## Regular Polygons

For the following formulas, n is the number of sides in the polygon and s is the length of each side. q is the measure of one of the interior angles. The radius of the inscribed circle is r, and the radius of the circumscribed radius is R.

Sum of interior angles:  $180(n-2)^{\circ}$ 

Interior angle measure:  $q = \frac{180(n-2)}{n}$ 

Area:  $K = \frac{rns}{2}$ 

| Polygon  | n | K                        | r   | R                               |
|----------|---|--------------------------|---|---------------------------------|
| Triangle | 3 | $\frac{s^2\sqrt{3}}{4}$  | $\frac{s\sqrt{3}}{6}$                       | $\frac{s\sqrt{3}}{3}$           |
| Square   | 4 | $s^2$                    | $\frac{s}{2}$                               | $\frac{s}{2}\sqrt{2}$           |
| Hexagon  | 6 | $\frac{3s^2\sqrt{3}}{2}$ | $\frac{s\sqrt{3}}{2}$                       | S                               |
| Octagon  | 8 | $2s^2(1+\sqrt{2})$       | $s\sqrt{\left(1+\frac{\sqrt{2}}{2}\right)}$ | $\frac{s\sqrt{3-2\sqrt{2}}}{2}$ |