

Effective Software Testing with a String-Constraint Solver

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Software Testing Aims To Find Errors Before Users (Or Hackers) Do



Software Testing Aims To Find Errors Before Users (Or Hackers) Do



Goal: help find errors by improving testing tools

Concolic Testing Is An Effective Software Testing Methodology

Implementation-based: exploit knowledge of program code

Dynamic: observe running program using combined <u>conc</u>rete and symb<u>olic</u> execution

Constraint solver systematically enumerate execution paths



Tools: DART, CUTE, CREST, SAGE, EXE, Klee, Apollo, jFuzz

Key idea: improve effectiveness, applicability of concolic testing with a string-constraint solver

Effective Software Testing With A String-Constraint Solver









Results Summary: String-Constraint Solver



✓ Novel solver for string constraints

✓ Supports context-free grammars, regular constraints

✓ Effective in concolic testing, program analysis

✓ Efficient: ~7x faster than a comparable solver

Results Summary: Concolic Security Testing



✓ Novel technique for creating SQL injection and XSS attacks on Web applications

✓ Uses Hampi for grammar constraints to construct attack inputs

✓ First to create damaging secondorder cross-site scripting (XSS) attacks

✓ 60 attacks (23 SQL injection, 37 XSS) on 5 PHP applications, 0 false positives

Results Summary: Grammar-based Concolic Testing



✓ Novel technique for testing programs with structured inputs

✓ Uses Hampi for input-format grammar constraints

✓ Improves coverage by 30–100%

✓ 3 new infinite-loop errors

Effective Software Testing With A String-Constraint Solver











XYZ

```
void main(char[] in){
    int count=0;
    if (in[0] == 'b')
        count++;
    if (in[1] == 'a')
        count++;
    if (in[2] == 'd')
        count++;
    if (count == 3)
        ERROR;
}
```



```
void main(char[] in){
    int count=0;
    if (in[0] == 'b')
    count++;
    if (in[1] == 'a')
        count++;
    if (in[2] == 'd')
        count++;
    if (count == 3)
        ERROR;
}
```

describes inputs that execute same path prefix

Path constraint: (in[0]≠'b')





Path constraint: $(in[0] \neq b') \land (in[1] \neq a')$





Path constraint: $(in[0] \neq b') \land (in[1] \neq a') \land (in[2] \neq d')$



Concolic Testing Combines Dynamic Symbolic Execution, Path Enumeration





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    if (in[2] == 'd')
        count++;
    if (count == 3)
        ERROR;
}
```

Path constraint: (in[0]≠'b')∧(in[1]='a')→xaz



Concolic Testing Combines Dynamic Symbolic Execution, Path Enumeration

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void main(char[] in){
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        count++;
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        ERROR;
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```



```
Path constraint: (in[0]='b')→byz
```



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        ERROR;
}
```











Concolic testing creates inputs for all program paths.

Effective Software Testing With A String-Constraint Solver











Many Program Analyses Reduce To Constraint Generation And Solving



Hampi: constraint solver for a theory of strings



String-Constraint Solver Finds Assignments For String Variables

Finite alphabet Σ (e.g., ASCII characters)



var v

String constraints - language membership:

assert v ∈ L

Context-free, regular, etc.

String operations

concat("foo", v, "bar")











more expressive

🔶 con	text-free	$L_1 \cap \cap L_N$	Undecidable	
regu	ular	$\mathbf{R_1} \cap \cap \mathbf{R_N}$	PSPACE-complete	
bou regi	nded Jlar	$r_1 \cap \cap r_N$	NP-complete	

more tractable









bound(any language) → bounded regular

Key Hampi idea: bound length of strings for high expressiveness, efficiency



"Find a 4-character string v, such that:

- (v) has balanced parentheses, and
- (v) contains substring ()()"



String variable >> var v:4;

cfg E := "()" | E E | "(" E ")";

reg Ebounded := bound(E, 6);

val q := concat("(" , v , ")");

assert q in Ebounded; assert q contains "()()";

"Find a 4-character string v, such that:

- (v) has balanced parentheses, and
- (v) contains substring ()()"



	var v:4;			
Context-free grammar	<pre>cfg E := "()" E E "(" E ")";</pre>			
	<pre>reg Ebounded := bound(E, 6);</pre>			
	val q := concat("(" , v , ")");			
	<pre>assert q in Ebounded; assert q contains "()()";</pre>			
"Find a 1 character string y such that				

- Find a 4-character string v, such that:
 (v) has balanced parentheses, and
- (v) contains substring ()()"



	var v:4;			
Regular lang. declaration	cfg E := "()" E E "(" E ")";			
	<pre>reg Ebounded := bound(E, 6);</pre>			
	<pre>val q := concat("(" , v , ")");</pre>			
	<pre>assert q in Ebounded; assert q contains "()()";</pre>			

"Find a 4-character string v, such that:

- (v) has balanced parentheses, and
- (v) contains substring ()()"



	var v:4;
	cfg E := "()" E E "(" E ")";
	<pre>reg Ebounded := bound(E, 6);</pre>
Declaration of (v)	<pre>val q := concat("(" , v , ")");</pre>
	<pre>assert q in Ebounded; assert q contains "()()";</pre>

"Find a 4-character string v, such that:

- (v) has balanced parentheses, and
- (v) contains substring ()()"



	var v:4;
	cfg E := "()" E E "(" E ")";
	<pre>reg Ebounded := bound(E, 6);</pre>
	<pre>val q := concat("(" , v , ")");</pre>
Constraints 🗪	<pre>assert q in Ebounded; assert q contains "()()";</pre>

"Find a 4-character string v, such that:

- (v) has balanced parentheses, and
- (v) contains substring ()()"

Hampi finds satisfying assignment v =)()(



Hampi Supports Rich String Constraints

 full support partial support 	Hampi	CFGAnalyzer	Wassermann	Bjorner	Hooijmeier	Emmi	MONA	Caballero
context-free grammars			-					
regular expressions		۲	-				•	
string concatenation								
stand-alone tool								
unbounded length								



Hampi Encodes String Constraints In Bit-Vector Logic




Core string constraint have only regular expressions

Expand grammars to regexps

- expand nonterminals
- eliminate inconsistencies
- enumerate choices exhaustively

cfg E := "(" E ")" | E E | "()";







Core string constraint have only regular expressions

Expand grammars to regexps

- expand nonterminals
- eliminate inconsistencies
- enumerate choices exhaustively

cfg *E* := "(" *E* ")" | *E E* | "()";





Core string constraint have only regular expressions

- expand nonterminals
- eliminate inconsistencies
- enumerate choices exhaustively

$$\stackrel{6}{\bullet} \stackrel{6}{(E)} + \stackrel{6}{E} \stackrel{6}{E} + \stackrel{6}{()}$$





Core string constraint have only regular expressions

- expand nonterminals
- eliminate inconsistencies
- enumerate choices exhaustively





Core string constraint have only regular expressions

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- eliminate inconsistencies
- enumerate choices exhaustively

$$\stackrel{4}{\blacktriangleright} (\stackrel{6}{E}) + \stackrel{6}{E}$$













Core string constraint have only regular expressions

Expand grammars to regexps

- expand nonterminals
- eliminate inconsistencies
- enumerate choices exhaustively

cfg E := "(" E ")" | E E | "()";

$$(E) + EE + EE$$





Core string constraint have only regular expressions

- expand nonterminals
- eliminate inconsistencies
- enumerate choices exhaustively

cfg
$$E := "(" E ")" | E E | "()";$$

 $([()() + (())]) +$
bound(E , 6) \rightarrow () $[()() + (())] +$
 $[()() + (())]()$





Hampi Normalizer Uses Compact Representations Of Expressions

$$E_{2} \qquad E_{4}$$
() [()() + (())] + [()() + (())] () + [()() + (())] () + E_{6}
([()() + (())])

shared graph nodes for common subexpressions





Bit Vectors Are Ordered, Fixed-Size, Sets Of Bits

Bit vector B (length 6 bits)





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Bit vector B (length 6 bits)



Bit-vector solver finds the solution B = 010101



Hampi Encodes Core Constraints As Bit-Vector Constraints





Hampi Encodes Regular Expressions Recursively



- union + → disjunction ∨
- concatenation \rightarrow conjunction \wedge
- Kleene star $* \rightarrow$ conjunction \wedge
- constant
- → bit-vector constant







Hampi Encoder Exploits Shift-Symmetry In Constraints

Shift-symmetric constraints = identical modulo offset in bit vector

Hampi reuses encoding templates for symmetric constraints







Hampi Encoder Exploits Shift-Symmetry In Constraints

Shift-symmetric constraints = identical modulo offset in bit vector

Hampi reuses encoding templates for symmetric constraints





Shift-symmetric constraints



Hampi Uses Bit-Vector Solver And Decodes Solution





Result 1: Hampi Is Effective In Static SQL Injection Analysis

1367 string constraints from [Wassermann PLDI'07]



Hampi scales to large grammars

Hampi solved 99.7% of constraints in < 1 sec per constraint All solvable constraints had short solutions N \leq 4



Result 2: Hampi Is Faster Than The CFGAnalyzer Solver

CFGAnalyzer encodes bounded grammar problems in SAT [Axelsson et al ICALP'08]



For size 50, Hampi is 6.8x faster on average (up to 3000x faster)

Effective Software Testing With A String-Constraint Solver











Ardilla Mutates Generated Inputs To Construct Attacks





SQL Injection Attacks Modify Structure Of Database Queries

Innocuous input: $v \rightarrow 1$

SELECT msg FROM messages WHERE topicid='1'



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Symbolic expression for SQL query

user input

concat(SELECT msg FROM messages WHERE topicid=' v ')



SQL Injection Attacks Modify Structure Of Database Queries

Innocuous input: $v \rightarrow 1$

SELECT msg FROM messages WHERE topicid='1'

Symbolic expression for SQL query

user input

concat(SELECT msg FROM messages WHERE topicid=' v ')



Attacker gets access to all messages



Example: Hampi Constraints That Create SQL Injection Attacks





Example: Hampi Constraints That Create SQL Injection Attacks



Hampi finds an attack input: $v \rightarrow 1' \text{ OR } 0'=0'$



Result: Ardilla Finds New Attacks

4 cases of data corruption

19 cases of information leak

60 attacks on 5 PHP applications

- 23 SQL injection
- 29 XSS first order
 - 8 XSS second order

0 false positives

216 Hampi constraints solved

- 46% of constraints in < 1 second per constraint
- 100% of constraints in < 10 seconds per constraint

Effective Software Testing With A String-Constraint Solver











Randomly mutates bytes seed inputs

Random Fuzz Testing

50 well-formed seed inputs

Concolic Testing 50 well-formed seed inputs

Program under test: JavaScript interpreter






























Most Generated Inputs Get Rejected Quickly



Key idea: generate only valid inputs



Input-Format Grammar Guides Creation Of Effective Inputs





Input-Format Grammar Guides Creation Of Effective Inputs





String-Constraint Solver Helps Create Valid Inputs

```
Seed input (for JavaScript interpreter):
  function f() { var v = 3; }
```

Constraints on tokens (created during execution)

```
token_{\theta} = function

token_{1} = id

token_{2} = (

token_{3} = )

token_{4} = \{

token_{5} = var

...
```



String-Constraint Solver Helps Create Valid Inputs

```
Seed input (for JavaScript interpreter):
function f(){ var v = 3; }
Constraints on tokens
(created during execution)
token<sub>0</sub> = function
token<sub>1</sub> = id
token<sub>2</sub> = (
token<sub>3</sub> = )
token<sub>4</sub> = {
Normal solver → nonparsable input
```



String-Constraint Solver Helps Create Valid Inputs

```
Seed input (for JavaScript interpreter):
   function f() { var v = 3; }
```

Constraints on tokens (created during execution)



Normal solver → nonparsable input
function f(){ try v = 3; }





String-Constraint Solver Helps Avoid Dead-End Inputs

```
Seed input (for JavaScript interpreter):
function f(){ var v = 3; }
Constraints on tokens
(created during execution)
token₀ = function
token₁ = id
token₂ = (
token₃ = )
token₄ ≠ {
Normal solver → nonparsable input
```

function f() var var v = 3; }



String-Constraint Solver Helps Avoid Dead-End Inputs

```
Seed input (for JavaScript interpreter):
  function f() \{ var v = 3; \}
Constraints on tokens
(created during execution)
  token_{\Theta} = function
  token_1 = id
  token_2 = (
  token_3 = )
  token₄ ≠ {
                     Normal solver \rightarrow nonparsable input
                       function f() var var v = 3; }
```

Hampi solver \rightarrow no input tested, search tree pruned



Results: Grammar-Based Concolic Testing Improves Deep Reachability



Up to 20x deep reachability improvement: more generated inputs reach beyond the parser



Results: Grammar-Based Concolic Testing Improves Coverage



Up to 2x coverage improvement





Summary: Effective Software Testing With A String-Constraint Solver

Hampi String-Constraint Solver

- expressive: supports context-free grammars
- efficient: solver real-world constraint quickly

Concolic Security Testing

• creates attacks on Web applications by input generation and mutation with Hampi string-constraint solver

Grammar-Based Concolic Testing

 effectively tests programs with structured inputs by using Hampi string-constraint solver and input grammars





