# **Course Evaluations**

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4 Random Individuals will win an ATI Radeon<sup>tm</sup> HD2900XT





## A Gentle Introduction to Bilateral Filtering and its Applications

- From Gaussian blur to bilateral filter S. Paris
- Applications F. Durand
- Link with other filtering techniques P. Kornprobst

#### BREAK

- Implementation S. Paris
- Variants J. Tumblin
- Advanced applications J. Tumblin
- Limitations and solutions P. Kornprobst

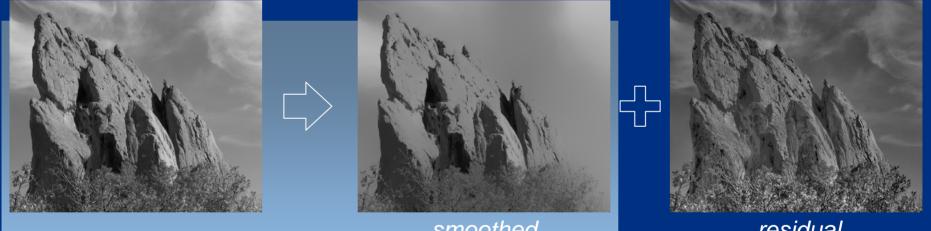
A Gentle Introduction to Bilateral Filtering and its Applications



# Recap

Sylvain Paris – MIT CSAIL

# Decomposition into Large-scale and Small-scale Layers



residual (texture, small scale)

smoothed (structure, large scale)

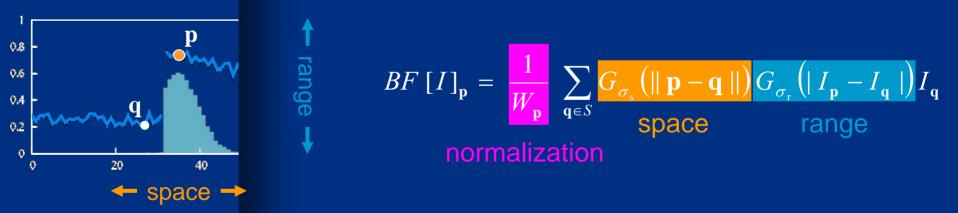
input

#### edge-preserving: Bilateral Filter

## Weighted Average of Pixels

 Depends on spatial distance and intensity difference

Pixels across edges have almost influence



A Gentle Introduction to Bilateral Filtering and its Applications



# Efficient Implementations of the Bilateral Filter

Sylvain Paris – MIT CSAIL

# Outline

Brute-force Implementation

Separable Kernel [Pham and Van Vliet 05]

Box Kernel [Weiss 06]

• 3D Kernel [Paris and Durand 06]

#### **Brute-force Implementation**

$$BF[I]_{\mathbf{p}} = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} G_{\sigma_{s}} \left( \| \mathbf{p} - \mathbf{q} \| \right) G_{\sigma_{r}} \left( \| I_{\mathbf{p}} - I_{\mathbf{q}} \| \right) I_{\mathbf{q}}$$

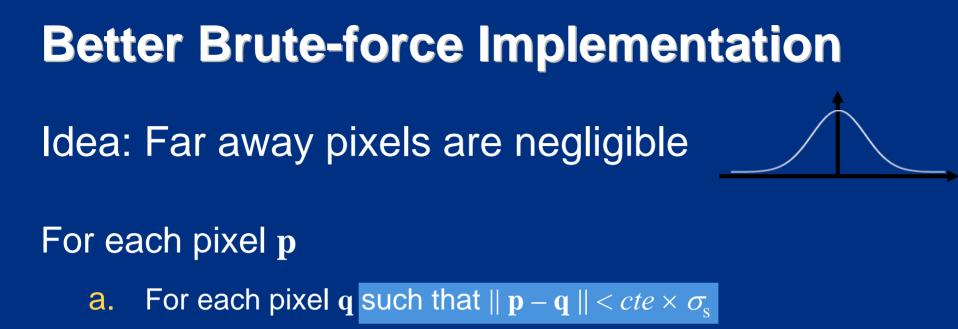
For each pixel  $\mathbf{p}$ For each pixel  $\mathbf{q}$ Compute  $G_{\sigma_s}(||\mathbf{p} - \mathbf{q}||) G_{\sigma_r}(|I_{\mathbf{p}} - I_{\mathbf{q}}|) I_{\mathbf{q}}$ 

8 megapixel photo: 64,000,000,000,000 iterations!

VERY SLOW! More than 10 minutes per image

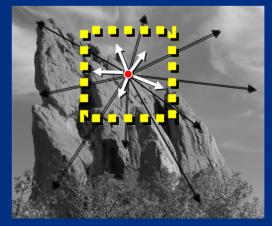
# Complexity

- Complexity = "how many operations are needed, how this number varies"
- *S* = space domain = set of pixel positions
- |S| = cardinality of S = number of pixels
  In the order of 1 to 10 millions
- Brute-force implementation:  $O(|S|^2)$



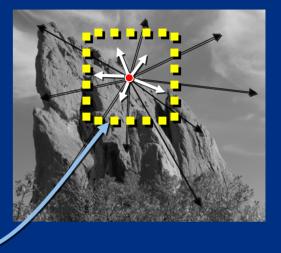


looking at neighbors only



# Discussion

# • Complexity: $O(|S| \times \sigma_s^2)$



neighborhood area

- Fast for small kernels:  $\sigma_s \sim 1$  or 2 pixels
- BUT: slow for larger kernels

# Outline

#### Brute-force Implementation

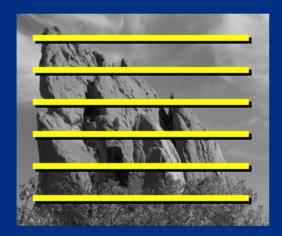
Separable Kernel [Pham and Van Vliet 05]

Box Kernel [Weiss 06]

• 3D Kernel [Paris and Durand 06]

## Separable Kernel [Pham and Van Vliet 05]

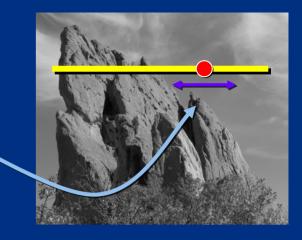
Strategy: filter the rows then the columns





 Two "cheap" 1D filters instead of an "expensive" 2D filter

# Discussion



- Complexity:  $O(|S| \times \overline{\sigma_s})$ 
  - Fast for small kernels (<10 pixels)
- Approximation: BF kernel not separable
  - Satisfying at strong edges and uniform areas
  - Can introduce visible streaks on textured regions





#### separable kernel mostly OK, some visible artifacts (streaks)

# Outline

Brute-force Implementation

Separable Kernel [Pham and Van Vliet 05]

Box Kernel [Weiss 06]

• 3D Kernel [Paris and Durand 06]

#### Box Kernel [Weiss 06]

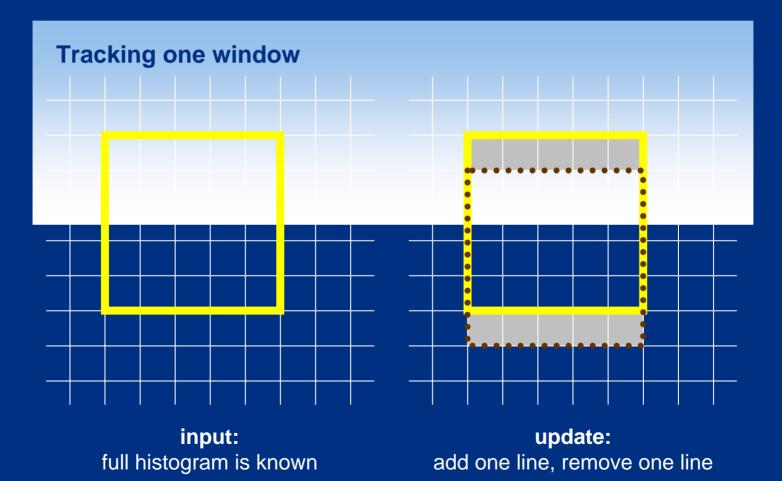
Bilateral filter with a square box window [Yarovlasky 85]

$$Y[I]_{\mathbf{p}} = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} B_{\sigma_{s}} (||\mathbf{p} - \mathbf{q}||) G_{\sigma_{r}} (|I_{\mathbf{p}} - I_{\mathbf{q}}|) I_{\mathbf{q}}$$
  
box window  
$$Y[I]_{\mathbf{p}} = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in B_{\sigma_{s}}} G_{\sigma_{r}} (|I_{\mathbf{p}} - I_{\mathbf{q}}|) I_{\mathbf{q}}$$
  
independent of position **q**

 The bilateral filter can be computed only from the list of pixels in a square neighborhood.

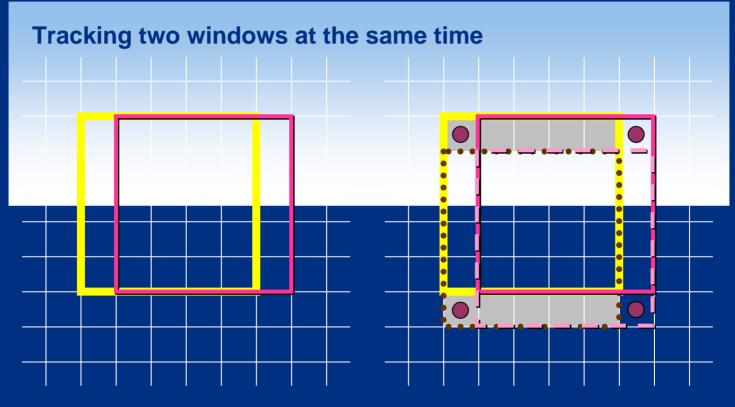
## Box Kernel [Weiss 06]

#### Idea: fast histograms of square windows



## Box Kernel [Weiss 06]

Idea: fast histograms of square windows



input: full histograms are known update: add one line, remove one line, add two pixels, remove two pixels

# Discussion

- Complexity:  $O(|S| \times \log \sigma_s)$ – always fast
- Only single-channel images
- Exploit vector instructions of CPU
- Visually satisfying results (no artifacts)
  - 3 passes to remove artifacts due to box windows (Mach bands)

#### 1 iteration



#### 3 iterations







box kernel visually different, yet no artifacts

# Outline

Brute-force Implementation

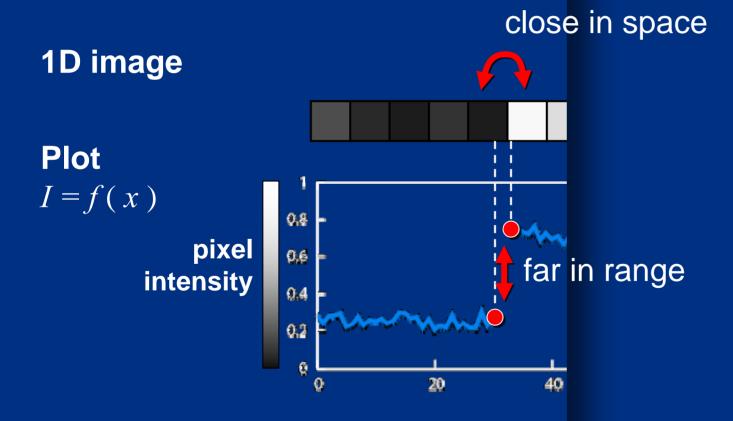
Separable Kernel [Pham and Van Vliet 05]

Box Kernel [Weiss 06]

• 3D Kernel [Paris and Durand 06]

#### **3D Kernel** [Paris and Durand 06]

 Idea: represent image data such that the weights depend only on the distance between points



# 1<sup>st</sup> Step: Re-arranging Symbols

$$BF [I]_{\mathbf{p}} = \frac{1}{W_{\mathbf{p}}} \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{r}} (|I_{\mathbf{p}} - I_{\mathbf{q}}|) I_{\mathbf{q}}$$
$$W_{\mathbf{p}} = \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{r}} (|I_{\mathbf{p}} - I_{\mathbf{q}}|)$$

Multiply first equation by  $W_{\mathbf{p}}$ 

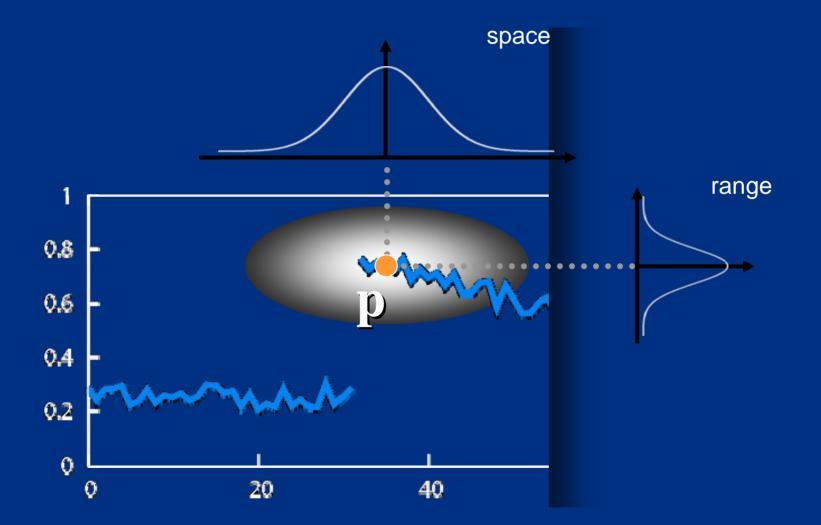
$$W_{\mathbf{p}} BF [I]_{\mathbf{p}} = \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\| \mathbf{p} - \mathbf{q} \|) G_{\sigma_{r}} (| I_{\mathbf{p}} - I_{\mathbf{q}} |) I_{\mathbf{q}}$$
$$W_{\mathbf{p}} = \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\| \mathbf{p} - \mathbf{q} \|) G_{\sigma_{r}} (| I_{\mathbf{p}} - I_{\mathbf{q}} |) 1$$

## 1<sup>st</sup> Step: Summary

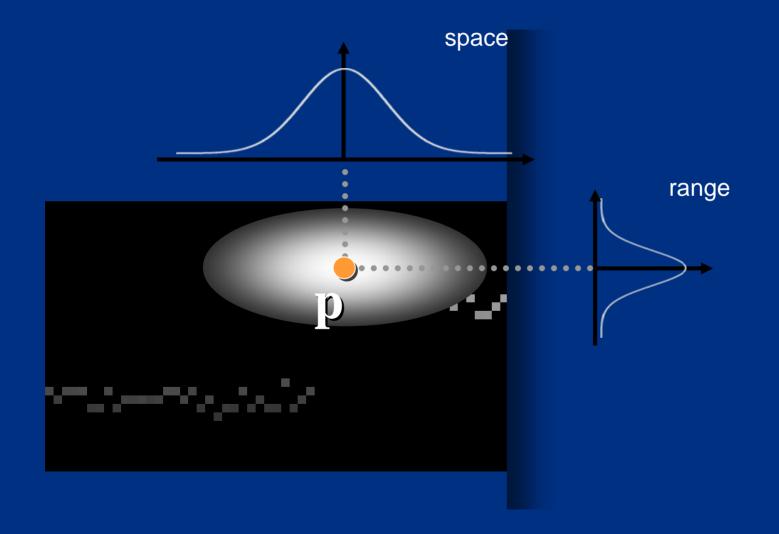
$$W_{\mathbf{p}} BF [I]_{\mathbf{p}} = \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{r}} (|I_{\mathbf{p}} - I_{\mathbf{q}}|) I_{\mathbf{q}}$$
$$W_{\mathbf{p}} = \sum_{\mathbf{q} \in S} G_{\sigma_{s}} (\|\mathbf{p} - \mathbf{q}\|) G_{\sigma_{r}} (|I_{\mathbf{p}} - I_{\mathbf{q}}|) 1$$

- Similar equations
- No normalization factor anymore
- Don't forget to divide at the end

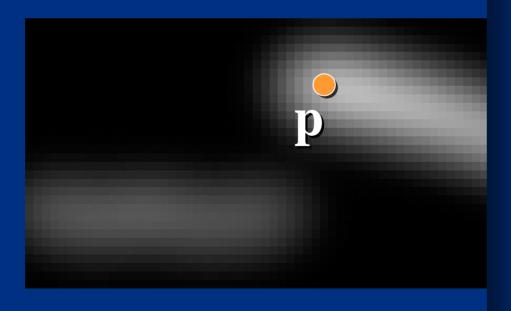
"Product of two Gaussians" = higher dim. Gaussian



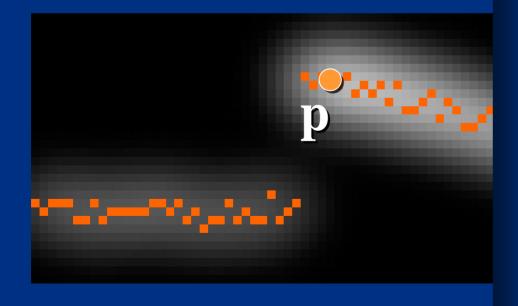
• 0 almost everywhere, I at "plot location"

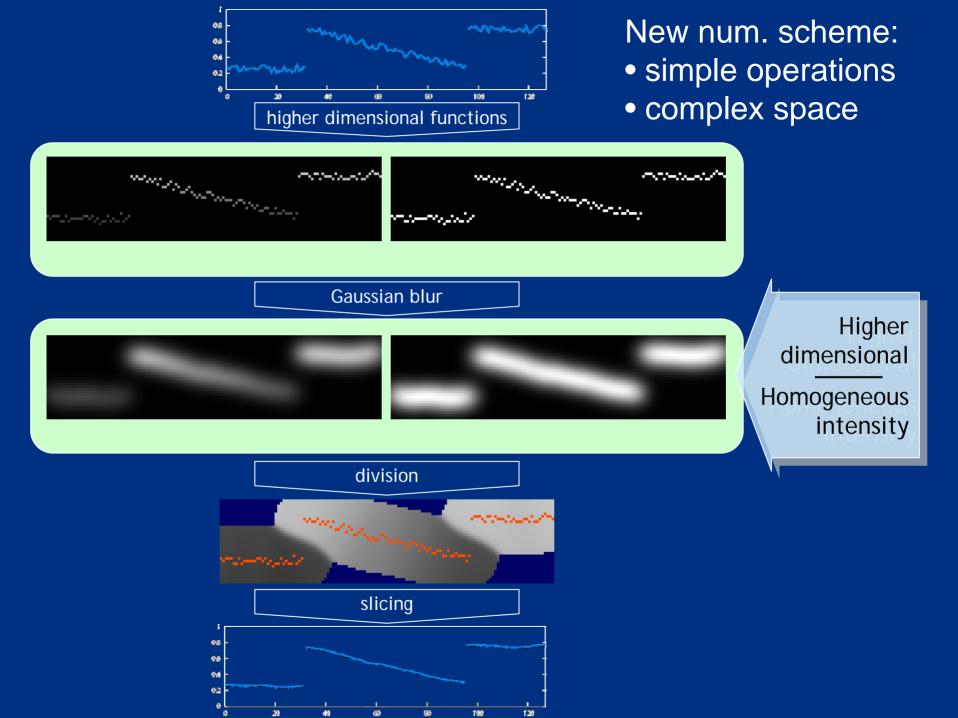


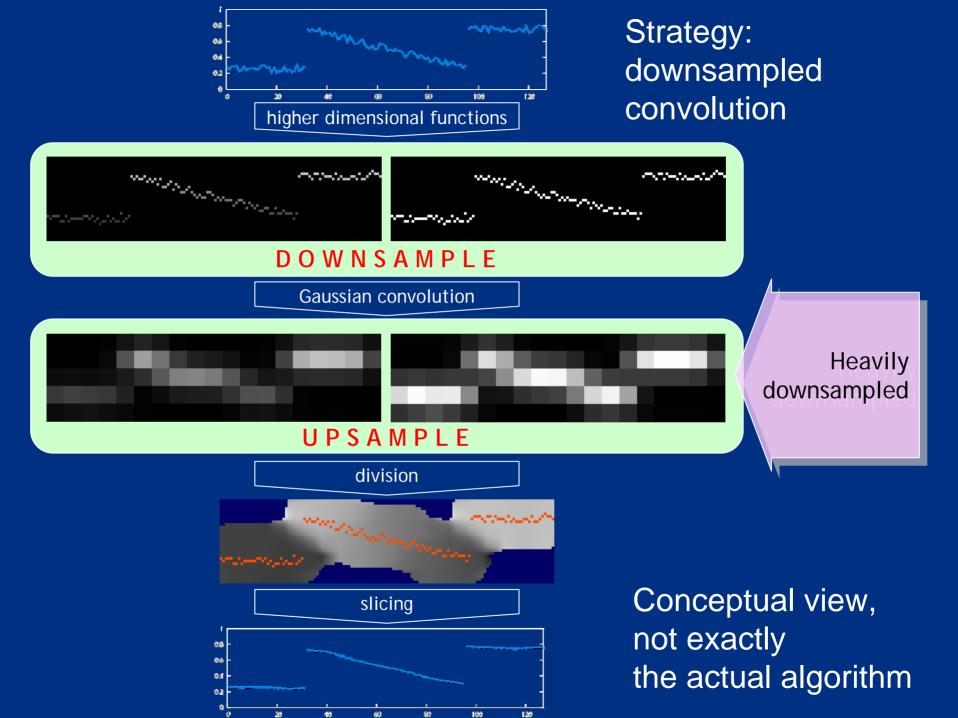
- 0 almost everywhere, I at "plot location"
- Weighted average at each point = Gaussian blur



- 0 almost everywhere, I at "plot location"
- Weighted average at each point = Gaussian blur
- Result is at "plot location"







# **Actual Algorithm**

Never compute full resolution
 On-the-fly downsampling
 On-the-fly upsampling

• 3D sampling rate =  $(\sigma_s, \sigma_s, \sigma_r)$ 

## **Pseudo-code: Start**

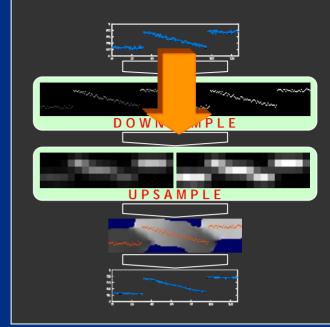
- Input
  - image I
  - Gaussian parameters  $\sigma_{\rm s}$  and  $\sigma_{\rm r}$

• Output: *BF* [*I*]

• Data structure: 3D arrays wi and w (init. to 0)

## Pseudo-code: On-the-fly Downsampling

• For each pixel  $(X, Y) \in S$ 



- Downsample:  $(x, y, z) = \left( \left[ \frac{X}{\sigma_{s}} \right], \left[ \frac{Y}{\sigma_{s}} \right], \left[ \frac{I(X, Y)}{\sigma_{r}} \right] \right)$ 

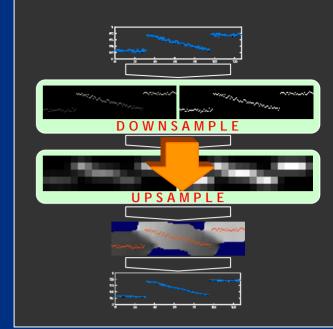
[] = closest int.

– Update:

wi(x, y, z) += I(X, Y)w(x, y, z) += 1

# Pseudo-code: Convolving

• For each axis X, Y, and Z



- For each 3D point (x, y, z)

• Apply a Gaussian mask (1,4,6,4,1) to *wi* and *w* e.g., for the *x* axis:

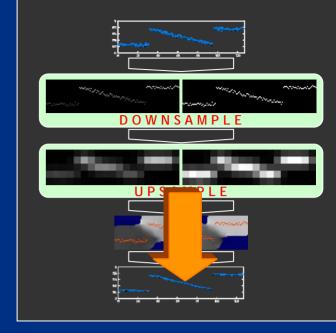
wi'(x) = wi(x-2) + 4.wi(x-1) + 6.wi(x) + 4.wi(x+1) + wi(x+2)

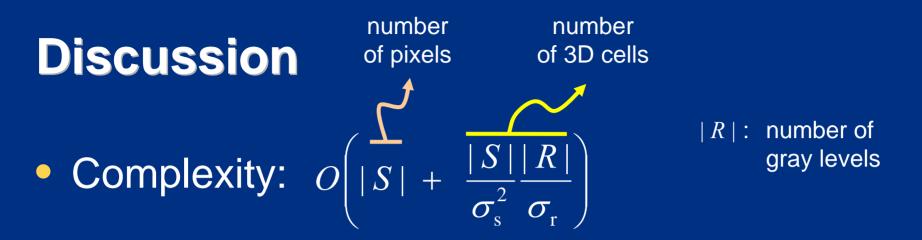
# Pseudo-code: On-the-fly Upsampling



- Linearly interpolate the values in the 3D arrays

 $BF[I](X,Y) = \frac{\text{interpolate}(wi, X, Y, I(\overline{X}, Y))}{\text{interpolate}(w, X, Y, I(X, Y))}$ 





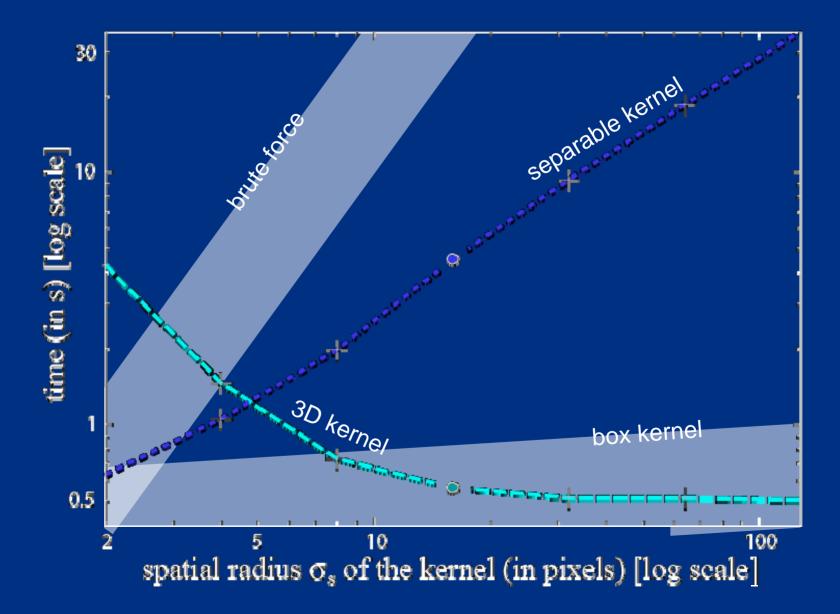
- Fast for medium and large kernels
   Can be ported on GPU [Chen 07]: always very fast
- Can be extended to color images but slower
- Visually similar to brute-force computation







# **Running Times**



# **How to Choose an Implementation?**

Depends a lot on the application. A few guidelines:

- Brute-force: tiny kernels or if accuracy is paramount
- Box Kernel: for short running times on CPU with any kernel size, e.g. editing package
- 3D kernel:
  - if GPU available
  - if only CPU available: large kernels, color images, cross BF (e.g., good for computational photography)

**Questions?**