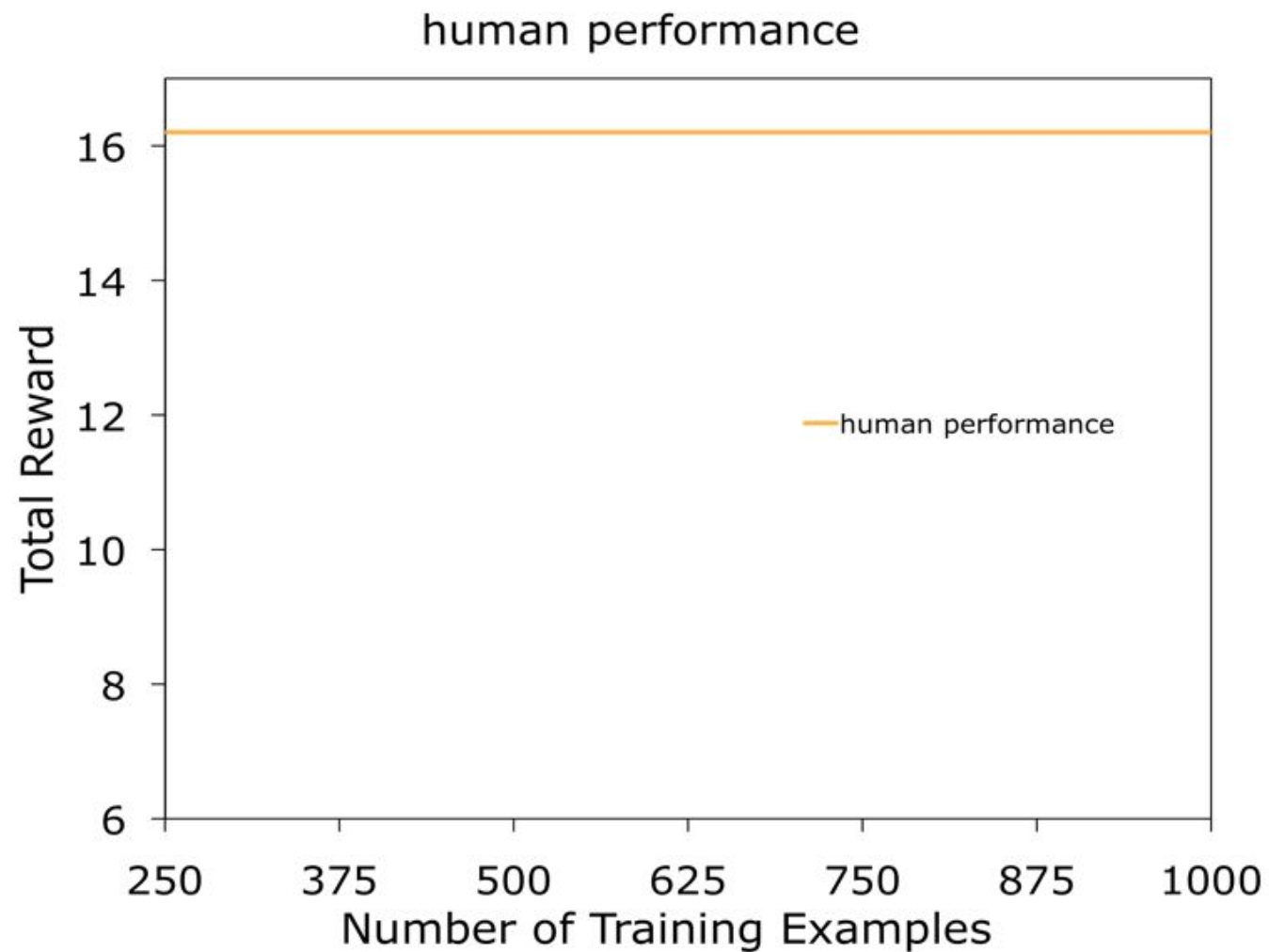
```
pickup(X): {T: table(T)}, {Y: on(X,Y), on(Y,T)}  
clear(X), inhand-nil, size(X)<2 →  
    0.105 :¬on(X,Y)  
    0.582 :¬on(Y,T)  
    0.312 : no change
```



if a tiny block is on another block that is on the table, and we try to pick up the tiny block, we'll often pick up the other block as well, or fail

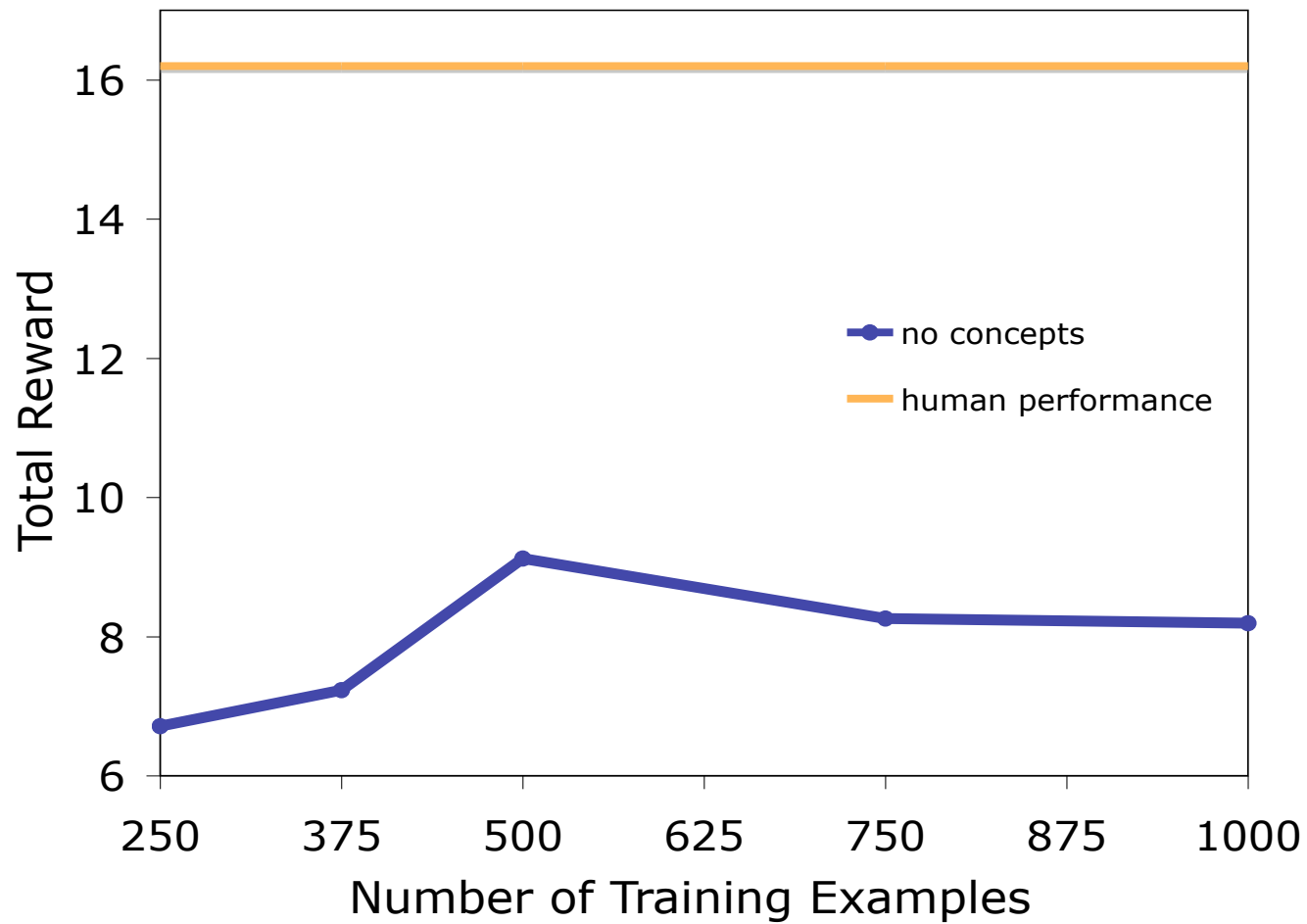
# Planning with learned rules

---



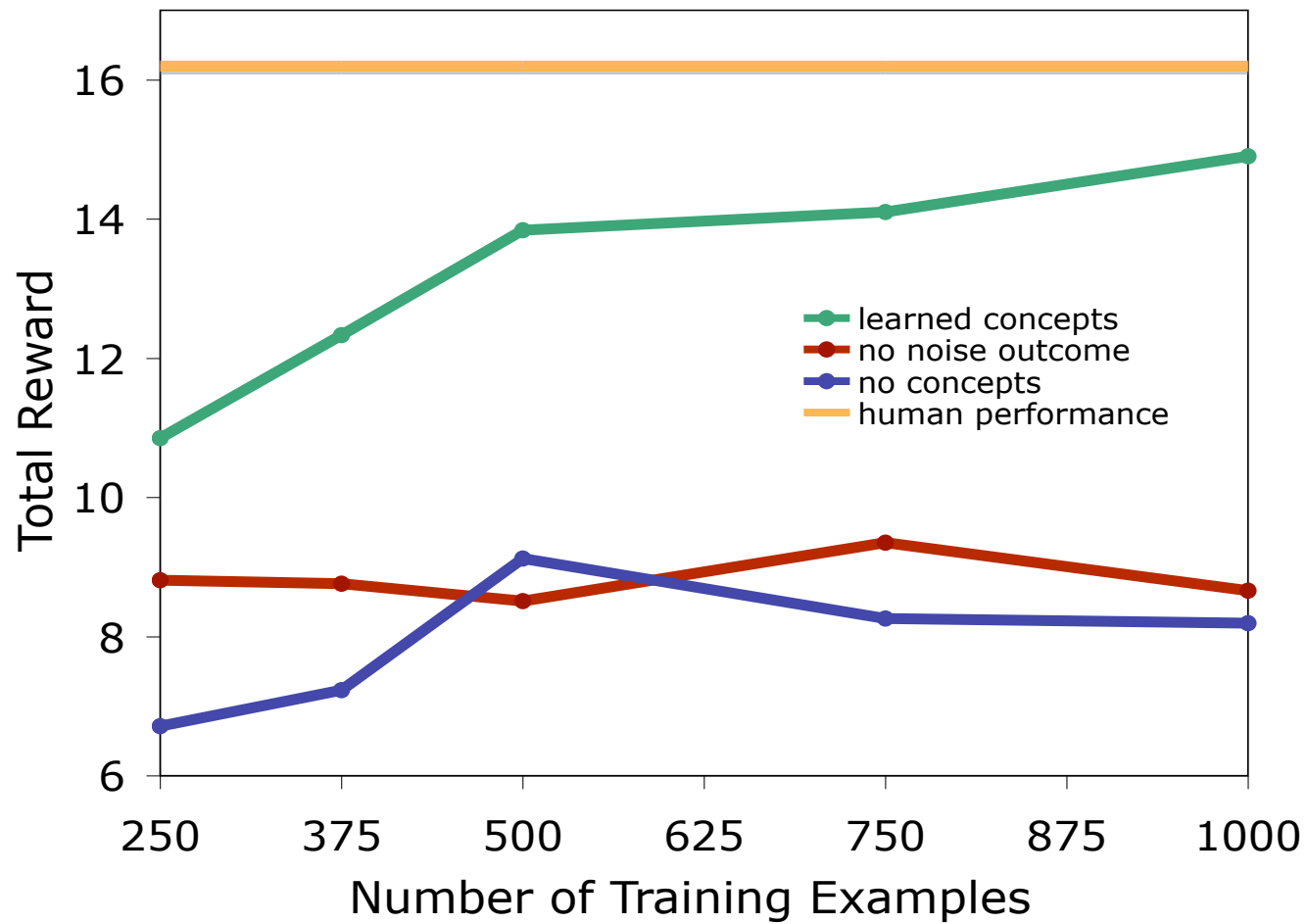
# Planning with learned rules

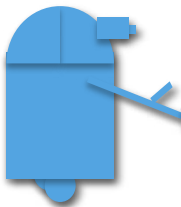
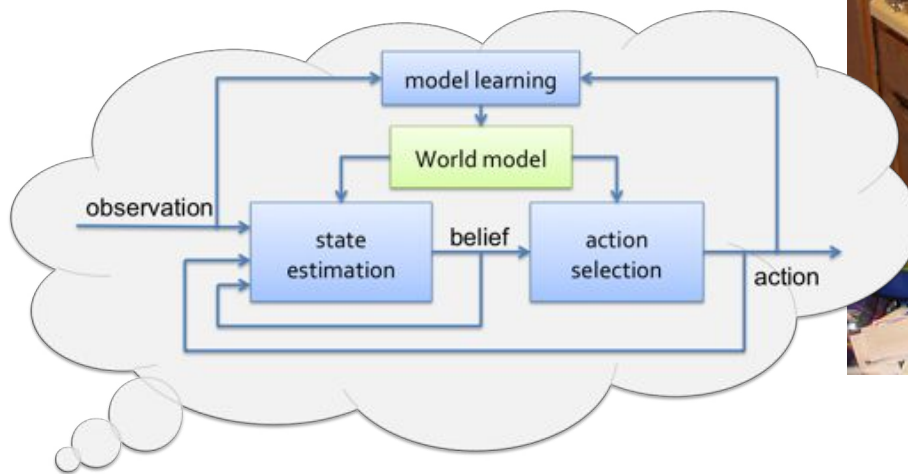
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# Planning with learned rules

---





compact representation  
explicit uncertainty modeling  
approximation

# What should we be doing?

---

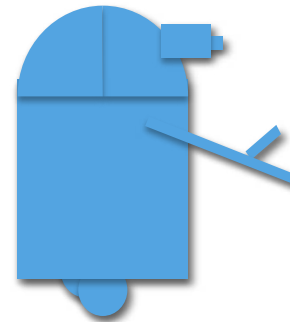
## Thinking hard about representation in open, uncertain domains

- What do you know about your house?

## Everything else: planning, learning, reasoning, ...

## Talking to each other

- vision, natural language, robotics, logic, probability, learning, ...



# Thanks!

---

**Collaborators:** Stan Rosenschein, Tom Dean, Tomas Lozano-Perez, Michael Littman, Tony Cassandra, Hagit Shatkay, Jim Kurien, Nicolas Meuleau, Milos Hauskrecht, Jak Kirman, Ann Nicholson, Bill Smart, Luis Ortiz, Leon Peshkin, Mike Ross, Kurt Steinkraus, Yu-Han Chang, Paulina Varshavskaya, Sarah Finney, Kaijen Hsiao, Luke Zettlemoyer, Han-Pang Chiu, Natalia Hernandez, James McLurkin, Emma Brunskill, Meg Aycinena Lippow, Tim Oates, Terran Lane, Georgios Theocharous, Kevin Murphy, Bruno Scherrer, Hanna Pasula, Brian Milch, Bhaskara Marthi, Kristian Kersting, Sam Davies, Dan Roy, Jenny Barry, Selim Temizer, Rob Platt, Russ Tedrake

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