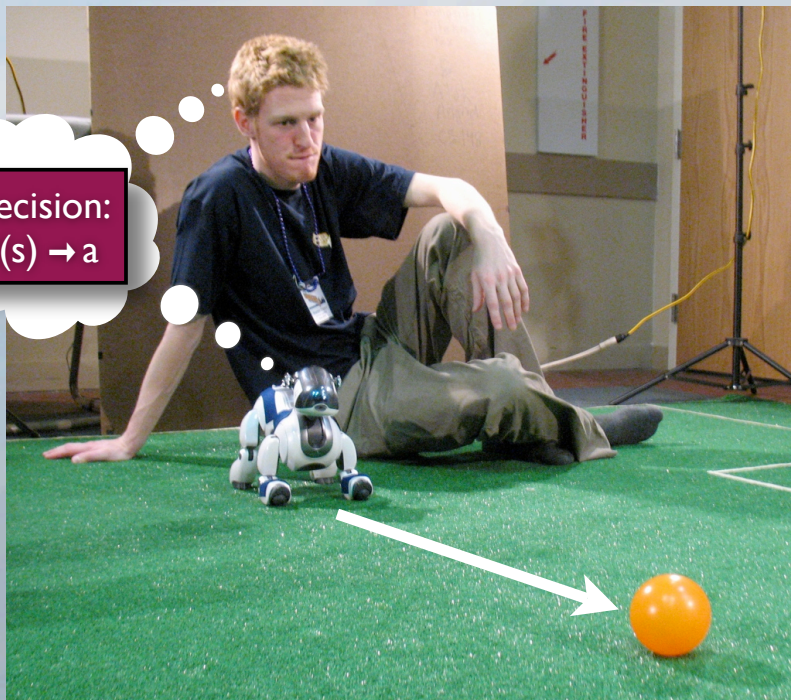



# Robot Learning from Multivalued Demonstration



Decision:  
 $\pi(s) \rightarrow a$

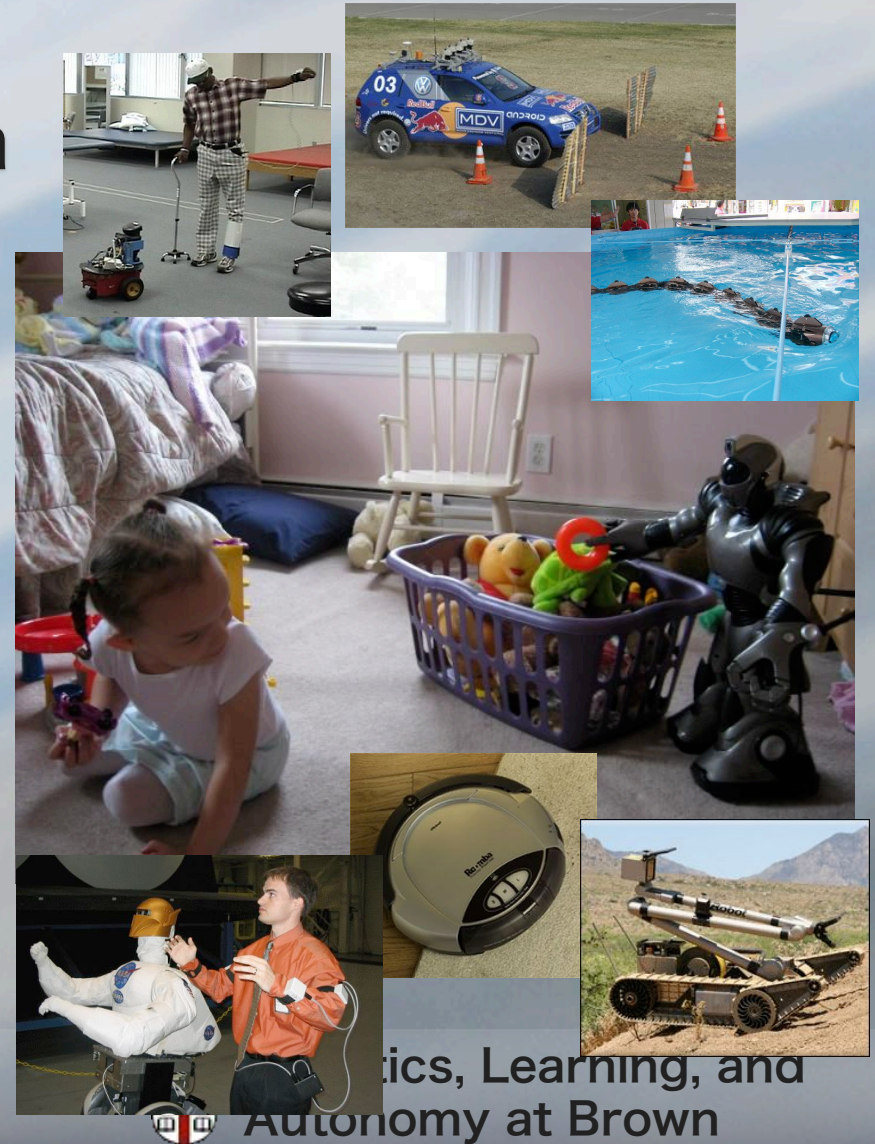
Chad Jenkins  
Assistant Professor

Brown University  
Computer Science 

IROS 2008 Workshop on Robotics  
Challenges for Machine Learning  
Sep 22, 2008  
Nice, France

# My Goal for Robotics

- Robot collaborators in human endeavors
  - Tools to enhance users' productivity
  - Become the path of least resistance
  - Critical path tasks?
  - Learning can broaden societal involvement



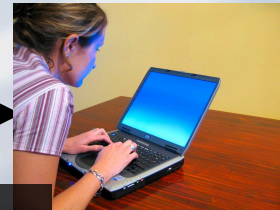
Personal Computing



ENIAC



Apple II



Laptop



OLPC

Research

Novelty tech

Pervasive tools

Jenkins  
Multivalued Robot Learning



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Autonomy at Brown

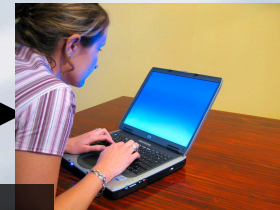
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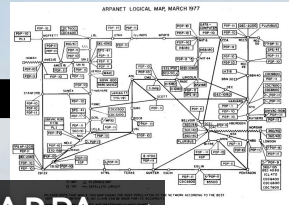


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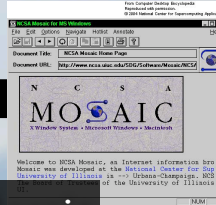


OLPC

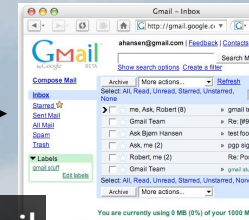
Internet



ARPANET



Mosaic

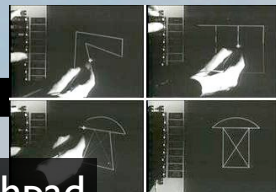


Gmail



YouTube

Graphics



Sketchpad



Tron



Final Fantasy



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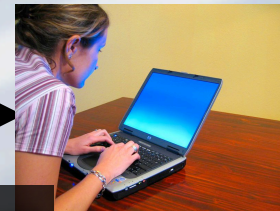
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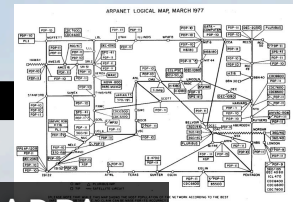


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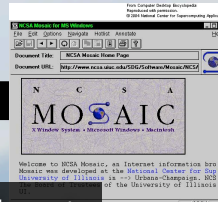


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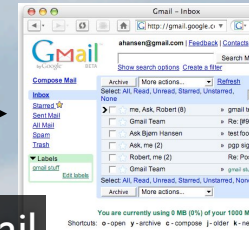
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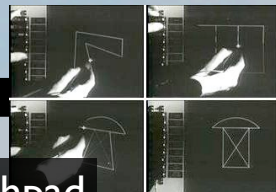


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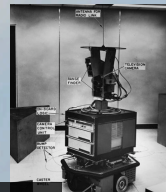


Final Fantasy



Madden

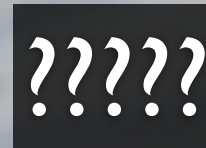
Robotics



Shakey



Roomba



Research

Novelty tech

Pervasive tools

Jenkins  
Multivalued Robot Learning



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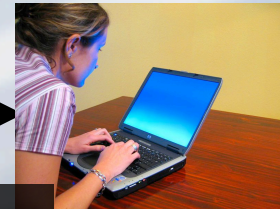
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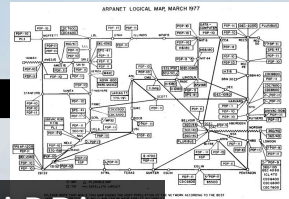


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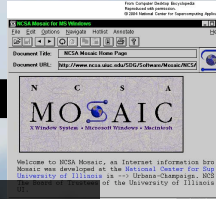


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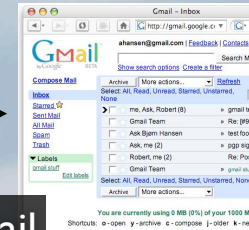
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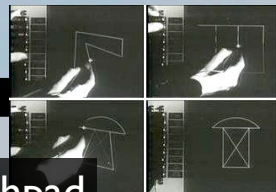


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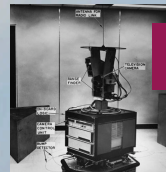


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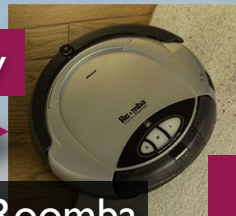
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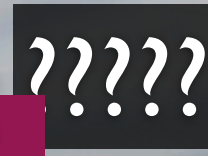
Shakey

Currently



Roomba

"Personal Robotics Revolution"



Research

Novelty tech

Pervasive tools

Jenkins Multivalued Robot Learning



Robotics, Learning, and Autonomy at Brown

# Challenges for the Personal Robotics Revolution

- **Programming Autonomous Robots?**
  - developing policies that accord with user's intended behavior
- **Manipulation?**
  - achieving desired physical effects, uncertainty
- **Communication?**
  - coordination between many humans and robots
- **Integration**
  - reproducible evaluation, feedback loop w/usability



# Where Learning Plays A Role

- **Programming Autonomous Robots?**
  - **learn policies from demonstration (LfD)**  
[Jenkins,Mataric 00-04] [Grollman,Jenkins 07-08]
- **Manipulation?**
  - **manifold learning to form subspace priors**  
[Jenkins,Peters 05-06] [Tsoli,Jenkins 07-08]
- **Communication?**
  - **Multi-robot MRFs;** [Butterfield, Jenkins, et al. 07-08]
  - **Peer-to-peer HRI** [Loper, Jenkins, et al. 07-08]
- **Integration**





# Where Learning Plays A Role

Focus of this talk:  
Multivalued functions in robot LfD

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  - learn policies from demonstration (LfD)  
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Thursday at 13:30: "Neighborhood Denoising for Learning High-Dimensional Grasping Manifolds"



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Wednesday during CPS session  
"MRFs for Cyber-Physical Systems"



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IJCAI 09 Robotics Challenges

Multivalued Robot Learning



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# Learning from Demonstration

- Assume: true policy is a function  $\pi(S) \rightarrow A$ 
  - maps states  $S$  to actions  $A$ , plus noise
- Training: dataset of state-action pairs  $(s_i, a_i)$ 
  - instances of user policy  $\pi(s_i) \rightarrow a_i$
  - latent task objective  $G$  (known to user)
- Estimate: policy  $\hat{\pi}$  to perform task, meet  $G$ :
  - bootstrapped reinforcement learning
  - function approximation (regression)

# GP Regression Basics

$$C_{ij} = q(\mathbf{x}_i, \mathbf{x}_j) + \delta_{ij}\sigma_\nu^2$$

Compute similarity matrix  $C$

$$q(\mathbf{x}_i, \mathbf{x}_j) = \exp \frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma_k^2}$$

Input similarity kernel

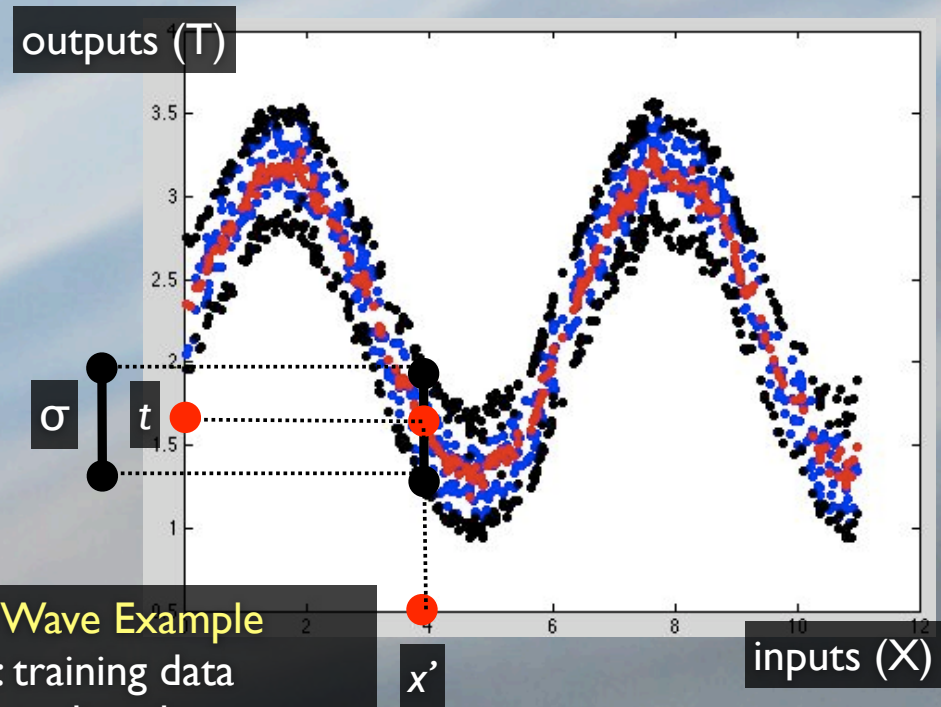
$$k_i = q(\mathbf{x}', \mathbf{x}_i)$$

$$\hat{\mathbf{t}} = \mathbf{k}^\top \mathbf{C}^{-1} \mathbf{T}$$

Predict output  $t$  from similarity matrix

$$\sigma_{\hat{\mathbf{t}}}^2 = (1 + \sigma_\nu^2) - \mathbf{k}^\top \mathbf{C}^{-1} \mathbf{k}$$

Compute confidence variance



Sine Wave Example

blue: training data

red: predicted outputs

black: confidence bounds

# Object Tracking Example Using Gaussian Process Regression

[Grollman, Jenkins 07]



Jer  
Mu

d

# Conjecture

- Desired controllers  $\nRightarrow$  math. functions
  - demonstrated control can be multivalued
    - single perceived state  $\rightarrow$  multiple actions
- When would this occur?
  - training has multiple underlying policies
    - learn a FSM? or robot soccer?
  - ambiguous state spaces
    - “state space race”





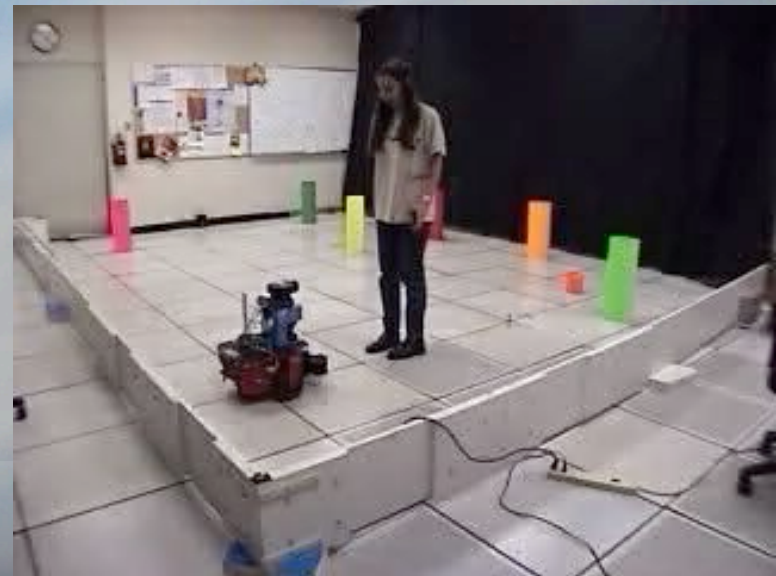
# Open Area? Multivalued LfD

- “Multivaluedness” partitions LfD work:
  - skill-level: learn policy for single objective
    - [Schaal,Atkeson 98; Abbeel,Ng 04; Smart,Kaelbling 02]



# Open Area? Multivalued LfD

- “Multivaluedness” partitions LfD work:
  - **skill-level**: learn policy for single objective
    - [Schaal,Atkeson 98; Abbeel,Ng 04; Smart,Kaelbling 02]
  - **task-level**: given skills, learn transitions
    - [Nicolescu,Mataric 03; Bentivegna et al 01; Lockerd,Breazeal 06]



# Multivalued Demonstration

- Partition true world state  $S = \{S_0, S_U\}$ 
  - $S_0$ : robot observable state variables
  - $S_U$ : unobservable by robot, maybe human
    - objectives, task context, other features
- Demonstration data:  $(s_{0i}, a_i) ; \pi (s_{0i}, s_{Ui}) \rightarrow A$

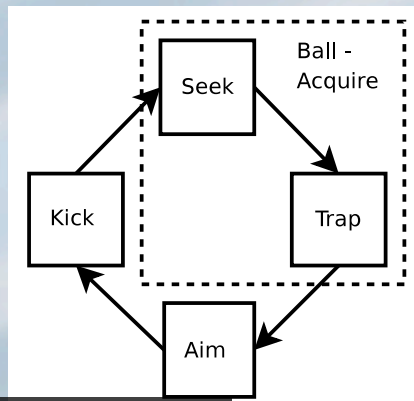


# Multivalued Demonstration

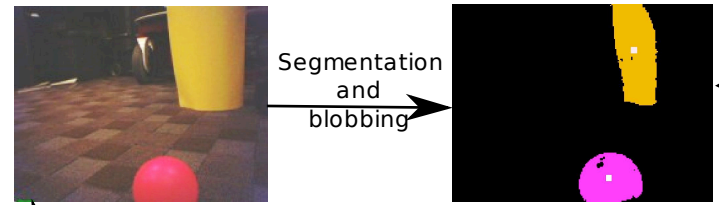
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    - objectives, task context, other features
- Demonstration data:  $(s_{0i}, a_i) ; \pi (s_{0i}, s_{Ui}) \rightarrow A$
- If  $S_0 \approx S$ , then  $p(a|s_0')$  is unimodal distribution
- Otherwise,  $p(a|s_0')$  potentially multimodal



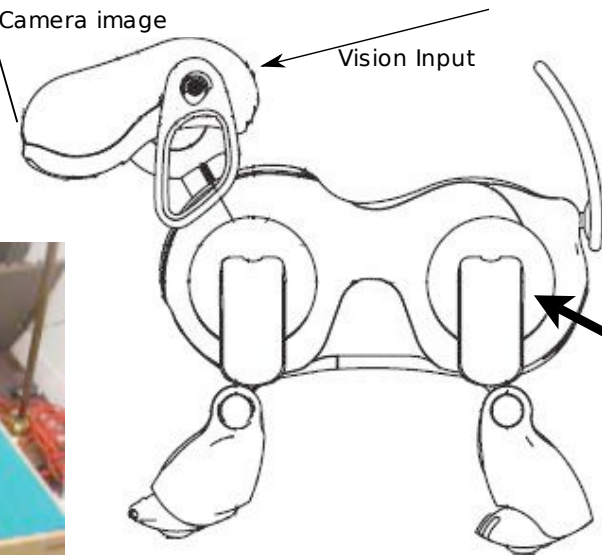
# Can Robot Soccer Be Learned from Demonstration?



Attacker FSM



input state (S):  
color blobs



find mapping from S to A:  
 $\pi(s) = a$

action outputs (A):  
movement (speed, direction)  
moves (trap, kick, block)

Sony AIBO

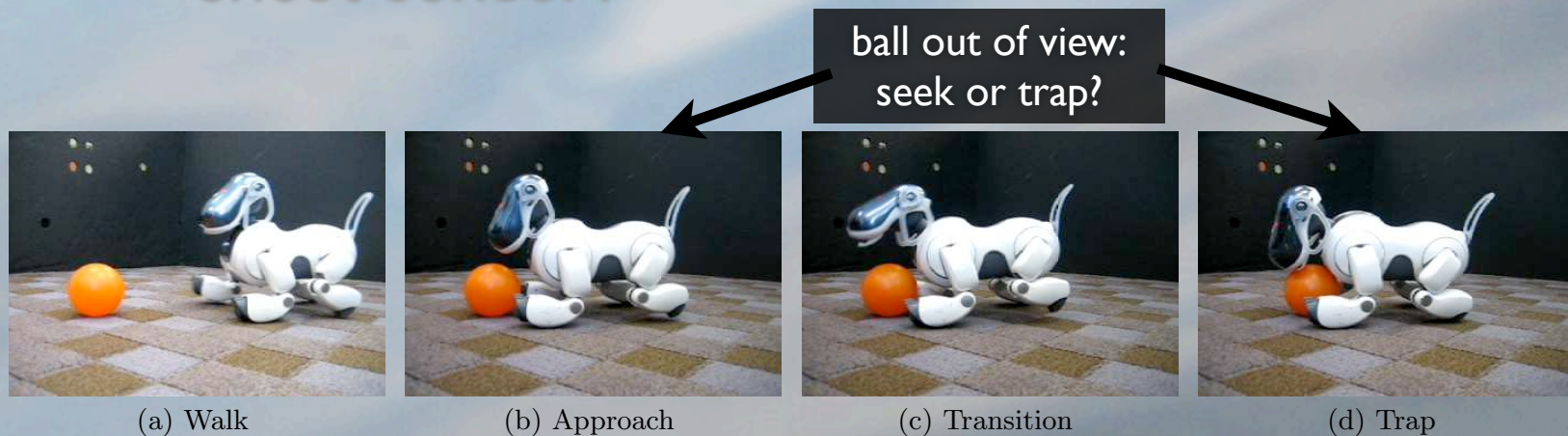


Basic robot soccer attack move

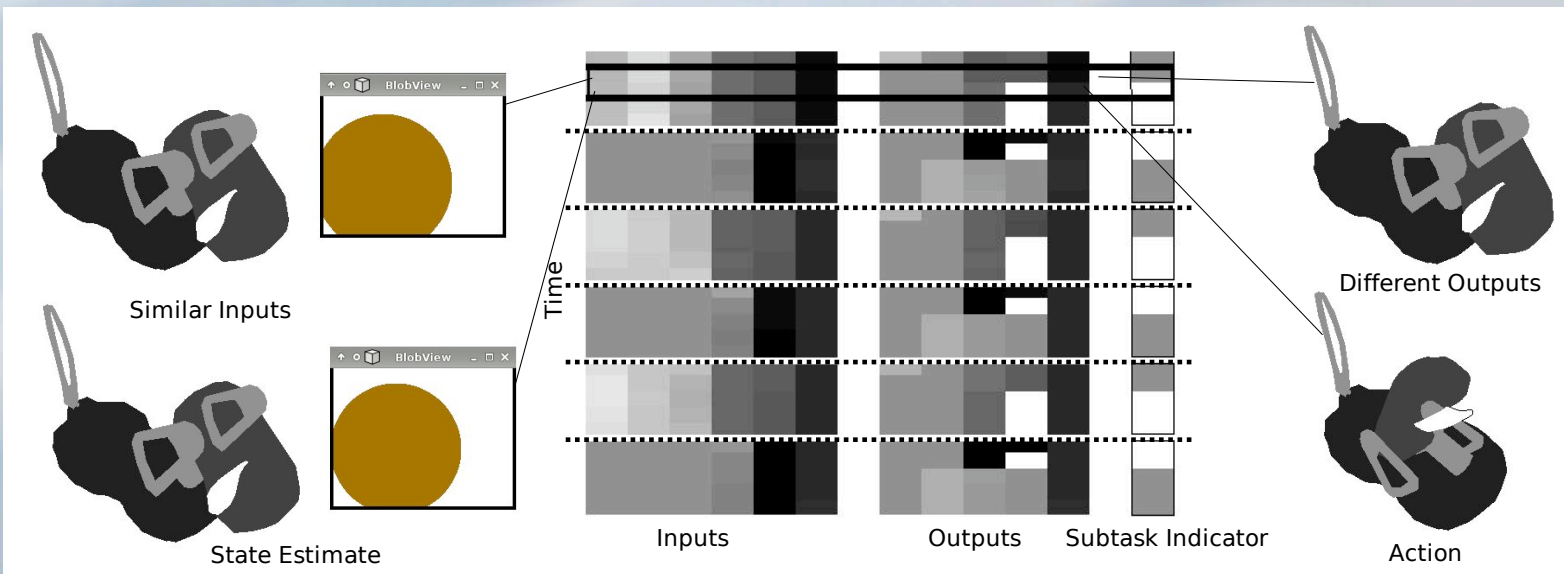


# Internal Context

- **Ball Acquire needs a context bit**
  - during trap, ball goes out of view
  - similar states produce different actions
    - based on unobserved context
    - chest sensor?



# Internal Context



ball out of view:  
seek or trap?



(a) Walk



(b) Approach



(c) Transition



(d) Trap

# Multivalued LfD

- Our approach: extract multiple policies
  - Cause of multivalued data is unimportant
  - Only distinguishing modes of actions|state
- Research roadmap
  - Uncover multiple policies as “experts”
    - Infinite “multimap” regression [Grollman poster]
  - Estimate FSMs over experts [Nicolescu, Mataric 03]
  - Optimize individual experts [Abbeel, Ng 04]

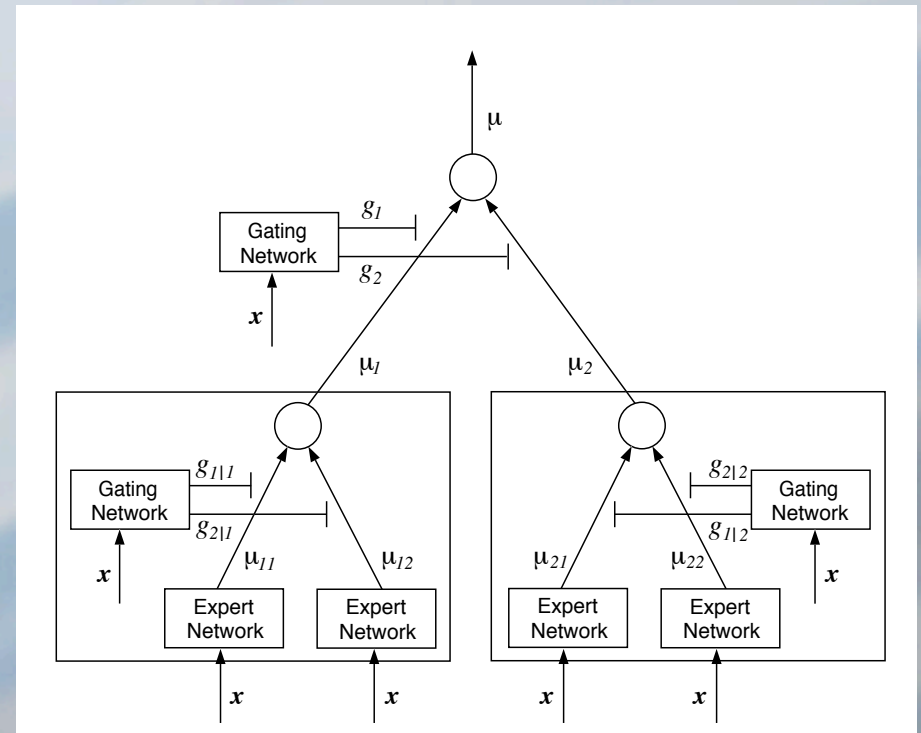




# Multimap Regression

- Learn data gating function partition
  - based on input-output likelihood
- Expert learns policy for each gate
  - Sparse Online Gaussian Processes

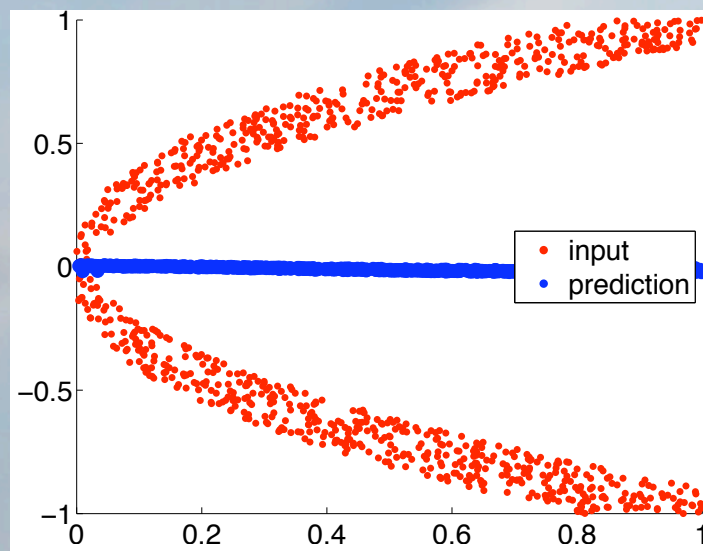
[Csato, Opper 02]



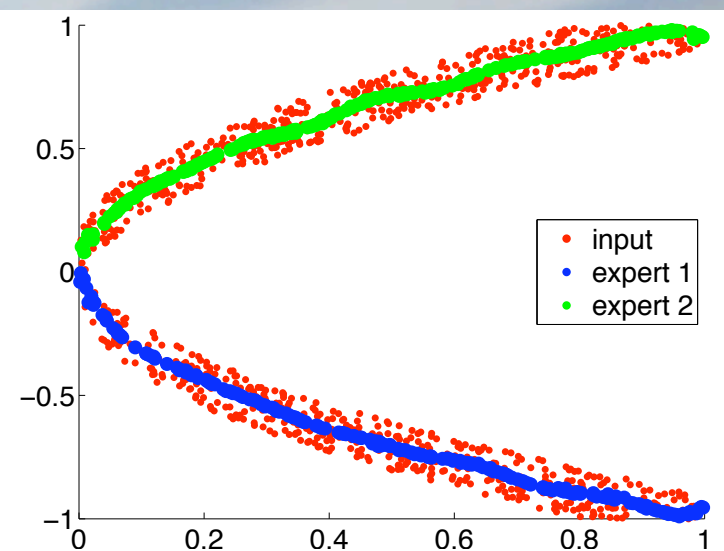
Hierarchical Mixtures of Experts  
[Jordan, Jacobs 94]:  
Experts learn pieces of function  
Gates blend these pieces together

# Square Root Example

- Consider  $y = \sqrt{x}$
- averaging outputs will be incorrect
- 2 regressors needed for pos. and neg.



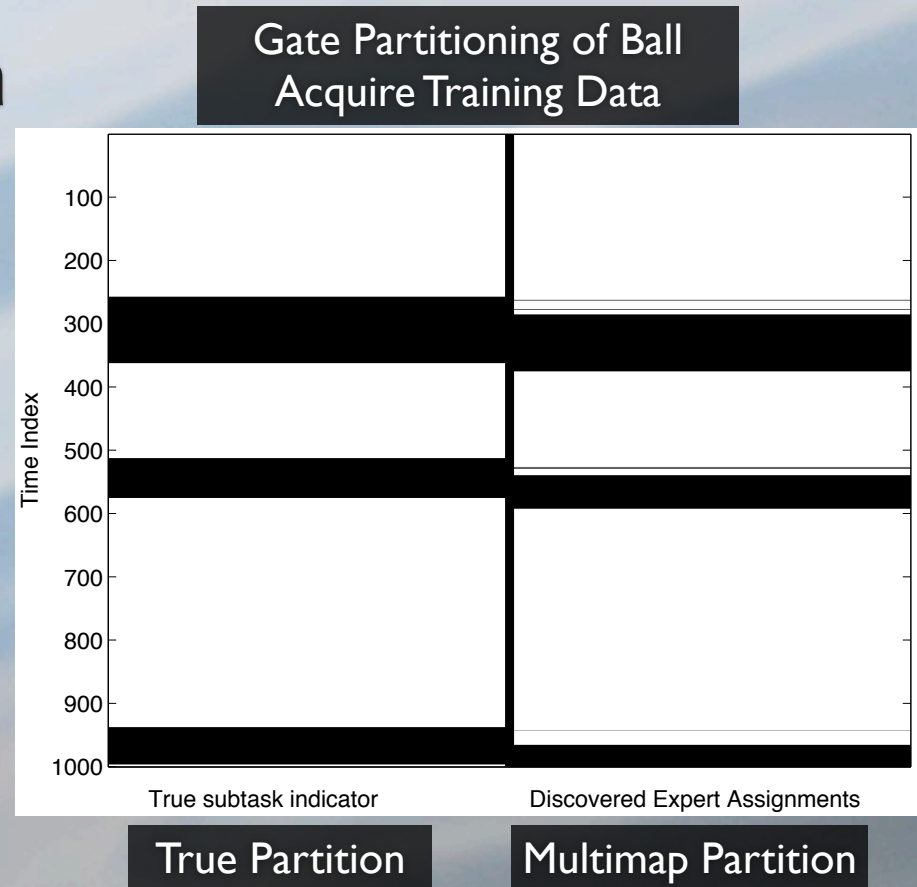
Locally Weighted Projection Regression



Multimap Regression

# Preliminary Results

- Multimap regression on Ball Acquire data
  - (+) Data partitions into “seek” & “trap”
  - (-) Both experts do both seek and trap
  - (+) Experts perform correctly from initialized partition



# Summary

- Learning from demonstration as a means to program autonomous robots
- Multivalued demonstration data
  - perceived state maps to multiple actions
- Infinite mixtures of experts regression
  - promising results for learning robot soccer



# Acknowledgments

Funding:

ONR YIP

ONR PECASE

NSF IIS

Brown Salomon

Dan Grollman

Brendan Dickinson

Micah Lapping-Carr

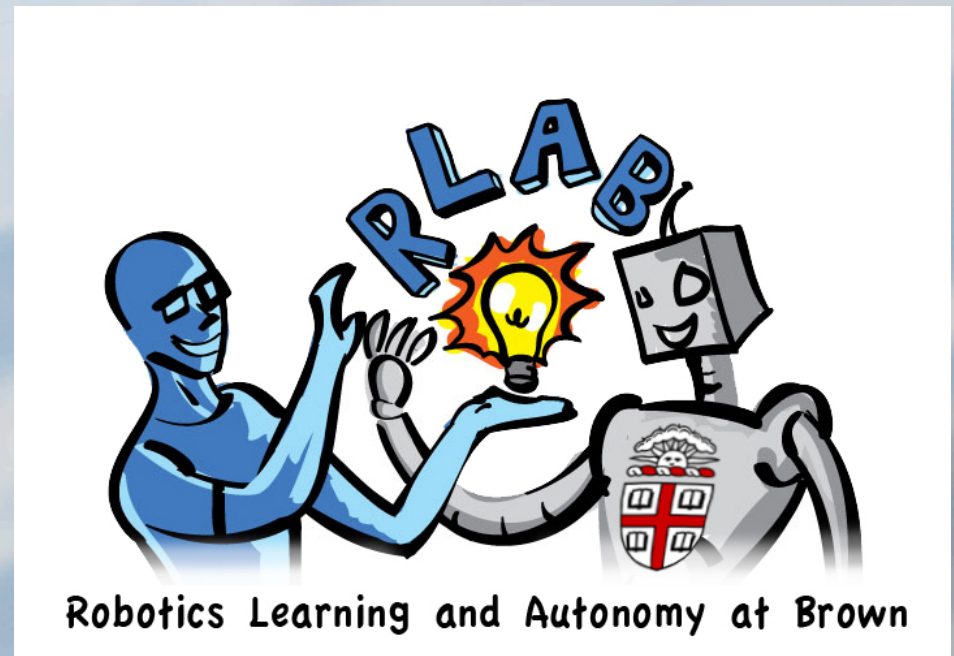
Mark Moseley

Dan Byers

Jessica Chermayeff

Frank Wood

Katherine Heller



Jenkins

Multivalued Robot Learning

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