

# Guided Image Filtering

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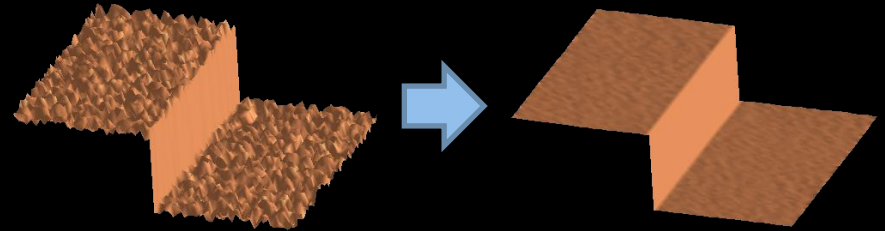
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Microsoft Research Asia

Xiaoou Tang

The Chinese University of Hong Kong

# Introduction

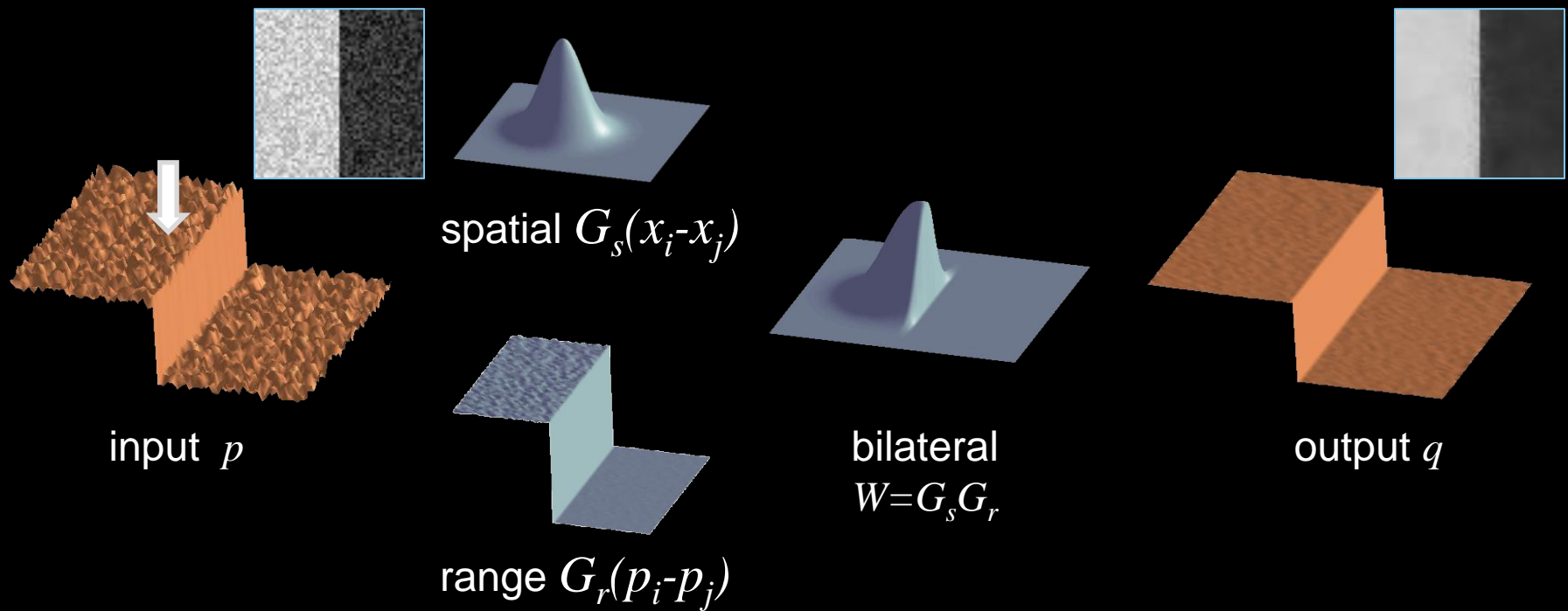


- Edge-preserving filtering
  - An important topic in computer vision
    - Denoising, image smoothing/sharpening, texture decomposition, HDR compression, image abstraction, optical flow estimation, image super-resolution, feature smoothing...
  - Existing methods
    - Weighted Least Square [Lagendijk et al. 1988]
    - Anisotropic diffusion [Perona and Malik 1990]
    - Bilateral filter [Aurich and Weule 95], [Tomasi and Manduchi 98]
    - Digital TV (Total Variation) filter [Chan et al. 2001]

# Introduction

- Bilateral filter

$$q_i = \sum_{j \in N(i)} W_{ij}(p) p_j$$

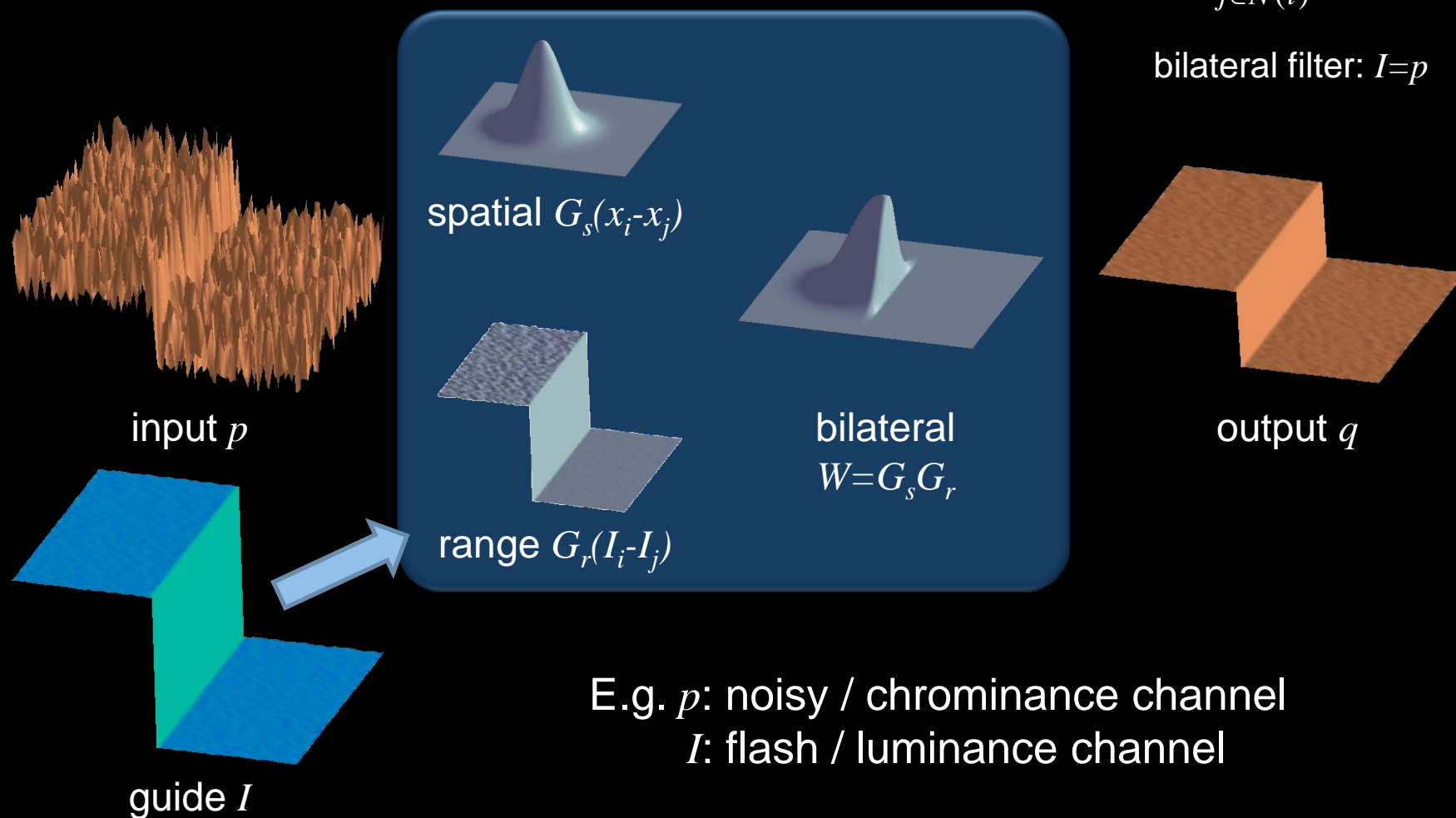


# Introduction

- Joint bilateral filter [Petschnigg et al. 2004]

$$q_i = \sum_{j \in N(i)} W_{ij}(I) p_j$$

bilateral filter:  $I=p$



# Introduction

- Advantages of bilateral filtering
  - Preserve edges in the smoothing process
  - Simple and intuitive
  - Non-iterative

# Introduction

- Problems in bilateral filtering

- Complexity

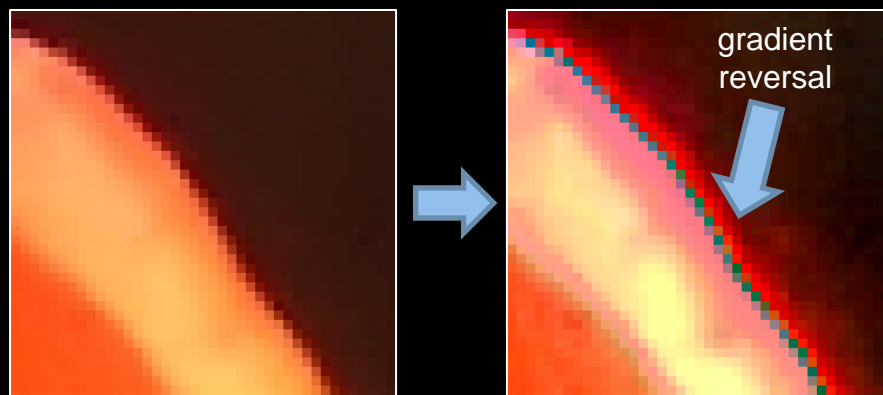
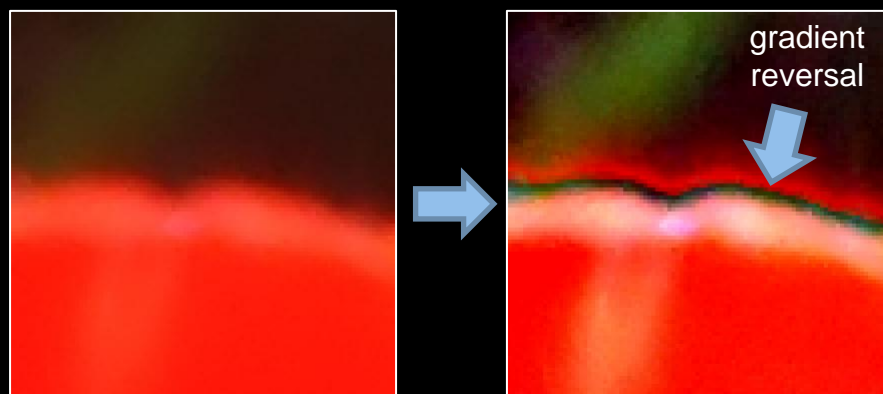
- Brute-force:  $O(r^2)$
  - Distributive histogram:  $O(\log r)$  [Weiss 06]
  - Bilateral grid: band-dependent [Paris and Durand 06], [Chen et al. 07]
  - Integral histogram:  $O(1)$  [Porikli 08], [Yang et al. 09]
- } Approximate (quantized)

# Introduction

- Problems in bilateral filtering

- Complexity
- Gradient distortion
  - Preserves edges, but not gradients

Example: detail enhancement



input

enhanced

# Introduction

- Our target - to design a new filter
  - Edge-preserving filtering
  - Non-iterative
  - $O(1)$  time, fast and non-approximate
  - No gradient distortion



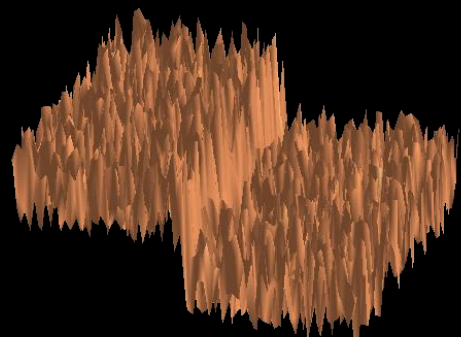
Advantages of bilateral filter



Overcome bilateral filter's problems



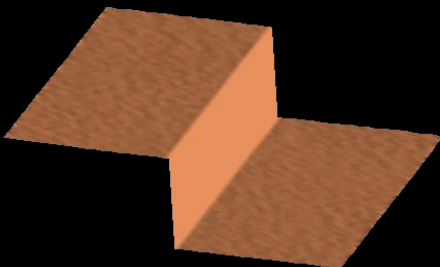
# Guided filter



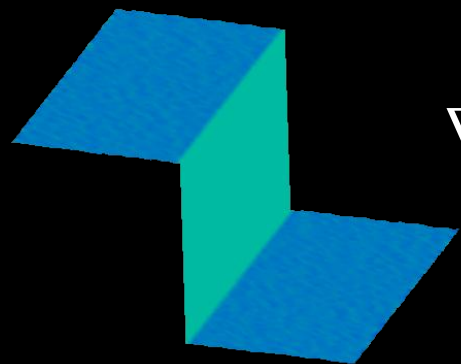
input  $p$

$$q_i = p_i - n_i$$

$n_i$  - noise / texture



output  $q$



guide  $I$

$$\nabla q_i = a \nabla I_i$$

$$q_i = a I_i + b$$

$$\min_{(a,b)} \sum_i (a I_i + b - p_i)^2 + \epsilon a^2$$

Linear regression

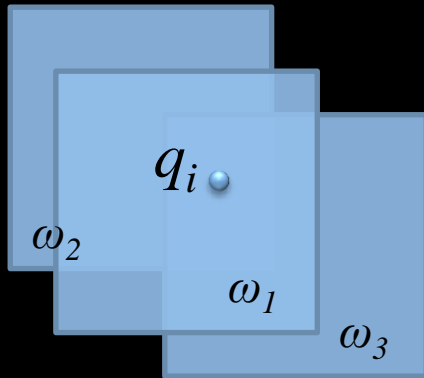
$$a = \frac{\text{cov}(I, p)}{\text{var}(I) + \epsilon}$$

$$b = \bar{p} - a \bar{I}$$

Bilateral/joint bilateral filter does not have this linear model

# Guided filter

- Extend to the entire image
  - In all local windows  $\omega_k$ , compute the linear coefficients
  - Compute the average of  $a_k I_i + b_k$  in all  $\omega_k$  that covers pixel  $q_i$



## Definition

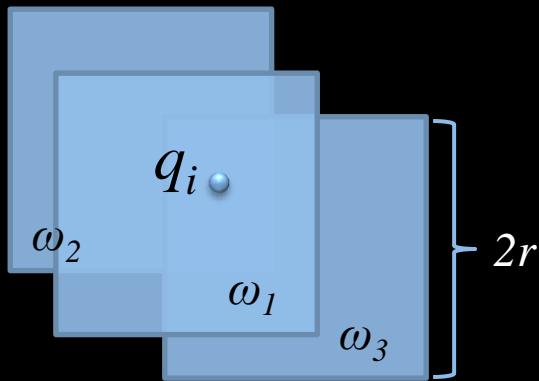
$$a_k = \frac{\text{cov}_k(I, p)}{\text{var}_k(I) + \varepsilon}$$

$$b_k = \bar{p}_k - a \bar{I}_k$$

$$\begin{aligned} q_i &= \frac{1}{|\omega|} \sum_{k|i \in \omega_k} (a_k I_i + b_k) \\ &= \bar{a}_i I_i + \bar{b}_i \end{aligned}$$

# Guided filter

- Parameters
  - Window radius  $r$
  - Regularization  $\varepsilon$



## Definition

$$a_k = \frac{\text{cov}_k(I, p)}{\text{var}_k(I) + \varepsilon}$$

$$b_k = \bar{p}_k - a\bar{I}_k$$

$$q_i = \frac{1}{|\omega|} \sum_{k|i \in \omega_k} (a_k I_i + b_k)$$
$$= \bar{a}_i I_i + \bar{b}_i$$

# Guided filter: smoothing

$$a = \frac{\text{cov}(I, p)}{\text{var}(I) + \varepsilon}$$

$$b = \bar{p} - a\bar{I}$$

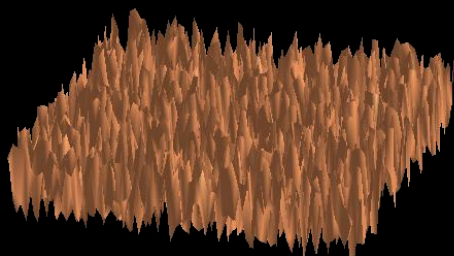
$$\begin{aligned} \text{var}(I) &\ll \varepsilon \\ \text{cov}(I, p) &\ll \varepsilon \end{aligned}$$

$$a \approx 0$$

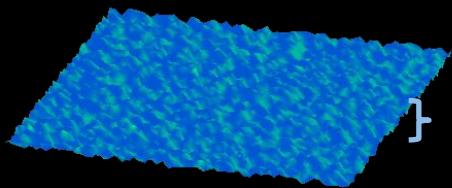
$$b \approx \bar{p}$$

a cascade of  
mean filters

$$q_i = \bar{a}I_i + \bar{b} \approx \bar{p}$$

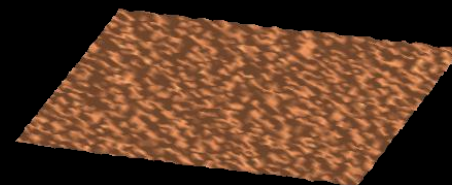


input  $p$



guide  $I$

$$\text{var}(I) \ll \varepsilon$$



output  $q$

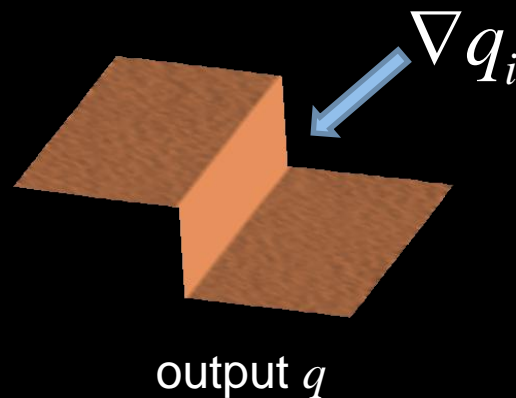
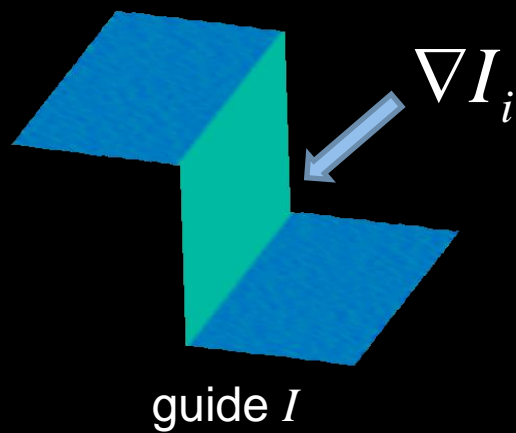
$r$  : determines  
band-width  
(like  $\sigma_s$  in BF)

# Guided filter: edge-preserving

$$q_i = \bar{a}I_i + \bar{b} \implies \nabla q_i = \bar{a}\nabla I_i + I_i\nabla\bar{a} + \nabla\bar{b}$$

$$\varepsilon \downarrow \implies a = \frac{\text{cov}(I, p)}{\text{var}(I) + \varepsilon} \uparrow$$

$\varepsilon$  : degree of edge-preserving  
(like  $\sigma_r$  in BF)



# Example – edge-preserving smoothing

input &  
guide



guided  
filter  
(let  $I=p$ )



$$r=4, \epsilon=0.1^2$$



$$r=4, \epsilon=0.2^2$$



$$r=4, \epsilon=0.4^2$$

bilateral  
filter



$$\sigma_s=4, \sigma_r=0.1$$



$$\sigma_s=4, \sigma_r=0.2$$



$$\sigma_s=4, \sigma_r=0.4$$

- Our target - to design a new filter

- Edge-preserving filtering



- Non-iterative



Advantages of bilateral filter

- $O(1)$  time, fast and non-approximate



Overcome bilateral filter's problems

- No gradient distortion

# Complexity

- *mean, var, cov* in all local windows
- Integral images [Franklin 1984]
  - O(1) time – independent of  $r$
  - Non-approximate

Definition

$$a_k = \frac{\text{cov}_k(I, p)}{\text{var}_k(I) + \varepsilon}$$

$$b_k = \bar{p}_k - a\bar{I}_k$$

$$q_i = \bar{a}_i I_i + \bar{b}_i$$



O(1) bilateral  
(32-bin, 40ms/M)  
[Porikli 08]



O(1) bilateral  
(64-bin, 80ms/M)

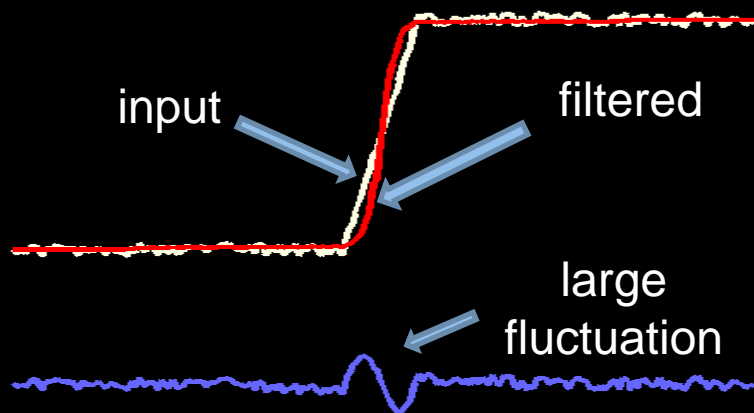


O(1) guided  
(exact, 80ms/M)

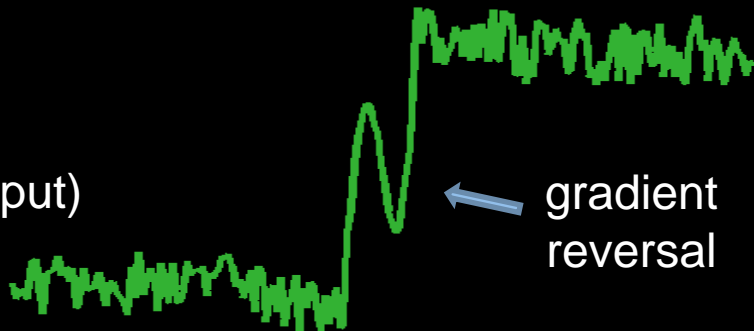


# Gradient Preserving

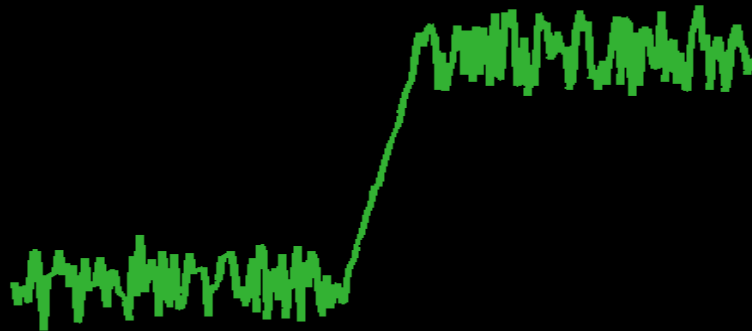
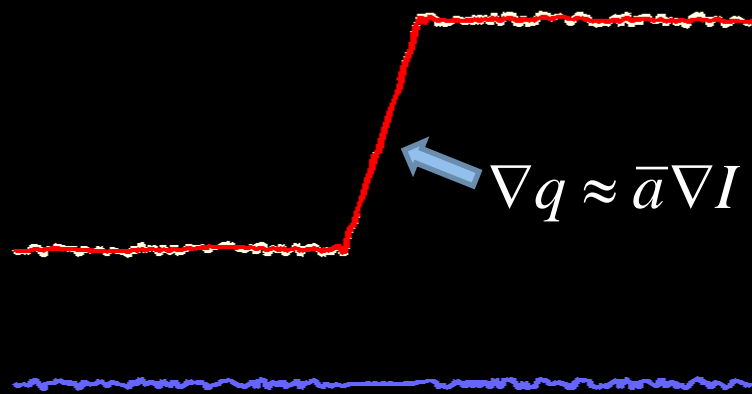
bilateral filter



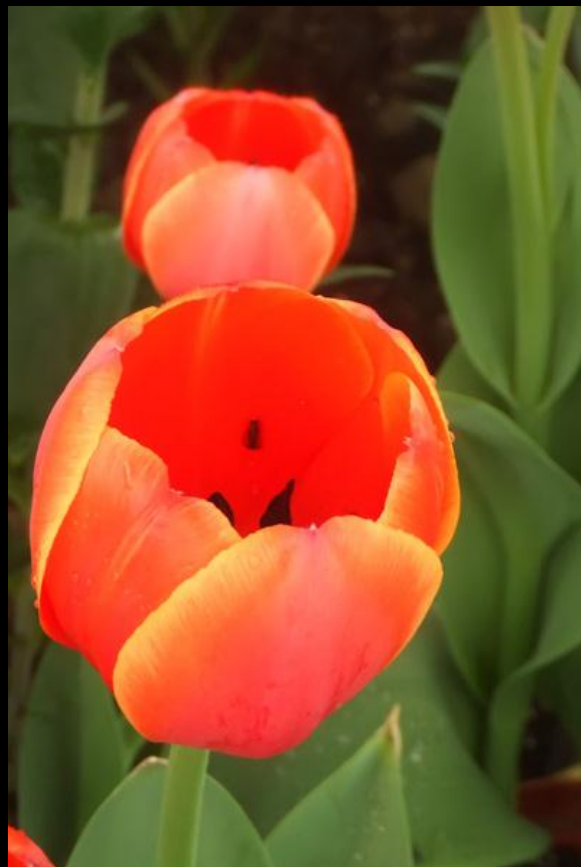
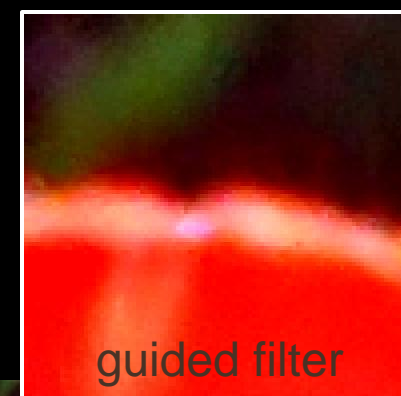
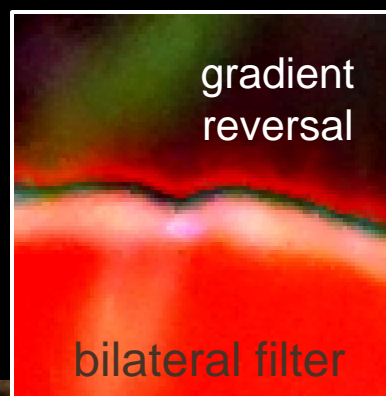
enhanced (detail \* 5 + input)



guided filter



# Example – detail enhancement



input ( $I=p$ )

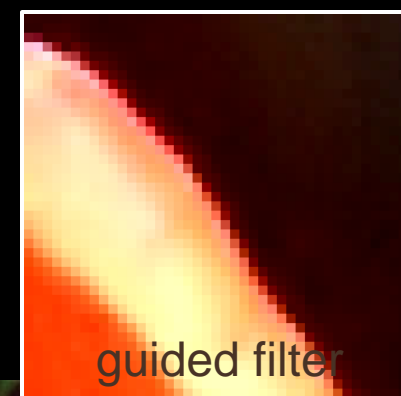
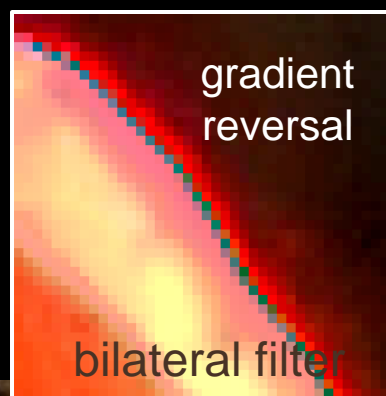


bilateral filter  
 $\sigma_s=16, \sigma_r=0.1$



guided filter  
 $r=16, \varepsilon=0.1^2$

# Example – detail enhancement



# Example – HDR compression



input HDR



bilateral filter



guided filter



bilateral filter  
 $\sigma_s=15, \sigma_r=0.12$



guided filter  
 $r=15, \varepsilon=0.12^2$

# Example – flash/no-flash denoising



input  $p$   
(no-flash)



joint bilateral filter  
 $\sigma_s=8, \sigma_r=0.02$



guide  $I$   
(flash)

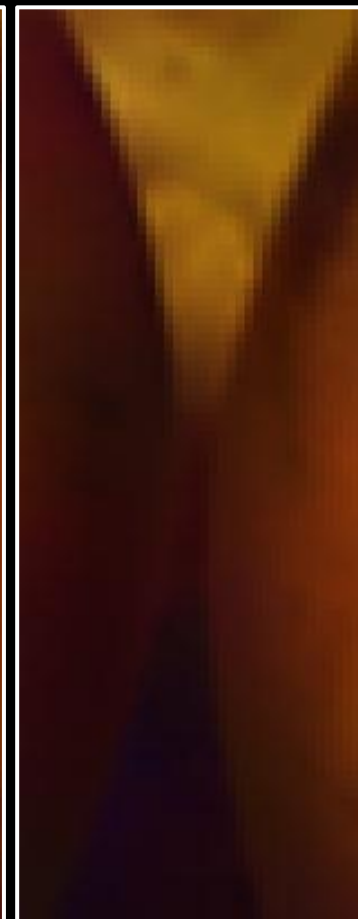


guided filter  
 $r=8, \epsilon=0.02^2$



gradient reversal

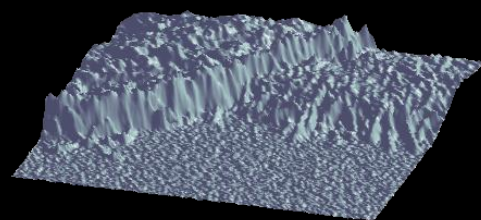
joint bilateral



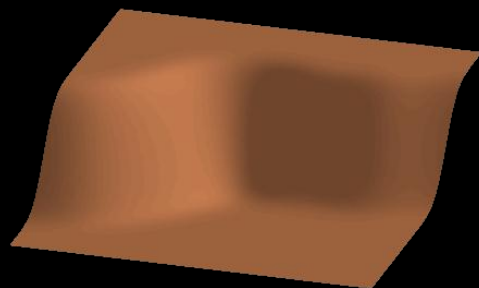
guided filter

# Beyond smoothing

- Applications: feathering/matting, haze removal

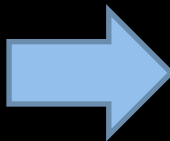


guide  $I$

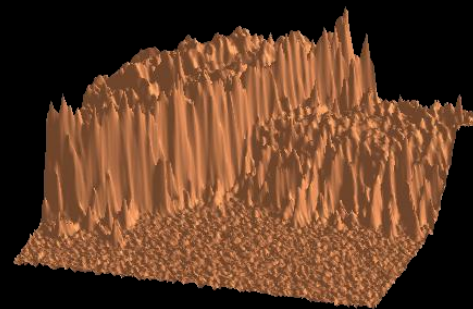


input  $p$

very small  $\varepsilon$



preserve most  
gradients



output  $q$

$$\nabla q \approx \bar{a} \nabla I$$

## Example – feathering



guide *I*  
(size 3000x2000)

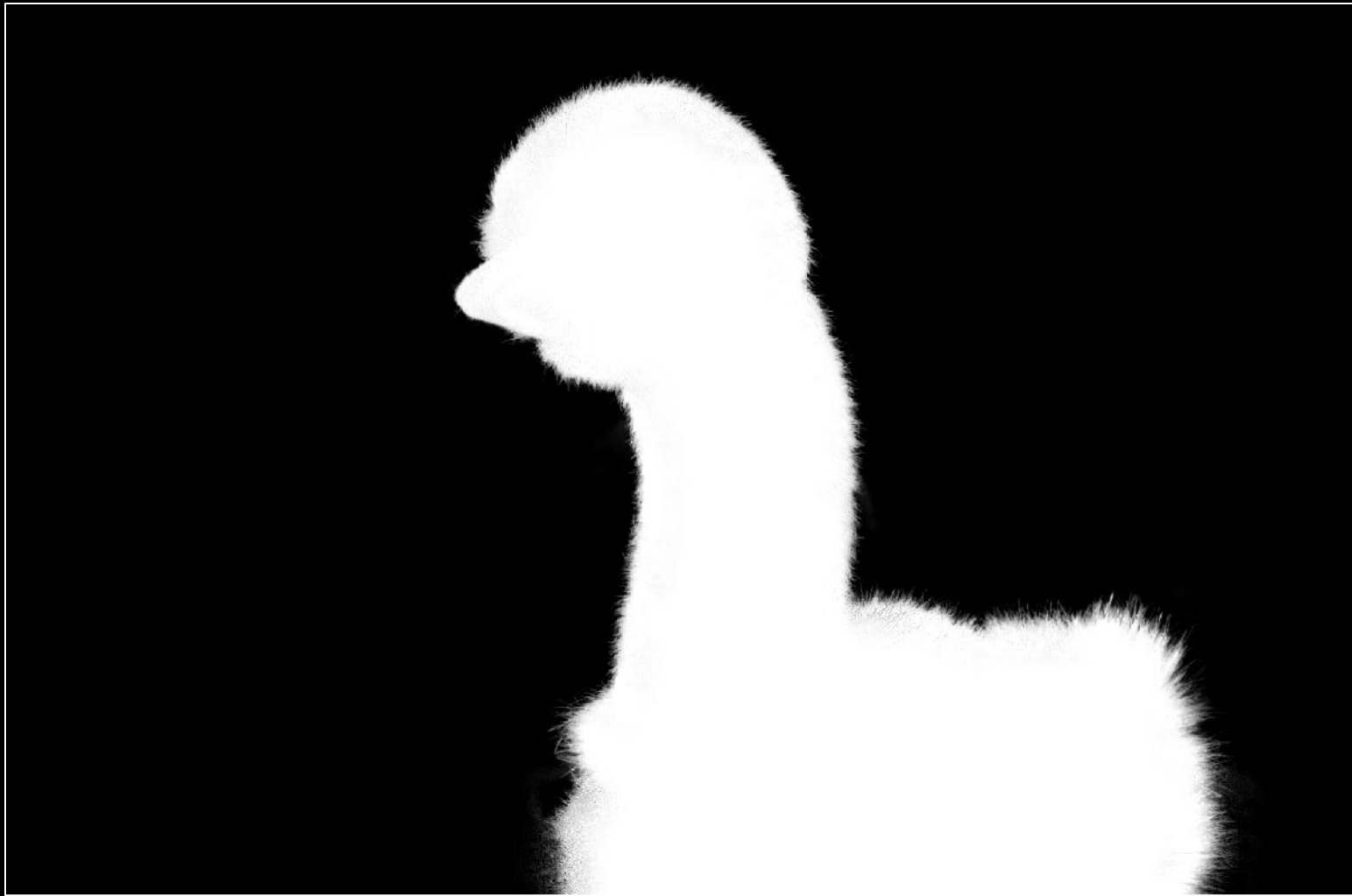
## Example – feathering



filter input  $p$  (binary segmentation)

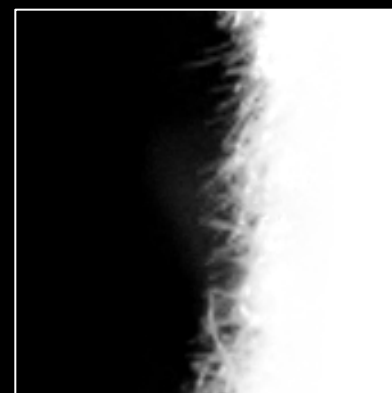
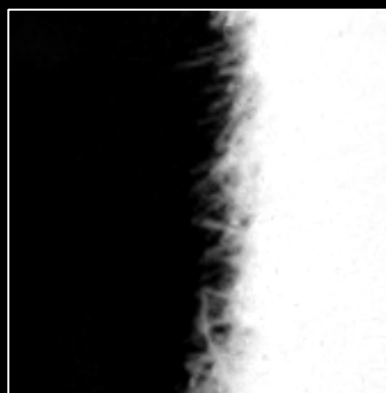
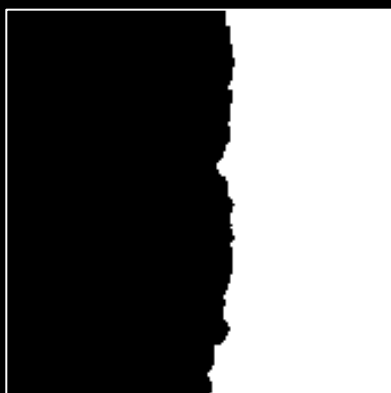
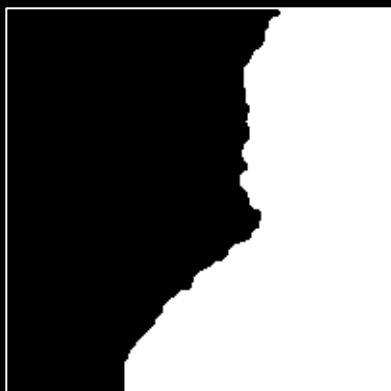
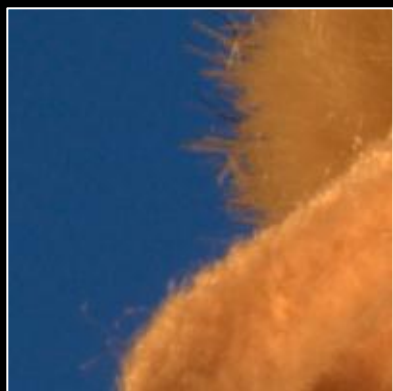


## Example – feathering



filter output  $q$  (alpha matte)

## Example – feathering



guide  $I$

filter input  $p$

filter output  $q$   
0.3s  
image size 6M

matting Laplacian  
[Levin et al. 06]  
2 min

# Example – haze removal



guide  $I$



filter input  $p$   
(dark channel prior  
[He et al. 09])



filter output  $q$

# Example – haze removal



guide *I*



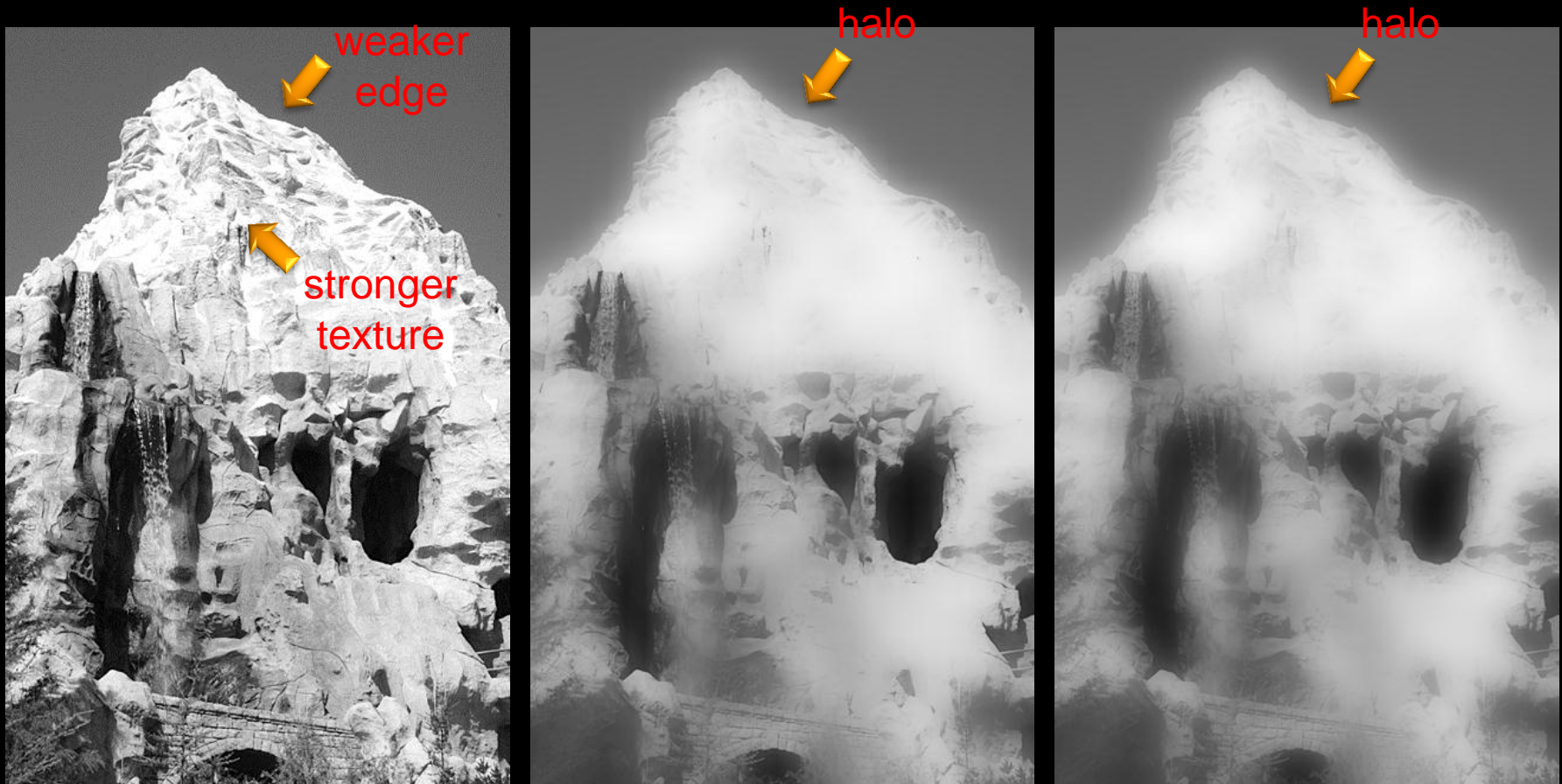
guided filter  
( $<0.1s$ ,  $600 \times 400p$ )



global optimization  
(10s)

# Limitation

- “What is an edge” – inherently ambiguous, context-dependent



Input

Bilateral filter  
 $\sigma_s=16, \sigma_r=0.4$

Guided filter  
 $r=16, \varepsilon=0.4^2$

# Conclusion

- We go from “BF” to “GF”
  - Edge-preserving filtering
  - Non-iterative
  - $O(1)$  time, fast, accurate
  - Gradient preserving
  - More generic than “smoothing”

**Thank you!**