

GEOMETRIC PROBABILITY

CROSSROADS ACADEMY
AMC-8 PREPARATION

- I) In rectangle ABCD, $AB=1$ and $BC=2$. Point X is selected at random within the rectangle. What is the probability that the area of triangle ABX is more than twice the area of triangle BCX?
- II) Concentric circles have radii of 3, 4, 5, and 6 cm. What is the probability that a random point selected with the large circle is in only the largest circle or inside the 4cm circle but outside the 3cm circle?
- III) A point is randomly selected inside the right triangle ABC. The point X lies on the hypotenuse AC with $AX=3$ and $CX=2$. What is the probability that a random point selected inside the triangle lies in BCX?
- IV) The square ABCD has side length 3. If a point X is selected at random what is the probability that the quadrilateral ABXD has an area greater than 4 square units?
- V) One side of a triangle is 5cm long. Two (not necessarily integer) numbers are randomly selected between 0 and 10. What is the probability that the two numbers can be the lengths of the other two sides of the triangle?

- a) Point X is randomly selected within square $ABCD$. What is the probability that angle AXB is acute?
- b) Three circles of integral diameter are arranged so that each is entirely within the next larger circle. The probability that a random point selected inside the largest circle lands within the middle circle but not the smallest circle is exactly $1/2$. What is the smallest possible area of the middle circle?
- c) Two distinct pairs of vertices are randomly selected on a cube and each pair is connected by a line segment. What is the probability that the two line segments intersect?
- d) A stick is broken at random into three pieces. What is the probability that the pieces can form a triangle?