DICCIVC

6898: Advanced Topics in Software Design MIT Lab for Computer Science March 18, 2002 Daniel Jackson

topics for today

familiar notions (from Scheme)

> let bindings, functions, closures, lists

new notions (from ML)

- inferred types and parametric polymorphism
- > side-effects and the unit type
- > datatypes (variants)

functions

applying an anonymous function
(fun x -> 2 * x) 3;;
- : int = 6

declaring a function and applying it
let dbl = fun x -> 2 * x;;
val dbl : int -> int = <fun>
dbl 3;;
- : int = 6

functionals, or higher-order functions
let twice = fun f -> (fun x -> (f (f x)));
val twice : ('a -> 'a) -> 'a -> 'a = <fun>
(twice dbl) 3;;
- : int = 12

let bindings

let x = 3 and y = 4 in x + y;; -: int = 7a let expression binds a variable to a value

X;; val x : int = 5# let x = 5;;read-eval-print-loop uses let instead of define -: int = 5

fact 4;; val fact : int -> int = <fun> # let rec fact i = if i = 0 then 1 else i * fact (i - 1);; recursive let -: int = 24

let vs. define

let k = 5;; val k : int = 5 # let f = fun x -> x + k;; val f : int -> int = <fun> # f 3;; -: int = 8 # let k = 6;; val k : int = 6 # f 3;; -: int = 8 let is lexical

> no side-effecting top-level define built-in

tuples

fst x;; - : int = 1 # snd x;; -: int = 2# let x = 1, 2;; val x : int * int = 1, 2 tuple constructor

empty tuple, used instead of 'void' # ();;

- : unit = ()
print_string;;

- : string -> unit = <fun>

function arguments

```
# (diff 3 4);;
                                                                                                                                                                                    # diff (3, 4);;
                                                                                                                                                                                                                     val diff : int * int -> int = <fun>
                                                                                                                                                                                                                                                                                                   tupled form: like in an imperative language
curried form: stages the computation
                                                                     This function is applied to too many arguments
                                                                                                                                                                                                                                                             # let diff (i,j) = if i < j then j-i else i-j;;</pre>
                                                                                                                                                    -: int = 1
```

```
curried form: stages the computation
# let diff i j = if i < j then j-i else i-j;;
val diff : int -> int -> int = <fun>
# (diff 3) 4;;
-: int = 1
# (diff 3 4);;
-: int = 1
```

[1;[2]];; # [[1]];; - : int list list = [[1]] lists are homogeneous This expression has type 'a list but is here used with type int

empty list is polymorphic # [];; - : 'a list = []

polymorphic functions

fun x -> x;; the simplest polymorphic function -: 'a -> 'a = <fun>

cons 1 [];; a polymorphic function over lists # cons 1 2;; val cons : 'a -> 'a list -> 'a list = <fun> # let cons e l = e :: 1;;

This expression has type int but is here used with type 'a list

- : int list = [1]

datatypes

```
a simple datatype
# type color = Red | Green | Blue;;
type color = Red | Green | Blue
# Red;;
-: color = Red
# [Red ; Green];;
-: color list = [Red; Green]
```

Tree (Empty, 3, Empty);; # Empty;; - : numtree = Tree (Empty, 3, Empty) type numtree = Empty | Tree of numtree * int * numtree # type numtree = Empty | Tree of numtree * int * numtree;; constructors can take arguments : numtree = Empty

patterns

let tt = Tree (Tree (Empty, 1, Empty), 3, Tree (Empty, 2, Empty));; # type numtree = Empty | Tree of numtree * int * numtree;; # let rec treesum t =a function on number trees val treesum : numtree -> int = <fun> -: int = 6...# treesum tt;; match t with Empty -> 0 | Tree (t1, i, t2) \rightarrow i + treesum t1 + treesum t2;;

sum [1;2;3;4];; val sum : int list -> int = <fun> # let rec sum l = match l with $[] \rightarrow 0 l e :: rest \rightarrow e + sum rest;;$ a function on lists -: int = 10

puzzle: poly functional over lists

write the function map val map : ('a -> 'b) -> 'a list -> 'b list

```
match l with [] -> [] | x :: xs -> (f x) :: (map f xs);;
val map : ('a -> 'b) -> 'a list -> 'b list = <fun>
                            # map dbl [1;2];;
                                                                                                                # let rec map f1 =
                                                                                                                                                    solution
-: int list = [2; 4]
```

puzzle: user-defined poly datatypes

type 'a tree = Empty | Tree of 'a tree * 'a * 'a tree # type 'a tree = Empty | Tree of ('a tree) * 'a * ('a tree);; a polymorphic tree

let rec treefold f b t = what is the type of treefold? Tree (left, v, right) -> f (treefold f b left, v, treefold f b right);; match t with Empty -> b

val treefold : ('a * 'b * 'a -> 'a) -> 'a -> 'b tree -> 'a = <fun>

side-effects

mutable cells
let seed = ref 0;;
val seed : int ref = {contents=0}

dereference
!seed;;
- : int = 0

assignment
seed := 1;;
- : unit = ()
!seed;;
- : int = 1

puzzle

- write a function *next*which produces 0, 1, 2, etc
- takes no arguments

closures and cells

```
# next ();;
- : int = 2
                                        # next ();;
- : int = 1
                                                                                                   # (next);;
                                                                                   - : unit -> int = <fun>
                                                                                                                            val next : unit -> int = <fun>
                                                                                                                                                                                           \# let next =
                                                                                                                                                                     (let seed = ref 0 in
                                                                                                                                                function () -> seed := !seed+1; !seed);;
```

lazy lists or 'streams'

type 'a stream = Nil | Cons of 'a * (unit -> 'a stream) # type 'a stream = Nil | Cons of 'a * (unit \rightarrow 'a stream);; define a datatype for streams

let hd s = match s with Cons $(x,f) \rightarrow x;;$ Here is an example of a value that is not matched: Nil val cons : 'a -> 'a stream -> 'a stream = <fun> # let cons x s = Cons (x, fun () -> s);; Warning: this pattern-matching is not exhaustive val hd : 'a stream \rightarrow 'a = <fun>

Here is an example of a value that is not matched: Nil # let tl s = match s with Cons (x, f) -> f ();; val tl : 'a stream \rightarrow 'a stream = <fun> Warning: this pattern-matching is not exhaustive

using streams

hd (tl (from 3));; # (from 3);; - : int stream = Cons (3, <fun>) # let rec from $k = Cons (k, fun () \rightarrow from (k+1));;$ -: int = 4val from : int -> int stream = <fun>

puzzle

given type 'a tree = Empty | Tree of 'a * 'a tree list # type 'a tree = Empty | Tree of 'a * 'a tree list;;

write a function that

- performs a depth-first traversal of a tree
- > gives result as a stream

you can assume an infix function @

> for appending streams