6.896 Sublinear Time Algorithms September 9, 2004

Course Information
Lecturer: Ronitt Rubinfeld

Lectures: T,Th 1-2:30, Room 36-156.

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Course topics In this course we will study techniques for designing algorithms that output a solution by only considering a very small portion of the data, in particular, algorithms which run in sublinear time. The study of sublinear time algorithms has been applied to problems from a wide range of areas, and many beautiful techniques have been applied to analyzing such algorithms, including the Szemeredi Regularity Lemma, low rank approximations of matrices, Fourier analysis, and other tools from number theory, combinatorics, linear algebra, optimization theory and probability theory.

For most problems, sublinear time algorithms must necessarily return an approximate answer. We will consider both classical approximation algorithms, as well as property testing algorithms. We will also consider natural extensions of these notions to estimating quantities associated with distributions over large domains. A detailed list of topics to be covered is given below. The list is subject to change due to my personal whims, class interest, timing issues and other constraints.

- Combinatorial objects
  - Graphs: Testing for properties of connectivity, low diameter, bipartiteness, triangle-freeness. Estimating minimum spanning tree weight, maximum cut weight, normal forms for graph property testers.
  - Linear programming
  - Using decompositions of matrices
  - Testing of clusterability and other metric properties of points
  - Strings: Testing membership in regular languages. Estimating edit distance.
- Testing properties of functions
  - Monotonicity: over linearly ordered, hypercube and general poset domains.
  - Convexity
  - Algebraic properties: Linearity and low total degree polynomial testing. Locally testable codes.
  - Dependence on few variables: Singletons, Juntas
- Global properties of distributions (given by samples): Testing closeness of two distributions. Testing monotonicity, independence. Estimating entropy.

Course Requirements Approximately 4-5 homework sets (50%). Scribe notes(25%). Class participation (25%). Since there is no TA, as part of class participation, students will be asked to help with grading of assignments and solution sets.

Prerequisites 6.045J or 6.046J

Office hours By appointment.