

lightweight formalism

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crisis of dependability

We have become dangerously dependent on large software systems whose behavior is not well understood

-- *PITAC report, February 1999*

software is

- **unreliable**

fails in unpredictable ways

- **inflexible**

changes make it worse

- **expensive**

not much reuse of designs or code

traditional approaches

testing

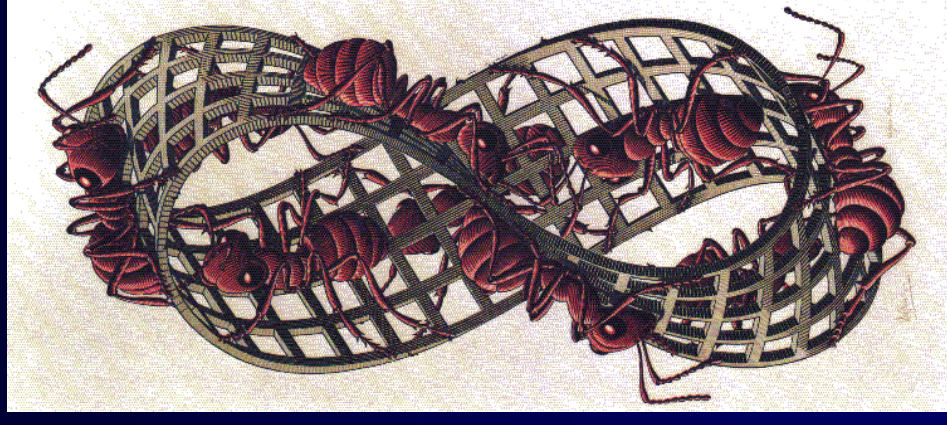
- can't replicate real world
- tiny proportion of cases covered
- no help with incompleteness of spec

prototyping

- too costly for all but GUI
- temptation to build on prototype
- no guarantees for final product

process

- focus on human resources alone
- insensitive to nature of software
- can be major burden (hence XP, etc)



a new approach

models

- capture essence of spec & design
- much smaller than standard docs

patterns

- recognize recurring themes
- codify and reuse them

escaping from code

- not nimble enough for exploration
- poor communication medium
- our basic asset, but a huge liability



why formalism?

English + pictures

- ambiguous & imprecise
- not analyzable

formal notations

- based on mathematics
- offer simulation, calculation, analysis
like conventional engineering

Praxis's CDIS system for UK air-traffic

- offered warranty to client
- formal specification: 8% of total cost
- low defect rate, overall cost saving

the alloy approach

automation

- simulation & checking of models
- tradeoff for full analyzability
- exploit Moore's law

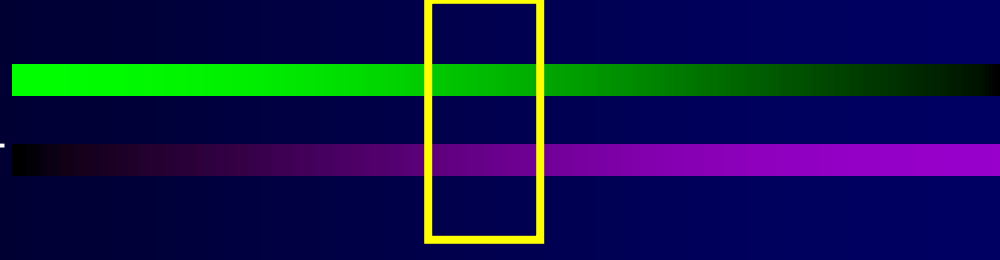
process

- incremental and risk-driven
- apply in all phases of development
- at all levels from models to bytecode

origins

- Z formalism (Oxford)
- SAT solving technology (Bell Labs et al)
- semantic data models

tractable
inexpressive



expressive
intractable

applications of alloy

case studies

- Intentional Naming System
- Chord peer-to-peer nameservice
- rule-based access control
- COM interface rules

ongoing work

- models of conflict probe
- network topology protocols
- secure VPN
- object interaction in Java

what I'll show you

a typical problem

- from a text-processing program
- express essence in Alloy
- apply automatic analysis

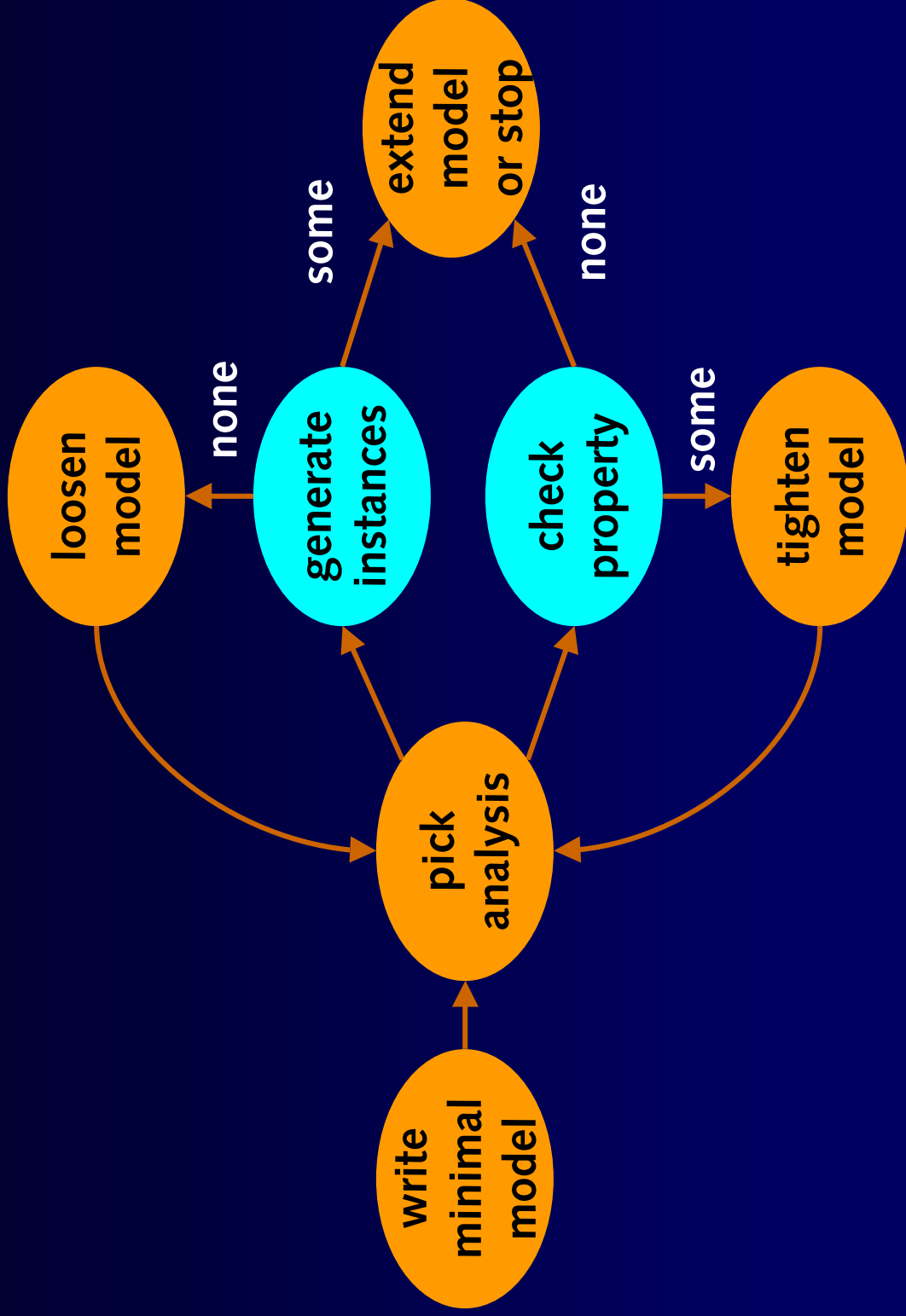
widely applicable

- based on common patterns (Command, Observer)
- same as our 1998 design of CTAS CM
- avoid failure with generic discipline

two levels: abstract design & code

- same notation, same analysis

how to use Alloy



the key to Alloy

partiality

- if my system has property P, will property Q follow?
- is environmental assumption A enough?

Alloy is a constraint language (ie, a logic)

- the less you say, the more can happen
- can express property
without mechanism to achieve it

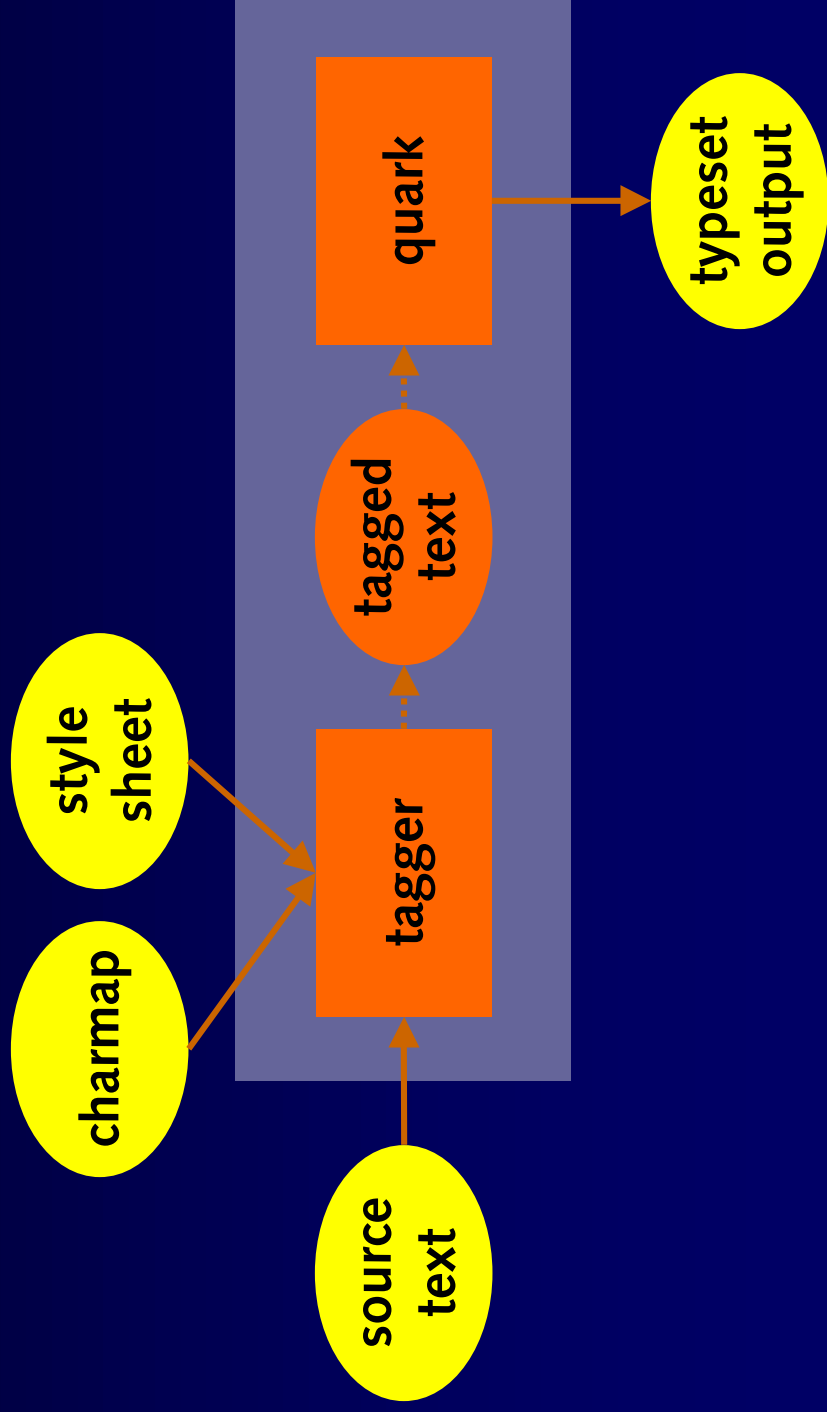
programming languages

- the less you say, the less can happen
- every property has to be achieved

example: tagger program

combine

- typographic quality & flexibility of Quark Xpress
- with convenience of textual input of TeX



sample translation

source

```
\point _A constraint solving technique_. We use a technology developed  
previously [\cite{alloy-algorithm}] to analyze the skeleton
```

style sheet

```
<style:point><next:noindent><leader:\periodcentered>
```

charmap

```
<char:periodcentered><index:183>
```

tagged

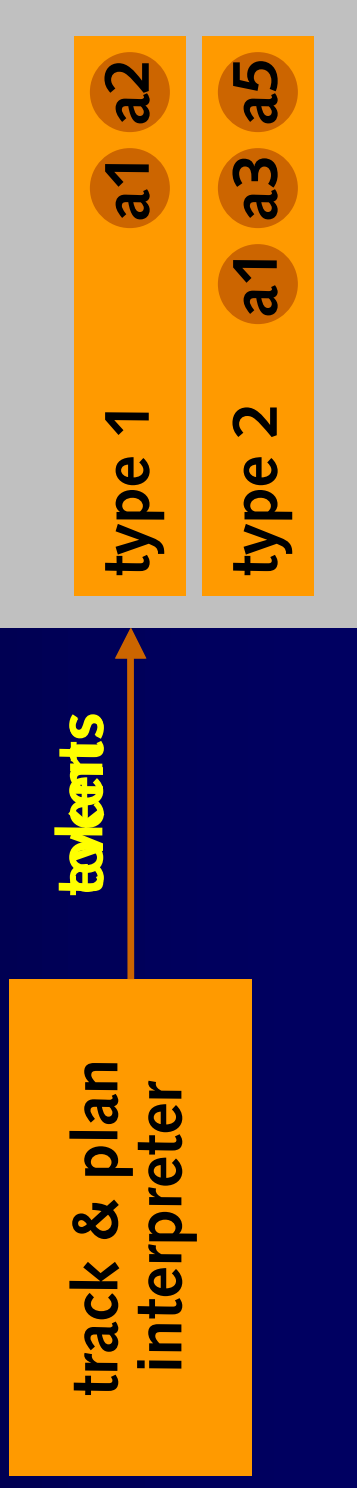
```
@point:<\#183><I>A constraint solving technique<I>. We use a technology  
developed previously [6] to analyze the skeleton
```

output

· *A constraint solving technique*. We use a technology developed previously
[6] to analyze the skeleton

abstract design

- source converted to stream of tokens
- each token consumed by engine
- engine executes all actions registered for token type
- actions may read & write files, register/deregister actions



why are actions nice?

- flexible, context-sensitive behaviour
- without one huge, monolithic piece of code
- easy to turn behaviours on & off
- can have subengines: eg, for numbering strings

example: math mode

- $$ starts and ends ‘math mode’: puts all letters in italics
- implemented as 2 actions
 - for $$ token: `dollar_action`
 - for alphabetic string token: `italicize_action`
- `dollar_action`
 - encapsulates mode
 - registers/deregisters `italicize_action`

alloy basic concepts (ABC)

atom

- an indivisible, uninterpreted entity
a token, a token type, a person, a string, an aircraft

set

- an unordered collection of atoms
Token, Type, Person, String, Aircraft

relation

- a set of tuples of atoms
type: Token -> Type
myPhoneBk: Name -> Num
phoneBk: Name -> Num

alloy operators

set operators

$s + t$ union

$s \& t$ intersection

$s - t$ difference

relation operators

$s . r$ image

$p + q$ union, etc

myPhoneBk: Name -> Num

myFriends: set Name

myFriends.myPhoneBk

phoneBk: Name -> Name -> Num

me: Name

me.phoneBk

myFriends.phoneBk

mother: Name -> Name

me.mother.phoneBk

(me + me.mother).phoneBk

me.phoneBk - me.mother.phoneBk

a design model of an action machine

```
sig Token {type: Type}
sig Type {}
sig Action {regs, deregs: Type -> Action}
sig Engine {table: Type -> Action}

fun execute (e, e': Engine, t: Token) {
  doActions (e, e', t.type.(e.table))
}

fun doActions (e, e': Engine, actions: set Action) {
  e'.table = e.table - actions.deregs + actions.regs
}
```

simulation

Token = to1, to2
Type = ty1, ty2
Action = a1, a2
Engine = e1, e2

type = to1 -> ty1, to2 -> ty2
regs = a1 -> ty1 -> a2, a2 -> ty2 -> a1
deregs = a1 -> ty1 -> a1, a1 -> ty2 -> a1
table = e1 -> ty1 -> a1, e2 -> ty1 -> a2

e = e1

e' = e2

t = to1

a design question

can implementation do actions in any order?

```
assert {  
  all e, ei, e', e'' : Engine, t: Type,  
  ax, ay: set t.(e.table) |  
    doActions (e, ei, ax) && doActions (ei, e', ay)  
    && doActions (e, e'', ax+ay)  
  ==> e'.table = e''.table  
}
```

counterexample

the scenario

- first **doAction** registers an action
- second **doAction** deregisters it
- but aggregate **doAction** collects deregisters upfront

design challenge

what strategy for order independence?

- must be simple and static

here's one strategy

- group actions that reg/dereg each other
- say that ≤ 1 action of a group may register for type t
- rule out arbitrary initialization of engine

to check it

- write definition of grouping
- write registration and initialization rules
- recheck assertion

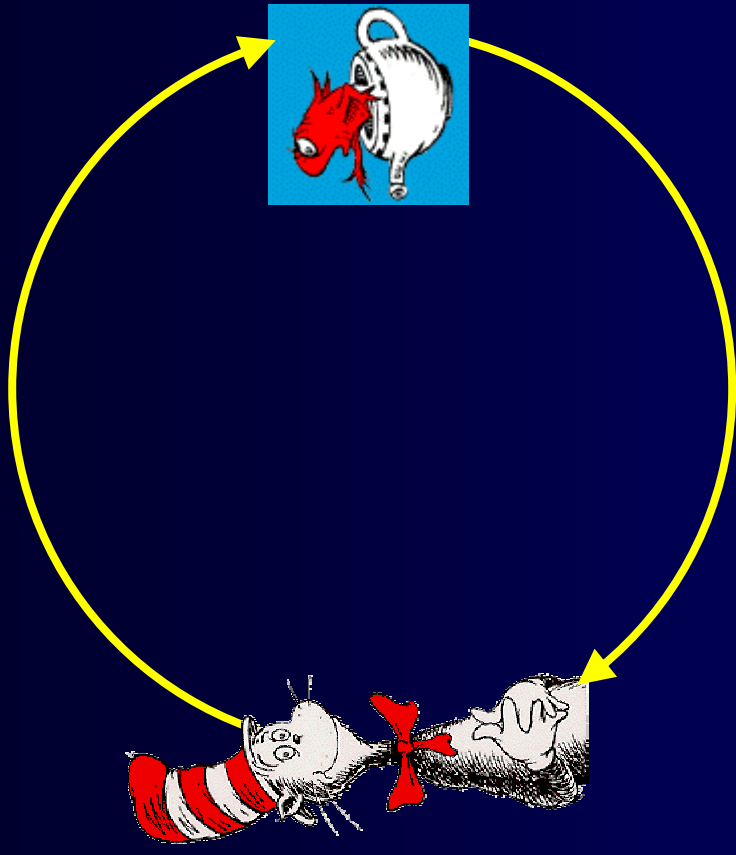
what the rest looked like ...

```
sig GroupedAction extends Action {group: set Action}
fact {
  let depends = Action$regs + Action$deregs |
    Action$group = *(depends + ~depends)
}
fact {Action = GroupedAction}

fact NoClashes () {
  all t: Type | no a: Action, a': a.group - a |
    a + a' in t.Action::regs
}

fact NoArbitraryInits () {all e: Engine | e.table in Action.regs}
```

experience



- took me 2 hours to develop this strategy
- lots of false attempts on the way
 - rapidly exposed by tool
- about 100 lines of Alloy written
 - for 3 actions, 10^{54} cases
 - counterexample < 1 second
 - exhausting space < 1 minute

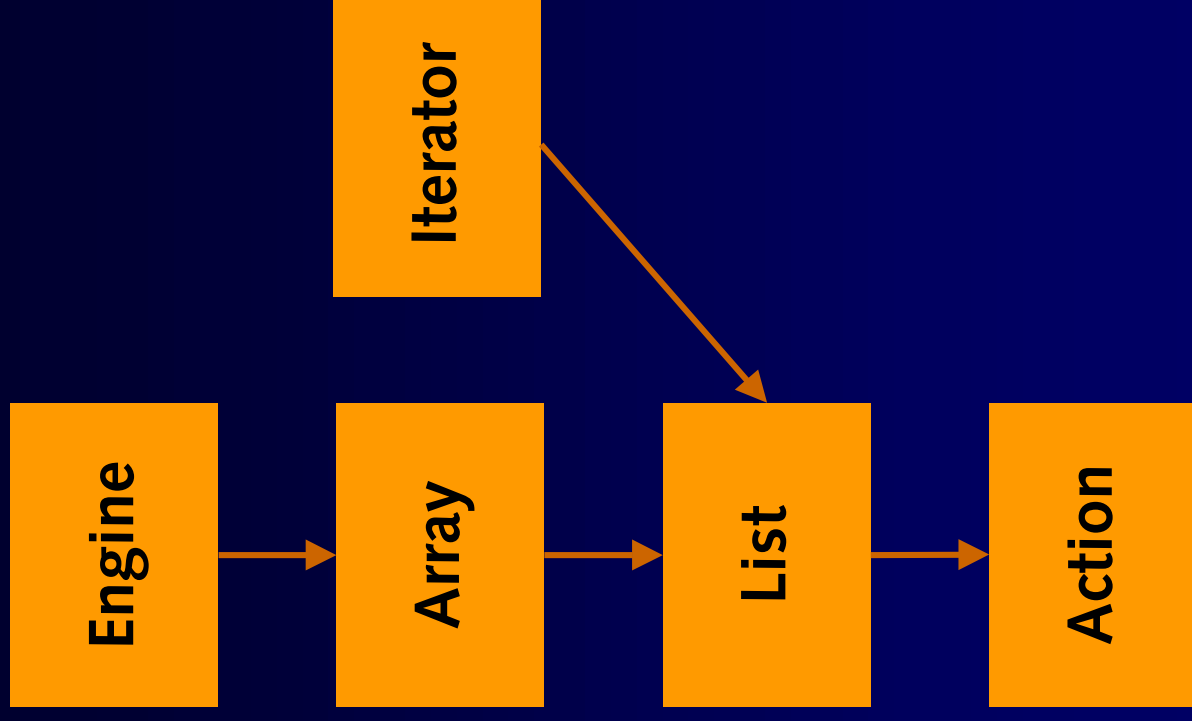
moving to code

Engine class

- holds action lists
- in array indexed on token type

consuming token

- creates iterator object
- yields each action in turn
and performs it

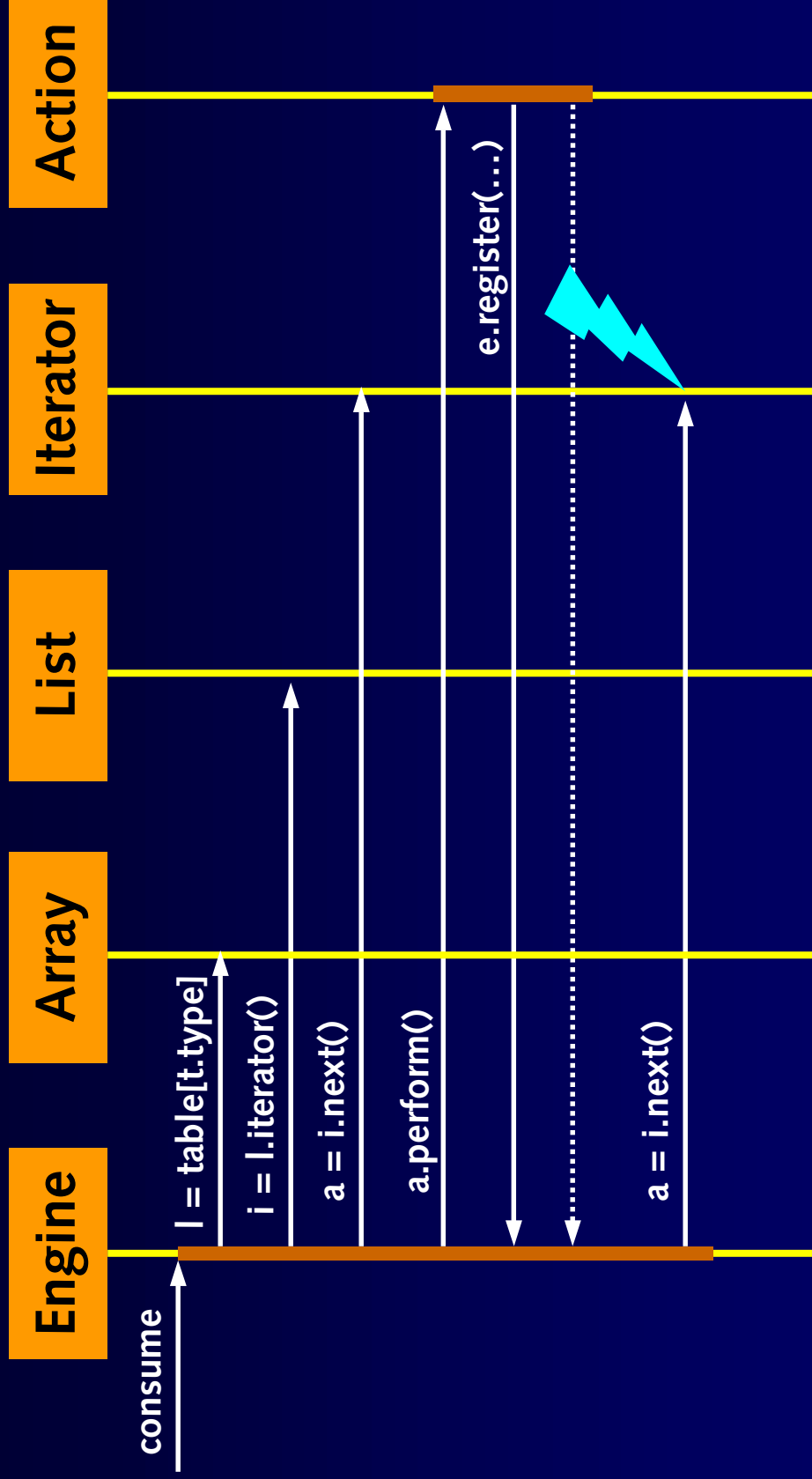


code of engine

```
private LinkedList [] table;
...
public void register (Action action, int type) {
    actions[type].add (action);
}

public void consume_token (Token token) {
    Iterator i = table[token.type].iterator ();
    while (i.hasNext ()) {
        Action a = (Action) i.next ();
        a.perform (token, i);
    }
}
```

failure!



comodification

problem

- iterator shares state with list
- holds cursor into representation
- call to list's **add** may invalidate cursor

Java's solution

- iterator and list have **version** numbers
- list's **iterator** creates iterator with same version
- list's **add/remove** increments list version
- at start of iterator's **next**
 - check versions match
 - if not, throw exception

approach

build minimal Alloy models

- of list and iterator
- of engine structure

translate engine method

- into Alloy assertion
- and analyze it

to fix problem

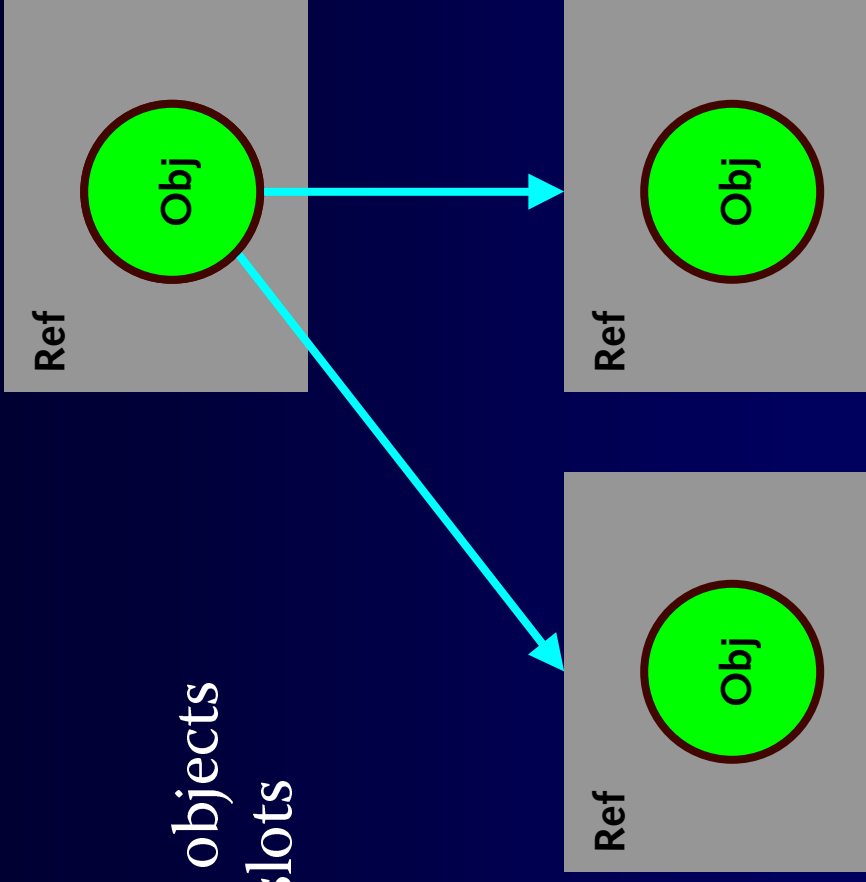
- develop general discipline
- add to model and reanalyze
- (check code against discipline)

modelling the heap

two kinds of Alloy atoms

- **references:** slots that hold objects
- **objects:** values that go in slots

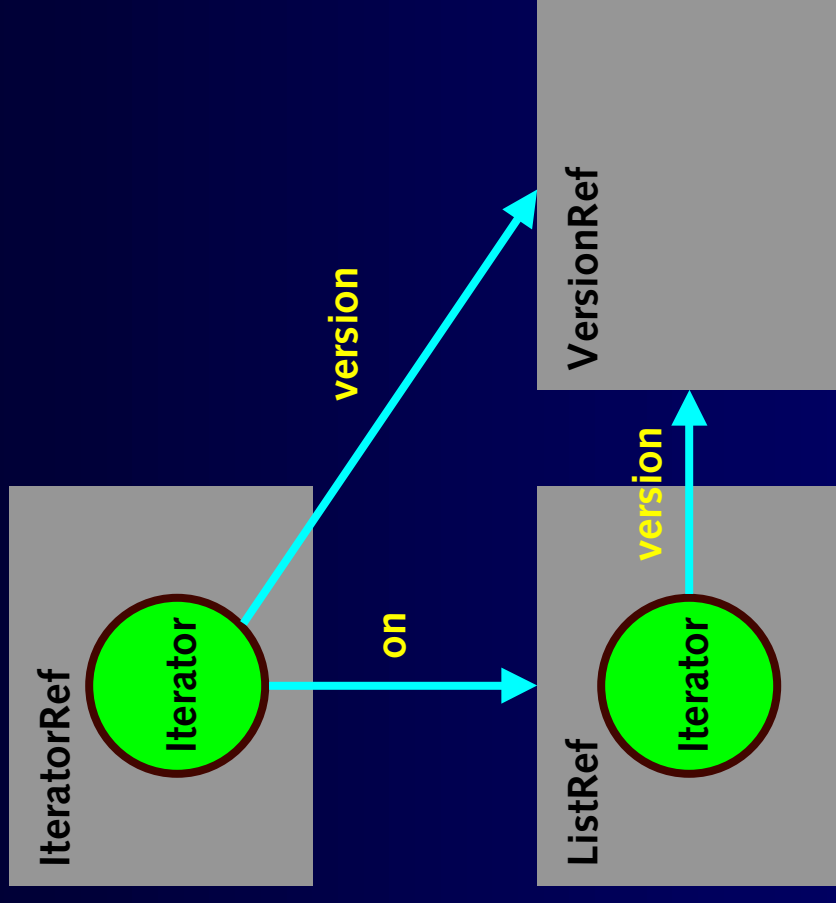
```
sig Ref {}  
sig Obj {}  
sig State {  
  refs: set Ref,  
  obj: Ref ->? Obj  
}
```



modelling iterators & lists

```
sig IteratorRef extends Ref{}  
sig Iterator extends Obj {  
  on: ListRef,  
  left: set Ref  
  version: VersionRef  
}
```

```
sig ListRef extends Ref{}  
sig List extends Obj {  
  elts: set Ref  
  version: VersionRef  
}
```



modelling iterator methods

```
fun next (s, s': State, this: IteratorRef, x: Ref) {  
  x in this.(s.obj).left  
  this.(s'.obj).left = this.(s.obj).left - x  
  this.(s'.obj).version = this.(s.obj).version  
  modifies (s, s', this)  
}  
  
fun next-pre (s, s': State, this: IteratorRef) {  
  this.(s.obj).version = this.(s.obj).on.(s.obj).version  
}  
  
fun modifies (s, s': State, rs: set Ref) {  
  all x: s.refs - rs | x.(s'.obj) = x.(s.obj)  
}
```

modelling list methods

```
fun iterator (s, s': State, this: ListRef, result: IteratorRef) {  
  result.(s'.obj).on = this  
  result.(s'.obj).version = this.(s.obj).version  
  result.(s'.obj).left = this.(s.obj).elts  
  modifies (s, s', {})  
}  
  
fun add (s, s': State, this: ListRef, x: Ref) {  
  this.(s'.obj).elts = this.(s.obj).elts + x  
  modifies (s, s', this)  
}
```


modelling the engine

```
sig Engine extends Obj {  
  table: TypeRef ->! ListRef  
}
```

```
fun register (s,s': State, this: EngineRef, a: ActionRef, t: TypeRef){  
  let l = t.(this.s'.obj).table) {  
    add (s, s', l, a)  
    modifies (s, s', l)  
  }  
}
```

translating engine_consume

```
assert {
  all s0, s1, s2, s3: State,
  e, e': EngineRef, l: ListRef, i: IteratorRef,
  t: TokenRef, a: ActionRef, a': a.group l
  {
    l = t.(s0.obj).type.(e.(s0.obj).table)
    iterator (s0, s1, l, i)
    next (s1, s2, i, a)
    register (s2, s3, e', a')
  }
  ==> next-pre (s3, i)
}
```

Array

Engine

consume

l = table[t.type]

i = l.iterator()

a = i.next()

a.perform()

a = i.next()

bug!

tool finds a counterexample

- what if one list for two types?
- fix multiplicity of table
- (and check code)

```
sig Engine extends Obj {  
  table: TypeRef ? -> ! ListRef  
}
```

so what?

nimble modelling

- models are tiny
- analysis is fast
- feedback is motivating

levels & phases

- abstract & code design
- early and late

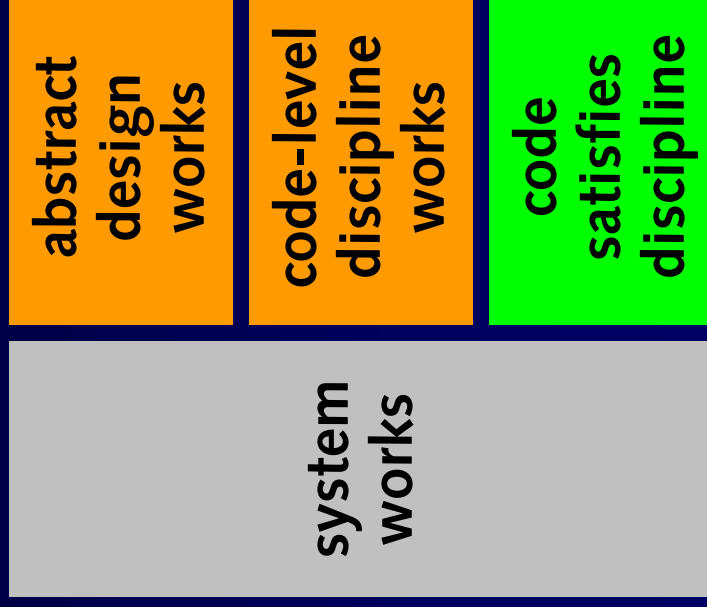
systematic

- developed general rules
- discipline for future changes

context

design conformance

- NSF/IITR grant with Martin Rinard
- combines Alloy with Rinard's shape analysis



related research

verifying state machines

- Pathfinder: applies Spin to Java (Ames)
- Bandera: translates Java to finite state model (Kansas)
- SLAM: translates code to 'boolean programs' (Microsoft)
for events not heap structure

lightweight code analysis

- LCLint (Maryland), PreFIX (Msft), ESC (Compaq)
for simpler properties, eg null derefs
uniform across code

acknowledgments

Alloy language and tool

- Ilya Shlyakhter
- Manu Sridharan
- Brian Lin

Alloy case studies

- Sarfraz Khrushid
- Mandana Vaziri
- Gregory Dennis
- Michal Mirvis
- Hoeteck Wee

Tagger example

- Alan Fekete

links

<http://sdg.lcs.mit.edu/~dnj/publications>

research papers

alloy language

alloy analysis technology

object model extraction

object models

lecture notes

software design with object models

<http://sdg.lcs.mit.edu/alloy>

alloy analyzer

new tool released mid-september