

Resolving Over-constrained Temporal Problems with Uncertain Durations

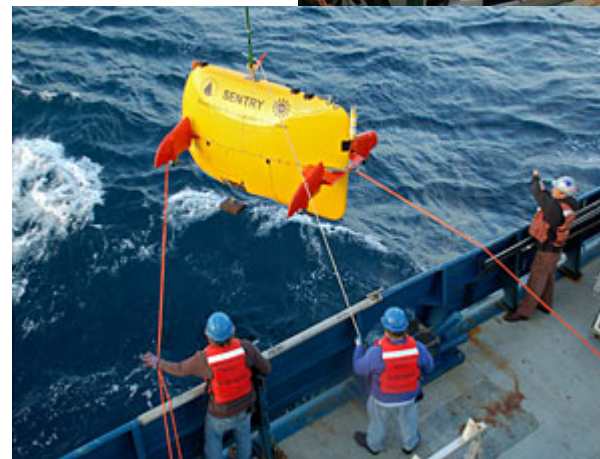
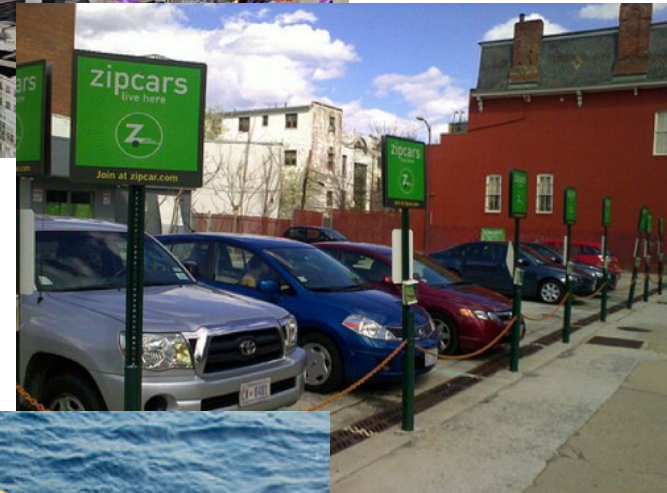
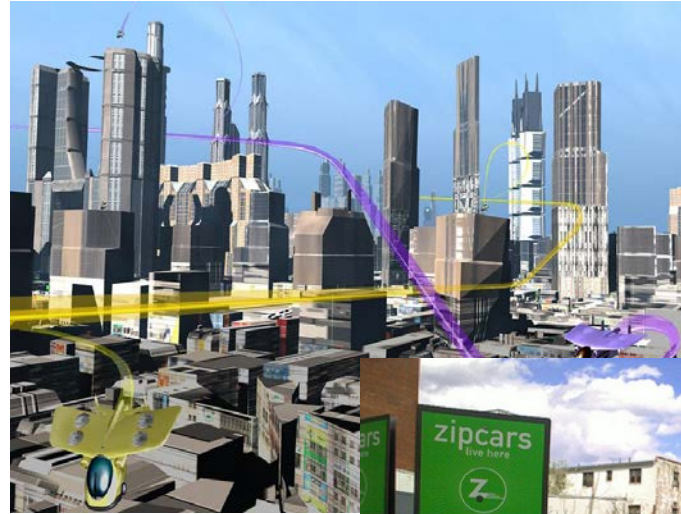
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March 7, 2014

Take Away Messages

- Over-constrained temporal problems can be better resolved by relaxing the temporal constraints **continuously**, instead of removing them **discretely**.
- The fundamental concepts of **conflicts** and **minimal relaxations** naturally generalize to the continuous case.
- Restoring controllability requires both **tightening** uncertain durations and **relaxing** constraints.
- We can efficiently enumerate relaxations in **best-first order**, by generalizing the Conflict-Directed A* algorithm, first developed for diagnosis.

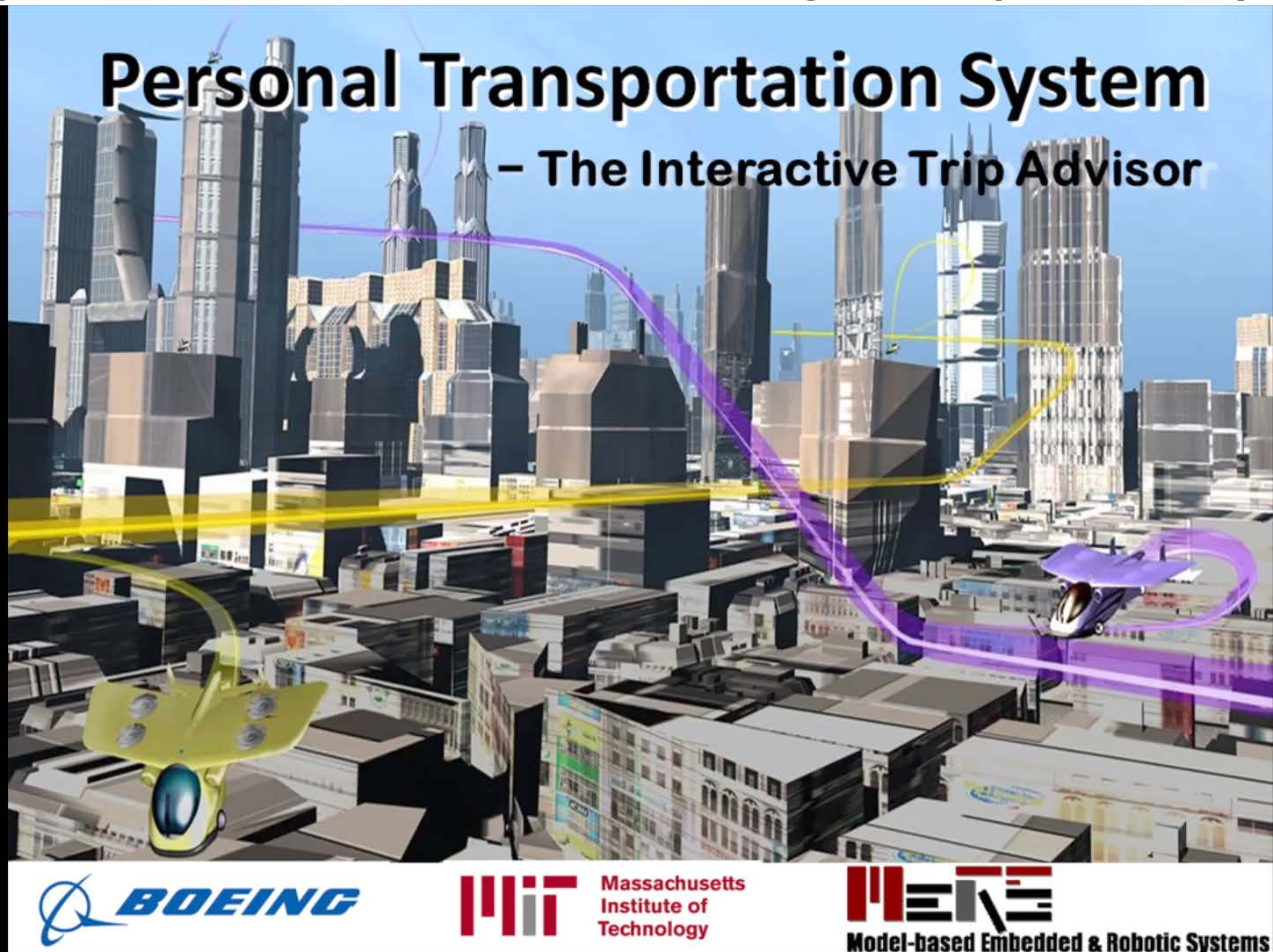
Ongoing Projects

- Personal Transportation System.
- Trip advisor for commuters.
- Mission advisory system for deep sea exploration.



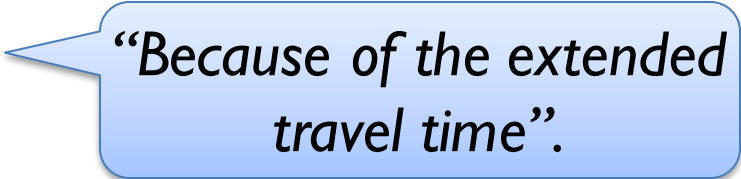
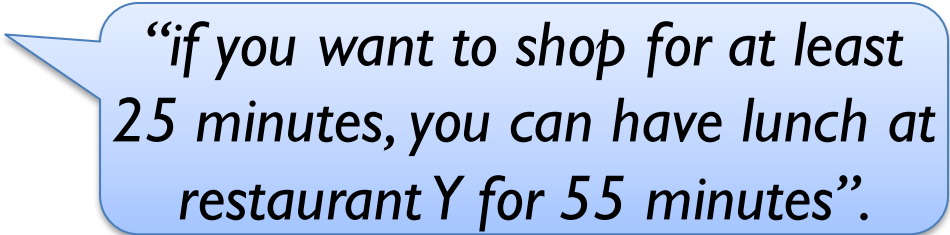


Robotic Personal Transportation System

- A personal air taxi with an intelligent trip advisory



Key features

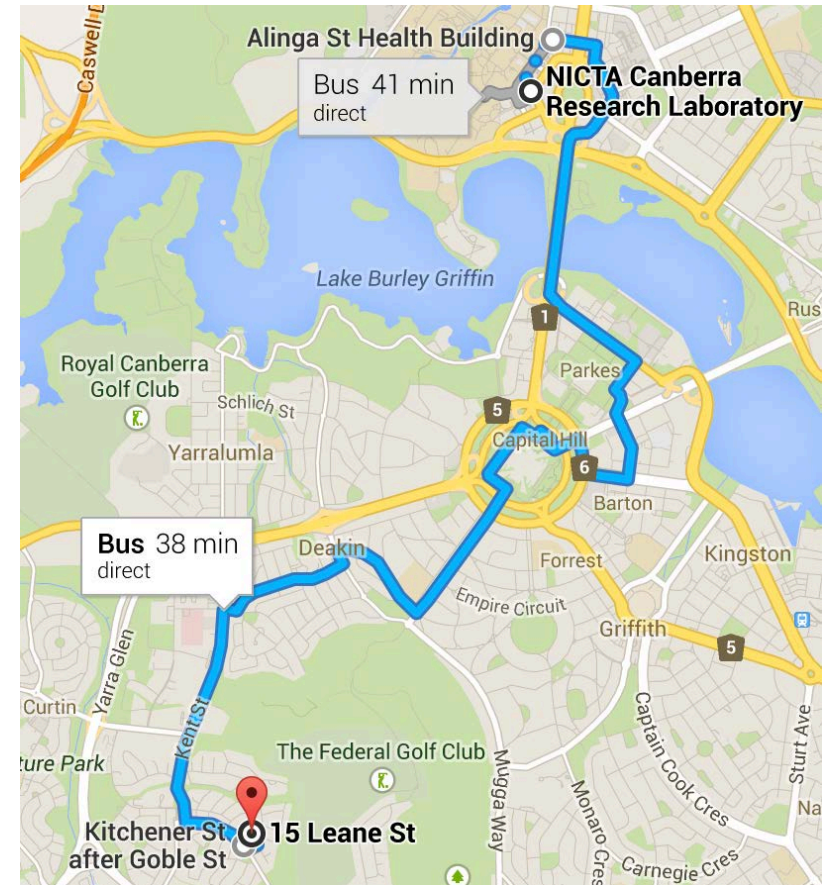
- Find alternative solutions that are **simple** and **preferred**.
- Provide **insights** into cause of failure and its resolution.
 - Minimize the perturbations;
*“Delay your arrival by 5 minutes”.*
 - Prioritize alternatives;
*“OK, then how about having lunch at restaurant Y”.*
 - Explain the cause of failure;
*“Because of the extended travel time”.*
 - Adapt incrementally to new constraints.
*“if you want to shop for at least 25 minutes, you can have lunch at restaurant Y for 55 minutes”.*

When There Is Uncertainty

- Uncertainty Sensitive Transit Advisor.

It is **6pm** now and Brian is leaving NICTA for home.

- He wants to **be home in 40 minutes**, and is only willing to take buses.
- Right now, he is looking up Google Map for directions...

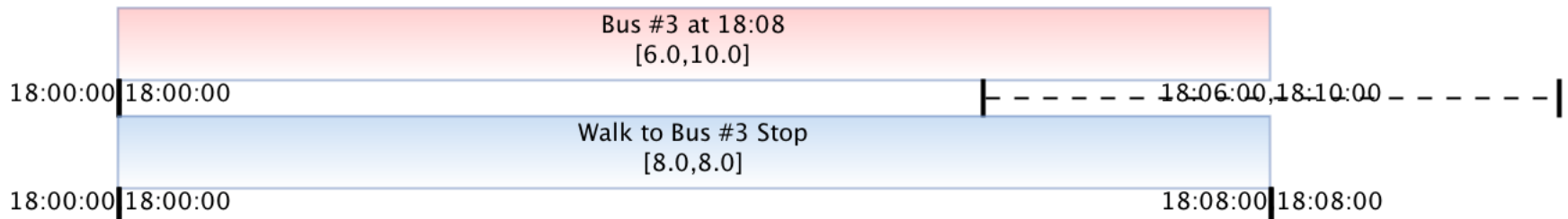


Which Bus To Take

- Google Map returns two options (leaving NICTA at 1800), ranked based on trip duration
- Option 1:
 - Take the **18:08 Bus #3** (Ride time 23 mins).
 - Walking to departure stop: 8 mins.
 - Walking from arrival stop to home: 3 mins.
- Option 2:
 - Take the **18:11 Bus #934** (Ride time 26 mins).
 - Walking to departure stop: 10 minutes.
 - Walking from arrival stop to home: 3 minutes.

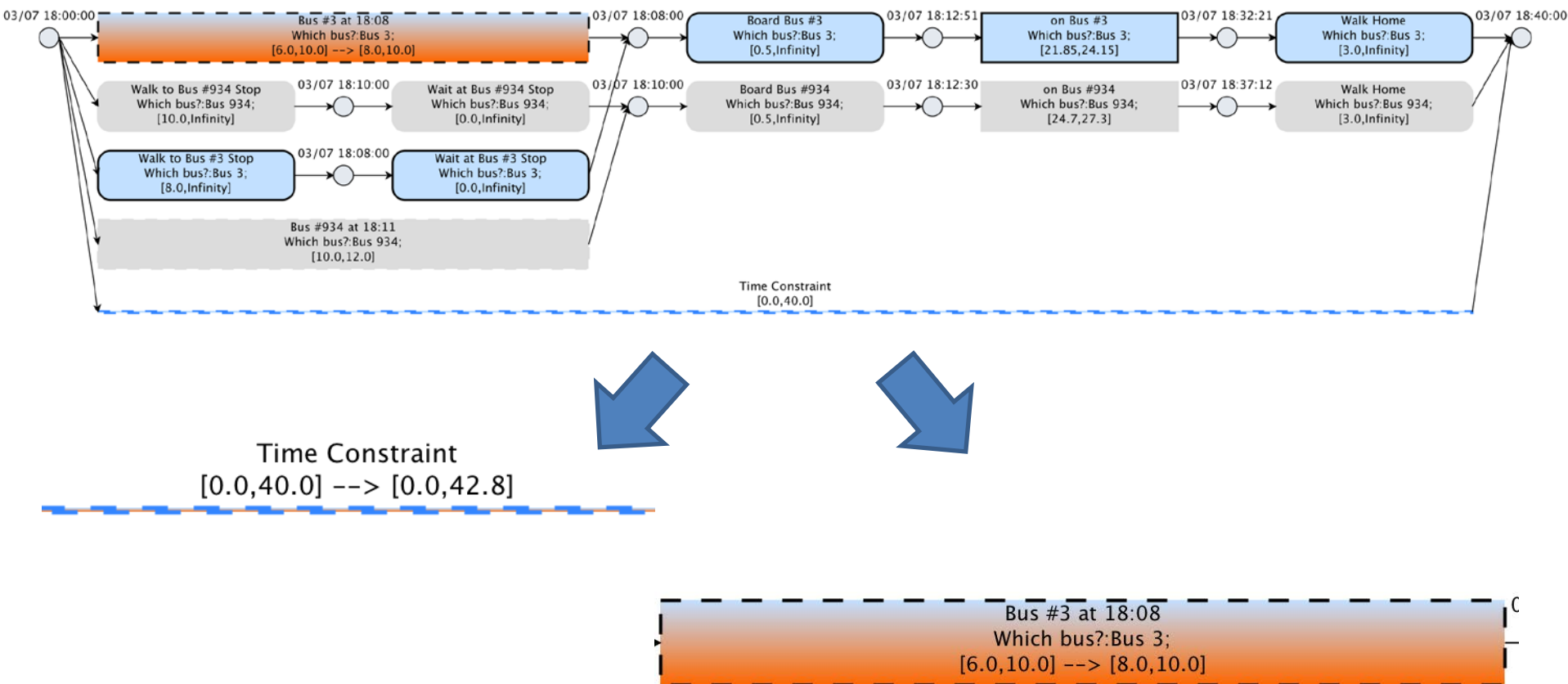
Uncertainty Affects Our Decision

- Buses may be late or early:
 - Bus #3: 18:08 \pm 2 minutes.
 - Bus #934: 18:11 \pm 1 minute.
- Brian may miss the bus if he takes the Google preferred option.



Cope With the Uncertainty

- “You can catch Bus #934 and arrive home **3 minutes late**.”
- “Or, you can take Bus #3 and arrive home on time, but **taking the risk** of missing the bus, if it arrives early.”



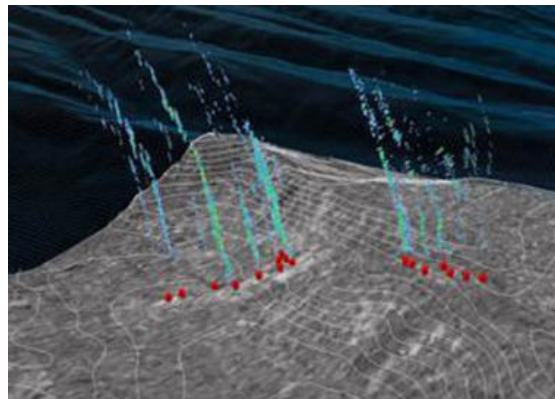
Mission Advisor for Woods Hole Oceanographic Inst.

- During an expedition cruise, the chief scientist needs assistance for planning and scheduling activities, especially when things go wrong.
 - Task sequencing and scheduling.
 - Goal relaxation and failure recovery.
 - Human resources and assets management.



A WHOI Mission

- Duration: Sep 26th – Oct 17th.
- Vessel: R/V Atlantis.
- Location: Along the coast between SF and LA.
- Objectives:
 - Find and sample methane seeps near the coast.
 - Locate and sample a 60 year-old DDT dumping site.
 - Recover and replace incubators on the seafloor.



A 3-day Plan From the Cruise

From: "David Valentine" <scil@atlantis.whoiedu>
Subject: Plan of the day 9/28+
Date: Sat, September 28, 2013 6:37 am
To: pod@atlantis.whoiedu

Draft Cruise Plan 9/28-9/30

9/27/13

Sentry Dive at Partington Canyon	6hrs	Target start time 2000
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9/28/13

Depart Partington Canyon		Estimated Departure Time 0230
Transit to Paull's Pingo	27 hrs	ETA 0530 hrs (9/29/13)
Science Meeting 10AM!		
Multibeam pass of SBB-2H Pockmark		Line Z to Z'
Multibeam pass in Southern SB Channel and D to D'		Lines A to A', B to B', C to C'
Multibeam pass of SW Mounds area		Lines E to E' and F to F'

9/29/13

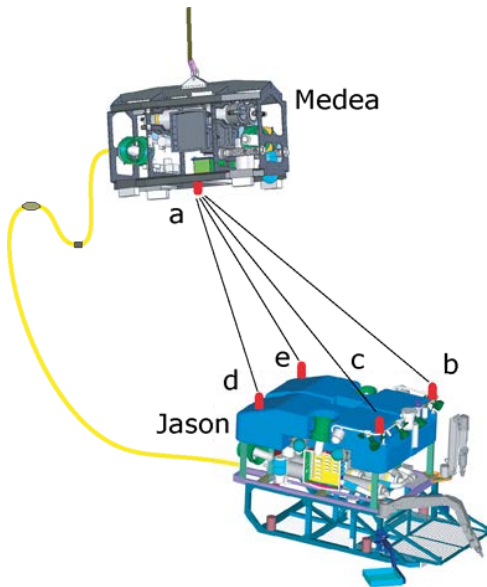
Arrive at Paull's Pingo		ETA 0530 hrs
Jason Operations at Paull's Pingo Deployments	15 hrs	Deploy by 0730; 2 Elevator
Transit to SW mounds	1.5 hrs	Arrive SW Mounds ~2400

9/30/13 and beyond

Sentry deployment at SW Mounds	16 hrs	Deploy at 0000
Jason Deployment at SW Mounds	24 hrs	Multiple Elevators

Everything can Go Wrong

- [Day 1] Jason failed after 30 min into its first dive, entered an uncontrollable spin and broke its optic fiber tether.
- [Day 1] The new camera installed on Sentry did not work well in low light situations. It had been replaced during its second dive.



Everything can Go Wrong

- [Day 2] Jason entered an uncontrollable spin and broke its optic fiber tether again during its second dive. It turned out that there is a bug in its newly updated code.
- [Day 3] Sentry's mass spectrometer failed during its second dive. They sent Rich to Pittsburg to get it fixed.

... ..

- [Day 7] Sentry aborted its mission 1 hour after launch. Atlantis aborted its mapping routes and went back to recover Sentry. The failure was caused by a burned wire.

Our Deliverable

- A mission advisory system that assists the chief scientists of expeditions on the following tasks:
 - Scheduling Activities with Uncertainty.
 - Failure and Downtime Recovery Scheduling.
 - Assets Managements.



- Relaxations of Conditional Temporal Problems;
- Continuous Relaxation and Conflict Resolution;
- Restoring Controllability with Uncertainty Durations;
- Best-first Enumeration through Conflict-directed Relaxation;
- Experiments.

Problem Formulation

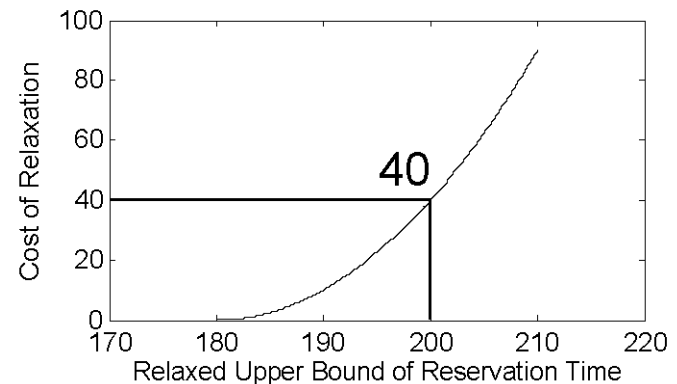
- Model: (Over-constrained) Controllable Conditional Temporal Problems with Uncertainty.
 - All choices are **controllable**.
 - Allowing temporal constraints to be **relaxed**.
 - Allowing uncertain durations to be **tightened**.
- A solution is a pair with:
 - A complete set of **decisions**.
 - A set of continuous **relaxations** for temporal constraints.
 - A set of continuous **tightening** for uncertain durations.such that the set of activated durations and constraints is consistent/controllable.

Define User Preferences

- Preference functions are defined over decisions and constraint relaxations.
 - Each decision is mapped to a positive reward by function f_p .
 - Each constraint relaxation/duration tightening is mapped to a positive cost by function f_e .

Store	A	40
	B	100
Lunch	X	70
	Y	80
	Z	30

Assignment: $\{Store = B, Lunch = Y\}$
Reward: $100 + 80 = 180$

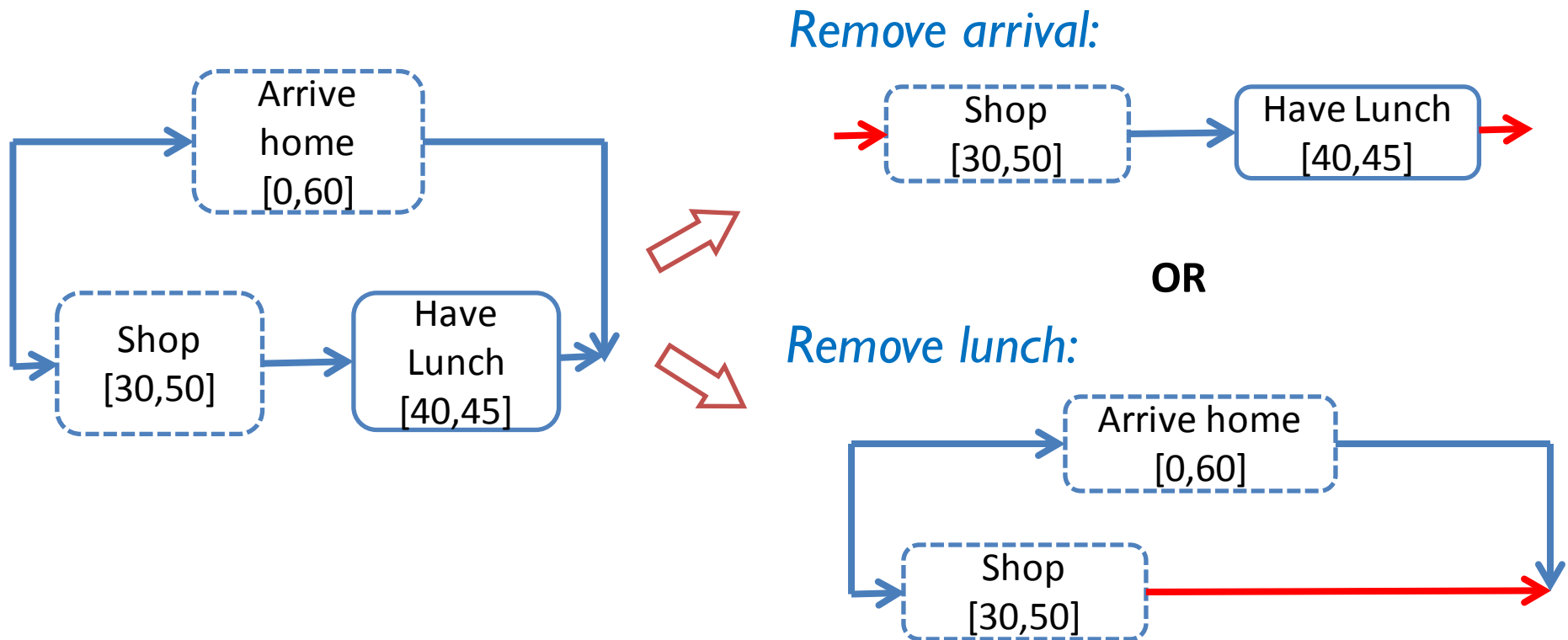


Relaxation: $Reservation[0,180] \rightarrow [0,200]$
Cost: $f_e(200 - 180) = 40$

- Relaxations of Conditional Temporal Problems;
- **Continuous Relaxation** and Conflict Resolution;
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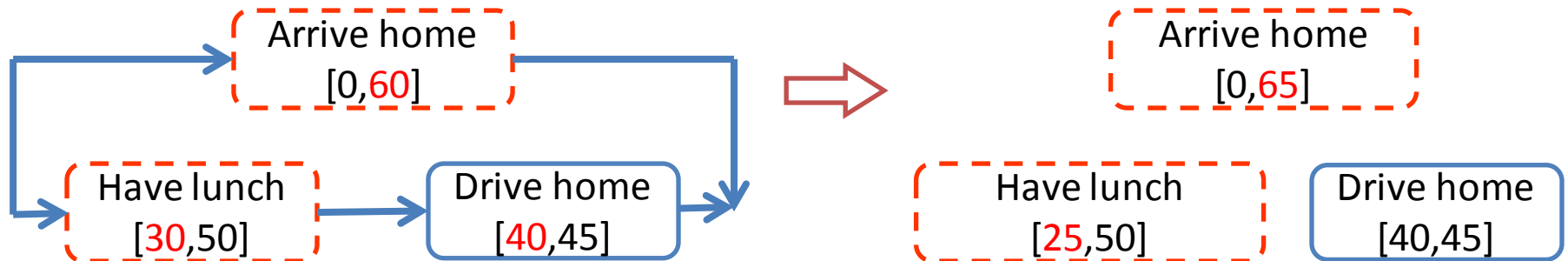
(Minimal) Discrete Relaxation

- Resolve over-constrained temporal problem C by **removing** constraints.
 - Resolved: $M \subseteq C$ such that $C \setminus M$ is consistent.
 - Minimal: $\forall c \in M$ $(C \setminus M) \cup \{c\}$ is inconsistent.



Continuous Relaxation

- Relax a constraint partially
by **continuously** modifying its temporal bounds:
 - A continuous relaxation, CR_i , weakens a temporal constraint: $[LB, UB] \rightarrow [LB', UB']$ where $LB' \leq LB$ and $UB' \geq UB$.
 - Continuous relaxations only apply to **relaxable** constraints.



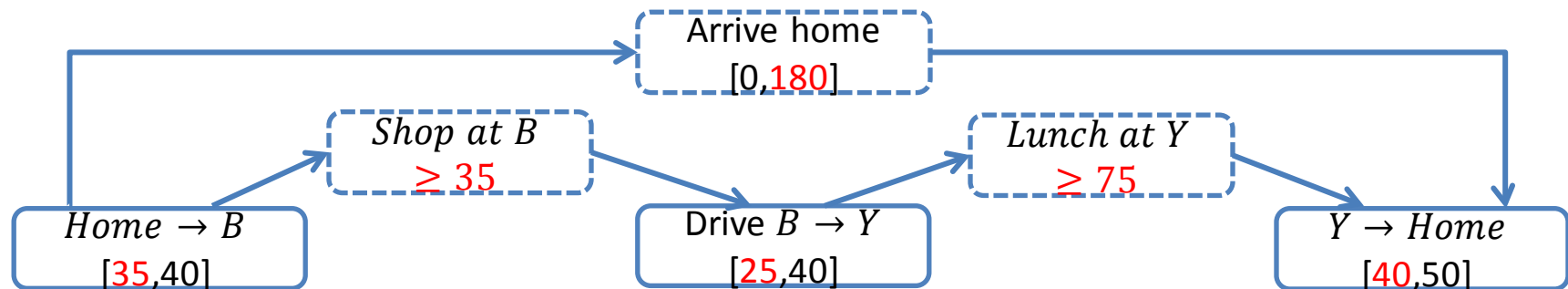
“Shorten lunch to 25 minutes and delay arrival by 5 minutes”

- Relaxations of Conditional Temporal Problems;
- Continuous Relaxation and **Conflict Resolution**;
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- Best-first Enumeration through Conflict-directed Relaxation;
- Experiments.

I. Learn Discrete Conflicts

- A discrete conflict is an inconsistent set of temporal constraints.

Choosing **Store=B** and **Lunch=Y** produces:



**Discrete
Conflict:**

Store = B;
Home → B ≥ 35 ;
Drive B → Y ≥ 25 ;
Y → Home ≥ 40 ;

Lunch = Y;
Shop at B ≥ 35 ;
Lunch at Y ≥ 75 ;
Arrive Home ≤ 180 .

2. Weaken to Continuous Conflicts

- A continuous conflict is an equation formed from the discrete conflict.
- It specifies the deviation needed to resolve the conflict.

Discrete Conflict:

$\text{HometoB} \geq 35;$
 $\text{ShopatB} \geq 35;$
 $\text{BtoY} \geq 25;$
 $\text{LunchatY} \geq 75;$
 $\text{YtoHome} \geq 40;$
 $\text{ArriveHome} \leq 180.$



Continuous Conflict:

$$\text{ArriveHome} - \text{HometoB} - \text{ShopatB} - \text{BtoY} - \text{LunchatY} - \text{YtoHome} = -30$$

3. Map to Constituent Continuous Relaxations

- Relaxations specified by linear inequalities:

$$\begin{aligned} & \textit{ArriveHome} - \textit{HometoB} - \textit{ShopatB} \\ & - \textit{BtoY} - \textit{LunchatY} - \textit{YtoHome} = -30 \end{aligned}$$



$$\Delta_{\textit{ShopatB}} + \Delta_{\textit{LunchatY}} + \Delta_{\textit{ArriveHome}} \geq 30$$

Discrete vs. Continuous Relaxations

- Resolve a conflict by relaxing constraints **completely** or **partially**.

Conflict:

Store = **B**, Lunch = **Y**;
Home \rightarrow B \geq 35; Shop at B \geq **35**;
Drive B \rightarrow Y \geq 25; Lunch at Y \geq **75**;
Y \rightarrow Home \geq 40; Arrive Home \leq **180**.



**Discrete
Resolutions**

Remove Shop at B \geq **35**;
Remove Lunch at Y \geq **75**;
Remove Arrive Home \leq **180**



**Continuous
Resolutions**

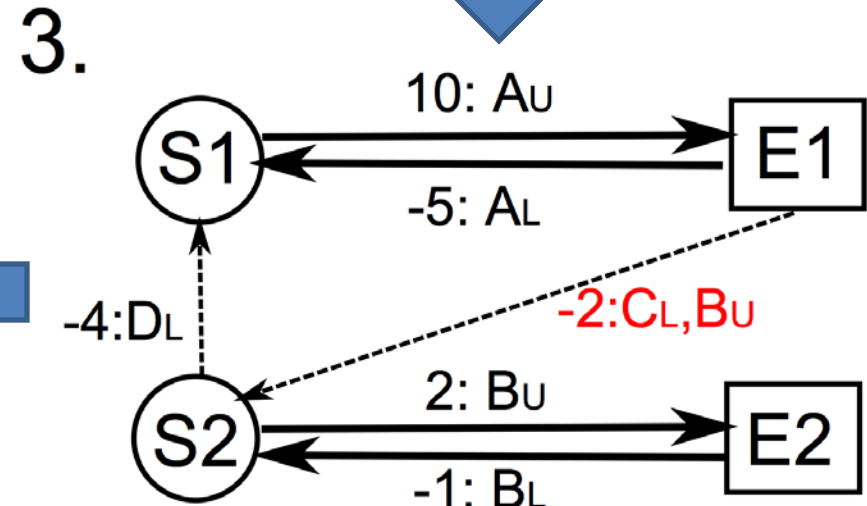
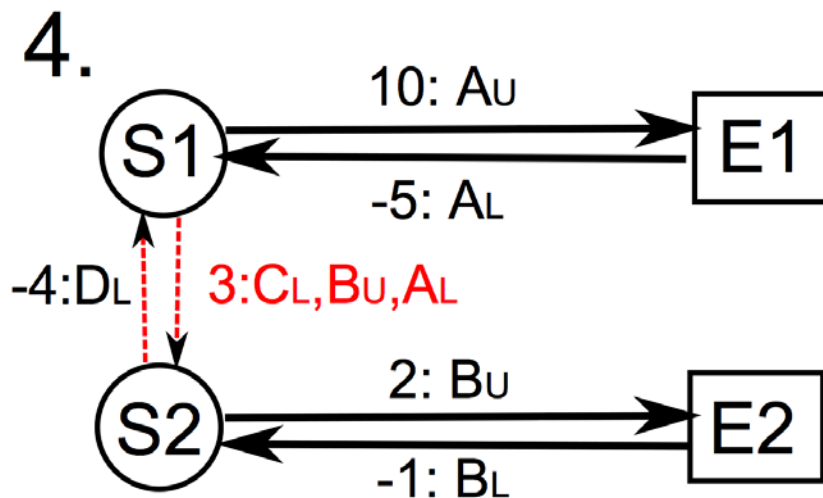
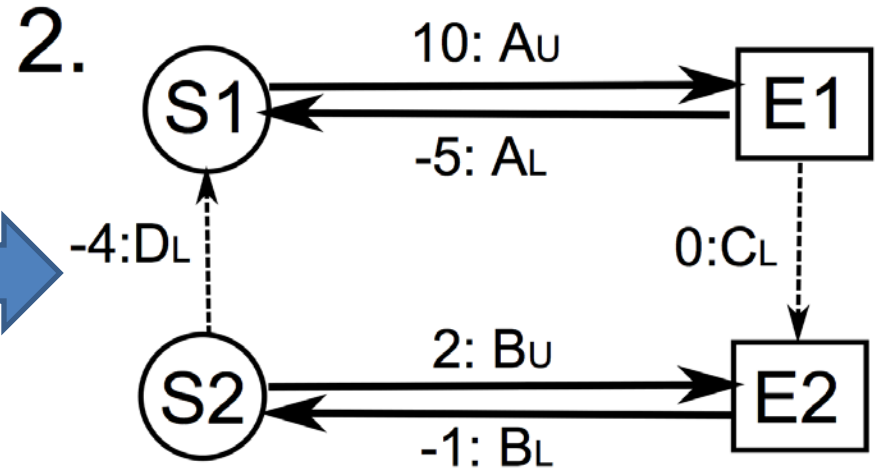
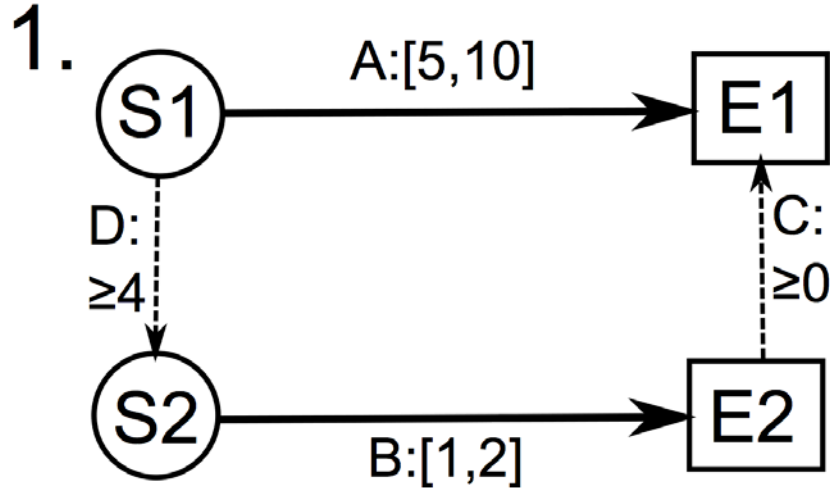
Lunch at Y \geq **45**;
Arrive Home \leq **210**;
Shop at B \geq **25** and Lunch at Y \geq **55**;
... ..
and many more

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- Continuous Relaxation and Conflict Resolution;
- Restoring Controllability with Uncertainty Durations;
- Best-first Enumeration through Conflict-Directed Relaxation;
- Experiments.

Learn Conflicts From Uncontrollable Problems

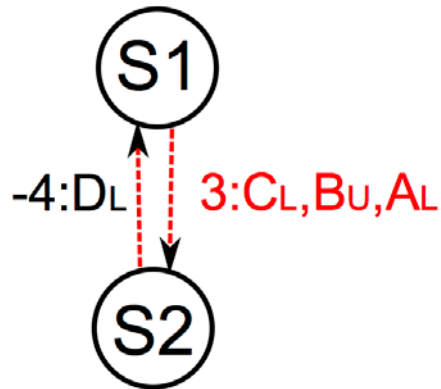
- Learning conflicts from controllability checking algorithms is difficult.
 - For consistency checking, there is a **one-to-one mapping** between the distance edges and the bounds of constraints.
 - No such mapping exists for controllability checking (strong and dynamic) **due to the reduction procedures**, making it difficult to extract conflicts from the reduced graph.
- Key: during the reduction, **record the ‘contribution’** of each constraint and duration in the temporal problem.

A Strong Controllability Example



Resolving Uncontrollable Conflicts

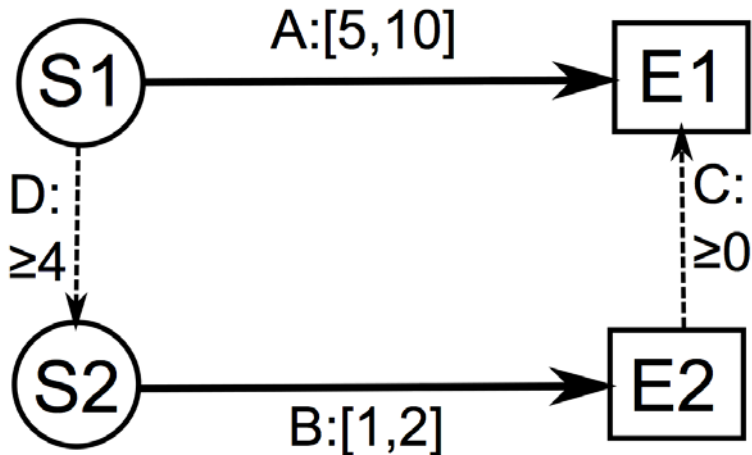
- Constraint for resolving continuous conflict (negative value -1):



$$\Delta D_L + \Delta C_L + \Delta B_U + \Delta A_L \geq 1$$

where:

- $\Delta C_L, \Delta D_L$ are relaxations for C and D.
- $\Delta A_L, \Delta B_U$ are tightening for A and B.



and

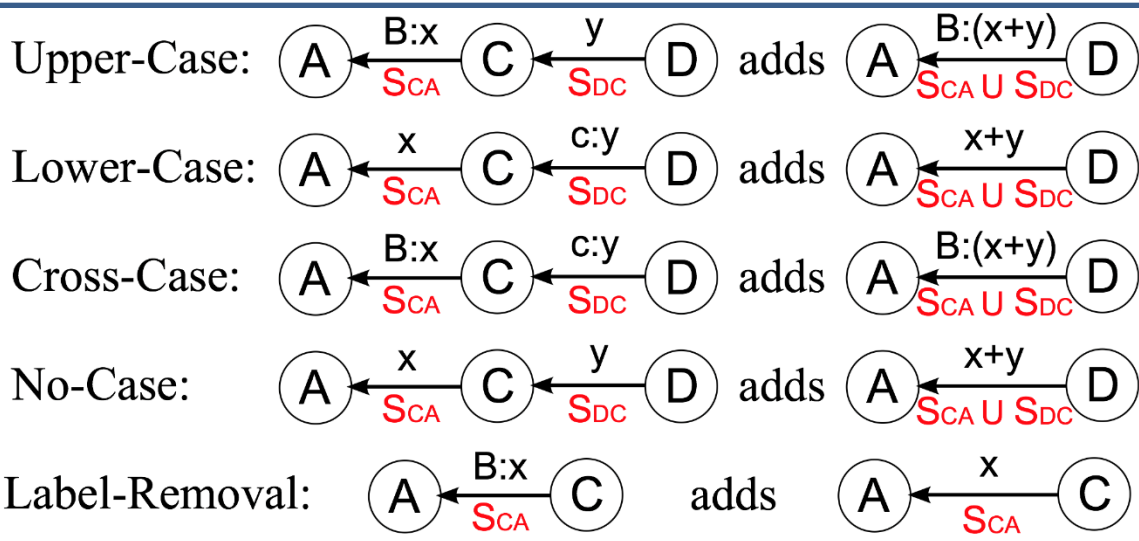
$$\Delta A_L \leq 5; \Delta B_U \leq 1.$$

Learn Dynamically Uncontrollable Conflict

- Record supporting constraints and durations during the iterative reduction procedure, and extract conflicts using the them.

```

1  DG ← GETNORMALDISTANCEGRAPH(T);
2  for 1 to K do
3    NCycle ← ALLMAXCONSISTENT(DG);
4    if NCycle == null then
5      for E in LOWERCASEEDGES(DG) do
6        moatPaths ← PROPAGATE(E);
7        for Path in moatPaths do
8          E' ← REDUCE(E, Path);
9          SUPPORTS(E') ← SUPPORTS(E, Path);
10         ADDTOGRAPH(E', DG)
11       end
12     end
13   else
14     return GETSUPPORTS(NCycle);
15   endif
16 end
17 NCycle ← ALLMAXCONSISTENT(DG);
18 return GETSUPPORTS(NCycle);
    
```



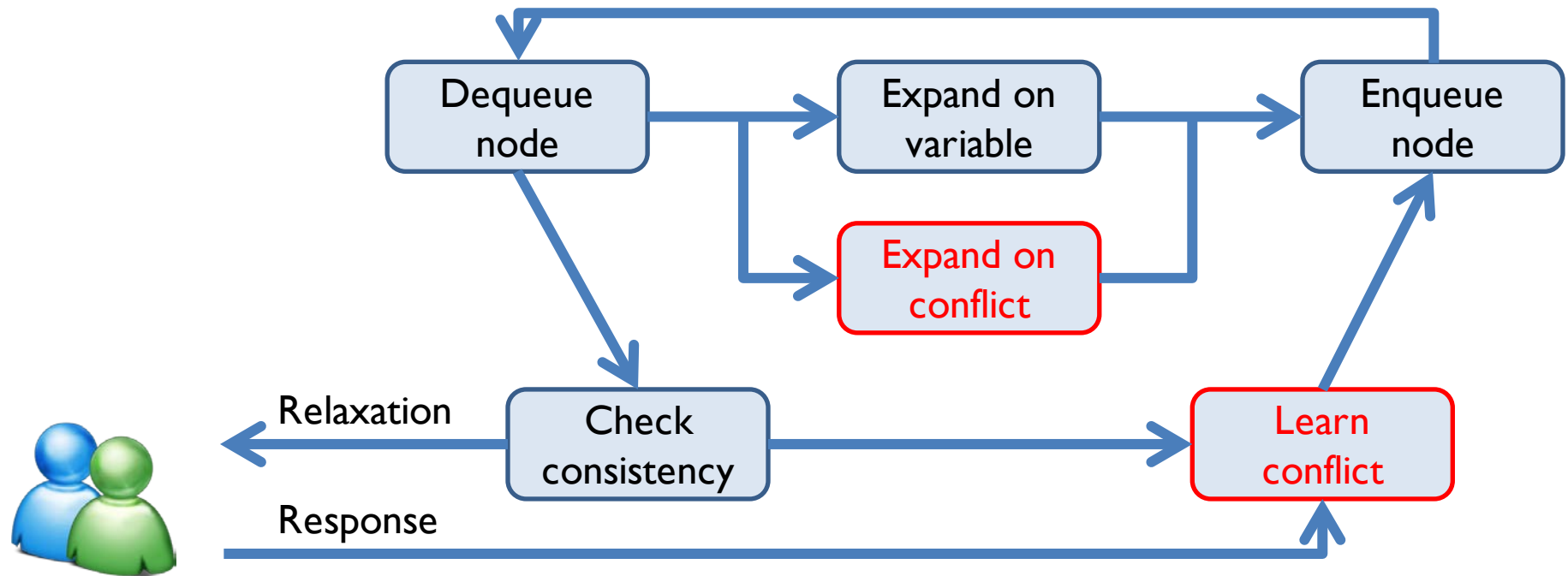
- Relaxations of Conditional Temporal Problems;
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Generalize CDA* to Continuous Relaxations

- Conflict-Directed A* (Williams and Ragno, 2004) can be applied to discrete relaxation problems:
 - Efficiently prunes search space using learned conflicts.
 - Enumerates minimal discrete relaxations in best-first order.
- To solve a relaxation problem:
 - Frame an equivalent constraint optimization problem.
 - A. Discrete relaxation: add binary variables.
 - B. Continuous relaxation/tightening: add non negative continuous variables.
 - The objective function represents the preference.

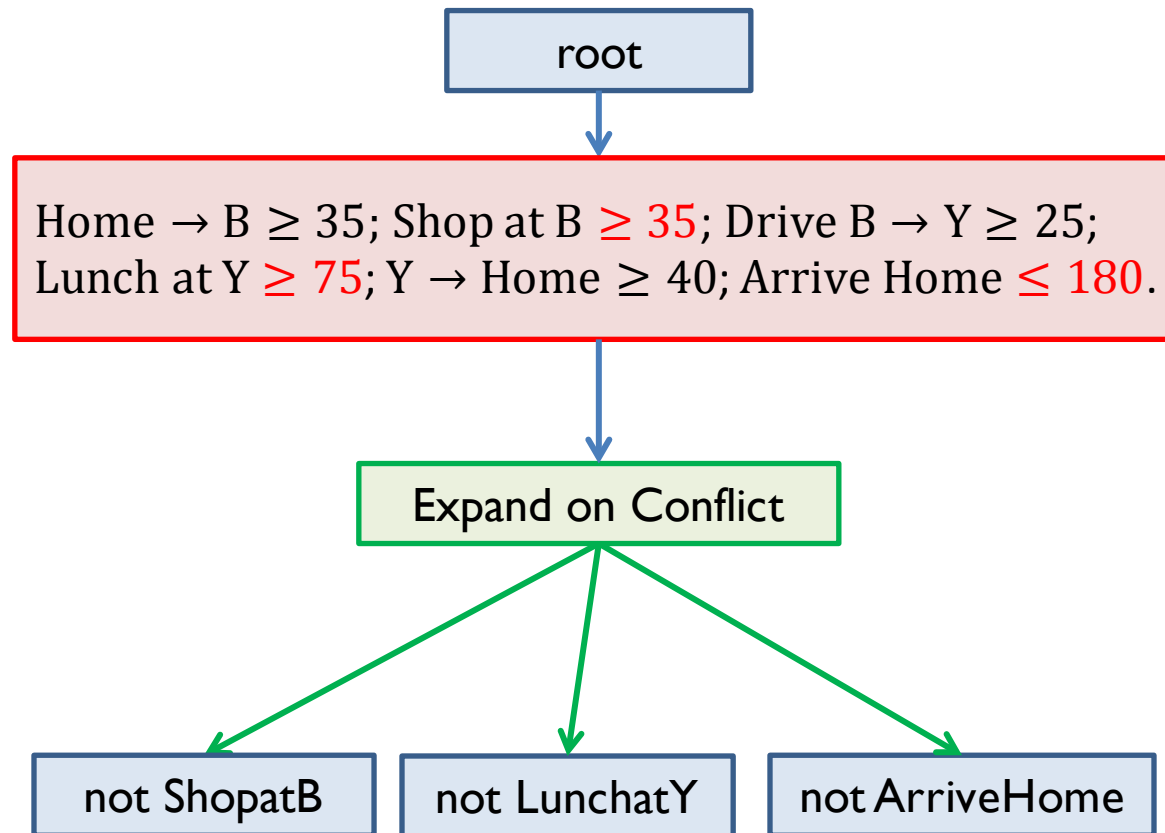
Best-first Conflict Directed Relaxation

- BCDR generalizes the conflict resolution procedure in CDA* to include constituent continuous relaxations.



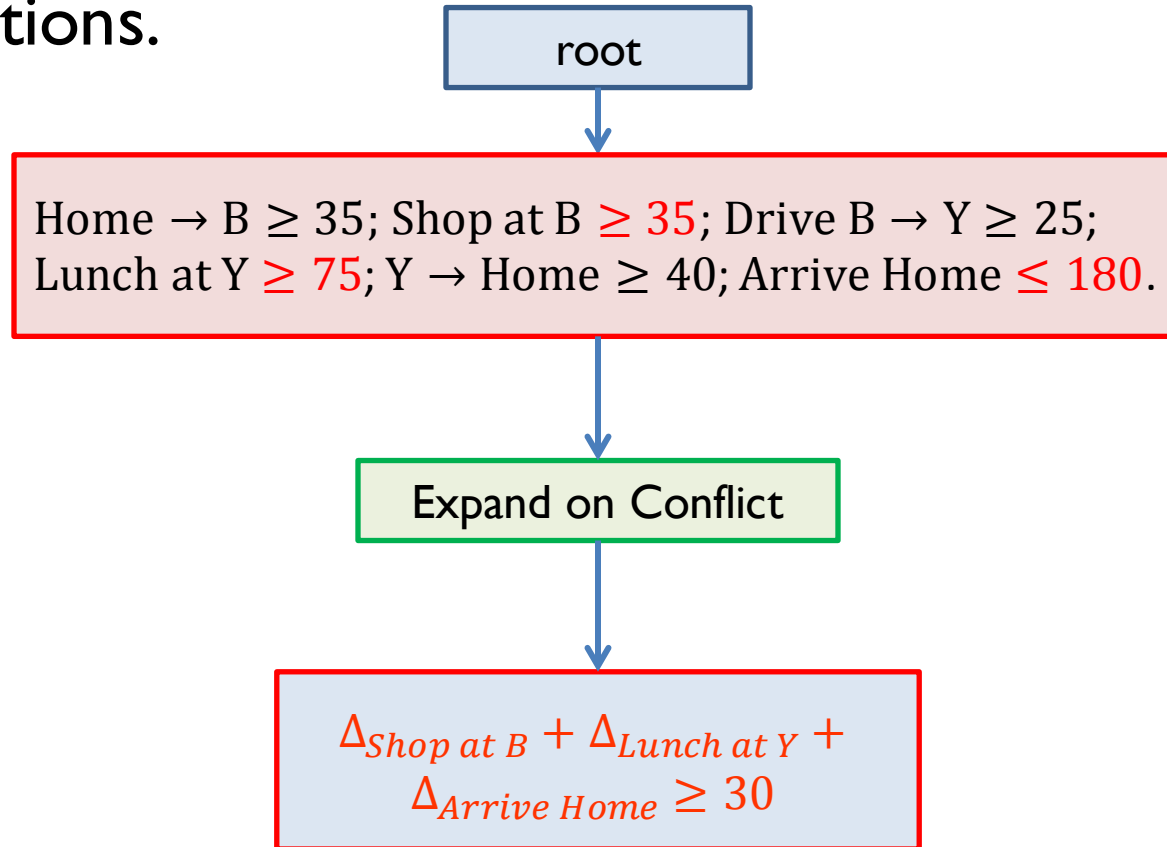
Conflict-Directed A*

- Key Ideas:
 - Split on conflict;
 - Best-first enumeration.



CDA* with Constituent Continuous Relaxation

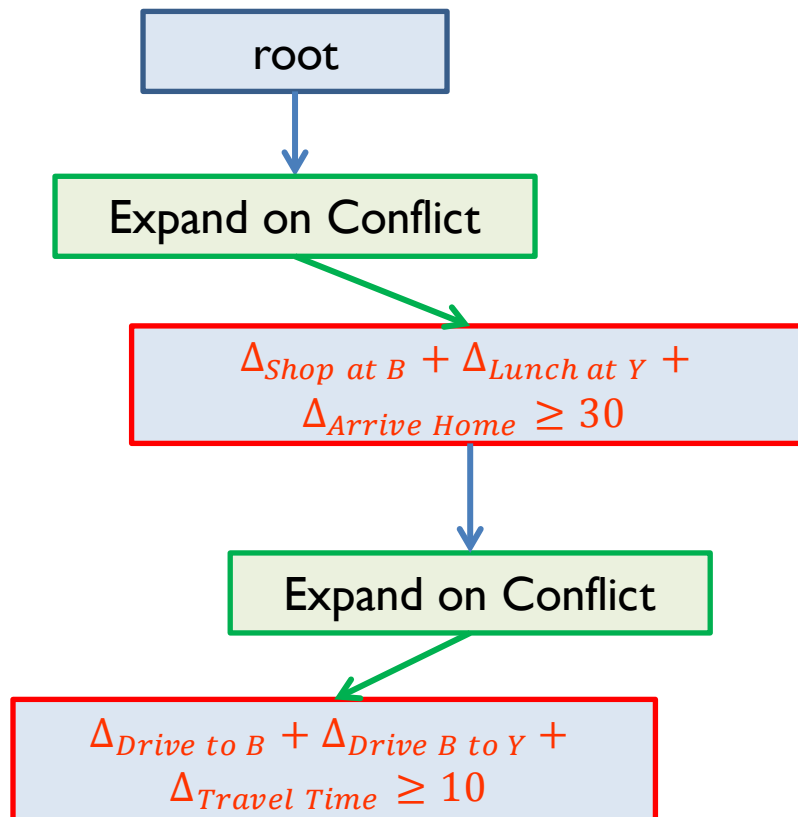
- Split a conflict using its constituent continuous relaxations.



$$\begin{aligned} \min & (f(\Delta_{\text{Shop at B}}) + f(\Delta_{\text{Lunch at Y}}) + f(\Delta_{\text{Arrive Home}})) \\ \text{s.t. } & \Delta_{\text{Shop at B}} + \Delta_{\text{Lunch at Y}} + \Delta_{\text{Arrive Home}} \geq 30 \end{aligned}$$

Continuous Relaxations for Multiple Conflicts

- For two or more continuous relaxations on the same branch, the utility is determined by the grounded solution that respects both inequalities.



$$\min(f(\Delta_{Shop\ at\ B}) + f(\Delta_{Lunch\ at\ Y}) + f(\Delta_{Arrive\ Home}) + f(\Delta_{Drive\ to\ B}) + f(\Delta_{Drive\ B\ to\ Y}) + f(\Delta_{Travel\ Time}))$$

s.t.

$$\Delta_{Shop\ at\ B} + \Delta_{Lunch\ at\ Y} + \Delta_{Arrive\ Home} \geq 30$$

and

$$\Delta_{Drive\ to\ B} + \Delta_{Drive\ B\ to\ Y} + \Delta_{Travel} \geq 10$$

Incorporating User Responses

- BCDR incrementally adapts to new requirements.
- These requirements are recorded as new conflicts.



No, I **do not** want to extend my reservation time.

No, I want to spend **at least 25** minutes on shopping.

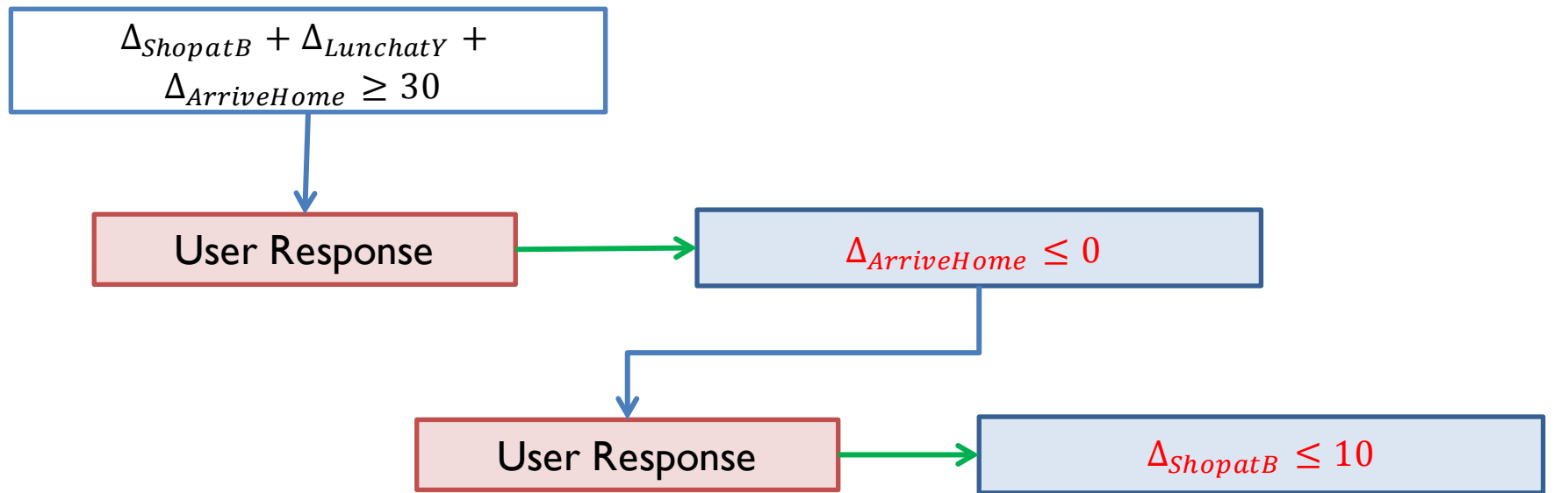
Required Continuous Relaxations

$$\Delta_{Arrive\ Home} \leq 0;$$

$$\Delta_{Shop\ at\ B} \leq 10;$$

New Requirements as Conflicts

- Expand search tree using user response conflicts.

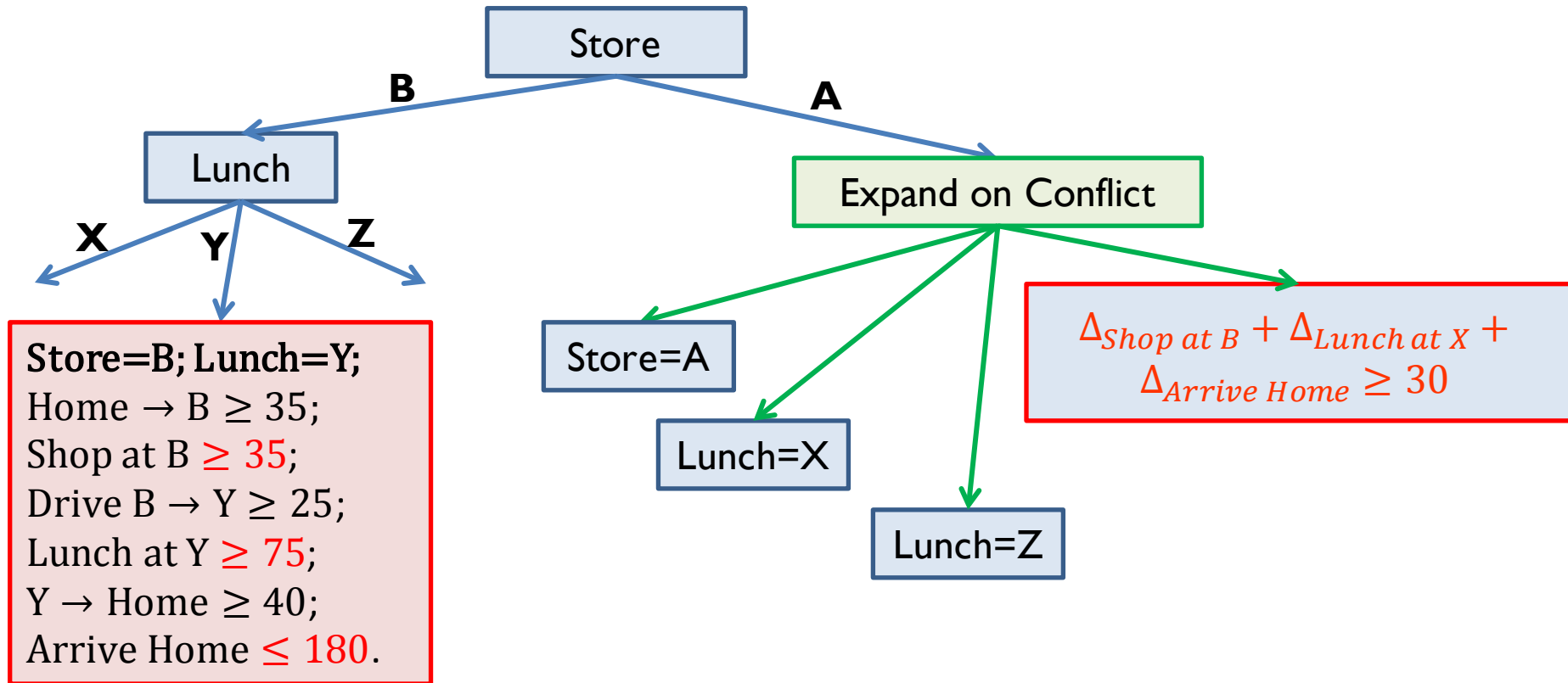


$$\min(f(\Delta_{ShopatB}) + f(\Delta_{LunchatY}) + f(\Delta_{ArriveHome}))$$

$$\begin{aligned} \text{s.t. } & \Delta_{ShopatB} + \Delta_{LunchatY} + \Delta_{ArriveHome} \geq 30; \\ & \Delta_{ArriveHome} \leq 0; \\ & \Delta_{ShopatB} \leq 10. \end{aligned}$$

Split on Conflicts for Conditional Problems

- If a node has an unresolved conflict, we expand it using both constituent **continuous** relaxation and **decisions** that deactivates its constraints.



Contents

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- Continuous Relaxation and Conflict Resolution;
- Restoring Controllability with Uncertainty Durations;
- Best-first Enumeration through Conflict-directed Relaxation;
- Experiments.

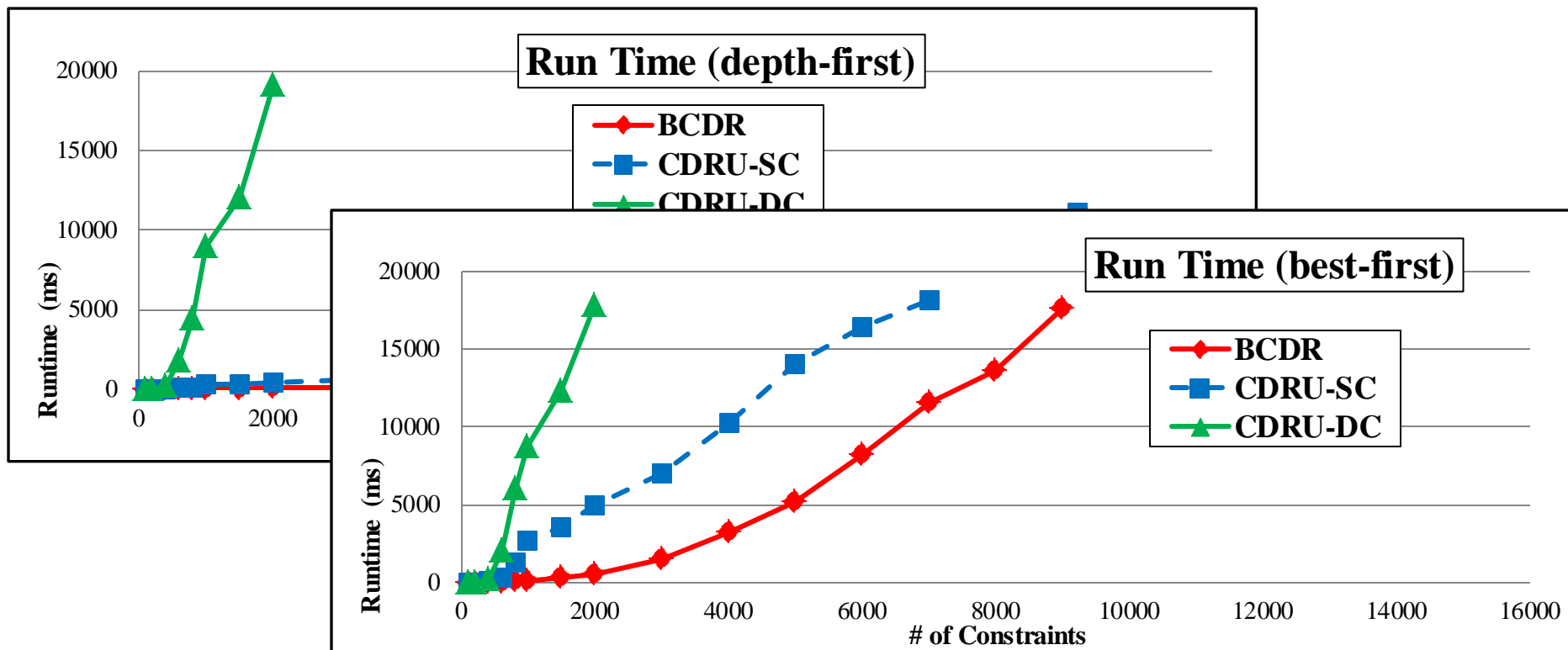
Experiment Setup

- We simulated a car-sharing network in Boston using randomly generated car locations and destinations.
- Test cases are characterized by:
 - Number of reservations per car.
 - Number of cars in the network.
 - Number of activities per reservation.
 - Number of alternative options per activity.
- Time change may affect neighboring reservations.

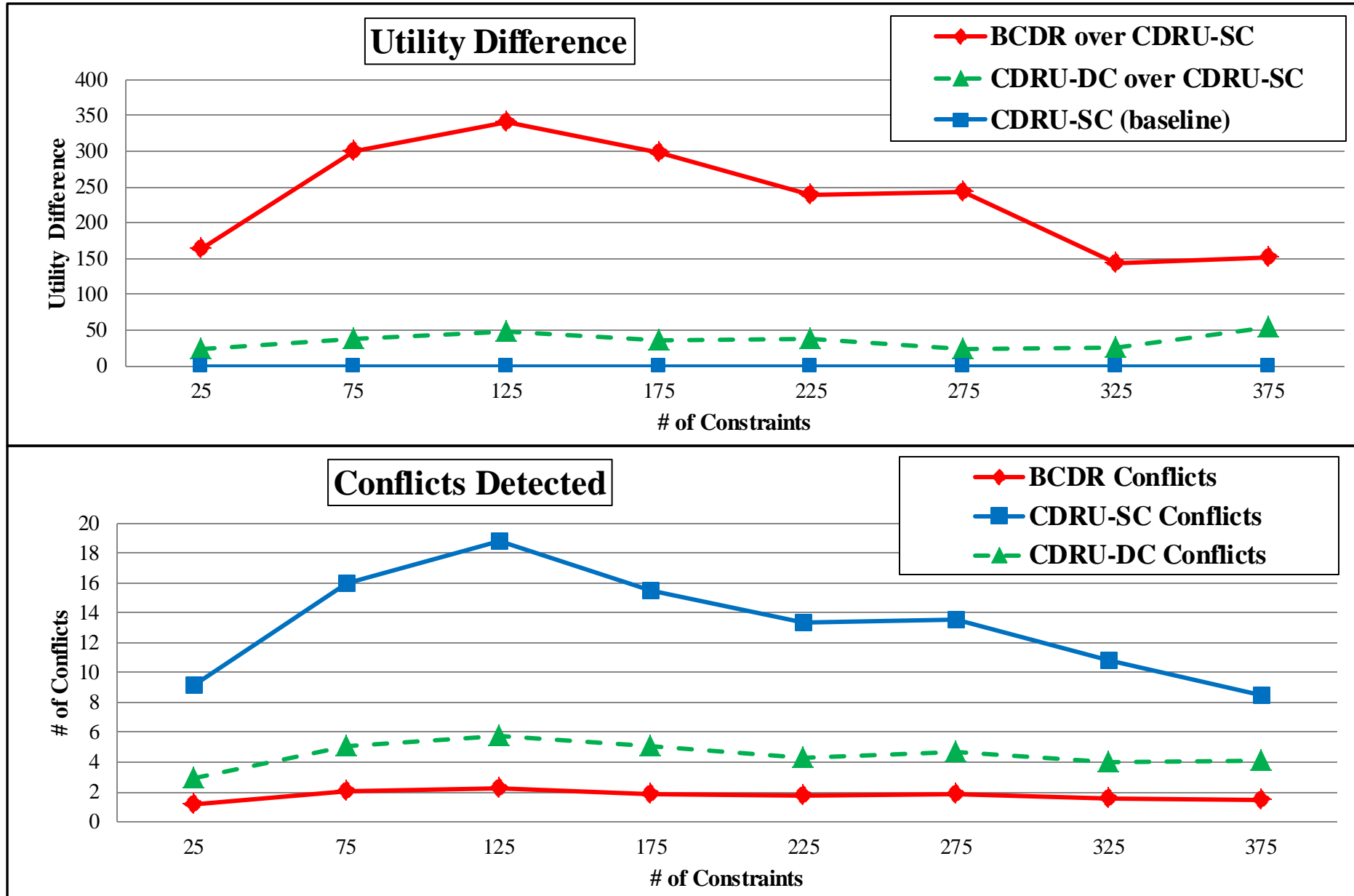


Empirical Results - Runtime

- We compare the performance of three algorithms:
 - BCDR (consistency).
 - CDRU-SC (strong controllability).
 - CDRU-DC (dynamic controllability).



Solution Utility and Conflicts Detected



Contributions

- Over-constrained temporal problems can be resolved by relaxing the temporal constraints **continuously**.
- The fundamental concepts of **conflicts** and **minimal relaxations** naturally generalize to the continuous case.
- The framework naturally extends to resolving uncontrollable problems with **uncertain durations**.
- We can efficiently enumerate **discrete and continuous** relaxations in **best-first order**, by generalizing the Conflict-Directed A* algorithm.

Next Step – Thesis Plan

Temporal Constraint Problems:

- Restore temporal **consistency**.
- Restore temporal **controllability** for uncertain durations.
- Resolve **chance constrained** problems with probabilistic durations.

VRP-TWs:

- Resolve over-constrained VRP-TWs through **temporal** and **resource** relaxations.

Temporal Planning Problems:

- Find **semantically** similar alternatives for goal and domain relaxations.
- Relax **goals** and **domain** specifications for resolving over-constrained planning problems.