# Optimal Transport Graph Neural Networks

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### **Graph Convolutions and Chemprop Model**



## Property smoothness & robustness of representations



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Molecule embedding distance

Property value distance

### From atom embeddings to molecule embedding



### From atom embeddings to molecule embedding



Green, red and orange sets have the same sum and same average.

#### From atom embeddings to molecule embedding



### **Prototypes Inspired From Functional Groups**

#### Our idea:

- learn a dictionary of structural basis functions that serve to highlight key facets of compounds
- express molecules by relating them to abstract molecular prototypes
- prototypes highlight property values associated with different structural features (e.g. solubility)



#### Prototype 2: Azo-type

### **Prototypes as GCN Embedding Point Clouds**

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#### **Wasserstein Prototypes**





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## Property smoothness: Latent Space for Real Models



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Solubility values in the latent space Left: using sum aggregation; Right: using Wasserstein with prototypes

## Property smoothness: Latent Space for Real Models



#### *Lipophilicity values in the latent space* Left: using sum aggregation; **Right:** using Wasserstein with prototypes

### **Results on Molecular Property Prediction**

	Solubility	Lipophilicity	Inhibitors of human β-secretase 1 (BACE-1)	Blood-brain barrier penetration (permeability)
	ESOL (RMSE) $\downarrow$	Lipo (RMSE) $\downarrow$	$ $ BACE (AUC) $\uparrow$ $ $	BBBP (AUC) $\uparrow$
# graphs / molecules	n = 1128	n = 4199	n = 1512	n = 2039
GNN/Chemprop	$.635 \pm .027$	$.646 \pm .041$	$.865 \pm .013$	$.915\pm.010$
ProtoS-L2	$.611 \pm .034$	$\textbf{.580} \pm \textbf{.016}$	$.865 \pm .010$	$.918 \pm .009$
ProtoW-Dot (no reg.)	$.608 \pm .029$	$.637 \pm .018$	$.867 \pm .014$	$.919 \pm .009$
ProtoW-Dot	$\textbf{.594} \pm \textbf{.031}$	$.629 \pm .015$	$.871 \pm .014$	$.919 \pm .009$
ProtoW-L2 (no reg.)	$.616 \pm .028$	$.615 \pm .025$	$.870 \pm .012$	$.920 \pm .010$
ProtoW-L2	$.605 \pm .029$	$.604 \pm .014$	$\textbf{.873} \pm \textbf{.015}$	$.920 \pm .010$