



Seam-Carving

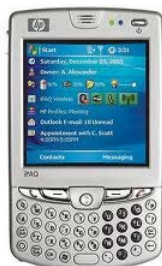
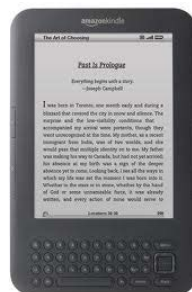
and Content-driven Retargeting of Images
(and Video)



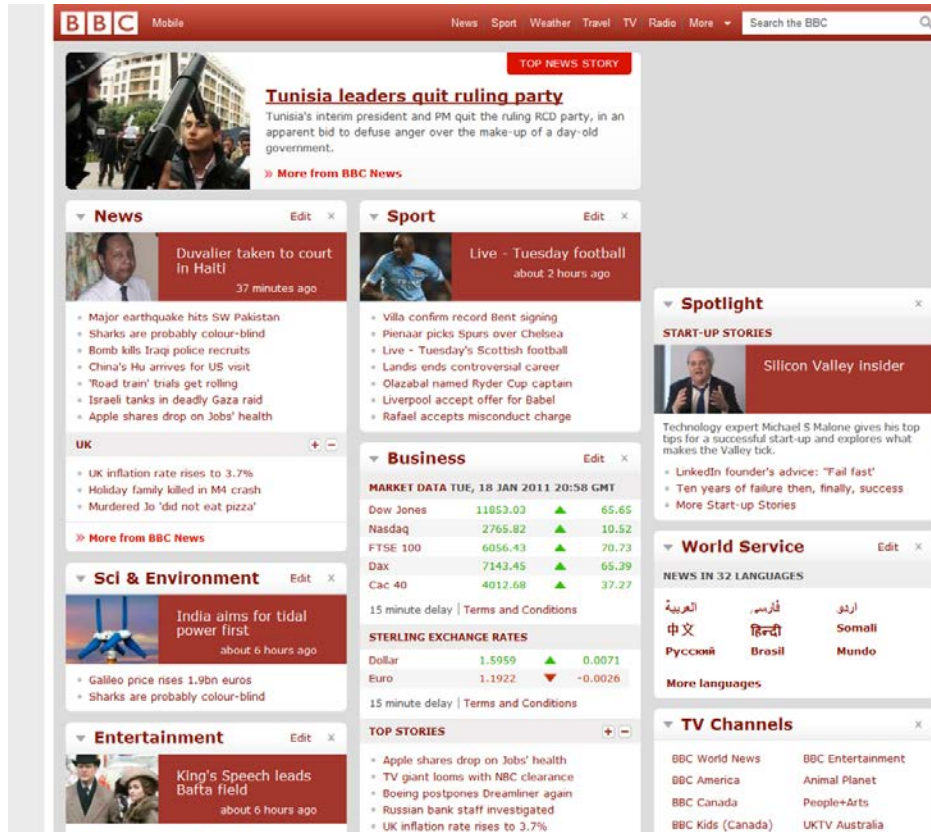
Michael Rubinstein
MIT

Some slides borrowed from Ariel Shamir and Shai Avidan

Display Devices



Content Retargeting



BBC Mobile News Sport Weather Travel TV Radio More Search the BBC

TOP NEWS STORY
Tunisia leaders quit ruling party
 Tunisia's interim president and PM quit the ruling RCD party, in an apparent bid to defuse anger over the make-up of a day-old government.
[More from BBC News](#)

News Edit x
 Duvalier taken to court in Haiti
 37 minutes ago
 • Major earthquake hits SW Pakistan
 • Sharks are probably colour-blind
 • Bomb kills Iraq police recruits
 • China's Hu arrives for US visit
 • 'Road train' trials get rolling
 • Israeli tanks in deadly Gaza raid
 • Apple shares drop on Jobs' health
[More from BBC News](#)

Sport Edit x
 Live - Tuesday football
 about 2 hours ago
 • Villa confirm record Bent signing
 • Pienaar picks Spurs over Chelsea
 • Live - Tuesday's Scottish football
 • Landis ends controversial career
 • Olazabal named Ryder Cup captain
 • Liverpool accept offer for Babel
 • Rafael accepts misconduct charge

Spotlight x
START-UP STORIES
 Silicon Valley Insider
 Technology expert Michael S Malone gives his top tips for a successful start-up and explores what makes the Valley tick.
 • LinkedIn founder's advice: 'Fail fast'
 • Ten years of failure then, finally, success
 • More Start-up Stories

Business Edit x
MARKET DATA TUE, 18 JAN 2011 20:58 GMT
 Dow Jones 11853.03 ▲ 65.65
 Nasdaq 2765.82 ▲ 10.52
 FTSE 100 6056.43 ▲ 70.73
 Dax 7142.45 ▲ 65.39
 Cac 40 4012.68 ▲ 37.27
 15 minute delay | Terms and Conditions
STERLING EXCHANGE RATES
 Dollar 1.5959 ▲ 0.0071
 Euro 1.1922 ▼ -0.0026
 15 minute delay | Terms and Conditions

Sci & Environment Edit x
 India aims for tidal power first
 about 6 hours ago
 • Galileo price rises 1.9bn euros
 • Sharks are probably colour-blind

Entertainment Edit x
 King's Speech leads Bafta field
 about 6 hours ago
 • Apple shares drop on Jobs' health
 • TV giant looms with NBC clearance
 • Boeing postpones Dreamliner again
 • Russian bank staff investigated
 • UK inflation rate rises to 3.7%

World Service Edit x
NEWS IN 32 LANGUAGES
 العربية, Urdu, اردو, 中文, हिन्दी, Somali, Русский, Brasil, Mundo
[More languages](#)

TV Channels x
 BBC World News, BBC America, BBC Canada, BBC Kids (Canada), BBC Entertainment, Animal Planet, People+Arts, UKTV Australia

PC



BBC News
 China's Hu arrives for US visit
 Duvalier taken to court in Haiti
 Tunisia leaders quit ruling party
[More from BBC News](#)

BBC Sport
 Live - Tuesday football
 Villa confirm record Bent signing
[More from BBC Sport](#)

BBC World Service
 Inside the IMF
 The King's Speech: A stammerer's perspective
 Hourly news bulletin
[More audio from BBC World Service](#)

Weather
 Find 5 day forecast

Languages
 Spanish
[News in more languages](#)

From BBC Mobile UK
 • Television
 • Radio & Music
 • Entertainment
 • BBC Children
 • Learning
 • Lifestyle
 • Food

Top
[FAQ](#)

iPhone

Page Layout



Simple Media Retargeting Operators

Scaling
Leads



Content-aware Retargeting Operators

Content-
aware



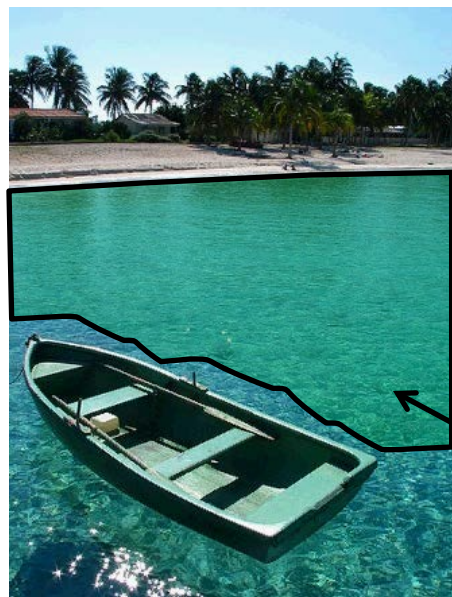
“Important”
content



Content-
oblivious



Content-aware Retargeting



Input



Scale



Crop



Content-aware

“less-Important”
content



Image Retargeting

- **Problem statement:**
 - Input Image I $n \times m$, and new size $n' \times m'$
 - Output Image I' of size $n' \times m'$ which will be “good representative” of the original image I
- **To date, no agreed definition, or measure, as to what a good representative is in this context!**

Image/Video Retargeting

- **In large, we would expect:**

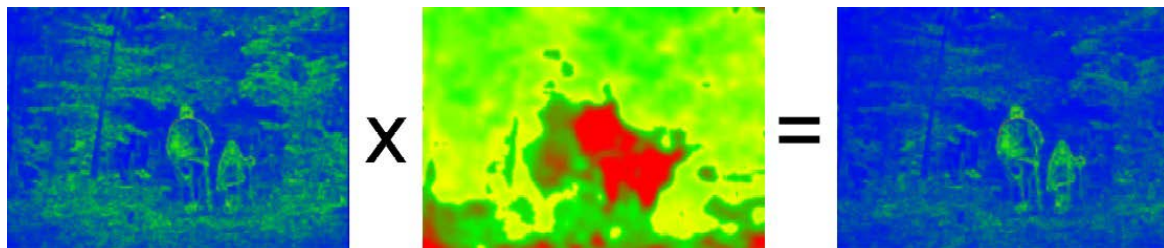
1. Adhere to the **geometric constraints** (display/aspect ratio)
2. Preserve the **important *content*** and *structures*
3. **Limit *artifacts***
4. Perhaps a new representation that will support different sizes?

- **Very Ill-posed!**

- How do we define important? Is there a universal ground truth?
- Would different viewers think the same about a retargeted image?
- What about artistic impression in the original content?

Importance (Saliency) Measures

- A function $S: p \rightarrow [0,1]$



Wang et al. 2008

- More sophisticated: attention models, eye tracking (gazing studies), face detectors, ...

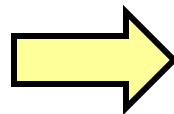


Judd et al. ICCV09 *Learning to predict where people look*

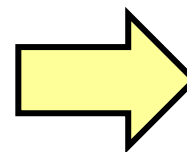
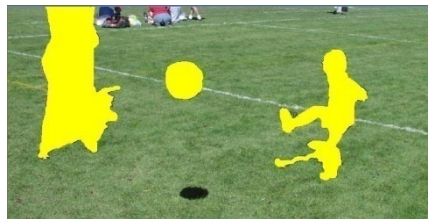
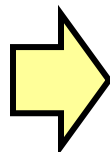


General Retargeting Framework

1. Define an energy function $E(I)$
(interest, importance, saliency)

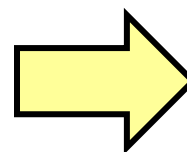
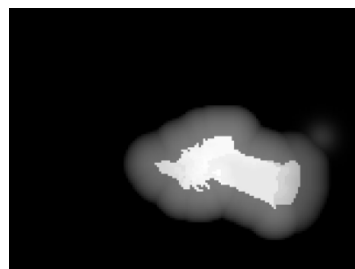
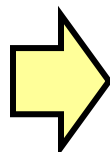


2. Use some operator(s) to
change the image I



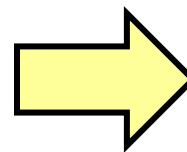
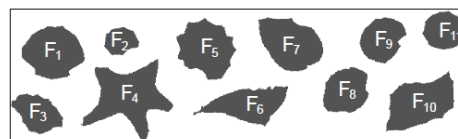
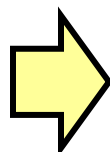
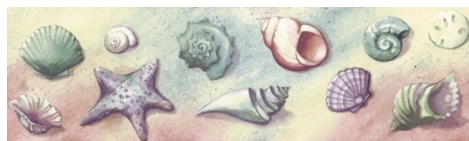
Recompose

Setlur et al.
[2005]



Crop

Santella et al.
[2005]



Warp

Gal et al.
[2006]

Previous Retargeting Approaches

- **Optimal Cropping Window**



- **For videos: “Pan and scan”**

Still done manually in the movie industry



Liu and Gleicher, **Video Retargeting: Automating Pan and Scan** (2006)

Cropping



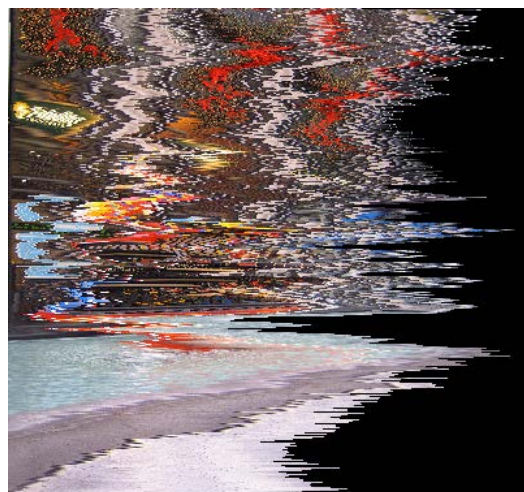
Seam Carving

- Assume $m \times n \rightarrow m \times n'$, $n' < n$ (summarization)
- **Basic Idea: remove unimportant pixels from the image**
 - Unimportant = pixels with less “energy”

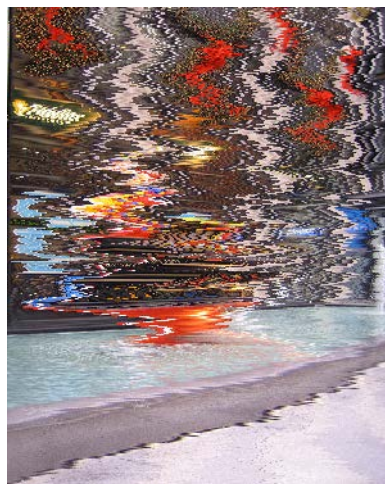
$$E_1(\mathbf{I}) = \left| \frac{\partial}{\partial x} \mathbf{I} \right| + \left| \frac{\partial}{\partial y} \mathbf{I} \right|.$$

- **Intuition for gradient-based energy:**
 - Preserve strong contours
 - Human vision more sensitive to edges – so try remove content from smoother areas
 - Simple, enough for producing some nice results
 - See their paper for more measures they have used

Pixel Removal



Optimal



Least-energy pixels
(per row)



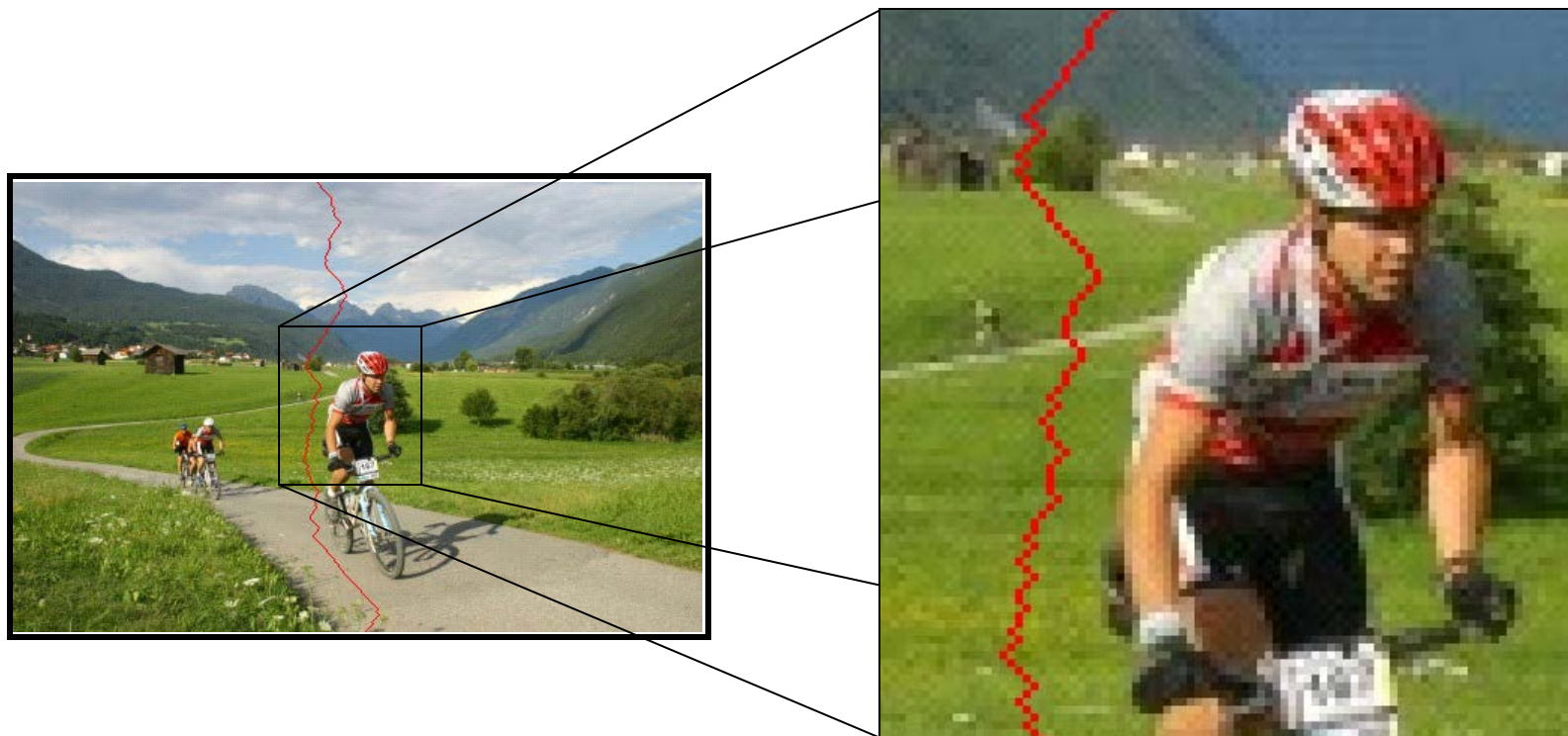
Least-energy columns

A Seam

- A connected path of pixels from top to bottom (or left to right). Exactly one in each row

$$s^x = \{s_i^x\}_{i=1}^n = \{(x(i), i)\}_{i=1}^n, \text{ s.t. } \forall i, |x(i) - x(i-1)| \leq 1$$

$$s^y = \{s_j^y\}_{j=1}^m = \{(j, y(j))\}_{j=1}^m, \text{ s.t. } \forall j, |y(j) - y(j-1)| \leq 1$$



Seams in Images

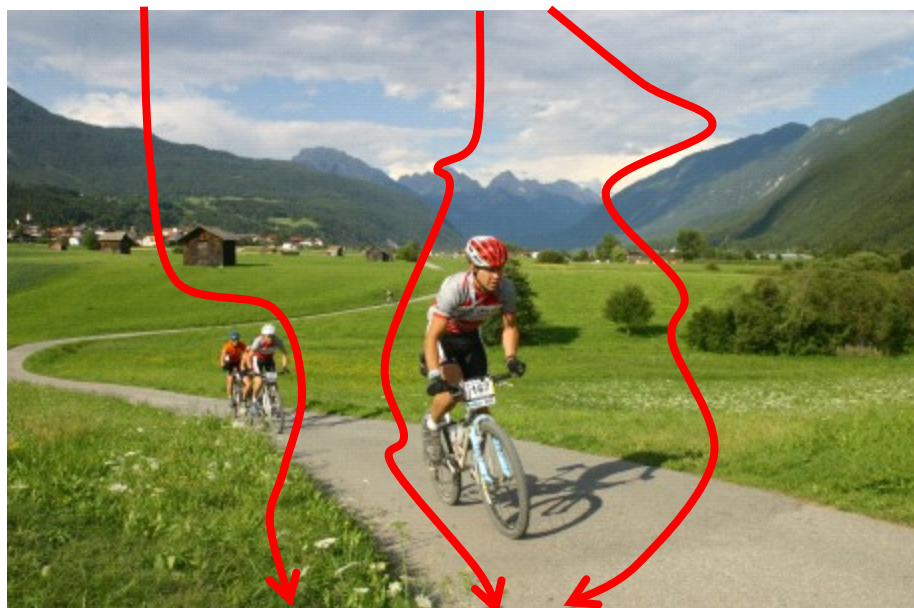
- Efros & Freeman [2001] – Texture synthesis
- Kwatra et al. [2003] – Image and video synthesis
- Agarwala et al. [2004] – Digital Photomontage
- Perez et al.
- Jia et al.
- Rother et al.
- Wang and Cohen [2006] – simultaneous matting and compositing

Mostly used for composition of two (or more) images or patches...

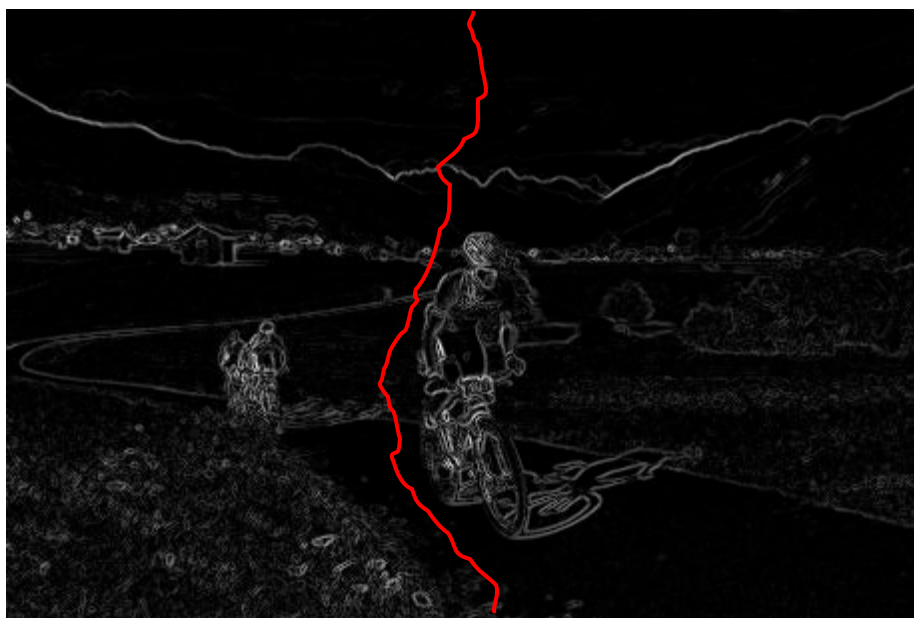


Agarwala et al., *Interactive Digital Photomontage*

Finding the Seam?



The Optimal Seam



$$E(\mathbf{I}) = \left| \frac{\partial}{\partial x} \mathbf{I} \right| + \left| \frac{\partial}{\partial y} \mathbf{I} \right| \Rightarrow s^* = \arg \min_s E(s)$$



The Optimal Seam

- **The recursion relation**

$$\mathbf{M}(i, j) = E(i, j) + \min(\mathbf{M}(i-1, j-1), \mathbf{M}(i-1, j), \mathbf{M}(i-1, j+1))$$

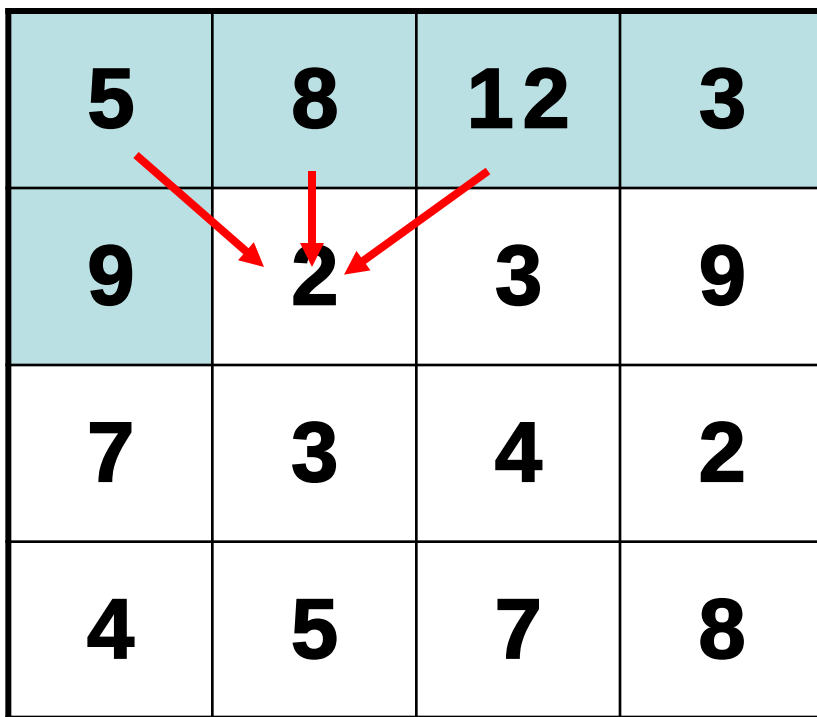
- **Can be solved efficiently using dynamic programming in**
 $O(s \cdot n \cdot m)$
($s=3$ in the original algorithm)

Dynamic Programming

- **Invariant property:**

- $M(i,j)$ = minimal cost of a seam going through (i,j) (satisfying the seam properties)

5	8	12	3
9	2	3	9
7	3	4	2
4	5	7	8

A 4x4 grid of numbers. The first row is highlighted in light blue. Red arrows indicate a path starting from the cell (0,0) with value 5, moving down-right to (1,1) with value 2, and then down-left to (1,2) with value 3.

Dynamic Programming

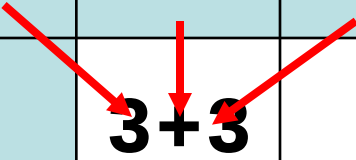
$$\mathbf{M}(i, j) = E(i, j) + \min(\mathbf{M}(i-1, j-1), \mathbf{M}(i-1, j), \mathbf{M}(i-1, j+1))$$

5	8	12	3
9	2+5	3	9
7	3	4	2
4	5	7	8

Dynamic Programming

$$\mathbf{M}(i, j) = E(i, j) + \min(\mathbf{M}(i-1, j-1), \mathbf{M}(i-1, j), \mathbf{M}(i-1, j+1))$$

5	8	12	3
9	7	3+3	9
7	3	4	2
4	5	7	8



Dynamic Programming

$$\mathbf{M}(i, j) = E(i, j) + \min(\mathbf{M}(i-1, j-1), \mathbf{M}(i-1, j), \mathbf{M}(i-1, j+1))$$

5	8	12	3
9	7	6	12
14	9	10	8
14	14	15	8+8

Searching for Minimum

- **Backtrack** (can store choices along the path, but do not have to)

5	8	12	3
9	7	6	12
14	9	10	8
14	14	15	16



Backtracking the Seam

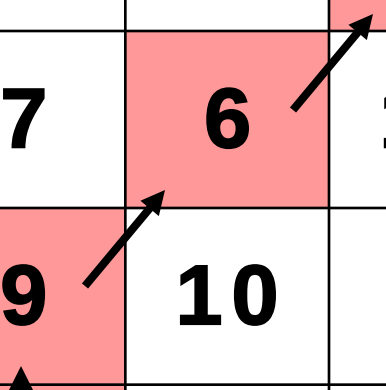
5	8	12	3
9	7	6	12
14	9	10	8
14	14	15	16

Backtracking the Seam

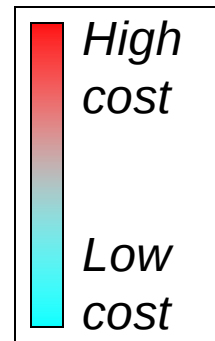
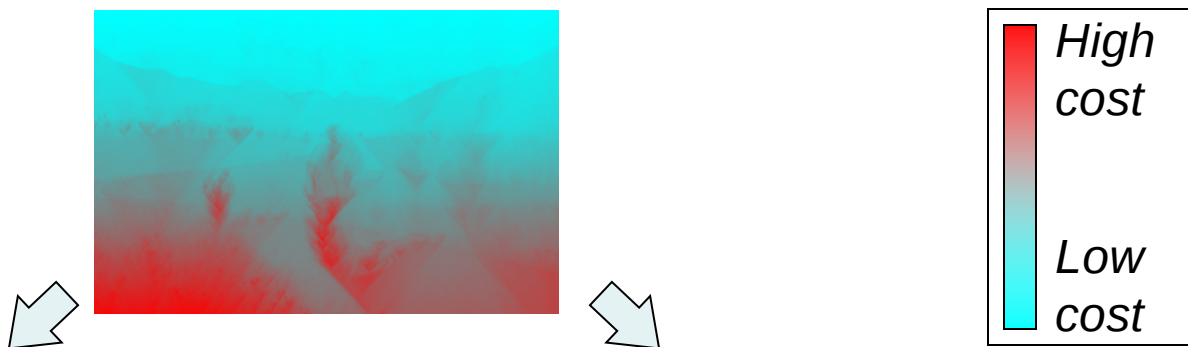
5	8	12	3
9	7	6	12
14	9	10	8
14	14	15	16

Backtracking the Seam

5	8	12	3
9	7	6	12
14	9	10	8
14	14	15	16

Three black arrows indicate the backtracking path from the top-right cell (3) to the bottom-left cell (14). The arrows point from (3) to (6), from (6) to (9), and from (9) to (14).

H & V Cost Maps



Horizontal Cost

Vertical Cost

Seam Carving



The Seam-Carving Algorithm

SEAM-CARVING(im,n') // size(im) = n

1. Do (n-n') times

- 2.1. $E \leftarrow$ Compute energy map on im
- 2.2. $s \leftarrow$ Find optimal seam in E
- 2.3. im $\leftarrow$ Remove s from im

2. Return im

- For vertical resize: transpose the image

- Running time:

2.1 $O(mn)$ 2.2 $O(mn)$ 2.3 $O(mn)$

$\rightarrow O(dmn)$ $d=n-n'$

```

1 function [J,S,out] = seamShrink(J,wnew,W,p)
2
3 M = rgb2gray(J);
4
5 S = zeros(size(J,1),size(J,2));
6 n = size(J,2)-wnew;
7 energy = zeros(1,n);
8 xp = zeros(size(J,1),n);
9 for i=1:n
10     fprintf(1,'Seam %d (%d)\n',i,n);
11
12     [xpath,cost] = p.seamFunc(M,W,p);
13     normEnergy = cost;%E(end,xpath(end))/length(xpath);
14     xp(:,i) = xpath;
15     energy(i) = normEnergy;
16
17     if (p.verbose >= 2)
18         T = seamOverlay(J,xpath);
19         imwrite(T,sprintf('seam%d.4d.png',i));
20     end
21
22     % update
23     J = seamRemoveCFF(J,xpath); % remove seam from original image
24     M = seamRemoveCFF(M,xpath); % remove seam from work image
25     W = seamRemoveCFF(W,xpath); % remove seam from weights
26     S = updateSurvivalImage(S,xpath,normEnergy);
27
28 end;
29
30 out.xp = xp;
31 out.energy = energy;
32

```

Changing Aspect Ratio



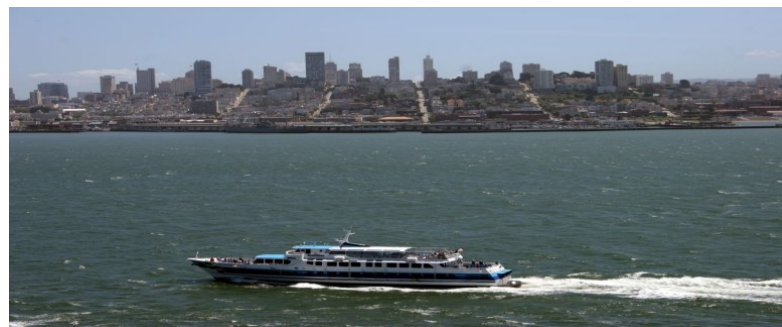
Changing Aspect Ratio



Original



Seam Carving



Scaling

Changing Aspect ratio



Cropping



Seams



Scaling

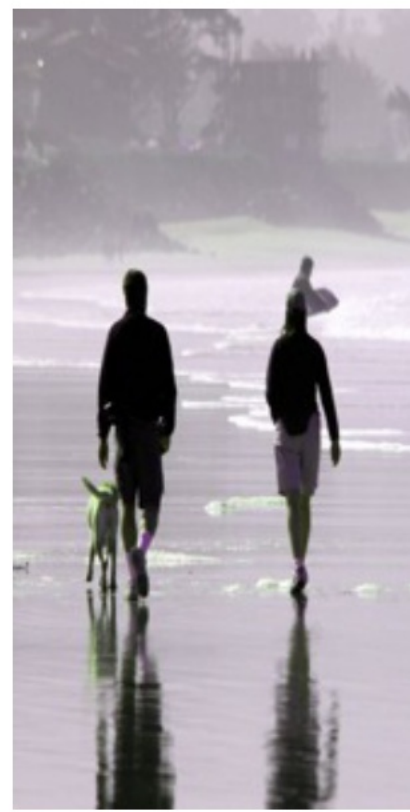
Changing Aspect Ratio



Original



Retarget



Scaling

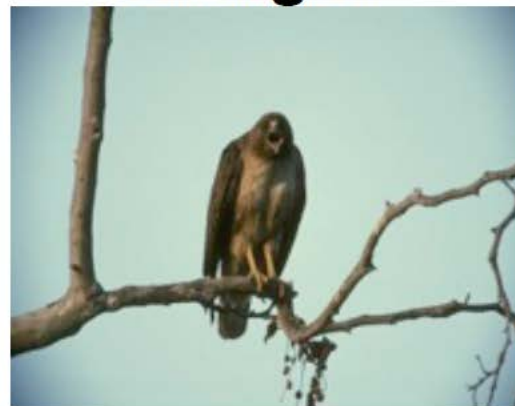
Changing Aspect Ratio



Original



Retarget

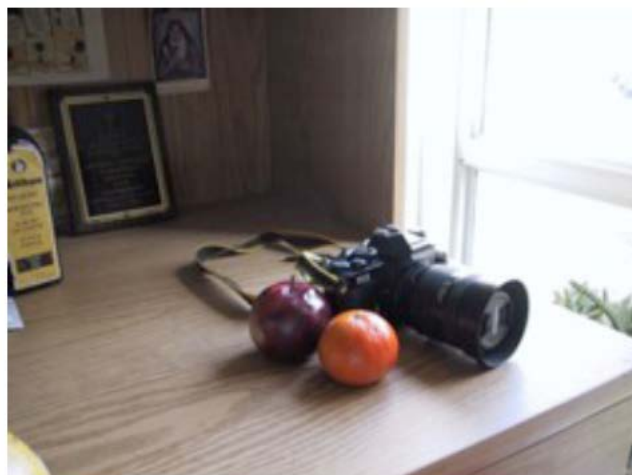


Scaling

Content Enhancement



Seam Carving in the Gradient Domain





Questions?

- **Q: Will the result be the same if the image is flipped upside down?**
- **A: Yes (up to numerical stability)**

- **Q: Can we improve the running time?**
- **A: Yes. by factor (account for locality of operations)**

A Local Operator





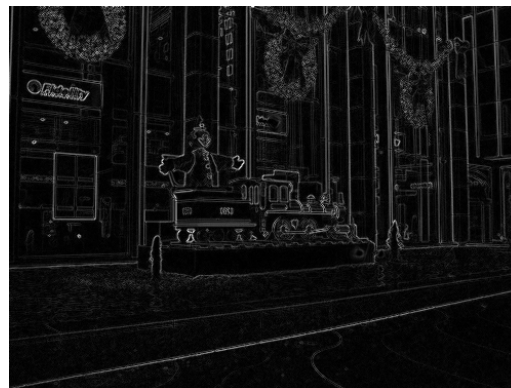
Questions?

- **Q: Will the result be the same if the image is flipped upside down?**
- **A: Yes (up to numerical stability)**

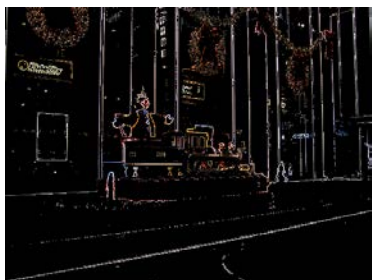
- **Q: Can we improve the running time?**
- **A: By factor (local operations)**

- **Q: What happens to the overall energy in the image during seam carving?**

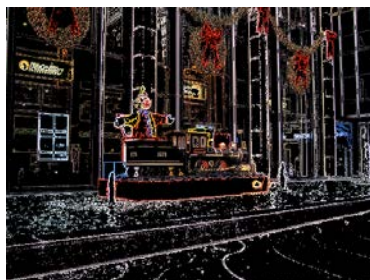
Preserved Energy



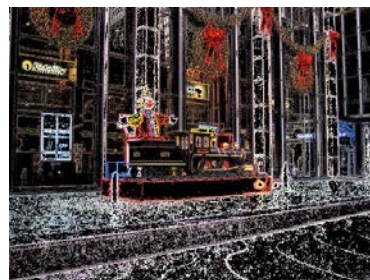
Energy



10%



30%



40%



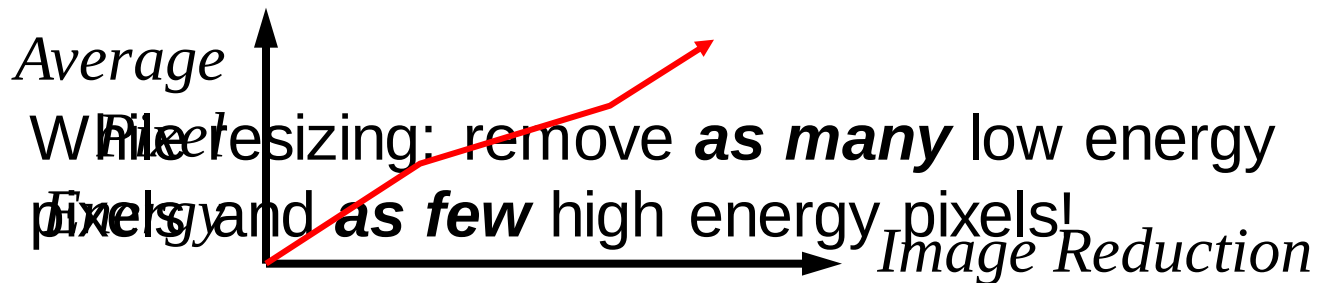
75%

While resizing: remove *as many* low energy pixels and *as few* high energy pixels!

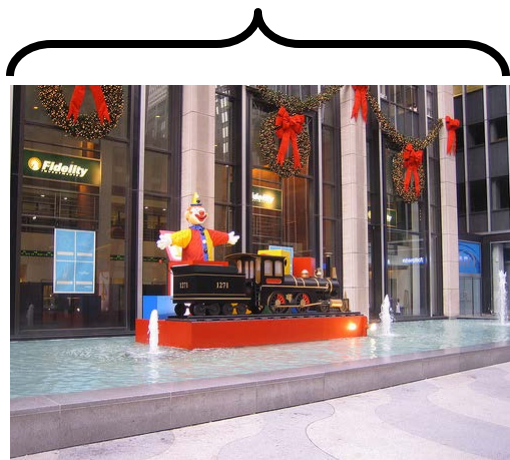
Preserved Energy

If we measure the average energy of pixels in the image after applying a resizing operator...

...the average should increase!



Preserved Energy



Average
Pixel
Energy

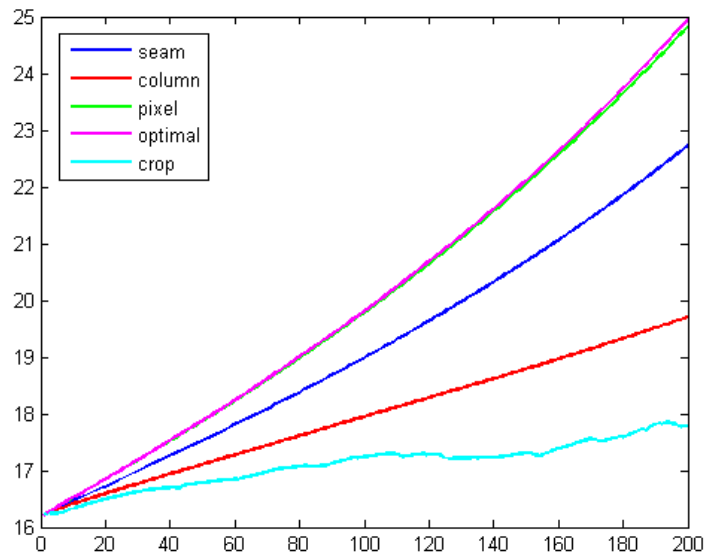


Image Reduction



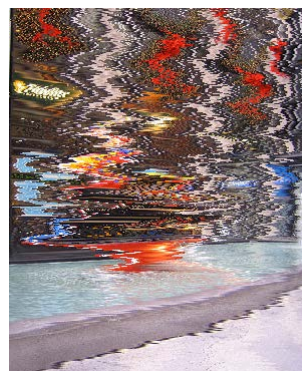
crop



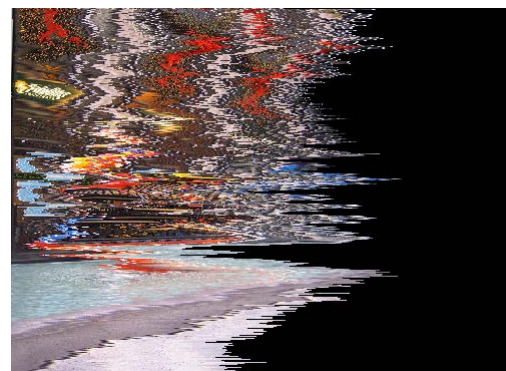
column



seam



pixel



optimal

Both Dimensions?

- $m \times n \rightarrow m' \times n'$
- Remove horizontal seam first?
- Remove vertical seams first?
- Alternate between the two?
- The optimal order can be found! $\rightarrow$ Dynamic Prog (again)



Retargeting in Both Dimensions

- The recursion relation:

$$\mathbf{T}(r, c) = \min(\mathbf{T}(r-1, c) + E(\mathbf{s}^x(\mathbf{I}_{n-r-1 \times m-c})), \mathbf{T}(r, c-1) + E(\mathbf{s}^y(\mathbf{I}_{n-r \times m-c-1})))$$

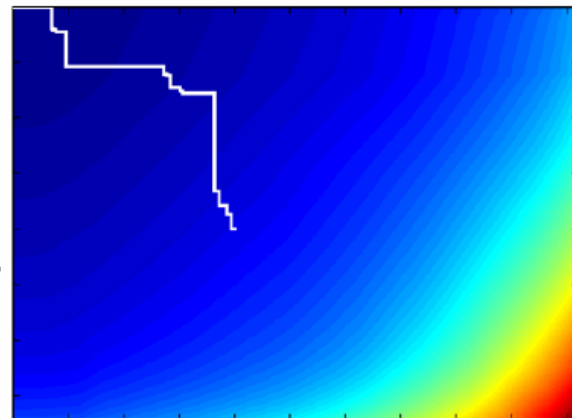


Optimal Order Map

*Removal of **vertical** seams*

*Removal of **vertical** seams*

*Removal of **horizontal** seams*



*Removal of **horizontal** seams*

0 ←	13	16	19		
16 ↑	17	22	28		
19 ↑	31	25	35		
24 ↑	28	29	???		
32 ↑	35	33			
41 ↑	38	35			

Optimal?

- In a greedy sense...
- Seam costs are not absolute
 - Consider HVV (how many possibly orderings?)
 - $\text{Cost}(V)$ on HV not necessarily equal $\text{Cost}(V)$ on VH
 - But we keep track of only one: $\min(\text{HV}, \text{VH})$...

Horizontal Seams

Vertical Seams

0	V	VV
H	$\min(\text{HV}, \text{VH})$	?

Image Expansion (Synthesis)

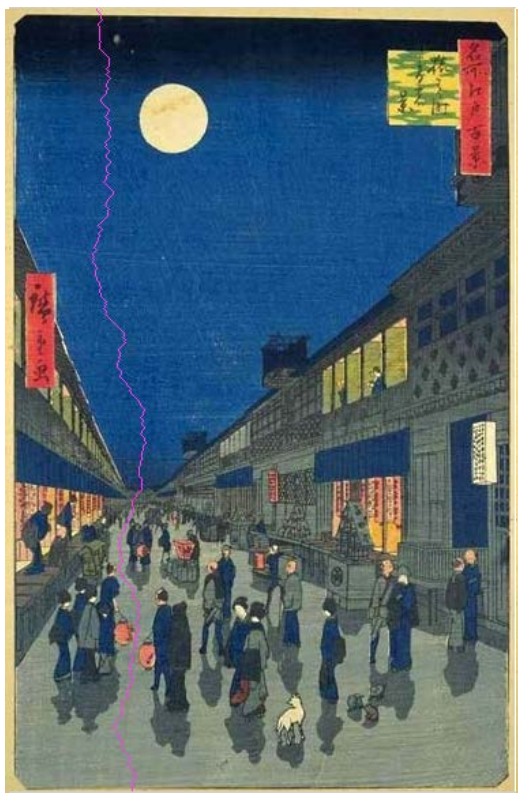
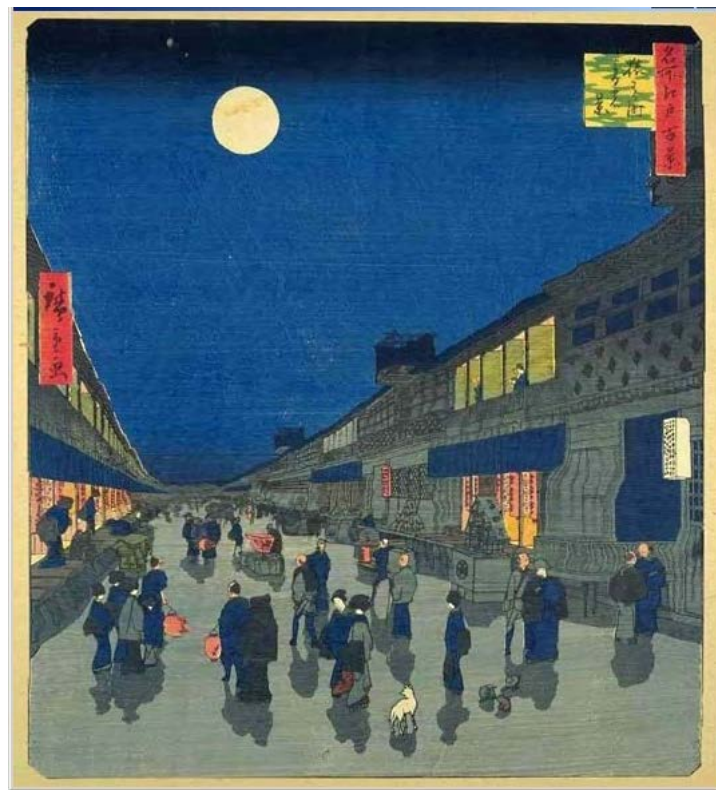


Image Expansion – take 2



Scaling

Enlarged or Reduced?



Combined Insert and Remove



Insert & remove seams



Scaling



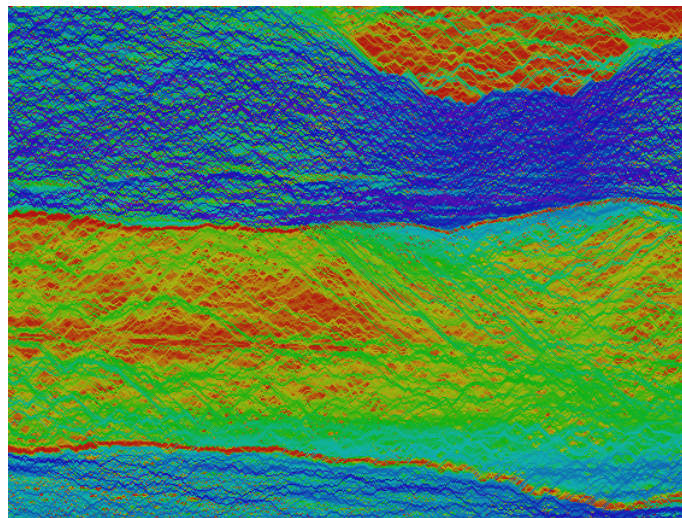
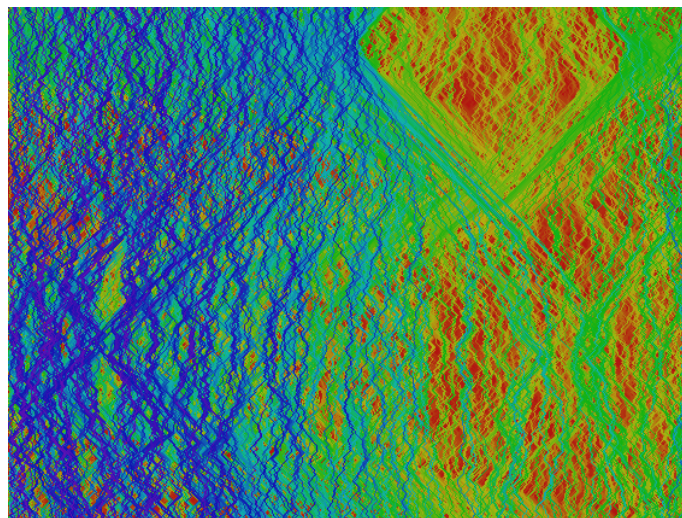
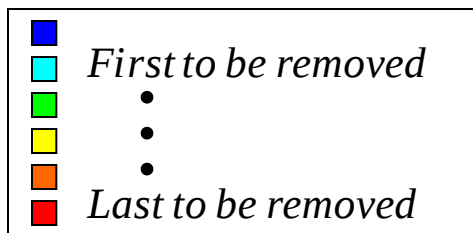
Questions?



Multi-Size Images

- We can create a new representation of an image that will allow adapting it to different sizes!
1. Precompute all seams once
 2. Realtime resizing / transmit with content

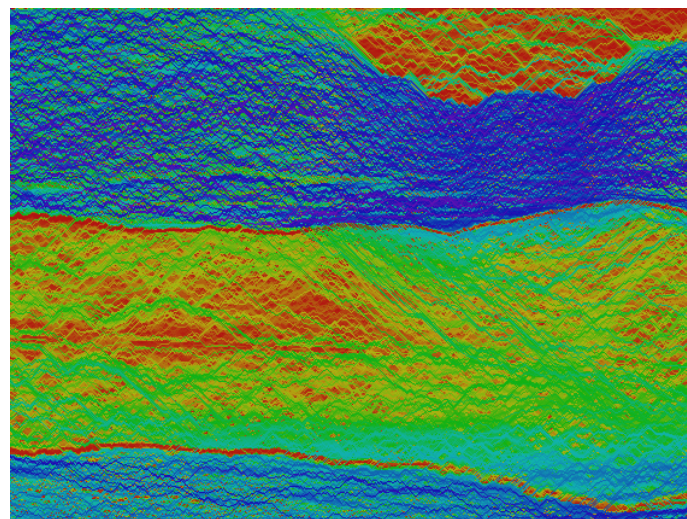
Multi-Size Images



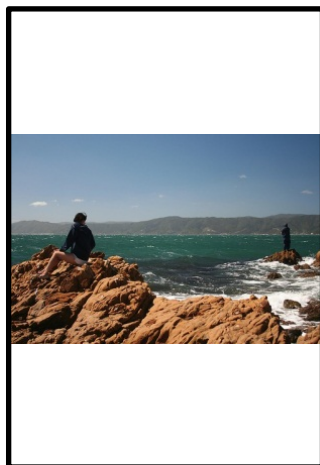
Multi-Size Image Representation



+



Multi-Size Image Representation





2D Multi-Size Representation?

- **Consistent index maps (see appendix in their paper)**
- **Alternatives**
 - Use seams in one direction, row/column seams in the other direction
 - Compute seams in one direction and use them to constrain seams in the other direction
 - **If you can do that you'll have a nice publication 😊**



Auxiliary Energy

- Recall our seam equation

$$\mathbf{M}(i, j) = E(i, j) + \min(\mathbf{M}(i-1, j-1), \mathbf{M}(i-1, j), \mathbf{M}(i-1, j+1))$$

With face detector



With User Constraints



Object Removal



Object Removal



Input



Retargeted



Pigeon Removed



Girl Removed

Find the Missing Shoe!



Solution



Limitations

Content



Structure



Preserved Energy - Revisited



Average
Pixel
Energy

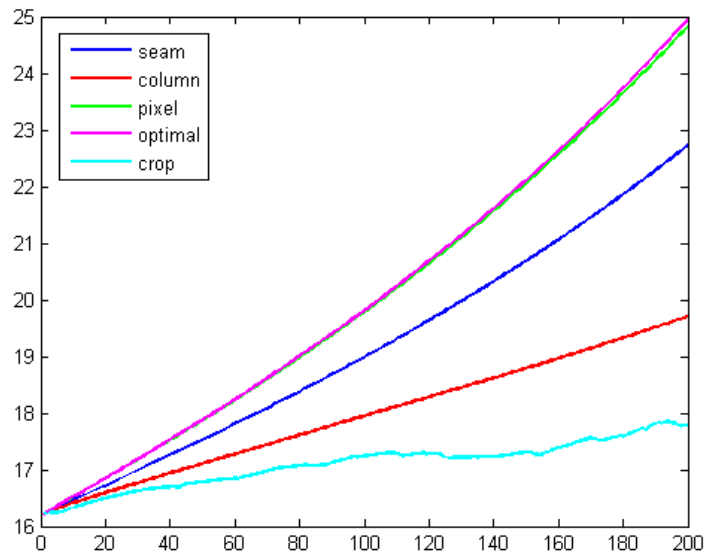


Image Reduction



crop



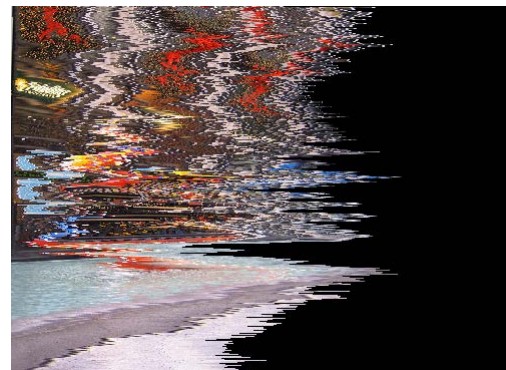
column



seam

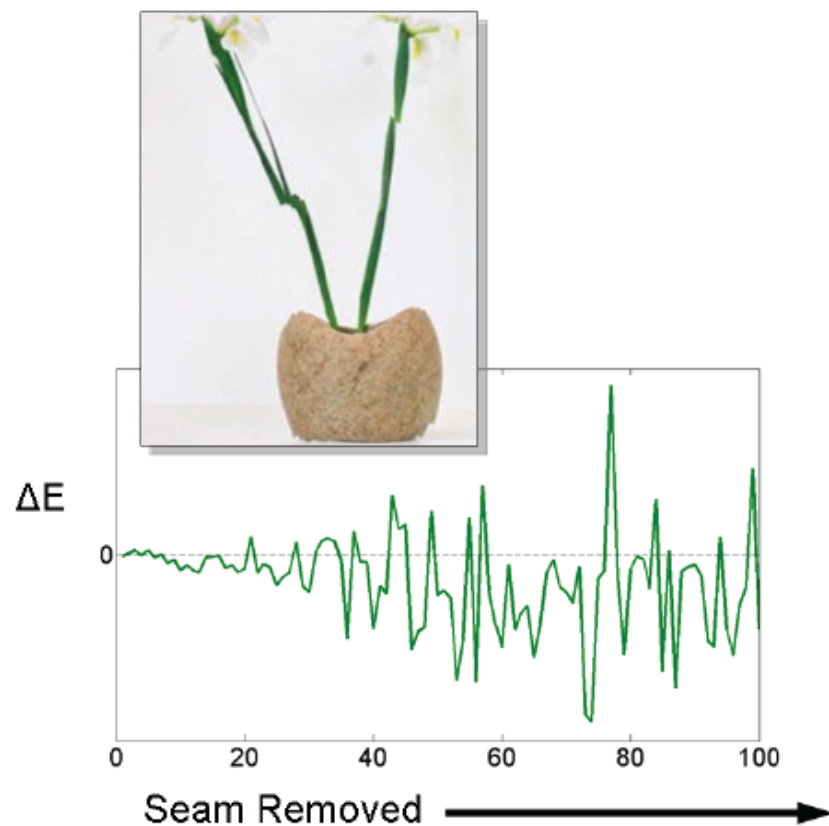
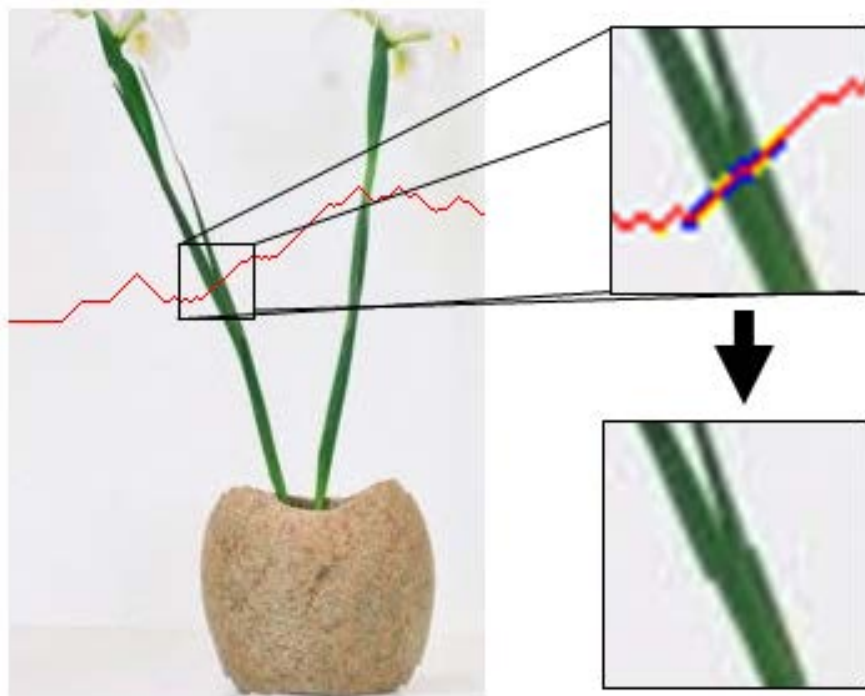


pixel



optimal

Inserted Energy

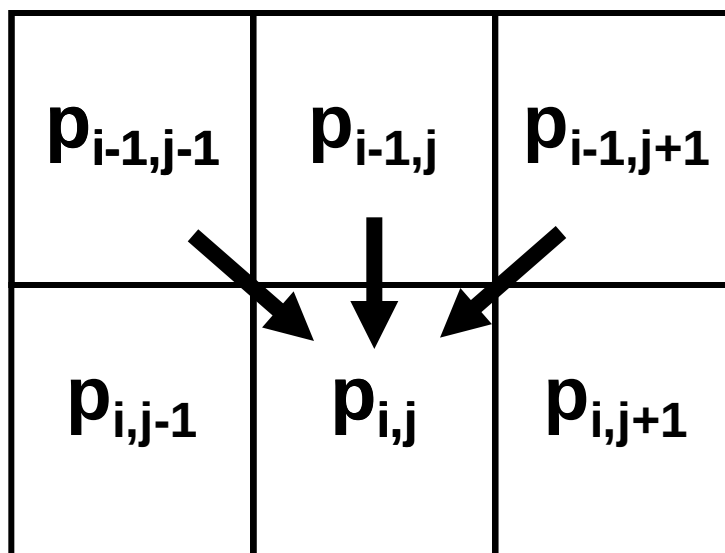




Minimize Inserted Energy

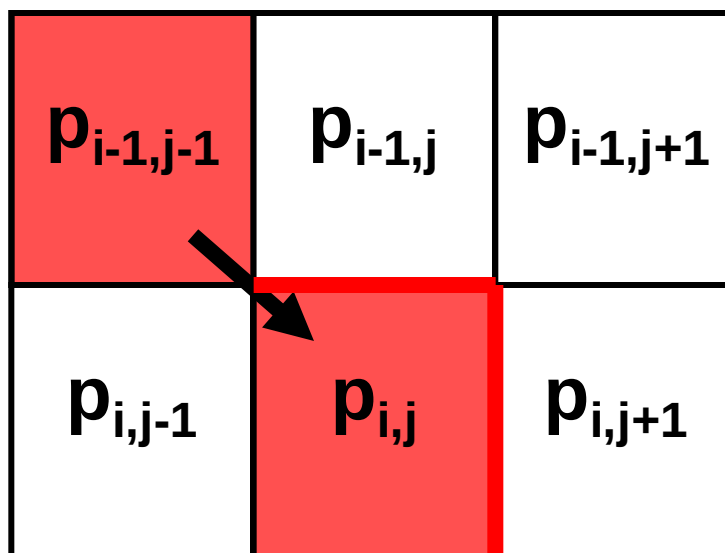
- Instead of removing the seam of least energy, remove the seam that *inserts the least energy* to the image !

Tracking Inserted Energy



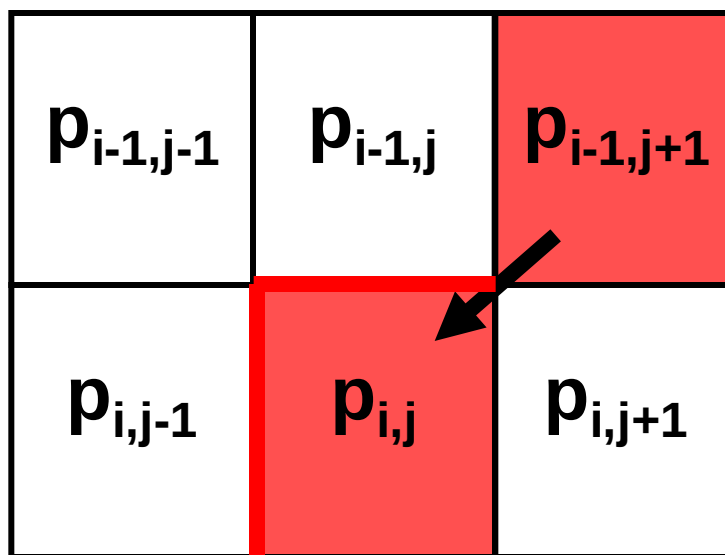
- Three possibilities when removing pixel $P_{i,j}$

Pixel $P_{i,j}$: Left Seam



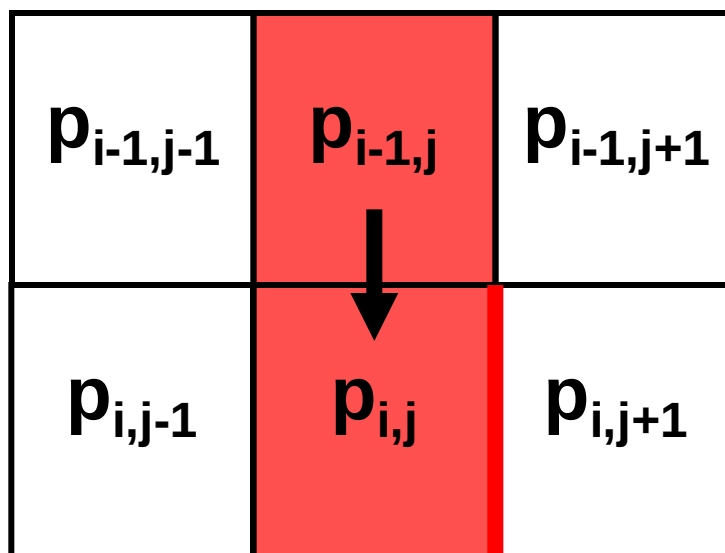
$$C_L(i, j) = |I(i, j + 1) - I(i, j - 1)| + |I(i - 1, j) - I(i, j - 1)|$$

Pixel $P_{i,j}$: Right Seam



$$C_R(i, j) = |I(i, j + 1) - I(i, j - 1)| + |I(i - 1, j) - I(i, j + 1)|$$

Pixel $P_{i,j}$: Vertical Seam



$$C_V(i, j) = |I(i, j + 1) - I(i, j - 1)|$$

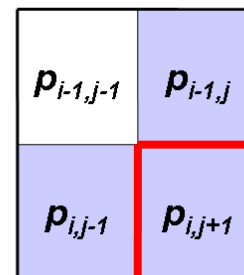
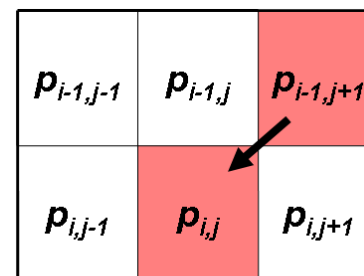
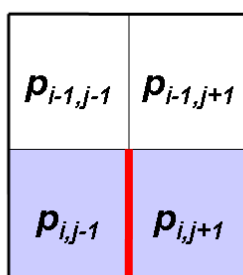
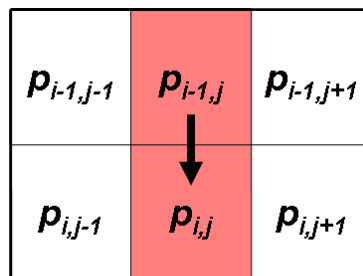
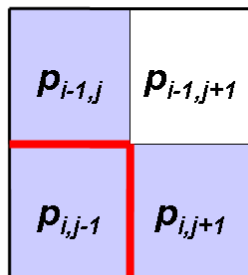
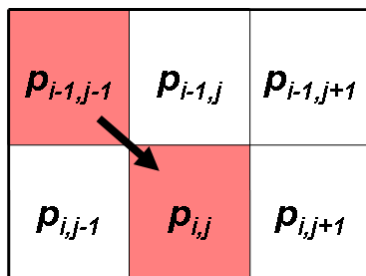


Old “Backward” Energy

$$M(i, j) = E(i, j) + \min \begin{cases} M(i - 1, j - 1) \\ M(i - 1, j) \\ M(i - 1, j + 1) \end{cases}$$

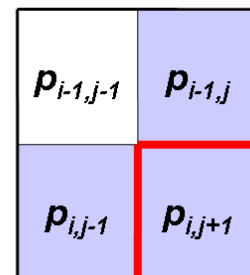
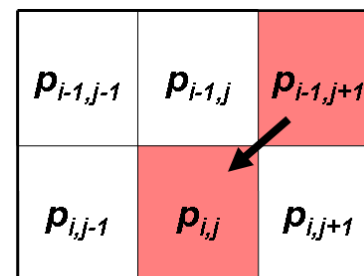
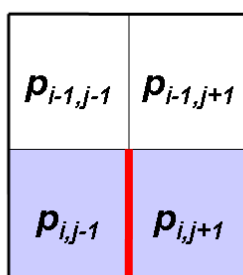
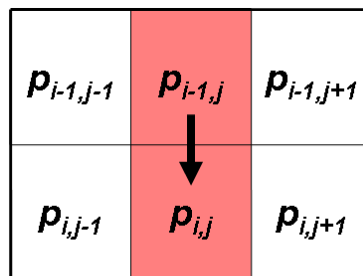
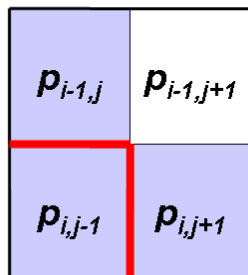
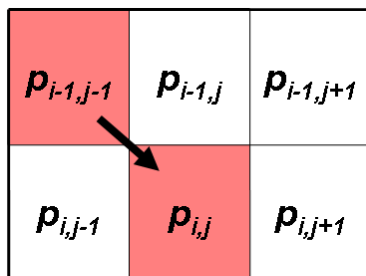
New Forward Looking Energy

$$M(i, j) = \min \begin{cases} M(i-1, j-1) + C_L(i, j) \\ M(i-1, j) + C_U(i, j), \\ M(i-1, j+1) + C_R(i, j) \end{cases}$$



Adding “Pixel Energy”

$$M(i, j) = P(i, j) + \min \begin{cases} M(i-1, j-1) + C_L(i, j) \\ M(i-1, j) + C_U(i, j), \\ M(i-1, j+1) + C_R(i, j) \end{cases}$$



Results



Input



Backward

Forward



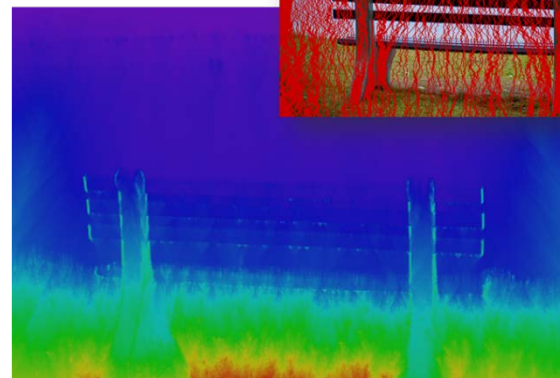
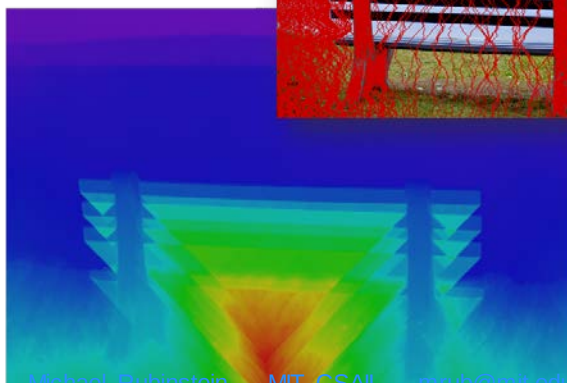
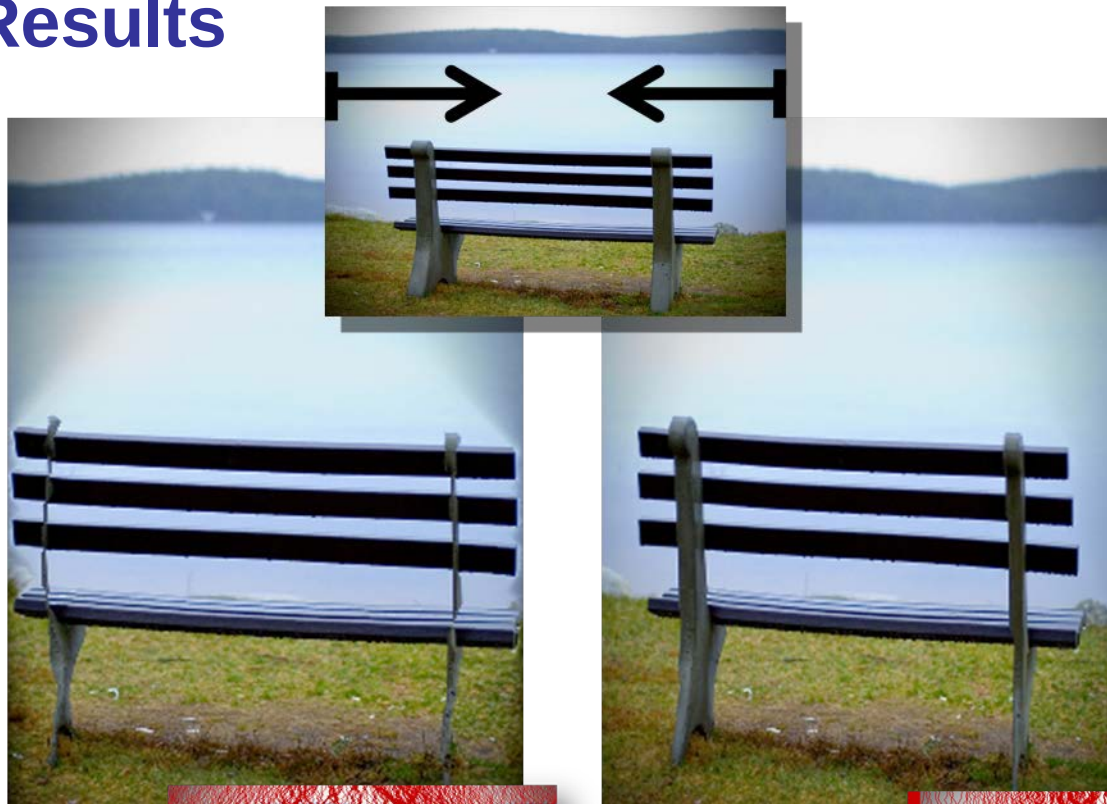
Input

Backward



Forward

Results



Backward vs. Forward

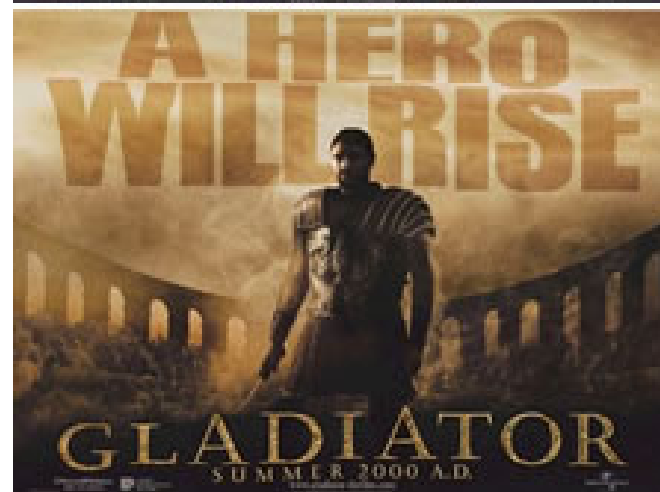
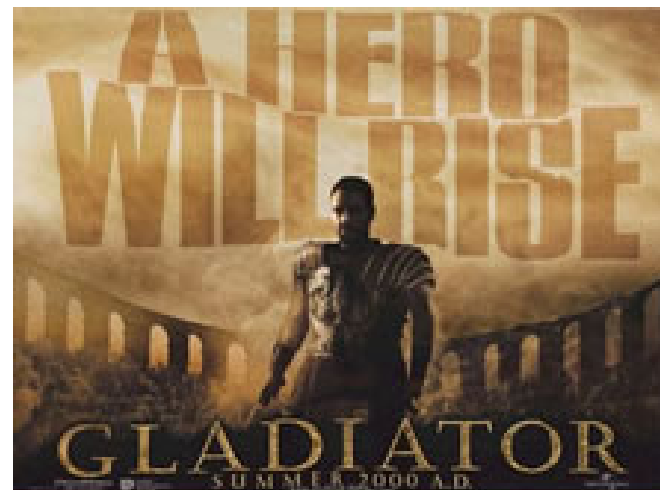
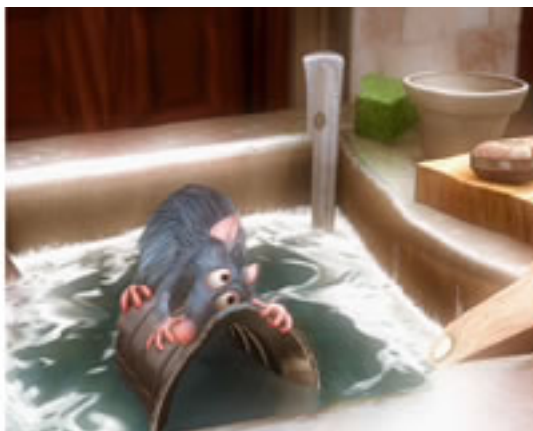


Backward



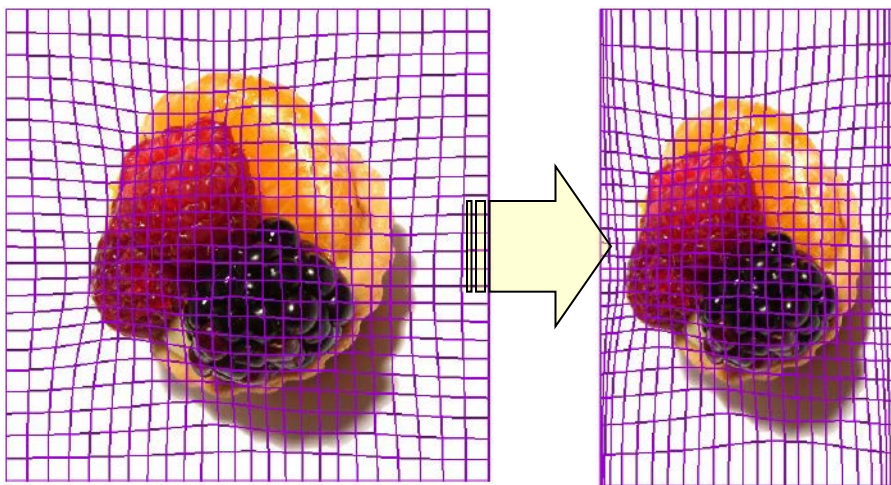
Forward

Results



Discrete vs. Continuous

[Wang et al 2008]



Continuous

[Avidan and Shamir 2007]



Discrete

Non-homogeneous Scaling

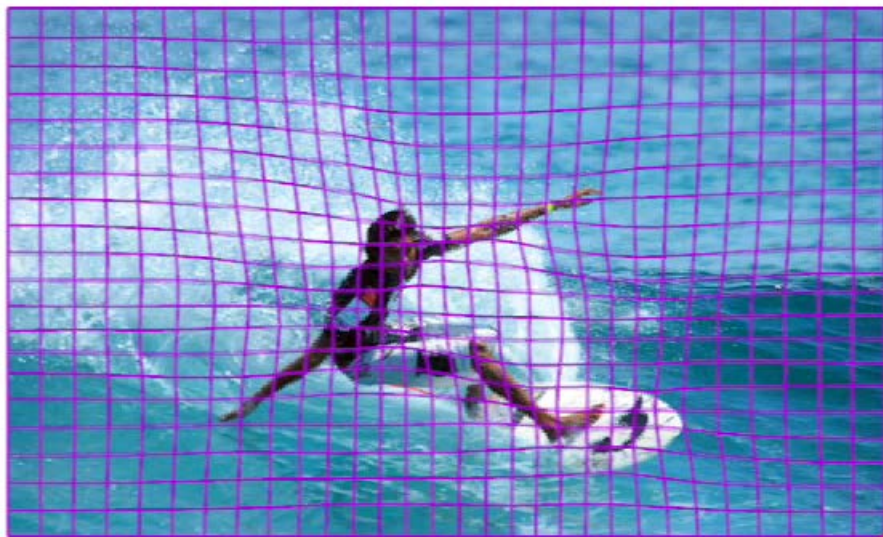


Seam Carving



Scale-and-Stretch

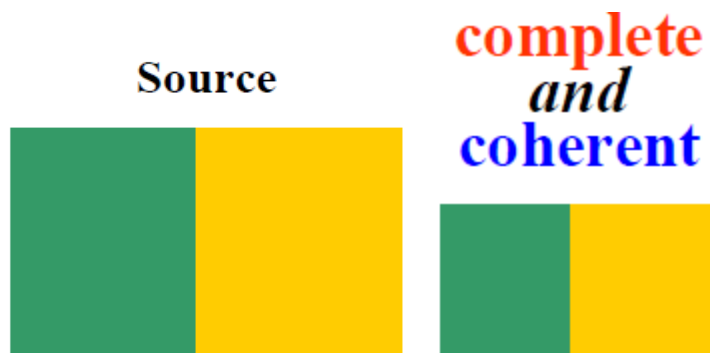
Non-homogeneous Scaling



[Wang et al 2008]

Bidirectional Similarity [Simakov et al. CVPR 08]

$$d(S, T) = \underbrace{\frac{1}{N_S} \sum_{P \subset S} \min_{Q \subset T} D(P, Q)}_{d_{\text{complete}}(S, T)} + \underbrace{\frac{1}{N_T} \sum_{Q \subset T} \min_{P \subset S} D(Q, P)}_{d_{\text{cohere}}(S, T)}$$



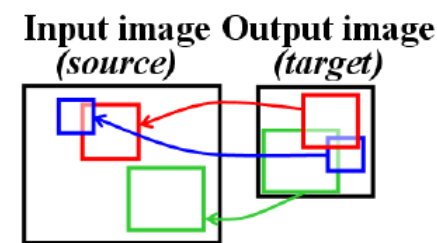
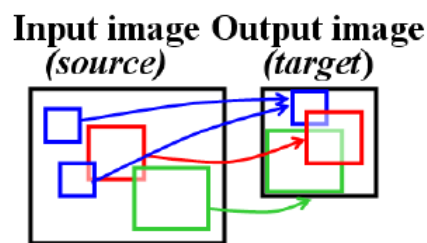
~~complete~~
~~coherent~~ **complete**
~~coherent~~



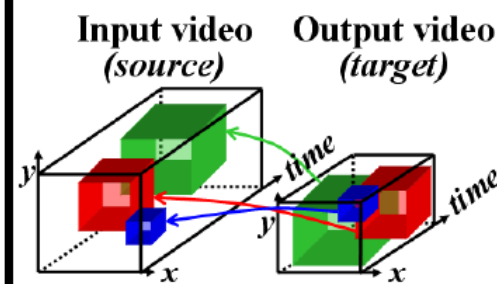
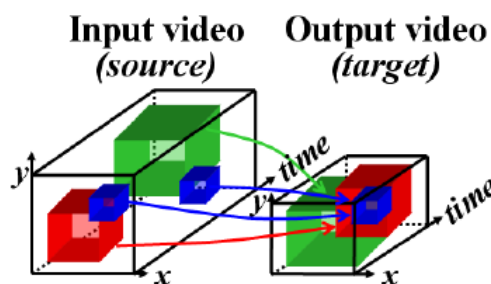
Completeness:

Coherence:

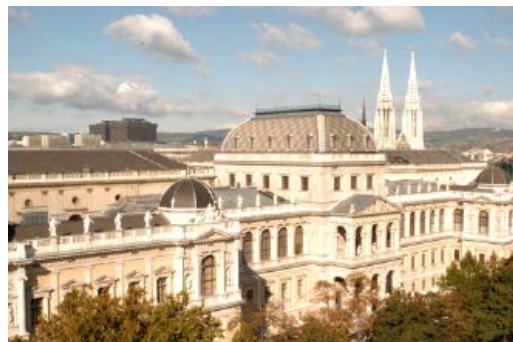
(a) The bidirectional spatial (image) similarity:



(b) The bidirectional space-time (video) similarity:



Bidirectional Similarity





From Images to Videos

- In general, video processing is a much (much!) harder problem

1. Cardinality

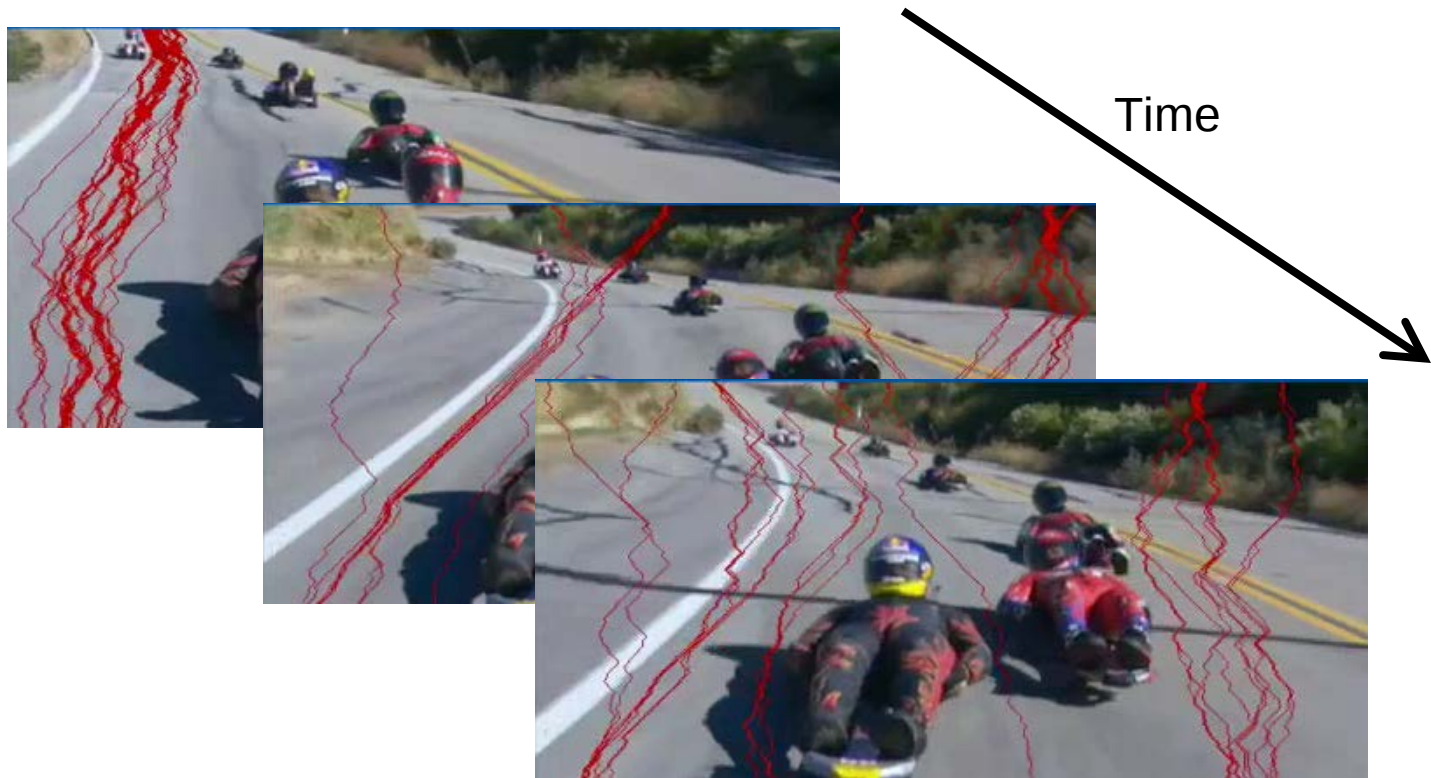
- Suppose 1min of video x 30 fps = 1800 frames
- Say your algorithm processes an image in 1 minute → **30 hours !!**

2. Dimensionality/algorithmic

- Temporal coherency: human visual system is highly sensitive to motion!

Seam-Carving Video?

- Naive... frame by frame independently



Frame-by-frame Seam-Carving

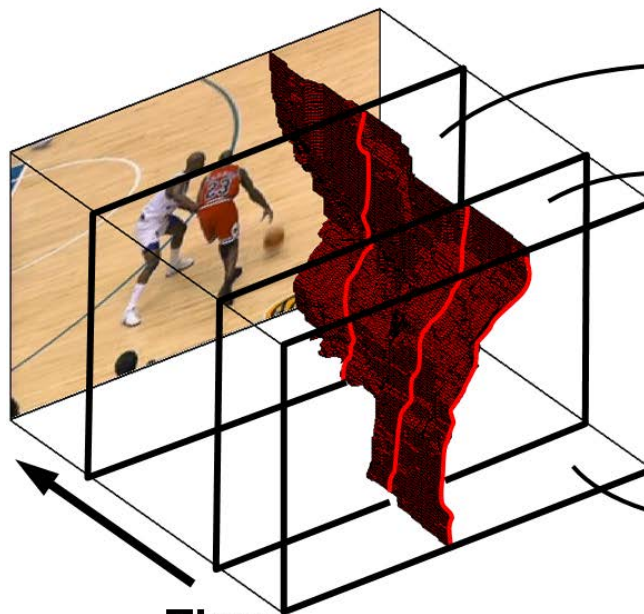
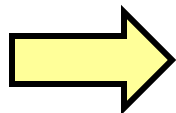


*Representative seams

From 2D to 3D



1D paths in images



Time



2D manifolds in video cubes

Challenges

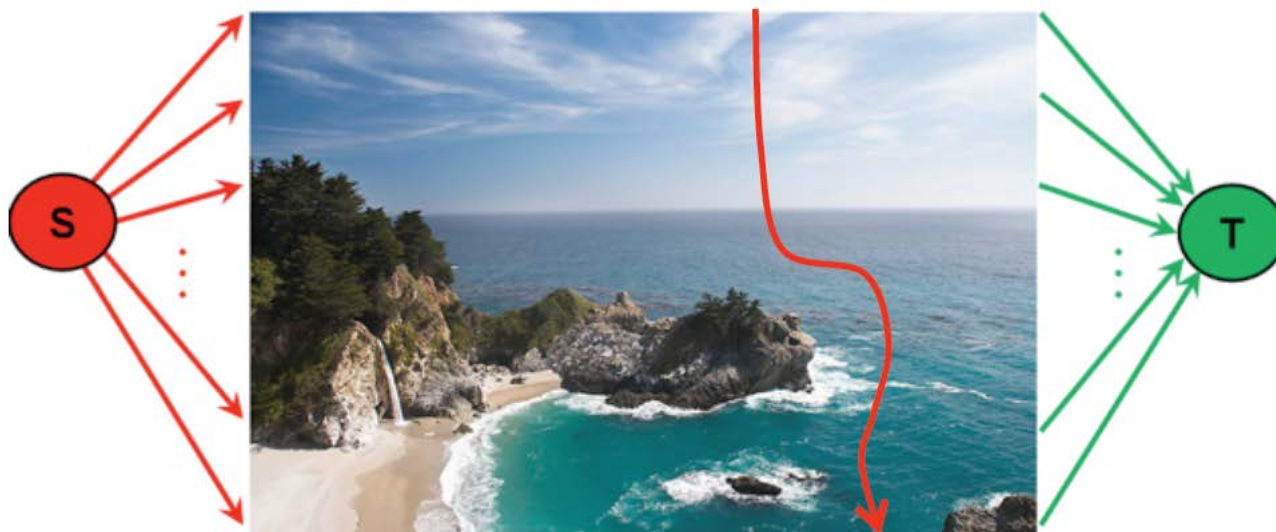
- **Dynamic Programming no longer applicable**

- Reduction to min-cut graph problem

- **Cut must fulfill seam constraints**

1. *Monotonic* (cut each row exactly once)
2. Connected

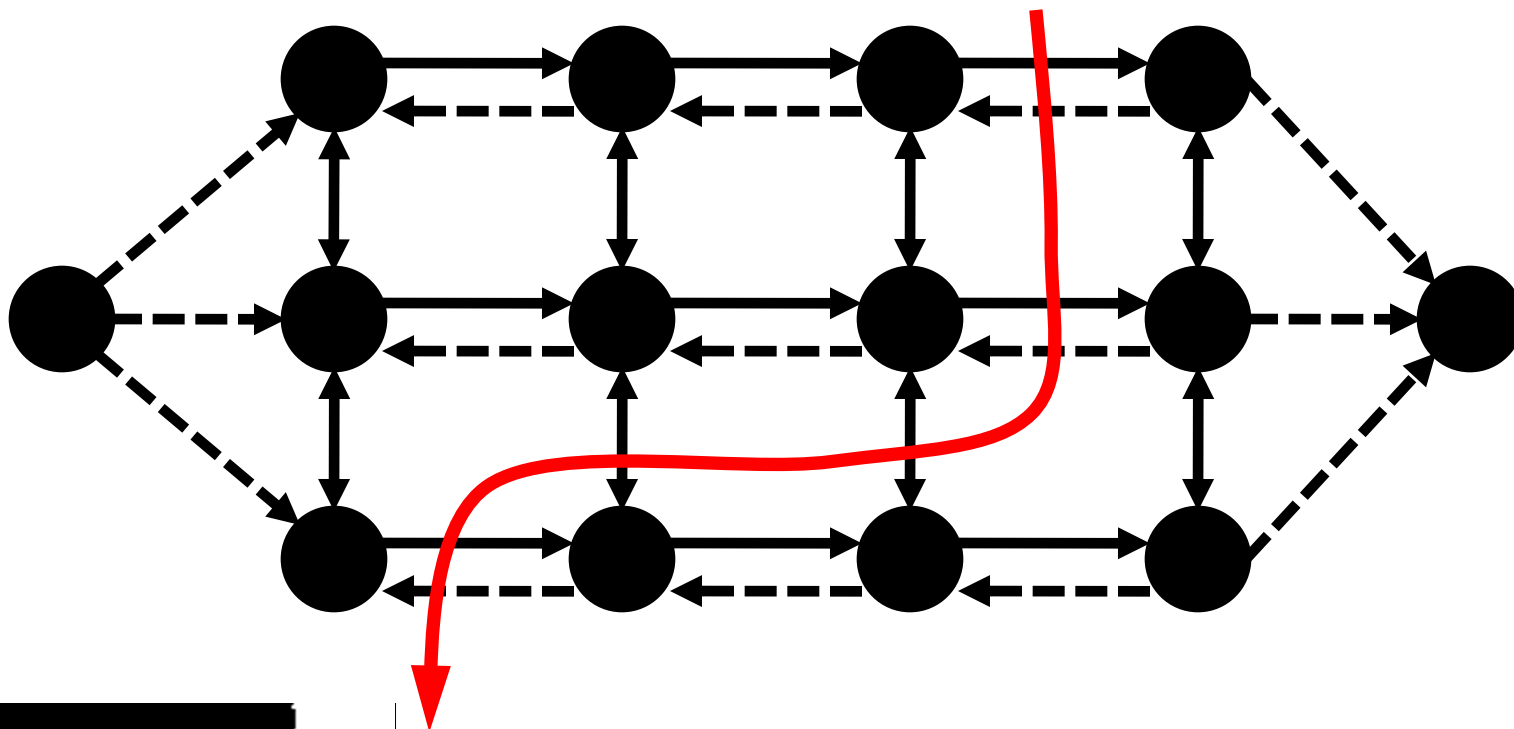
Cut should be a function!





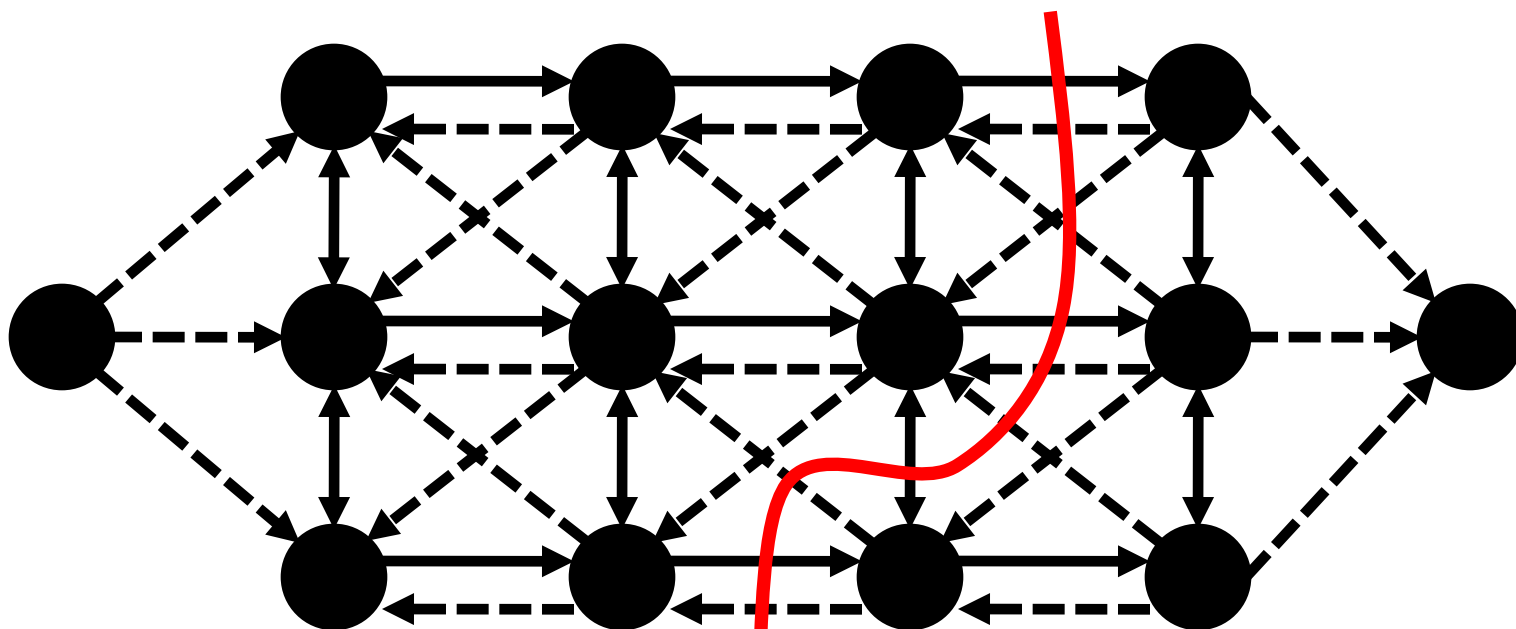
Not monotonic

Graph Construction

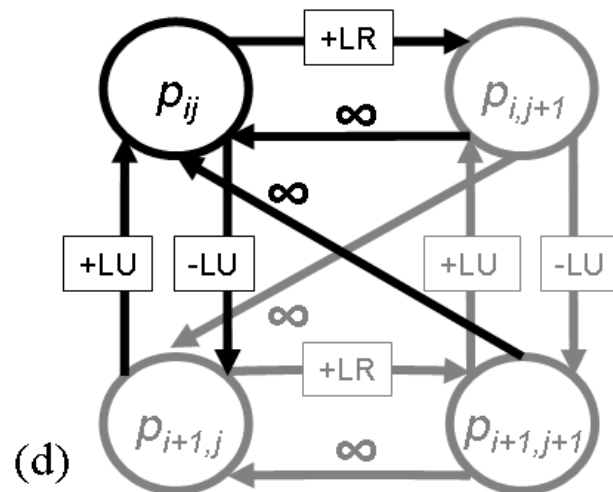


Monotonic, not connected

Graph Construction



Backward
Energy



Multiresolution Graph Cut

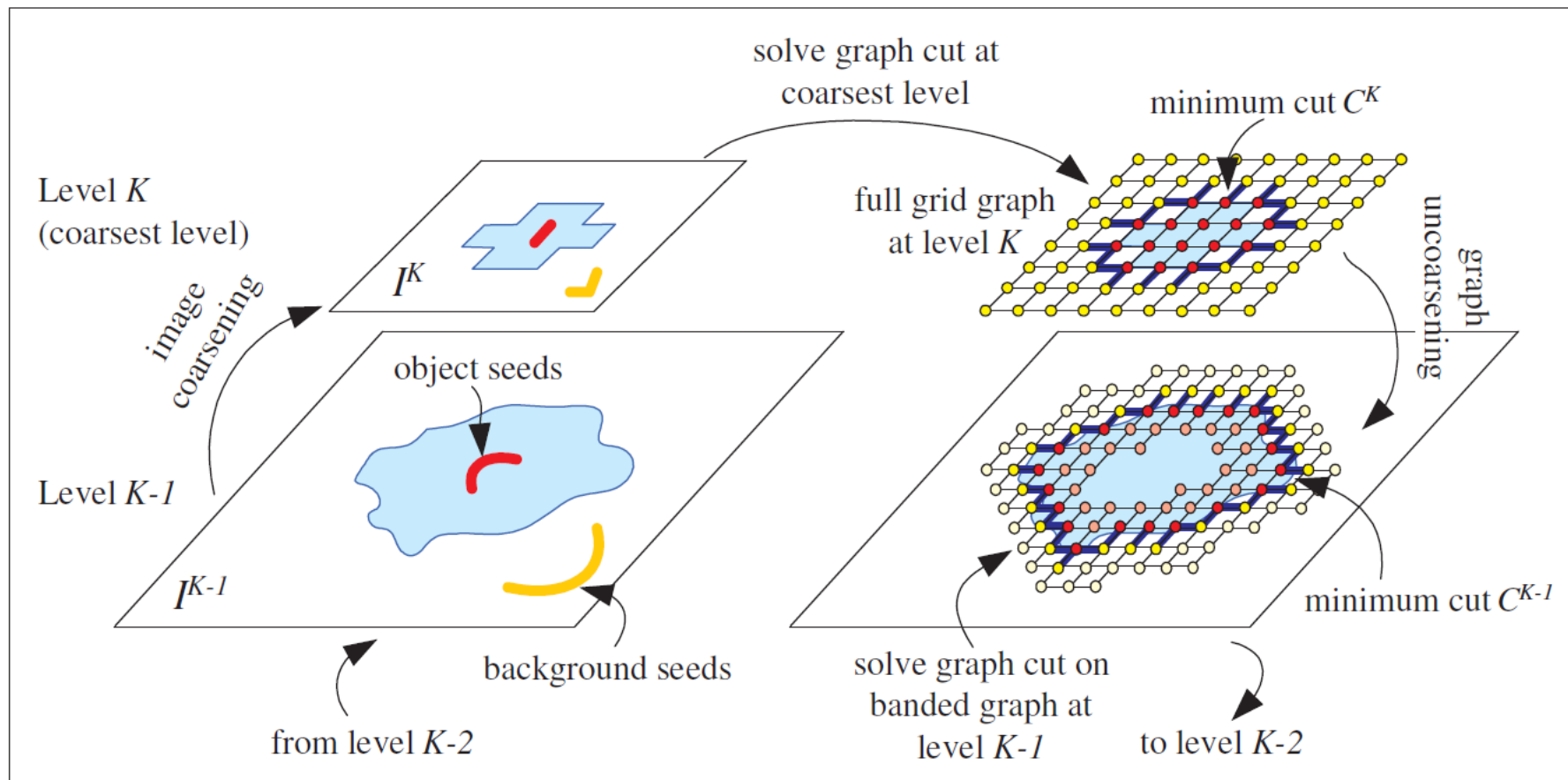


Figure 1. Multilevel banded graph cuts algorithm

Lombaert et al. [2005]

Results

Rescale



Retarget



Results



Seams

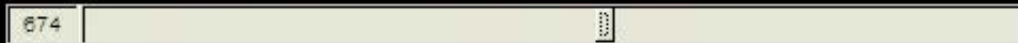


Backward



Forward

Multi-size Video



Object Removal...





References

- **Seam Carving for Content-Aware Image Resizing – Avidan and Shamir 2007**
- **Content-driven Video Retargeting – Wolf et al. 2007**
- **Improved Seam Carving for Video Retargeting – Rubinstein et al. 2008**
- ***Optimized Scale-and-Stretch* for Image Resizing – Wang et al. 2008**
- **Summarizing Visual Data Using Bidirectional Similarity – Simakov et al. 2008**
- **Multi-operator Media Retargeting – Rubinstein et al. 2009**
- **Shift-Map Image Editing – Pritch et al. 2009**
- **Energy-Based Image Deformation – Karni et al. 2009**

- **Seam carving in Photoshop CS4:**
http://help.adobe.com/en_US/Photoshop/11.0/WS6F81C45F-2AC0-4685-8FFD-DBA374BF21CD.html

References

RetargetMe A Benchmark for Image Retargeting

[Michael Rubinstein](#)

MIT CSAIL

[Diego Gutierrez](#)

Universidad de Zaragoza

[Olga Sorkine](#)

New York University

[Ariel Shamir](#)

The Interdisciplinary Center

