FreeSnell Thin-Film Optical Simulator Version 1c4

Aubrey Jaffer

This file documents FreeSnell 1c4 (released January 2024), a simulator for thin-film optics. Copyright © 2003, 2004, 2007, 2009, 2010 Aubrey Jaffer

Permission is granted to make and distribute verbatim copies of this manual provided the copyright notice and this permission notice are preserved on all copies.

Permission is granted to copy and distribute modified versions of this manual under the conditions for verbatim copying, provided that the entire resulting derived work is distributed under the terms of a permission notice identical to this one.

Permission is granted to copy and distribute translations of this manual into another language, under the above conditions for modified versions, except that this permission notice may be stated in a translation approved by the author.

Table of Contents

1	O	verview
	1.1	Background
	1.2	Theory of Operation
	1.3	Wrinkles
	1.4	Bibliography
2	O	ptical Properties of Materials 3
	2.1	nk Data Formats
3	\mathbf{N}	Iaterial Databases 6
	3.1	The nk script
	3.2	Wedged Databases7
	3.3	Creating Databases
	3.4	Listing the Database
	3.5	Querying the Database
4	\mathbf{S}_{1}^{2}	pecifying Designs 11
	4.1	Specifying Materials
	4.2	Optical Stack
	4.3	Plot-response
		.3.1 Ranges and Units
		.3.2 Traces
	4	.3.3 Other Outputs
5	P	rogram Interface19
6	A	bout FreeSnell
	6.1	Installation
	6	.1.1 i386 MS-Windows
	_	1.1.2 x86_64 GNU/Linux with RPM
		1.1.3 Unix (including GNU/Linux)
	6.2	Using FreeSnell
T.	do	ຸກ

1 Overview

Some wondrous optical technology can result from depositing coatings less than a few micrometers thick on glass, plastic, and other surfaces. These coatings are used to enhance the reflectivity of astronomical mirrors or diminish the reflections from visual displays and lenses; they can improve the efficiency of window glass and solar cells.

FreeSnell computes these effects for parallel layers of dielectric and conductive materials.

1.1 Background

I couldn't find a free implementation of thin-film optical calculations I needed for a project. So I rolled my own.

The first versions were based on webpages [NCSU] and [Nave], but differences in signs and conventions of the complex index of refraction caused havoc with metallic layers. [Sernelius] has a comprehensive treatment with signs consistent from start to finish. The current version is based on that.

The properties of granular films are taken from [Heavens] discussion of Maxwell Garnett theory. [Granfilm] computes properties of granular films with great sophistication, but appears to require a PhD in physics in order to use it.

Optics is wavelength based; so this package is also. These routines work out the complex voltages in the forward and reverse directions to find the transmitted and reflected amplitudes. This works only for intensities where the layers act linearly (superposition).

Each layer 0:n has an index of refraction and height. Because the P and S polarizations are independent, they are calculated separately. The square of the absolute value of computed field values expressing power ratios are the returned quantities.

1.2 Theory of Operation

The effects of coatings on light are determined by Snell's law and Fresnel's equations, which model the light's electric and magnetic fields.

Taking the Laplace-transform of the differential equations relating the fields at the surface of each parallel layer of materials yields algebraic equations relating the indexes-of-refraction and the (complex) attenuation and phase as functions of wavelength.

These algebraic equations can be organized into products of 2x2 matrices and 2-vectors. The 2-vectors represent the Laplace transforms of the forward and reverse radiation. Each interface between adjacent materials corresponds to a 2x2 matrix.

The product of the chain of 2x2 matrices produces a single 2x2 matrix expressing the transmittance and reflectance of the layered stack as a whole, solving the system of equations.

This method is not unique to thin-film optics; it is essentially the same as the 2-port method for analysis of linear electrical circuits.

1.3 Wrinkles

Because these optical systems are passive and linear, the attenuation of radiation passing through in one direction must be the same as the attenuation of radiation passing through in the opposite direction.

Radiation that is not transmitted through the stack must be either absorbed or reflected. The absorption at the top is not necessarily the same as the absorption at the bottom.

Rays impinging on the stack with non-normal incidence will leave the stack with non-normal incidence; the angles being identical if the indexes of refraction of the top and bottom materials are identical.

Rays impinging on the stack with non-normal incidence have different attenuation and reflectance depending on the polarization of the impinging radiation. FreeSnell computes outcomes for both polarizations; and can report these separately or averaged.

1.4 Bibliography

- [Heavens] Heavens, O. S., "Optical Properties of Thin Solid Films", ISBN: 0486669246, Dover Pubns, Dec 1991
- [Sernelius] Bo E. Sernelius, "Electrodynamics", Dept. of Physics and Measurement Technology, Linköping University

 http://www.ifm.liu.se/~boser/elma/, especially

 "REFLECTION FROM A METALLIC SURFACE"

 http://www.ifm.liu.se/~boser/elma/Lect13.pdf
- [CRC] Lide, D.R., Dr. Editor, "CRC Handbook of Chemistry and Physics (3rd Electronic Edition)", CRC Press, 2000
- [NCSU] "Fresnel's equations" from the chemistry department of North Carolina State University.

 http://web.archive.org/web/20041029131241/http://chsfpc5.chem.
 ncsu.edu/CH795Z/lecture/lecture8/fresnel/fresnel.html
- [Nave] "Fresnel's Equations: Reflection and Transmission" by Carl R. Nave, Department of Physics and Astronomy, Georgia State University.

 http://hyperphysics.phy-astr.gsu.edu/hbase/phyopt/freseq.html
- [Garnett] J. C. Maxwell Garnett, "Colours in Metal Glasses and in Metallic Films", Phil. Trans. Roy. Soc. London 203A, 385 (1904). http://rsta.royalsocietypublishing.org/content/203/359-371/385
- [Granfilm] R. Lazzari and I. Simonsen, "Granfilm: a software for calculating thin-layer dielectric properties and fresnel coefficients", Thin Solid Films, 419:124, 2002. http://www.insp.jussieu.fr/axe2/0xydes/GranFilm/GranularFilm.html
- [Bartl] Bartl J, Baranek M (2004), "Emissivity of aluminium and its importance for radiometric measurement", Measurement of Physical Quantities 43:31–36. http://www.measurement.sk/2004/S3/Bartl.pdf
- [Modest] Michael F Modest, "Radiative heat transfer", second edition, Academic Press 2003

2 Optical Properties of Materials

The salient optical properties of a material are specified by its *complex index of refraction*; which differs from the common index of refraction, n, by incorporating the extinction-coefficient, k/n. There are several conventions for the complex index of refraction. The one employed here follows [Sernelius]: $(n + k^*i)$.

Dielectric materials typically have k equal to zero and n which varies little with the wavelength of light being analyzed. They are often computed using a single n value.

Metallic or conductive materials have non-zero k and n which can vary wildly with the wavelength of light being analyzed. These values can be determined through a process called *ellipsometry*.

The Sopra company manufactures spectroscopic ellipsometers. A bundle of spectra for 278 materials available from

http://www.sopra-sa.com/more/database.asp (Nov 28, 2000) is included in the FreeSnell distribution database.

The Software Spectra company also distributes the Sopra data, although rewritten into their proprietary format. But their zip file

```
http://www.sspectra.com/files/misc/win/SOPRA.EXE (Macintosh http://www.sspectra.com/files/misc/mac/Sopra.sea.hqx) contains README.TXT identifying the Sopra files.
```

Included with FreeSnell are the following metal spectra from the CRC Handbook of Chemistry and Physics:

```
ag.nk: eV
                        k
                                 R(th=0); Silver
                n
al.nk: eV
                        k
                                 R(th=0); Aluminium
                n
au.nk: eV
                        k
                                 R(th=0); Gold, electropolished, Au (110)
                n
cr.nk: eV
                n
                        k
                                 R(th=0); Chromium
cu.nk: eV
                        k
                                 R(th=0); Copper
                n
fe.nk: eV
                        k
                                 R(th=0); Iron
                n
ge.nk: eV
                        k
                                 R(th=0); Germanium, single crystal
                n
li.nk: eV
                        k
                                 R(th=0); Lithium
                n
                                 R(th=0); Nickel
ni.nk: eV
                n
                        k
ta.nk: eV
                                 R(th=0); Tantalum
                        k
                n
ti.nk: eV
                                 R(th=0); Titanium (Polycrystalline)
                        k
                n
v.nk: eV
                                 R(th=0); Vanadium
                        k
                n
                                 R(th=0); Tungsten
w.nk: eV
                        k
                n
zn.nk: eV
                        k
                                 R(th=0); Zinc, E_{-} to c<sup>28</sup>
                n
zn-e.nk: eV
                        k
                                 R(th=0); Zinc, E || to c^28
                n
                                 R(th=0); Zirconium (Polycrystalline)
zr.nk: eV
                        k
                n
```

Many of these materials are included in the Sopra bundle; but the CRC data covers a wider wavelength span than the Sopra spectra. Combining the CRC and Sopra files produces wide bandwidth spectra with finer resolution in the visible and near-infrared bands.

2.1 nk Data Formats

FreeSnell supports SOPRA textual formats with their evenly spaced wavelengths or energies, as well as textual formats where the wavelength or energy of each nk pair is individually specified.

If the first non-whitespace character in the file is a digit, then the file is interpreted as a SOPRA format file. The first number indicates the spectral unit (1 = eV, 2 = um, 3 = 1/cm, 4 = nm). The second and the third numbers indicate the spectral range and the fourth one the number of intervals. The n and k values are then stored in the order N,K,N,K...; each value may be followed by a semicolon, whitespace, or both.

For example, the SOPRA file al2o3.nk has 27 values for wavelengths from 0.25.um to 0.9.um:

```
2,.25,.9,26
1.7331,0
1.7163,0
1.7042,0
1.6951,0
1.6881,0
1.6825,0
1.678,0
1.6743,0
1.6713,0
1.6687,0
1.6665,0
1.6646,0
1.6629,0
1.6614,0
1.6601,0
1.659,0
1.6579,0
1.657,0
1.6561,0
1.6553,0
1.6546,0
1.6539,0
1.6532,0
1.6526,0
1.652,0
1.6515,0
1.6509,0
```

The other formats ignore the first line if it begins with a semicolon. The first non-ignored word read indicates the spectral unit, either eV, /cm, um, or nm; the rest of that line is discarded. Each line which follows is a triple of the spectral index, the n value, and the k value, separated by whitespace. Extra data on the line (the normal reflectance in some files) is ignored.

This example (blackbody.nk) specifies constant n and k values over all wavelengths:

25.0 1.0 0.038

3 Material Databases

The FreeSnell package includes a SCM script (program) named nk to create, manage, and query a refractive-index spectra database.

Recent versions of the FreeSnell distribution include the relational database (nk.rwb) containing the refractive-index spectra. So use of the 'nk' script is optional.

3.1 The nk script

The nk.scm file in the distribution functions as a shell script named 'nk' on Unix systems; under MS-Windows, the nk icon invokes nk.scm as an interactive command-line shell with the prompt 'nk'.

Use the nk program to create, manage, and query a refractive-index spectra database.

The nk program can read Sopra format files. These files have a ".nk" suffix. A bundle of spectra for over 275 materials is available from: http://www.sopra-sa.com/index2.php?goto=dl&rub=4 (2010-06-14). Some metal spectra included with FreeSnell also have a ".nk" suffix, but with a different format.

The zip file http://www.sspectra.com/files/misc/win/SOPRA.EXE contains "README.TXT" identifying the Sopra files.

http://luxpop.com/RefractiveIndexList.html has 274 refractive-index files, mostly X-ray spectra.

The optional argument [-F path] sets the path to the database file to be accessed or created. If it is not given, then the environment variable "NK_DATABASE_PATH" names the database file if defined, defaulting to "nk.rwb" in the current directory. The name for each spectrum in the database is taken from its filename sans the ".nk" or "ir.nk" suffix.

Usage: nk [-F path]

Starts the nk shell. Type nk commands without the nk; ^Z to exit.

Usage: nk [-F path] --add FILEGLOB.nk ...

Add spectra matching FILEGLOB to database. Wildcards must be in the leaf directory only.

Usage: nk [-F path] --new FILEGLOB.nk ...

Add new or replace spectra matching FILEGLOB to database. Wildcards must be in the leaf directory only.

Usage: nk [-F path] --del 'GLOB' ...

Delete spectra of names matching GLOB from database.

Usage: nk [-F path] --plot 'GLOB' ...

```
Usage: nk [-F path] --lin-lin 'GLOB' ...
Usage: nk [-F path] --log-log 'GLOB' ...
Usage: nk [-F path] --log-lin 'GLOB' ...
Usage: nk [-F path] --lin-log 'GLOB' ...
Usage: nk [-F path] --lin-eV 'GLOB' ...
Usage: nk [-F path] --log-eV 'GLOB' ...
Usage: nk [-F path] --lin-/cm 'GLOB' ...
Usage: nk [-F path] --log-/cm 'GLOB' ...
 Create encapsulated-PostScript (and view with Ghostview) spectra plots
 from database of names matching GLOB. The first symbol controls the
 y-axis.
Usage: nk [-F path] --list 'GLOB' ...
 List names of spectra matching GLOB in database.
Usage: nk [-F path] --range 'GLOB' ...
 List names and data ranges of spectra matching GLOB in database.
Usage: nk [-F path] --desc 'GLOB' ...
 List names and descriptions of spectra matching GLOB in database.
Usage: nk [-F path] --annotate sopra.txt
 Add chemical-symbol and description annotations to database.
Usage: nk [-F path] NAME NUMBER.UNIT ...
 Prints NAME's n+k*i values at each NUMBER.UNIT from database.
 NUMBER can be fixed or floating point; the UNIT either "eV"
  (electron-volt) or "m" (meter) with an optional metric prefix or
  "cm^-1" (wave-number).
Usage: nk --help
 Prints this help and exits.
```

3.2 Wedged Databases

Although it tries to be careful, if the 'nk' script encounters an unexpected condition while the database file (default 'nk.rwb') has a table open for writing, then the database file can become unusable from both the 'nk' script and design files. This damage will only result from the 'nk' script; all simulations should be read-only from database files.

To start afresh, delete these files (with all occurrences of 'nk.rwb' replaced by your database name):

- '~\$nk.rwb'
- '#nk.rwb' (isn't created on MS-Windows)
- 'nk.rwb'

If the wedged database was 'nk.rwb' from the distribution, then retrieve 'nk.rwb' from the distribution. Otherwise rebuild your database (using 'nk --add' commands).

3.3 Creating Databases

FreeSnell comes with a database of refractive-index spectra for several hundred materials. If you want to add spectra of your own, it is probably better to create a separate database for them using the '-F' option to the 'nk' script.

```
nk -F mynk.rwb --add *.nk
"sicrir" ==> "sicr"
"sio2ir" ==> "sio2"
                                R(th=0); Silver
ag.nk: ev
                        k
                                R(th=0); Aluminium
al.nk: ev
                        k
                n
                                R(th=0); Gold, electropolished, Au (110)
au.nk: ev
                        k
                n
cr.nk: ev
                        k
                                R(th=0); Chromium
                n
                        k
                                R(th=0); Copper
cu.nk: ev
                n
                        k
                                R(th=0); Iron
fe.nk: ev
                n
                        k
                                R(th=0); Germanium, single crystal
ge.nk: ev
                n
li.nk: ev
                        k
                                R(th=0); Lithium
                n
ni.nk: ev
                n
                        k
                                R(th=0); Nickel
ta.nk: ev
                        k
                                R(th=0); Tantalum
                n
                                R(th=0); Titanium (Polycrystalline)
ti.nk: ev
                        k
                n
                                R(th=0); Vanadium
v.nk: ev
                        k
                n
                                R(th=0); Tungsten
w.nk: ev
                        k
                n
zn-e.nk: ev
                n
                        k
                                R(th=0); Zinc, E \mid \mid to c^28
                                 R(th=0); Zinc, E_{-}|_{-} to c^28
zn.nk: ev
                        k
                n
                                R(th=0) ; Zirconium (Polycrystalline)
zr.nk: ev
                        k
```

Your new databse can be accessed from design files thus:

```
(define mynk (open-database "mynk.rwb" 'rwb-isam))
(define Ag (interpolate-from-table (open-table mynk 'Ag) 2))
```

3.4 Listing the Database

nklist					
7059	a-al2o3	a-c	a-sih	ag	againp0
againp1	againp10	againp3	againp6	againp7	al
al2o3	a12o3-e	alas	alas028t	alas052t	alas072t
alas098t	alas125t	alas152t	alas178t	alas204t	alas228t
alas305t	alas331t	alas361t	alas390t	alas421t	alas445t
alas469t	alas499t	alas527t	alas552t	alas578t	alas602t
alas626t	alcu	algaas0	algaas1	algaas10	algaas2
algaas3	algaas4	algaas5	algaas6	algaas7	algaas8
algaas9	alon	alsb	alsi	alsiti	arachi
asi	au	baf2	be	beo	bk7
bk7_abs	caf2	carbam	ccl4	cdse	cdte
СО	co_2	cor7059	cosi2-4	cr	cr3si
cr5si3	crsi2el2	csi	cu	cu2o	cuo
d-c	fe	fesi2el1	fesi2el2	fesi2epi	gaas
gaas031t	gaas041t	gaas060t	gaas081t	gaas100	gaas103t
gaas111	gaas126t	gaas150t	gaas175t	gaas199t	gaas224t

gaas249t gaas391t gaas546t gan-tit gap ge100 hg inasox ingasb5	gaas273t gaas415t gaas579t gan01 gap100 h2o hgcdte0 ingaas ingasb7	gaas297t gaas443t gaas603t gan02 gapox h2o-ice hgcdte2 ingasb0 ingasb9	gaas320t gaas465t gaas634t gan03 gasb hdpe hgcdte3 ingasb1 inp	gaas344t gaas488t gaas0 gan60 gasbox hfo2 hgte ingasb10 inpox	gaas367t gaas515t gaasox gan70 ge hfsi2 inas ingasb3 insb
insbox	ir	ir3si5e	ir3si5p	ito2	k
kbr	kcl	lasf9	li	lif	mgf2
mgo	mo	mosi2	mosi2-e	na	nacl
nb	nbsi	nbsi-e	ni	ni2si	ni3si
nisi	os	p_sias	p_siud	pbs	pbse
pd	pd2si	pd2si-e	pe	pt	resi1-75
resige0	resige1	resige22	resige39	resige51	resige64
resige75	resige83	resige91	rh	ringas0	ringas10
ringas20	ringas24	se	se-e	sf11	si
si-t02	si-t10	si-t15	si-t20	si-t25	si-t30
si-t35	si-t40	si-t45	si100_2	si110	si111
si11ge89	si20ge80	si28ge72	si3n4	si65ge35	si85ge15
si98ge02	siam1	siam2	sic	sige_ge	sige_si
sin_bf5	singas0	singas10	singas20	singas24	sio
sio2	sion0	sion20	sion40	sion60	sion80
siop	sipoly	sipoly10	sipoly20	sipoly30	sipoly40
sipoly50	sipoly60	sipoly70	sipoly80	sipoly90	sipore
snte	stsg0	stsg064	stsg123	stsg169	stsg229
ta	taox1	taox2	tasi2	tasi2-e	te
te-e	thf4	ti	tic	tin	tini
tio2	tio2-e	tisi-e	V	VC	vn
vsi2	vsi2-e	W	wsi2	wsi2-e	y2o3
zn	zn-e	zncdte0	zncdte1	zncdte10	zncdte3
zncdte5	zncdte7	zncdte9	zns	znse	znsete0
znsete1	znsete10	znsete3	znsete5	znsete7	znsete9
zr	zro2	zrsi2			

3.5 Querying the Database

Refractive index data can be retrieved at specified wavelengths, energies and wavenumbers.

```
$ nk co .3.um .5.um 1.3.eV
co: 1.218+2.11i  300.nm (4.13.eV) (33333.3.cm^-1)
co: 2.025+3.72i  500.nm (2.48.eV) (20000.cm^-1)
co: 3.85+4.77i  (954.nm) 1.3.eV (10485.2.cm^-1)
$ nk Al 400.cm^-1
al: 75.77+1.7e+02i  (25.0.um) (0.0496.eV) 400.cm^-1
```

The '--plot' option creates an encapsulated PostScript graph of n and k/n for the material specified.

nk --plot co

http://people.csail.mit.edu/jaffer/FreeSnell/co.png

4 Specifying Designs

Designs are coded in Scheme language files. More than one design can be specified in a design file, permitting sharing of code. A variety of design examples are contained in the validation suites dielectric.scm, metallic.scm, and granular.scm. The graphs output by these suites are shown and discussed in

```
http://people.csail.mit.edu/jaffer/FreeSnell/dielectric.html, http://people.csail.mit.edu/jaffer/FreeSnell/metallic.html, and http://people.csail.mit.edu/jaffer/FreeSnell/granular.html
```

4.1 Specifying Materials

The index-of-refraction of dielectric materials often varies little with wavelength. In these cases the index-of-refraction can be a number. It is often convenient to give a symbolic name to numbers. For example:

```
(define ZnS 2.2)
(define Ge 4.2)
```

After these definitions, layers can reference the identifiers:

```
(optical-stack
(substrate 1)
(layer ZnS 528.64e-9)
(layer Ge 178.96e-9)
(layer ZnS 250.12e-9)
(layer Ge 123.17e-9)
```

Sometimes the index-of-refraction is specified as a formula of wavelength. The *Refractive index database* at http://refractiveindex.info gives a formula for the refractive-index of the plastic PMMA over the range 0.4358.um to 1.052.um. We can use its formula as a Scheme function:

```
;; n^2 = C1 + C2*wl^2 + C3*wl^-2 + C4*wl^-4 + C5*wl^-6 + C6*wl^-8
(define PMMA
  (let ((C1 2.399964)
        (C2 - 8.308636E - 2)
        (C3 -1.919569E-1)
        (C4 8.720608E-2)
        (C5 -1.666411E-2)
        (C6 1.169519E-3))
    (lambda (w)
                                         ; wavelength in meters
      ;; wavelength in microns and limited to valid range
      (let* ((wl (max 0.4358 (min 1.052 (* w 1e6))))
             (w1^-2 (/ 1 wl wl)))
        (sqrt (+ C1
                 (* C2 wl wl)
                 (* (+ C3 (* (+ C4 (* (+ C5 (* C6
                                                wl^-2))
```

For more compliated material properties FreeSnell retrieves the wavelength-dependent index-of-refraction by calling functions which interpolate values from the materials database (see Chapter 3 [Material Databases], page 6).

In this example ge and zns can be passed as arguments to layer and substrate.

For dielectric films embedded with spherical metal granules much smaller than the thickness of the film and the wavelengths under consideration, Maxwell Garnett Theory provides a means to calculate the effective n and k. The thickness of the granular film must be several times the granule size; otherwise the more complicated machinations of [Granfilm] are required.

```
granular-IR ir q ir0
```

[Function]

The ir and $ir\theta$ arguments specify the indexes of refraction for the metallic and matrix materials respectively. Each can be either a (complex) number or function of one real argument returning a (complex) number. The real number q is the fractional volume occupied by the metal.

granular-IR returns a complex index-of-refraction (or function returning a complex index-of-refraction) for the composite layer.

If Au is a spectral function, the following three definitions are equivalent:

```
(define ruby-glass (granular-IR Au 8.0e-6 1.5))
(define (ruby-glass w) (granular-IR (Au w) 8.0e-6 1.5))
(define ruby-glass (lambda (w) (granular-IR (Au w) 8.0e-6 1.5)))
```

4.2 Optical Stack

```
\begin{array}{ll} \text{optical-stack } layer1 \dots & [\text{Function}] \\ \text{optical-stack } layer1 \dots bottom\text{-substrate} & [\text{Function}] \\ \text{optical-stack } top\text{-substrate } layer1 \dots bottom\text{-substrate} & [\text{Function}] \\ \end{array}
```

Returns a data structure combining its *layer* arguments. Each layer is returned from a call to layer or substrate. Substrate arguments must be first or last and default to having an index-of-refraction of 1. A substrate has arbitrarily large thickness, and is the source or sink of test inputs (radiation).

layer ir thick nom layer ir thick

[Function] [Function]

Returns a layer having the specified index-of-refraction and thickness.

If ir is a number, then the index-of-refraction is ir at all wavelengths. If ir is a procedure then the index-of-refraction at wavelength w is (ir w).

If the number thick is smaller than 1/50, then it is taken as the actual thickness. Note that the effective optical thickness will be larger than the actual thickness because light is slowed by the index-of-refraction.

If the number *thick* is larger than 1/50, then the thickness is *thick* times *nominal* divided by the real-part of the index-of-refraction at *nominal*, where *nominal* is either the third argument *nom* or the value set by the **nominal** function. This is a convenient notation for the fractional optical wavelengths often used to specify filter elements.

Layers specified by layer model the interference effects of reflections of reflections. This is correct for thin layers or if the modeled optical system will be illuminated by coherent light. But layers thicker than several wavelengths have variations extremely sensitive to incident angle.

Incoherent illumination will average over the wiggles. For these layers FreeSnell computes the transmitted and reflected power ratios, rather than E-fields.

layer* ir thick

[Function]

Returns an *incoherent* layer having the specified index-of-refraction and thickness.

substrate ir [Function]

Returns a substrate having the specified index-of-refraction.

If ir is a number then the index-of-refraction is ir at all wavelengths. If ir is a procedure then the index-of-refraction at wavelength w is (ir w).

If substrates are not specified, then their index-of-refraction defaults to 1 (vacuum).

To place a substrate between two sets of layers, use layer* instead.

nominal nom [Function]

Sets the default nominal thickness to *nom*. Multiple nominal commands are allowed interspersed with layer commands. The arguments to optical-stack are considered in order from the first to the last.

repeat j layer1 layer2 . . .

[Function]

Inserts j copies of the sequence layer1, layer2, . . . into the stack.

4.3 Plot-response

plot-response arg1 arg2 . . .

[Function]

One or more of arg1, arg2, . . . should be an optical stack returned by optical-stack, or a value returned by a call to IR. The other arguments should be values returned by the functions in sections Section 4.3.1 [Ranges and Units], page 14, Section 4.3.2 [Traces], page 16, and Section 4.3.3 [Other Outputs], page 18.

Plot-response creates a graph, data file, or color patches as directed by its arguments. If more than one optical stack is given, the same quantities are computed for each optical stack; but all are plotted to a single graph.

```
stack-colors color1 color2 ...
```

[Function]

Each color1, ... should be a string naming a Resene color, a saturate color, or a number between 0 and 100. If supplied, there should be one color for each optical-stack. color1, ... default to black (0). If stack-colors is called more than once, then its color arguments are appended together.

stack-colors causes the traces from each optical stack to be drawn in its corresponding color.

4.3.1 Ranges and Units

title str filebase [Function] title str

Sets title for the run to str. If the string filebase is given, then it is used for the output filename root; otherwise str is used.

```
\begin{array}{lll} \text{output-format} & sym & & [\text{Function}] \\ \text{output-format} & k1 & k2 & & [\text{Function}] \\ \text{output-format} & sym & k1 & k2 & & [\text{Function}] \end{array}
```

According to the symbol sym, sets the disposition of plots to be:

eps filebase.eps
ps filebase.ps
png filebase.png
jpg filebase.jpg
jpeg filebase.jpeg
pdf filebase.pdf

#t views filebase.eps using ps:viewer.

If output-format is not used, then the output-format defaults to the value of top-level identifier *output-format*, which defaults to #t.

If a pair of nonnegative exact integers, k1 and k2 follows sym, then the plot will be k1 pixels horizontally and k2 pixels vertically.

The output-format command does not affect the data written by output-data.

```
\begin{array}{lll} & & & & & & & & \\ \text{font} & & & & & & & \\ \text{font} & & & & & & & \\ \text{font} & & & & & & \\ \text{font} & x & & & & & \\ \text{font} & x & left\text{-}template & right\text{-}template & & \\ \text{font} & fnt & left\text{-}template & right\text{-}template & \\ \text{font} & fnt & x & left\text{-}template & right\text{-}template & \\ \text{font} & fnt & x & left\text{-}template & right\text{-}template & \\ \end{array}
```

If a string fnt is supplied, then it names the PostScript font which will be used. The default value is Times.

If a nonnegative real number x follows the fnt, then x is the fontsize.

If two strings follow, then they are used as the templates whose printed representation using fnt is used to size the left and right margins respectively. If not specified, the templates default to '-.0123456789'.

If x is not specified and k1 is, then the font height will be k1/33. If neither is specified, then the font height will be 12.

The font command does not affect the data written by output-data.

output-data file output-data file str1 [Function]

[Function]

output-data file str1 str2

[Function]

If the first character of file is '|', then lines of data are piped to the stdin of the command line in file; otherwise a file of data is written to file.

str1 and str2 are printf format strings for the first number and the rest of the numbers printed on one line. If #f is passed, then the corresponding numbers are written with full Scheme precision and tab delimited.

range low high

[Function]

Sets the ordinate range of the plot to low to high.

range low high 'db

[Function]

db low high

[Function]

Sets the ordinate range of the plot to low to high decibels.

wavelengths w

[Function]

Sets the abscissa range of the plot to be linear from wavelengths 0.75*w to 1.25*w.

wavelengths w1 w2

[Function]

Sets the abscissa range of the plot to be linear from wavelengths w1 to w2.

wavelengths w1 w2 g1 g2

[Function]

Sets the abscissa range of the plot to be linear from wavelengths w1 to w2 in a graph rectangle from wavelengths g1 to g2.

wavenumbers w

[Function]

Sets the abscissa range of the plot to be logarithmic from wavenumbers 0.666*w to 1.5*w.

wavenumbers w1 w2

[Function]

Sets the abscissa range of the plot to be logarithmic from wavenumbers w1 to w2.

wavenumbers w1 w2 g1 g2

[Function]

Sets the abscissa range of the plot to be linear from wavenumbers w1 to w2 in a graph rectangle from wavenumbers g1 to g2.

eVs x

[Function]

Sets the abscissa range of the plot to be linear from energy 0.666*x to 1.5*x electron Volts.

eVs x1 x2 [Function]

Sets the abscissa range of the plot to be linear from energy x1 to x2 electron Volts.

eVs $x1 ext{ } x2 ext{ } g1 ext{ } g2$ [Function]

Sets the abscissa range of the plot to be linear from energy x1 to x2 electron Volts in a graph rectangle from energies g1 to g2 electron Volts.

logarithmic w [Function]

Sets the abscissa range of the plot to be logarithmic from wavelengths 0.666*w to 1.5*w.

logarithmic w1 w2

[Function]

Sets the abscissa range of the plot to be logarithmic from wavelengths w1 to w2.

logarithmic $w1 \ w2 \ g1 \ g2$

[Function]

Sets the abscissa range of the plot to be logarithmic from wavelengths w1 to w2 in a graph rectangle from wavelengths g1 to g2.

angles theta [Function]

Sets the abscissa range of the plot to be linear from angles 0.75*theta to 1.25*theta.

angles theta1 theta2

[Function]

Sets the abscissa range of the plot to be linear from angles theta1 to theta2.

marker $w1 \ w2 \dots$ [Function]

Places vertical arrows at abscissa coordinates $w1, w2, \ldots$ The marker command does not affect the data written by output-data.

samples k [Function]

Sets the number of abscissa coordinates to k. The default value is 200.

samples k spacing

[Function]

Sets the number of abscissa coordinates to k. spacing is one of the (single-quoted) symbols 'eV', 'ratio', 'wavelength', or 'wavenumber', and determines the spacing of the samples. The default spacing is 'ratio' if the endpoint ratio is between 1.5 and 10000; and 'wavelength' otherwise.

Note that *spacing* does not need to match the abscissa scale. To generate 10 samples at evenly spaced wavelengths, do:

(samples 10 'wavelength)

smooth sigma [Function]

Convolves the traces (before converting values to decibels) with a Gaussian filter having wavelength standard deviation sigma.

4.3.2 Traces

These functions specify whether the plot holds angle constant and varies wavelength; holds wavelength constant and varies angle; or plots components of the index-of-refraction of a material. Multiple invocations of any one of these functions puts all those specified traces in one plot. To generate separate plots call plot-response multiple times.

The type of a trace appearing in a plot is specified by a symbol. The first ten in this table are for separate polarizations. The rest average the two polarizations.

T_s	S-plane transmission
$R_{-}s$	S-plane reflection from top
B_s	S-plane reflection from bottom
A_s	S-plane absorption from top
L_s	S-plane absorption from bottom
$T_{-}p$	P-plane transmission
$R_{-}p$	P-plane reflection from top
B_p	P-plane reflection from bottom
A_p	P-plane absorption from top
L_p	P-plane absorption from bottom
T	tranmission
R	reflection from top
В	reflection from bottom
A	absorption from top
L	absorption from bottom

A trace can also be a quoted scheme expression combining numbers and the symbols listed above with the operators +, -, *, /, ln, log_10, and average. The following example computes the reflectivity relative to a substrate reflectivity of 0.023:

```
(incident 45 '(/ (- R_p .023) .023))
```

incident angle trace1 trace2 ...

[Function]

A plot of *trace1*, *trace2*, . . . versus wavelength will be generated for radiation incident at *angle* degrees.

The angle argument can also be a list of angles in degrees. In this case the plots of trace1, trace2, ... will be averaged over the angles given.

This is useful when profiling materials whose thicknesses are several times wavelengths of interest. Plots at a single angle of incidence can oscillate wildly with wavelength as the reflections go in and out of phase, constructively and destructively interfering.

wavelength w trace1 trace2 ...

[Function]

A plot of trace1, trace2, . . . versus incident angle will be generated for radiation at wavelength w.

ir substance comp1 comp2 . . .

[Function]

Plots characteristics of procedure substance versus wavelength. Symbols comp1, comp2, . . . determine the characteristics to be plotted:

n real real-part

```
k
imag
imag-part
ec
extinction-coefficient
k
k/n k/n
r0
reflect
reflectance
```

Normal reflectance from a thick layer.

4.3.3 Other Outputs

color-swatch angle trace

[Function]

Computes the color of trace at angle degrees from normal using CIE illuminant D65.

The following statement will cause plot-response to compute the reflected color (average of both polarizations) at 30 degrees from the surface normal.

```
(color-swatch 30 'R)
```

If there are any color-swatch statements passed to plot-response, then a file named filebase-color.png will be written containing 64x64 pixels color squares, one for each color computed. The squares are arrayed horizontally in the order they are passed to plot-response. Vertically, one such row is generated for each optical stack.

The filebase string is that set by the title command.

```
solar angle token1 token2 . . .
```

[Function]

For each stack, prints out the results of integrating each trace specified (*token1*, *token2*, . . .) at *angle* with "Key Centre for Photovoltaic Engineering UNSW - Air Mass 1.5 Global Spectrum" solar irradiance.

5 Program Interface

(require 'fresnel-equations)

```
combine-layers th_i w layers
```

[Function]

layers is a list of lists of index-of-refraction and thickness. The index-of-refraction may be a complex number or a procedure of wavelength (w) in meters returning a complex number.

Layers with negative *thickness* are modeled as incoherent (with positive thickness); otherwise as coherent (with inteference fringing).

The index-of-refraction of the top and bottom media are given by the first and last layers, which must have thickness 0. w is probe wavelength. th_{-i} is the angle of the incident ray in radians.

Combine-layers returns a list of three non-negative real numbers:

- the ratio of transmitted power to incident power;
- the ratio of reflected power (from the top) to incident power; and
- the ratio of reflected power (from the bottom) to incident power.

The transmitted and forward ratios sum to 1.0 if *layers* are all dielectric (lossless). The transmitted and reverse ratios sum to 1.0 if *layers* are all dielectric (lossless).

Negative w computes the S-polarization, else the P-polarization.

snell-law z1 z2 th-i

[Function]

Complex numbers z1 and z2 are the indexes of refraction of the incident and opposite side of the boundary plane between two materials. th-i is the angle of incidence (from the normal of the boundary plane).

snell-law returns the exit angle (from normal) of an incident ray impinging at th-i from normal.

If the ray undergoes total internal reflection, then the returned angle will not be real. If z1 and z2 are real, then the real part of the returned value will be pi/2 and represents a quickly decaying evanescent wave. Otherwise, the real part of the return value tends toward pi/2. I don't know a physical interpretation of the imaginary part.

6 About FreeSnell

```
Free Software
Fre snel Equations
Snell's Law
=======
FreeSnell
```

The author can be reached as 'agj@alum.mit.edu'. The most recent information about FreeSnell can be found on the FreeSnell home page:

http://people.csail.mit.edu/jaffer/FreeSnell

6.1 Installation

6.1.1 i386 MS-Windows

- Download and run http://groups.csail.mit.edu/mac/ftpdir/scm/slib-3c1-1. exe.
- Download and run http://groups.csail.mit.edu/mac/ftpdir/scm/scm-5f4-1. exe.
- Download and run http://groups.csail.mit.edu/mac/ftpdir/scm/ FreeSnell-1c4-1.exe.

6.1.2 x86_64 GNU/Linux with RPM

```
#! /bin/sh
wget http://groups.csail.mit.edu/mac/ftpdir/scm/slib-3c1-1.noarch.rpm
wget http://groups.csail.mit.edu/mac/ftpdir/scm/scm-5f4-1.x86_64.rpm
wget http://groups.csail.mit.edu/mac/ftpdir/scm/wb-2b4-1.x86_64.rpm
rpm -U slib-3c1-1.noarch.rpm scm-5f4-1.x86_64.rpm wb-2b4-1.x86_64.rpm
wget http://groups.csail.mit.edu/mac/ftpdir/scm/FreeSnell-1c4.zip
unzip FreeSnell-1c4.zip
(cd FreeSnell; ./configure --prefix=/usr/local/; make install)
```

6.1.3 Unix (including GNU/Linux)

```
#! /bin/sh
wget http://groups.csail.mit.edu/mac/ftpdir/users/jaffer/slib.zip
wget http://groups.csail.mit.edu/mac/ftpdir/users/jaffer/scm.zip
wget http://groups.csail.mit.edu/mac/ftpdir/users/jaffer/wb.zip
wget http://groups.csail.mit.edu/mac/ftpdir/scm/FreeSnell.zip
unzip slib.zip
unzip slib.zip
unzip scm.zip
unzip wb.zip
unzip FreeSnell.zip
(cd slib; ./configure --prefix=/usr/local/; make install)
(cd scm; ./configure --prefix=/usr/local/;
make scmlit; make scm5; make mydlls; make wbscm.so; make install)
(cd FreeSnell; ./configure --prefix=/usr/local/; make install)
```

6.2 Using FreeSnell

To run FreeSnell from the C:\Program Files\SCM\FreeSnell directory, click on the FreeSnell desktop icon. In Unix, from the 'FreeSnell' directory run 'scm'.

You can then type expressions to the SCM interpreter. To run FreeSnell's regression suites type:

```
(load "dielectric.scm")
(dielectric)
(load "metallic.scm")
(metallic)
(load "granular.scm")
(granular)
(load "coherence.scm")
(coherence)
(load "polyethylene.scm")
(polyethylene)
```

I set up design directories as peers of 'FreeSnell'; that is, both are subdirectories of the same directory. I find it useful to put related designs in one directory.

In order to load FreeSnell files, you should create a local SLIB catalog (named usercat) within the design directory or your *HOME* directory. This catalog translates symbols to the pathnames of FreeSnell files. Here is the usercat included in the FreeSnell distribution, which is suitable to copy to design directories which are peers of FreeSnell:

Design files can then load FreeSnell with the expression:

```
(require 'FreeSnell)
```

Realize that this usercat file assumes that the FreeSnell directory is named FreeSnell. If your FreeSnell directory is named something else, then substitute its name for FreeSnell in the right hand side of lines in usercat.

Index

\mathbf{A}	${f M}$
angles	marker
\mathbf{C}	N
color-swatch 18 combine-layers 19 CRC 2	Nave 2 NCSU 2 nominal 13
D	O
db	optical-stack 12 output-data 15 output-format 14
E	
eVs	P
T3	plot-response
F	T.
font 14 FreeSnell 21	R range15
G	repeat
Garnett 2	\mathbf{S}
Granfilm 2	1-
granular-IR	samples 16 Sernelius 2
	SLIB
Н	smooth
Heavens 2	snell-law
HOME	solar 18 stack-colors 14
	substrate
T	
incident	${f T}$
ir	title
${f L}$	\mathbf{W}
layer	wavelength
layer*	wavelengths
${\tt logarithmic}16$	wavenumbers15