This is a list of references for the general submodular optimization part of the CVPR 2015 tutorial on energy minimization.

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