## Triangles

## Right Triangles

Pythagorean Theorem: $a^{2}+b^{2}=c^{2}$
Geometric relationships:

$$
\begin{aligned}
& h^{2}=d e \\
& a^{2}=d c
\end{aligned}
$$

Median to hypotenuse:


## General Triangles

Law of Sines: $\frac{\sin A}{a}=\frac{\sin B}{b}=\frac{\sin C}{c}$
Law of Cosines: $\quad c^{2}=a^{2}+b^{2}-2 a b \cos C$

In the following formulas, the semiperimeter is $s=\frac{a+b+c}{2}, K$ is the area of the triangle, $r$ is the radius of the inscribed circle, and $R$ is the radius of the circumscribed circle.

Area: $K=\frac{1}{2} a b \sin C=\frac{1}{2} h_{c} c$
Heron's Formula: $K=\sqrt{s(s-a)(s-b)(s-c)}$
Inscribed radius: $r=\frac{K}{s}$
Circumscribed radius: $R=\frac{a b c}{4 K}, \quad R=\frac{c}{2 \sin C}$


