

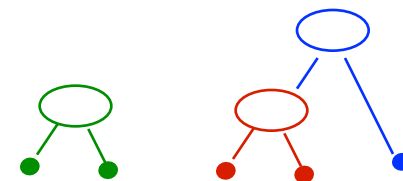
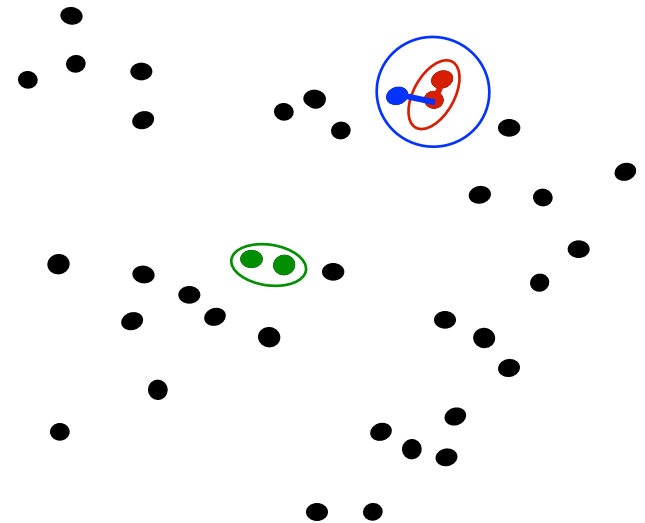
# **Hierarchical Clustering**

## **Lecture 15**

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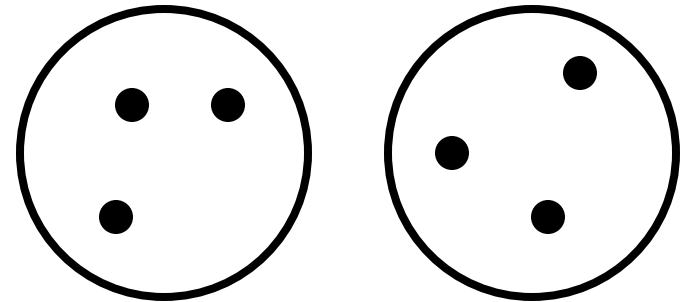
# Agglomerative Clustering

- Agglomerative clustering:
  - First merge very similar instances
  - Incrementally build larger clusters out of smaller clusters
- Algorithm:
  - Maintain a set of clusters
  - Initially, each instance in its own cluster
  - Repeat:
    - Pick the two **closest** clusters
    - Merge them into a new cluster
    - Stop when there's only one cluster left
- Produces not one clustering, but a family of clusterings represented by a **dendrogram**



# Agglomerative Clustering

- How should we define “closest” for clusters with multiple elements?



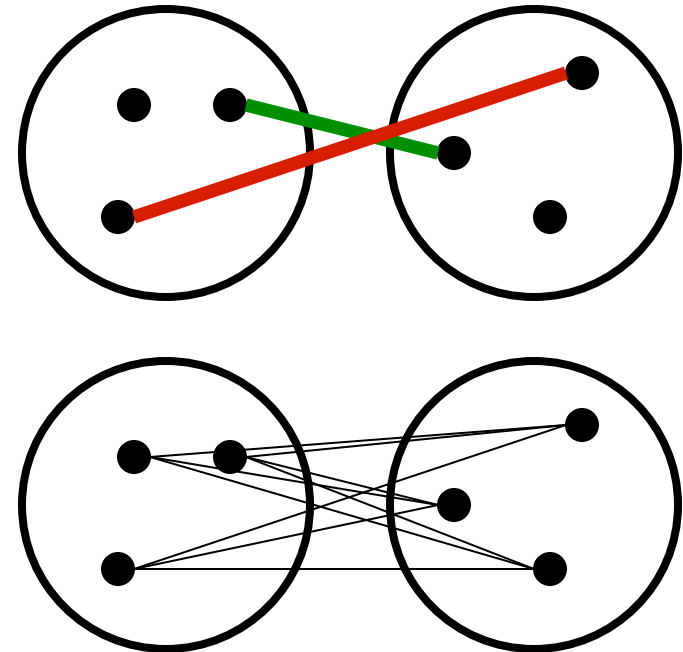
# Agglomerative Clustering

- How should we define “closest” for clusters with multiple elements?

- Many options:

- Closest pair  
(single-link clustering)
- Farthest pair  
(complete-link clustering)
- Average of all pairs

- Different choices create different clustering behaviors

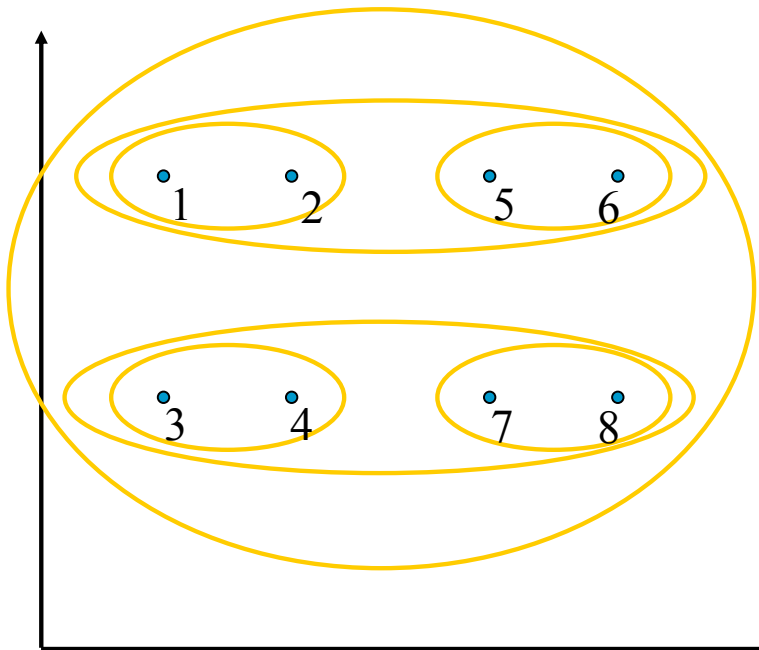


# Agglomerative Clustering

- How should we define “closest” for clusters with multiple elements?

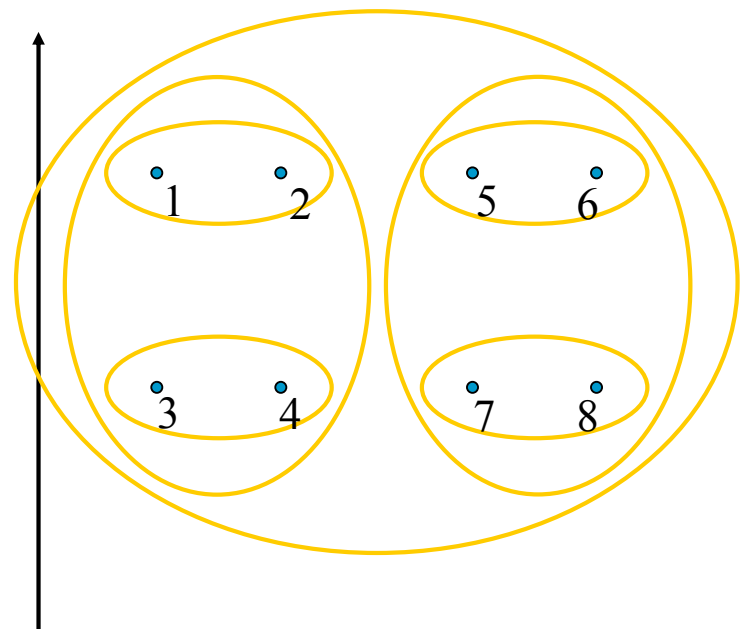
Closest pair

(single-link clustering)



Farthest pair

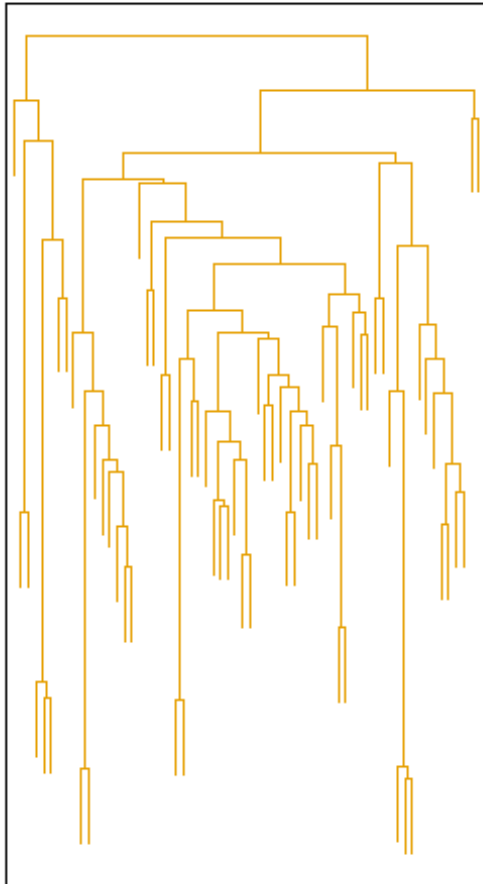
(complete-link clustering)



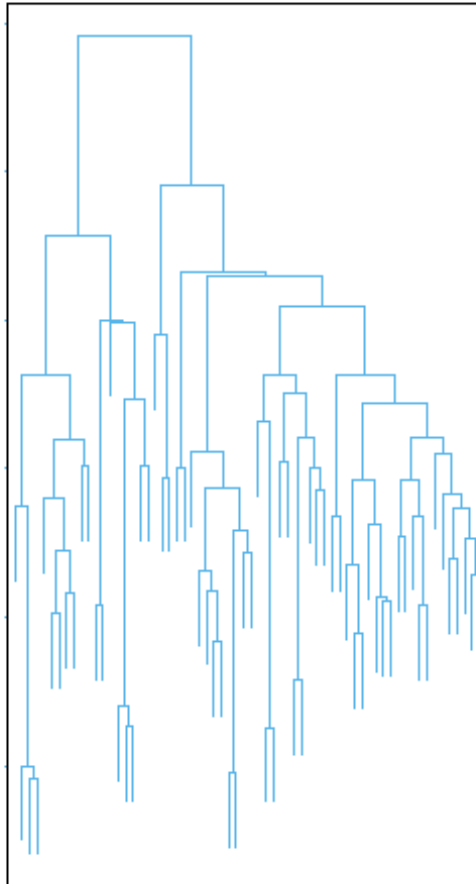
[Pictures from Thorsten Joachims]

# Clustering Behavior

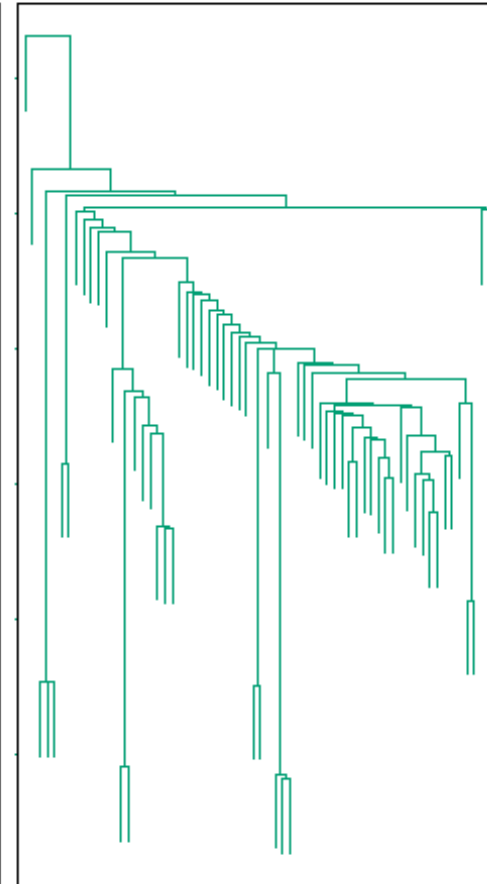
Average



Farthest



Nearest

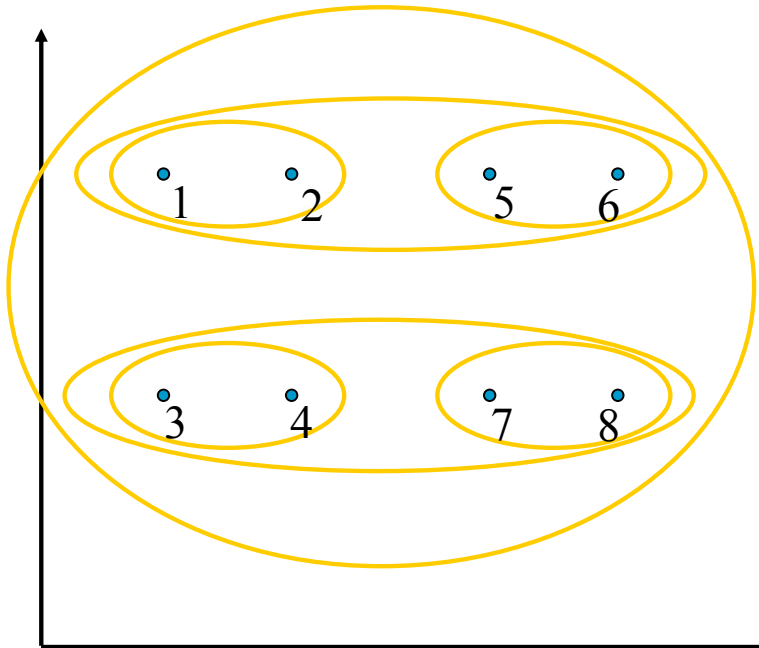


Mouse tumor data from [Hastie *et al.*]

# Agglomerative Clustering

When can this be expected to work?

**Closest pair**  
(single-link clustering)



**Strong separation** property:

*All points are more similar to points in their own cluster than to any points in any other cluster*

Then, the true clustering corresponds to some **pruning** of the tree obtained by single-link clustering!

Slightly weaker (stability) conditions are solved by average-link clustering

(Balcan et al., 2008)