

The 2016 Cybersecurity Speaker Series

On the Growth of Cryptography

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On the growth of cryptography¹

Ronald L. Rivest

Institute Professor
MIT, Cambridge, MA

Cybersecurity Seminar Series
Brown University
April 14, 2016

¹many slides from my MIT Killian award lecture

Outline

Some pre-1976 context

Invention of Public-Key Crypto and RSA

Early steps

The cryptography business

Crypto policy

Attacks

More New Directions

Crypto Wars 2.0

What Next?

Conclusions

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Euclid – 300 B.C.



There are infinitely many primes:
2, 3, 5, 7, 11, 13, ...

Euclid – 300 B.C.



There are infinitely many primes:
2, 3, 5, 7, 11, 13, ...

The greatest common divisor of two
numbers is easily computed
(using “Euclid’s Algorithm”):
 $\text{gcd}(12, 30) = 6$

Greek Cryptography – The Scytale



An unknown *period* (the circumference of the scytale) is the secret key, shared by sender and receiver.

Pierre de Fermat (1601-1665)

Leonhard Euler (1707–1783)



Fermat's Little Theorem (1640):

For any prime p and any a , $1 \leq a < p$:

$$a^{p-1} = 1 \pmod{p}$$

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Euler's Theorem (1736):

If $\gcd(a, n) = 1$, then

$$a^{\phi(n)} = 1 \pmod{n},$$

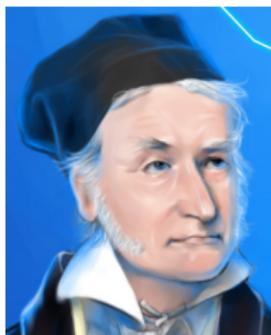
where $\phi(n) = \#$ of $x < n$ such that $\gcd(x, n) = 1$.

Carl Friedrich Gauss (1777-1855)



Published *Disquisitiones Arithmeticae* at age 21

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“The problem of *distinguishing prime numbers from composite numbers and of resolving the latter into their prime factors* is known to be one of the most important and useful in arithmetic. . . . the dignity of the science itself seems to require solution of a problem so elegant and so celebrated.”

William Stanley Jevons (1835–1882)



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Gave world's first *factoring challenge*:

“What two numbers multiplied together will produce 8616460799 ? I think it unlikely that anyone but myself will ever know.”

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Factored by Derrick Lehmer in 1903. (89681 * 96079)

World War I – Radio

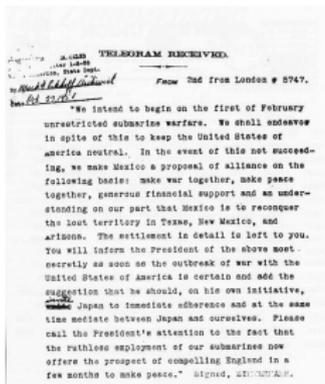
- ▶ A marvelous new communication technology—*radio* (Marconi, 1895)—enabled instantaneous communication with remote ships and forces, but also gave all transmitted messages to the enemy.

World War I – Radio

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- ▶ Use of cryptography soars.

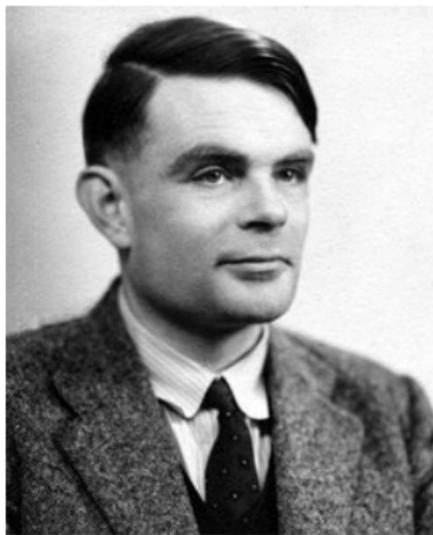
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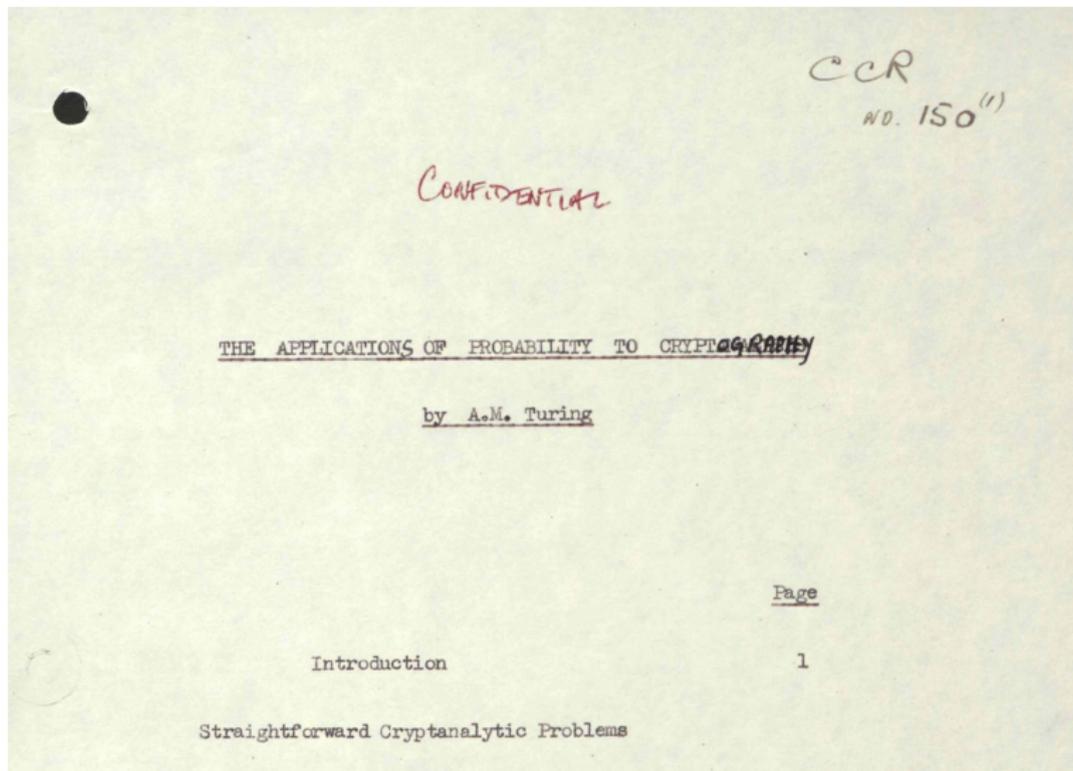
Decipherment of
Zimmermann Telegram by
British made American
involvement in World War I
inevitable.

Alan Turing (1912–1954)



Developed foundations of theory of computability (1936).

Still learning about Turing's contributions



World War II – Enigma, Purple, JN25, Naval Enigma



- ▶ Cryptography performed by (typically, rotor) *machines*.

World War II – Enigma, Purple, JN25, Naval Enigma



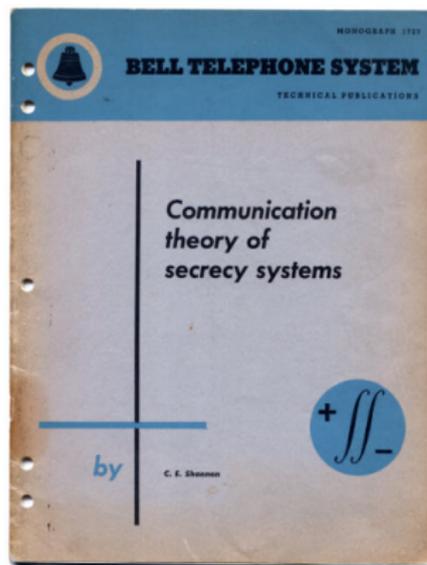
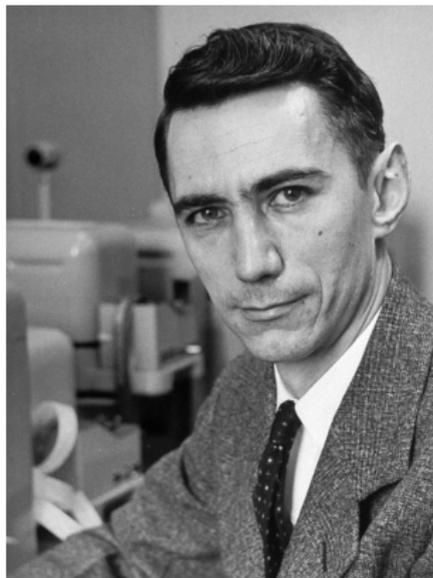
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- ▶ Work of Alan Turing and others at Bletchley Park, and William Friedman and others in the USA, on breaking of Axis ciphers had great success and immense impact.

World War II – Enigma, Purple, JN25, Naval Enigma



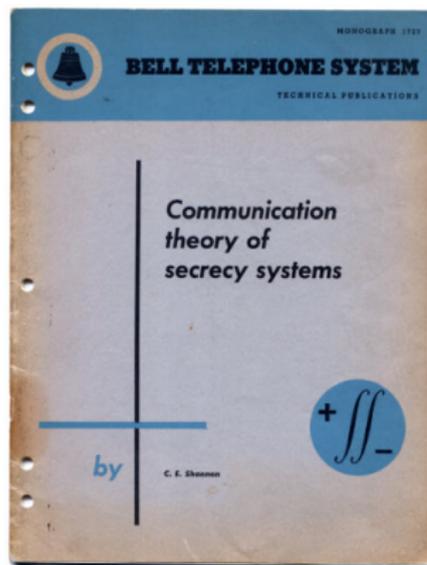
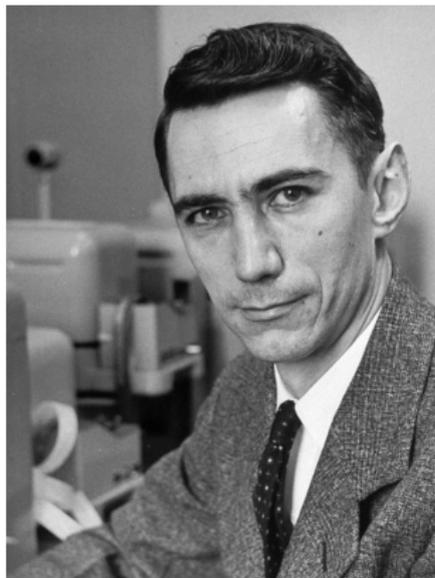
- ▶ Cryptography performed by (typically, rotor) *machines*.
- ▶ Work of Alan Turing and others at Bletchley Park, and William Friedman and others in the USA, on breaking of Axis ciphers had great success and immense impact.
- ▶ Cryptanalytic effort involved development and use of early computers (Colossus).

Claude Shannon (1916–2001)



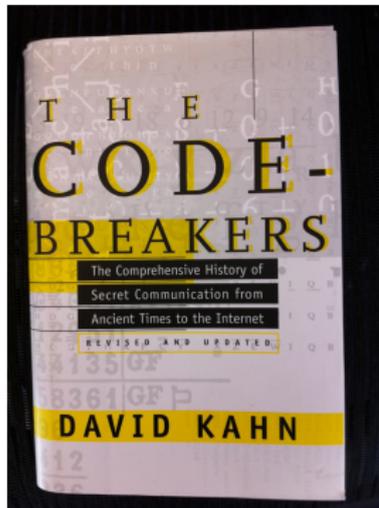
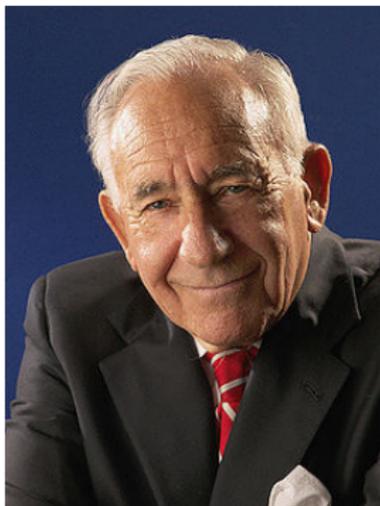
- ▶ “Communication Theory of Secrecy Systems” Sept 1945 (Bell Labs memo, classified).

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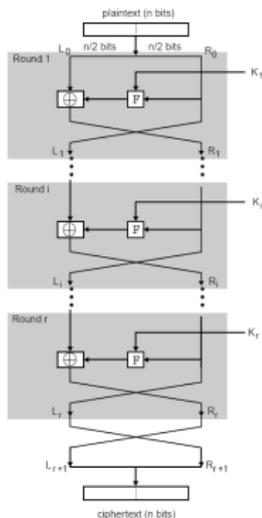
- ▶ “Communication Theory of Secrecy Systems” Sept 1945 (Bell Labs memo, classified).
- ▶ Information-theoretic in character—proves unbreakability of one-time pad. (Published 1949).

Kahn – The Codebreakers



In 1967 David Kahn published
The Codebreakers—The Story of Secret Writing.
A monumental history of cryptography.
NSA attempted to suppress its publication.

DES – U.S. Data Encryption Standard (1976)



DES Designed at IBM; Horst Feistel supplied key elements of design, such as ladder structure. NSA helped, in return for keeping key size at 56 bits.(?)

Computational Complexity



- ▶ Theory of Computational Complexity started in 1965 by Hartmanis and Stearns; expanded on by Blum, Cook, and Karp.
- ▶ Key notions: polynomial-time reductions; NP-completeness.

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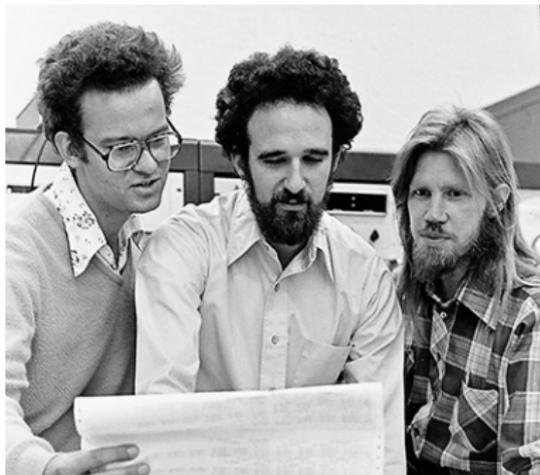
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Invention of Public Key Cryptography



- ▶ Ralph Merkle, and independently Marty Hellman and Whit Diffie, invented the notion of *public-key cryptography*.

Invention of Public Key Cryptography



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- ▶ In November 1976, Diffie and Hellman published *New Directions in Cryptography*, proclaiming
“We are at the brink of a revolution in cryptography.”

Public-key encryption (as proposed by Diffie/Hellman)

- ▶ Each party A has a *public key* PK_A others can use to encrypt messages to A :

$$C = PK_A(M)$$

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- ▶ It is easy to compute matching public/secret key pairs.
- ▶ **Publishing PK_A does not compromise SK_A !** It is *computationally infeasible* to obtain SK_A from PK_A . Each public key can thus be safely listed in a public directory with the owner's name.

Digital Signatures (as proposed by Diffie/Hellman)

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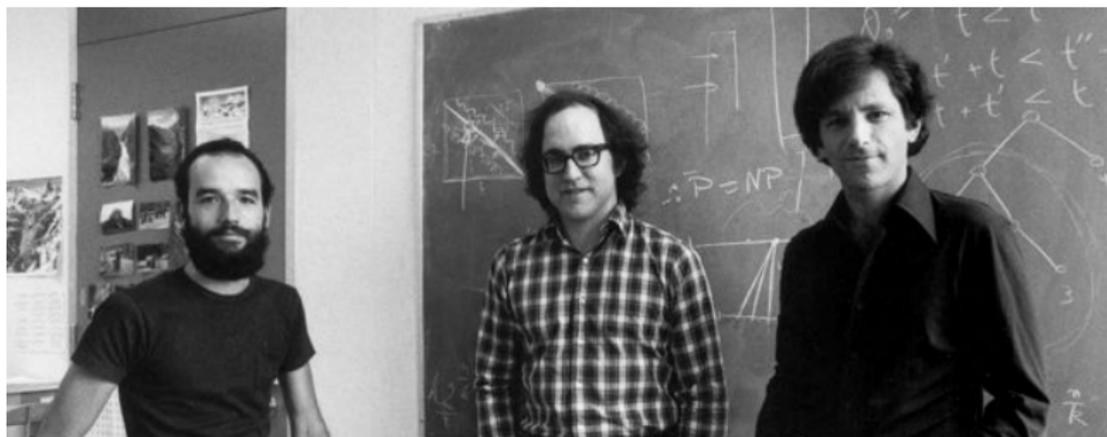
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- ▶ Amazing ideas!
- ▶ But they couldn't see how to implement them...

RSA (Ron Rivest, Adi Shamir, Len Adleman, 1977)



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- ▶ Shamir and Adleman in Math dept.; Rivest in EECS.

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- ▶ Adi I and proposed many methods; Len broke most of them.

Shamir's mysterious "Ski method"



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- ▶ R, S, A went skiing in February 1977.

Shamir's mysterious "Ski method"



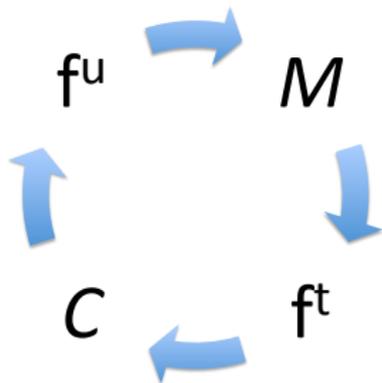
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Shamir's mysterious "Ski method"



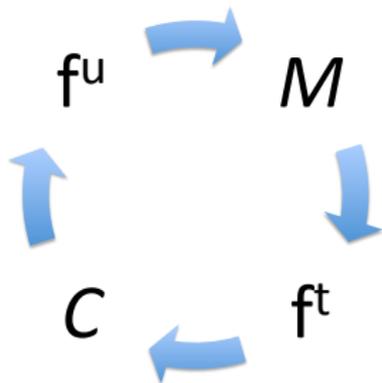
- ▶ R, S, A went skiing in February 1977.
- ▶ Shamir remembers "solving the PK problem" while skiing.
- ▶ Unfortunately, at the bottom of the run, he could no longer recall the solution...

“Almost there”—cycle with trapdoor period



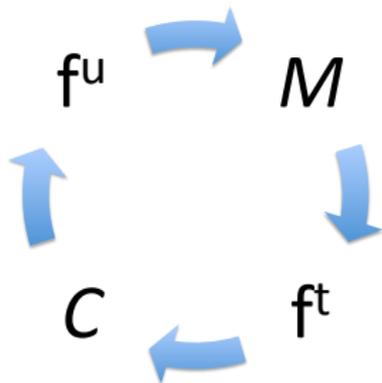
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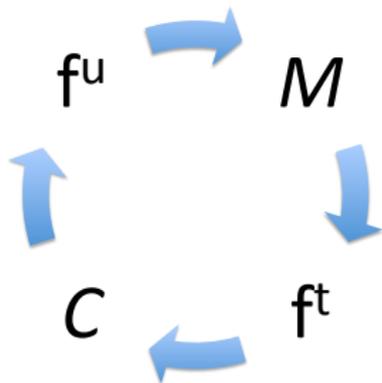
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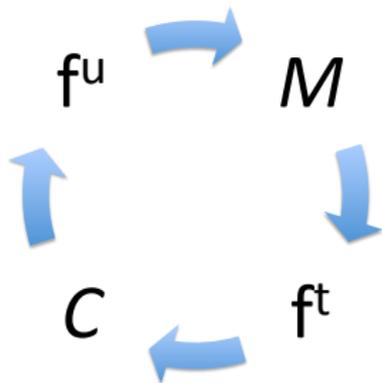
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- ▶ “*In vino veritas*” (Pliny \approx AD 50)



- ▶ Manichewitz wine + permutation polynomials + factoring...



RSA method

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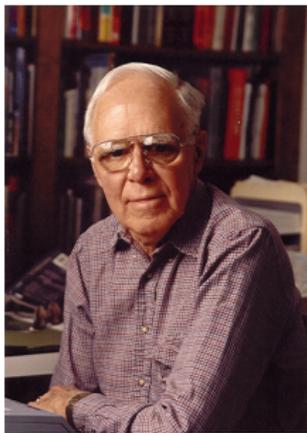
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- ▶ $PK = (n, e)$ where $n = pq$ and $\gcd(e, \phi(n)) = 1$
- ▶ $SK = d$ where $de = 1 \pmod{\phi(n)}$
- ▶ Encryption/decryption (or signing/verify) are simple:

$$C = PK(M) = M^e \pmod{n}$$

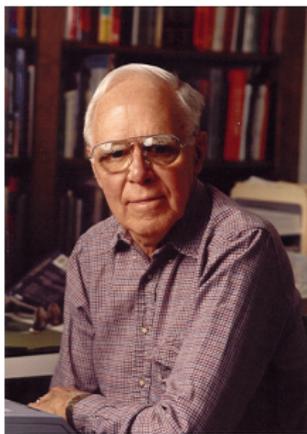
$$M = SK(C) = C^d \pmod{n}$$

Martin Gardner column and RSA-129 challenge



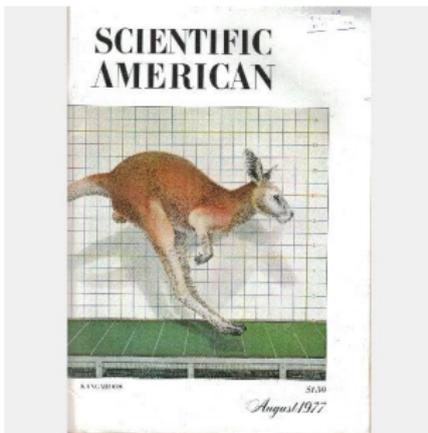
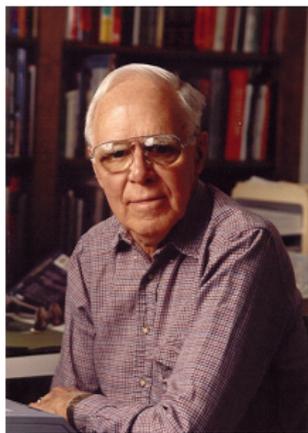
- ▶ Described public-key and RSA cryptosystem in his Scientific American column, *Mathematical Games*

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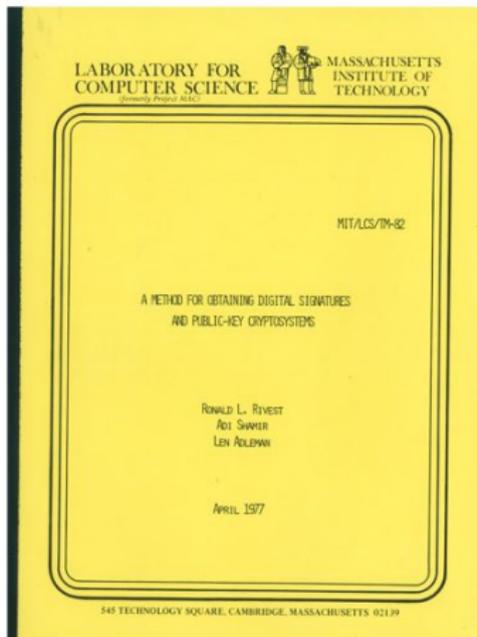
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- ▶ Offered copy of RSA technical memo.

Martin Gardner column and RSA-129 challenge



- ▶ Described public-key and RSA cryptosystem in his Scientific American column, *Mathematical Games*
- ▶ Offered copy of RSA technical memo.
- ▶ Offered \$100 to first person to break challenge ciphertext based on 129-digit product of primes.
(Our) estimated time to solution: 40 quadrillion years

Publication of RSA memo and paper



Programming S. L. Graham, R. L. Rivest
Techniques Editors

A Method for Obtaining Digital Signatures and Public-Key Cryptosystems

R. L. Rivest, A. Shamir, and L. Adleman
MIT Laboratory for Computer Science
and Department of Mathematics

An encryption method is presented with the novel property that publicly revealing an encryption key does not thereby reveal the corresponding decryption key. This has two important consequences:

- (1) Creation or other secure means are not needed to transmit keys, since a message can be encrypted using an encryption key publicly revealed by the intended recipient. Only he can decipher the message, since only he knows the corresponding decryption key.
- (2) A message can be "signed" using a privately held decryption key. Anyone can verify this signature using the corresponding publicly revealed encryption key. Signatures cannot be forged, and a signer cannot later deny the validity of his signature. This has obvious applications in "electronic mail" and "electronic funds transfer" systems. A message is encrypted by representing it as a number M , raising M to a publicly specified power e , and then taking the remainder when the result is divided by the publicly specified product, n , of two large secret prime numbers p and q . Decryption is similar, only a different, secret, power d is used, where $e \cdot d = 1 \pmod{(p-1)(q-1)}$. The security of the system rests in part on the difficulty of factoring the published division, n .

Key Words and Phrases: digital signatures, public-key cryptosystems, privacy, authentication, security, factoring, prime number, electronic mail, message-passing, electronic funds transfer, cryptography.

CR Categories: 2.12, 3.15, 3.80, 3.81, 5.25

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This research was supported by National Science Foundation grant MCS74-14248, and the Office of Naval Research grant number N00014-75-1-0740 (ONR).

* This paper was submitted prior to the time that Rivest became editor of the department, and original membership was unchanged until he left the department.

Authors' Address: MIT Laboratory for Computer Science, 545 Technology Square, Cambridge, MA 02139.
© 1978 ACM 0898-0130/78/0005-0000\$01.00

I. Introduction

The era of "electronic mail" [10] may seem be upon us; we must ensure that two important properties of the current "paper mail" system are preserved: (a) messages are private, and (b) messages can be signed. We demonstrate in this paper how to build these capabilities into an electronic mail system.

At the heart of our proposal is a new encryption method. This method provides an implementation of a "public-key cryptosystem," an elegant concept invented by Diffie and Hellman [1]. Their article motivated our research, since they presented the concept but not any practical implementation of such a system. Readers familiar with [1] may wish to skip directly to Section V for a description of our method.

II. Public-Key Cryptosystems

In a "public-key cryptosystem" each user places in a public file an encryption procedure E . That is, the public file is a directory giving the encryption procedure of each user. The user keeps secret the details of his corresponding decryption procedure D . These procedures have the following four properties:

- (1) Deciphering the enciphered form of a message M yields M . Formally,
 $D(E(M)) = M$.
- (2) Both E and D are easy to compute.
- (3) If E publicly revealing E the user does not reveal an easy way to compute D . This means that in practice only he can decipher messages enciphered with E , or compute D efficiently.
- (4) If a message M is first deciphered and then enciphered, M is the result. Formally,
 $E(D(M)) = M$.

An encryption (or decryption) procedure typically consists of a general method and an encryption key. The general method, which controls the key, enciphers a message M to obtain the enciphered form of the message, called the ciphertext C . Everyone can use the same general method; the security of a given procedure will rest on the security of the key. Reversing an encryption algorithm then means revealing the key.

When the user reveals E he reveals a very inefficient method of computing $D(C)$, testing all possible messages M until one such that $E(M) = C$ is found. If property (3) is satisfied the number of such messages to test will be so large that this procedure is impractical.

A function E satisfying (a)-(c) is a "trap-door one-way function"; if it also satisfies (d) it is a "trap-door one-way permutation." Diffie and Hellman [1] introduced the concept of trap-door one-way functions but

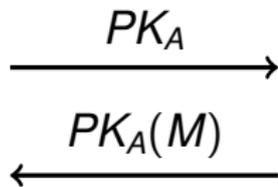
Communications February 1978
Volume 2
Number 2

LCS-82 Technical Memo (April 1977)
CACM article (Feb 1978)

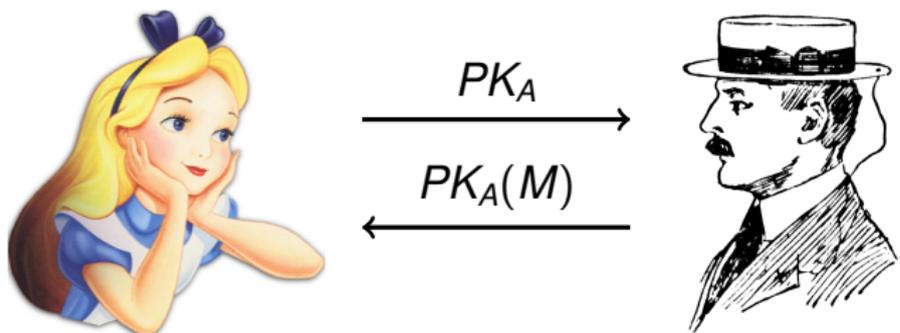
Alice and Bob (1977, in RSA paper)



Alice and Bob (1977, in RSA paper)



Alice and Bob (1977, in RSA paper)



Alice and Bob now have a life of their own—they appear in hundreds of crypto papers, in `xkcd`, and even have their own Wikipedia page:

The screenshot shows the Wikipedia article for "Alice and Bob". The page title is "Alice and Bob" and the subtitle is "From Wikipedia, the free encyclopedia". The article text begins with "The names **Alice and Bob** are commonly used [placeholder names](#) are used for convenience; for example, "Alice sends a message to Party B encrypted by Party B's public key within these fields—helping technical topics to be explained." The article also mentions "In [cryptography](#) and [computer security](#), there are a number of [various protocols](#). The names are conventional, somewhat".

Independent Invention of Public-Key Revealed



In 1999 GCHQ announced that James Ellis, Clifford Cocks, and Malcolm Williamson had invented public-key cryptography, the “RSA” algorithm, and “Diffie-Hellman key exchange” in the 1970’s, before their invention outside.

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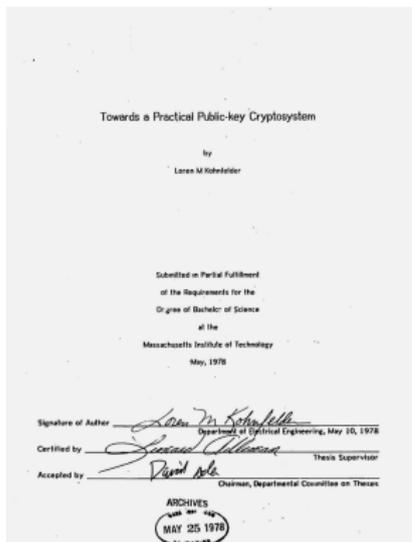
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Loren Kohnfelder – Invention of Digital Certificates



- ▶ Loren Kohnfelder's B.S. thesis (MIT 1978, supervised by Len Adleman), proposed notion of *digital certificate*—a digitally signed message attesting to another party's public key.

RSA on a chip (1980)

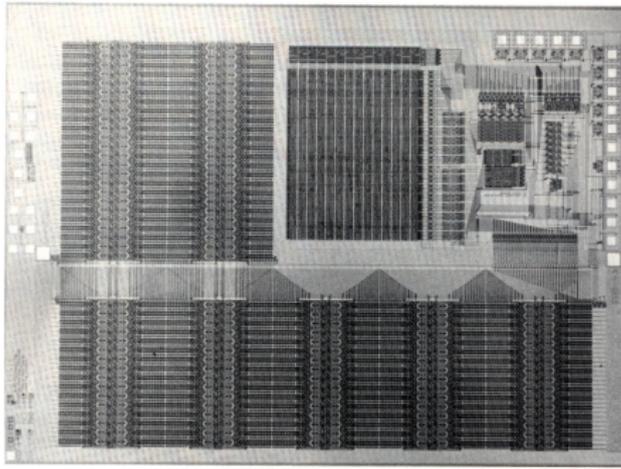


FIGURE 3. The RSA chip contains 40,000 transistors and measures 5.5 mm by 8 mm.

- ▶ MIT started VLSI effort.

RSA on a chip (1980)

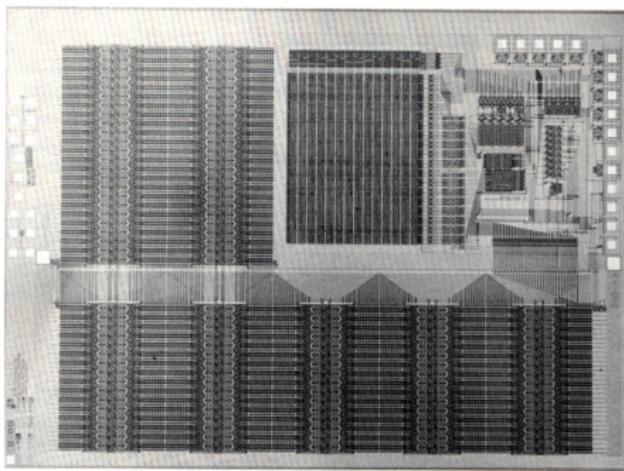


FIGURE 3. The RSA chip contains 40,000 transistors and measures 5.5 mm by 8 mm.

LAMBDA Fourth Quarter 1980 17

- ▶ MIT started VLSI effort.
- ▶ R, S, A designed “RSA chip” and fabbed prototype:

RSA on a chip (1980)

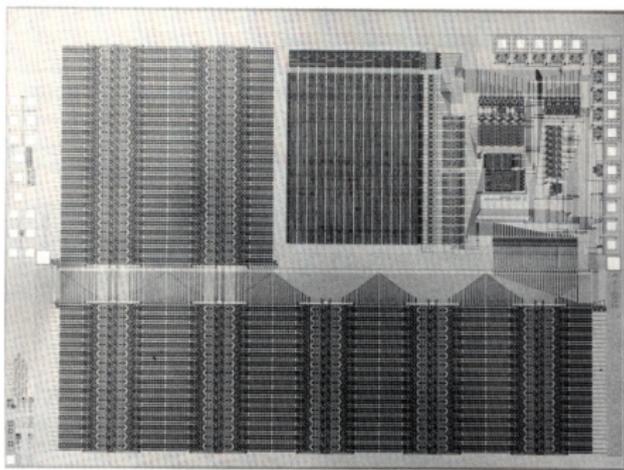


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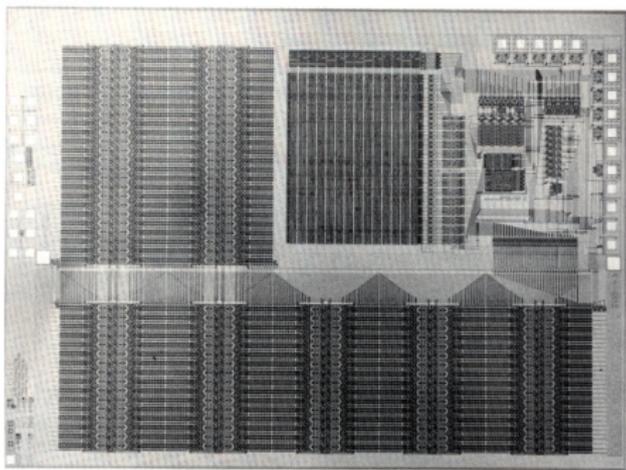


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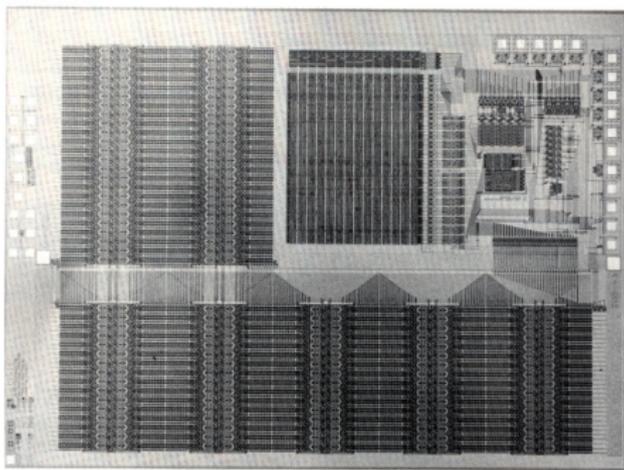


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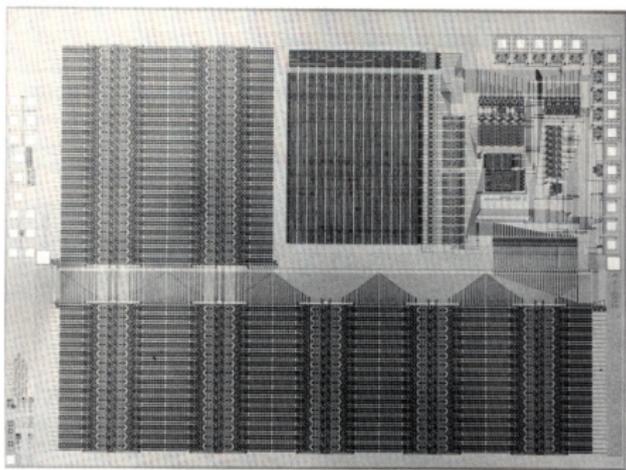


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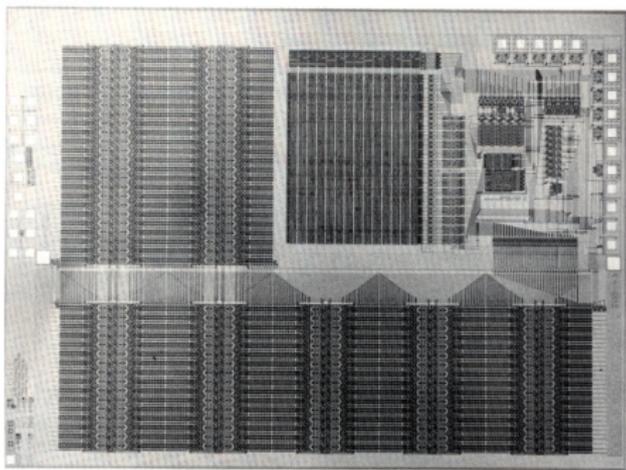


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 - ▶ 40,000 transistors; 5.5mm x 8mm chip.
- ▶ Fabrication was buggy/unreliable.

IACR—International Assn. for Cryptologic Research

- ▶ Established 1982 by David Chaum, myself, and others, to promote academic research in cryptology.
- ▶ Sponsors three major conferences/year (Crypto, Eurocrypt, Asiacrypt) and four workshops; about 200 papers/year, plus another 600/year posted on web. Publishes J. Cryptography
- ▶ Around 1600 members, (25% students), from 74 countries, 54 Fellows.



Theoretical Foundations of Security



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- ▶ “A Digital Signature Scheme Secure Against Adaptive Chosen Message Attacks” Goldwasser, Micali, Rivest (1988) (Uses well-defined *game* to define security objective.)

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- ▶ Extremely simple and fast: uses array $S[0..255]$ to keep a permutation of $0..255$, initialized using secret key, and uses two pointers i, j into S .

To output a pseudo-random byte:

```
i = (i + 1) mod 256
```

```
j = (j + S[i]) mod 256
```

```
swap S[i] and S[j]
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- ▶ Showing its age (statistical attacks)...

Spritz – RC4 replacement (w/ J. Schuldt, 2014)

RC4()

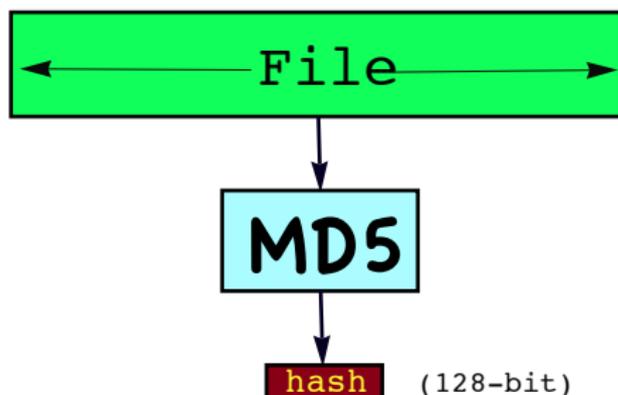
```
1  $i = i + 1$   
2  $j = j + S[i]$   
  
3 SWAP( $S[i], S[j]$ )  
4  $z = S[S[i] + S[j]]$   
5 return  $z$ 
```

SPRITZ()

```
1  $i = i + 1$   
2  $j = k + S[j + S[i]]$   
3  $k = i + k + S[j]$   
4 SWAP( $S[i], S[j]$ )  
5  $z = S[j + S[i + S[z + k]]]$   
6 return  $z$ 
```

- ▶ Spritz code found by computer search.
- ▶ About 50% longer and 4X slower (unoptimized).
- ▶ Uses new register k as well RC4 registers i, j ; output register z also used in feedback.
- ▶ 2^{81} samples seem necessary to distinguish SPRITZ-256 from random. (Compare: 2^{41} for RC4.)

MD5 Cryptographic Hash Function (Rivest, 1991)



- ▶ MD5 proposed as pseudo-random function mapping files to 128-bit fingerprints. (variant of earlier MD4; ARX-style)
- ▶ Collision-resistance was a design goal – it should be infeasible to find two files with the same fingerprint.
- ▶ Many, many uses (e.g. in digital signatures) – very widely used, and a model for many other later hash function designs.

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U.S. Patent 4,405,829

United States Patent [19]		[11]	4,405,829
Rivest et al.		[45]	Sep. 20, 1983
[54] CRYPTOGRAPHIC COMMUNICATIONS SYSTEM AND METHOD			
[75] Inventors: Ronald L. Rivest, Belmont; Adi Shamir, Cambridge; Leonard M. Adleman, Arlington, all of Mass.			
[73] Assignee: Massachusetts Institute of Technology, Cambridge, Mass.			
[21] Appl. No.: 860,586			
[22] Filed: Dec. 14, 1977			
[51] Int. Cl.: H04K 1/00; H04L 9/04			
[52] U.S. Cl.: 178/22.1; 178/22.11			
[54] Field of Search: 178/22, 22.1, 22.11, 178/22.14, 22.15			
[56] References Cited			
U.S. PATENT DOCUMENTS			
1,657,476 4/1972 Aiken 178/22			
OTHER PUBLICATIONS			
"New Directions in Cryptography", Diffie et al., <i>IEEE Transactions on Information Theory</i> , vol. IT-22, No. 6, Nov. 1976, pp. 644-654.			
"Theory of Numbers" Stewart, MacMillan Co., 1952, pp. 133-135.			
"Diffie et al., Multi-User Cryptographic Techniques", AFIPS, Conference Proceedings, vol. 45, pp. 109-112, Jun. 8, 1976.			
<i>Primary Examiner</i> —Sal Cangialosi <i>Attorney, Agent, or Firm</i> —Arthur A. Smith, Jr.; Robert J. Horn, Jr.			
ABSTRACT			
[57] A cryptographic communications system and method. The system includes a communications channel coupled to at least one terminal having an encoding device and to at least one terminal having a decoding device. A message-to-be-transferred is encrypted to ciphertext at the encoding terminal by first encoding the message as a number M in a predetermined set, and then raising that number to a first predetermined power (associated with the intended receiver) and finally computing the remainder, or residue, C, when the exponentiated number is divided by the product of two predetermined prime numbers (associated with the intended receiver). The residue C is the ciphertext. The ciphertext is deciphered to the original message at the decoding terminal in a similar manner by raising the ciphertext to a second predetermined power (associated with the intended receiver), and then computing the residue, M', when the exponentiated ciphertext is divided by the product of the two predetermined prime numbers associated with the intended receiver. The residue M' corresponds to the original encoded message M.			
40 Claims, 7 Drawing Figures			

```
graph TD
    M((M)) --> Enc[ENCODING]
    Enc --> CA[CA_s]
    CA --> CC[COMMUNICATIONS CHANNEL]
    CC --> CD[CD_s]
    CD --> Dec[DECODING]
    Dec --> M_prime((M))
```

Filed December 1977 (MIT TLO)
Issued September 1983

RSA the company (1983)

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- ▶ RSA acquired by Security Dynamics in 1996, now part of EMC.

World Wide Web (Sir Tim Berners-Lee, 1990)



- ▶ Just as radio did, this new communication medium, the World-Wide Web, drove demand for cryptography to new heights.
- ▶ Cemented transition of cryptography from primarily military to primarily commercial.

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U.S. cryptography policy evolves

- ▶ U.S. government initially tried to control and limit public-sector research and use of cryptography
- ▶ Attempt to chill research via ITAR (1977)
- ▶ MIT “Changing Nature of Information” Committee (1981; Dertouzos, Low, Rosenblith, Deutch, Rivest,...)

MIT Committee Seeks Cryptography Policy

Questions of who should do research on cryptography and how results should be disseminated are the first order of business

Within the next 10 years, networks consisting of tens of thousands of computers will connect businesses, corporations and homes in ways that make communications for individuals and for society if computers continue to be connected, as they are now, according to local decisions. The fact that it is now so easy to send computer programs between connected machines and to instruct a program to search for, select,

Science, 13 Mar 1981

U.S. cryptography policy evolves

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- ▶ Recently, this issue has re-surfaced...

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Factorization of RSA-129 (April 1994)

▶ RSA-129 =

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11438162575788886766923577997614661201021829  
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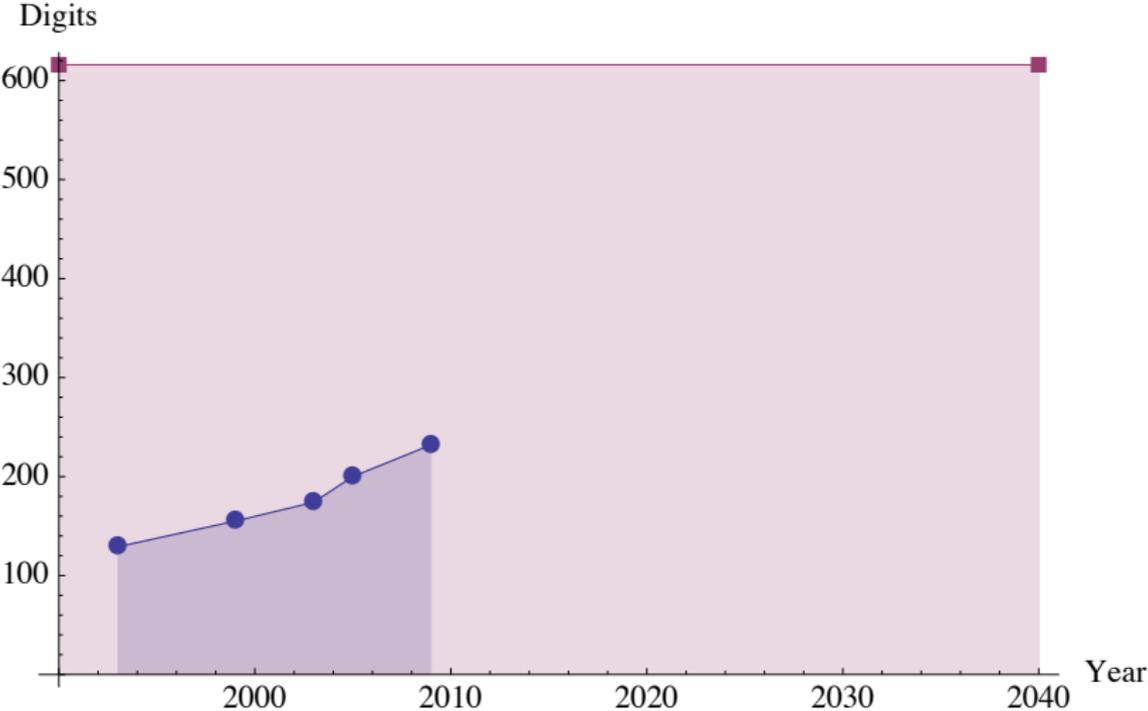
- ▶ 8 months work by about 600 volunteers from more than 20 countries; 5000 MIPS-years.
- ▶ secret message:

The Magic Words Are Squeamish Ossifrage



BayBank For Solving the Scientific American RSA Challenge		0254643
Massachusetts	53-235 113	Official Bank Check
Date		April 22, 1994
PAY	The sum of 100 dollars 00 cts	\$ *****100.00*****
		AMOUNTS IN EXCESS OF \$100,000.00 REQUIRE TWO SIGNATURES
To the order of	**Derek Atkins or Michael Graff or Arjen Lenstra or Paul Leyland**	 Authorized Signature
		Authorized Signature
⑈0254643⑈ ⑆011302357⑆ 317 83321⑈		

Factoring Records

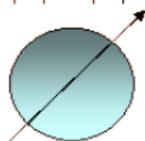


Factoring on a Quantum Computer?



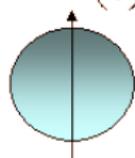
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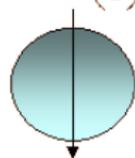
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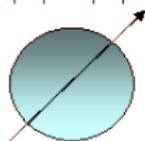
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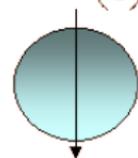


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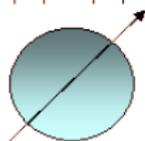
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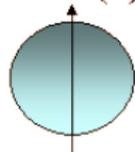
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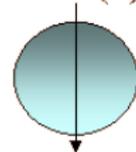
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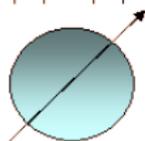
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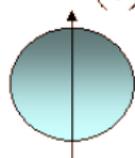
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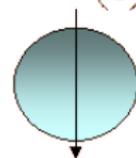
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- ▶ In 2001, researchers at IBM used this algorithm on a (real) quantum computer to factor $15 = 3 \times 5$.
- ▶ Recently (Dattani, 2014): $291311 = 557 \times 523$
- ▶ Dark clouds on horizon for RSA?

Hash Function Attacks



- ▶ In 2004 Xiaoyun Wang and colleagues found a way to produce *collisions* for MD5:

$$\text{MD5}(\textit{file1}) = \text{MD5}(\textit{file2}) \quad !!!$$

Also for SHA-1 and many other hash functions.
Major break!!

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- ▶ So NIST ran a competition for new hash function standard (SHA-3 = Keccak).

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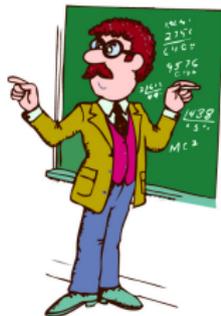
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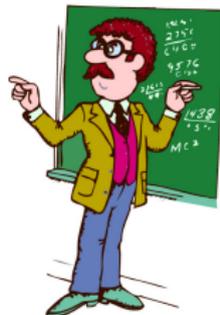
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Zero-Knowledge Proofs

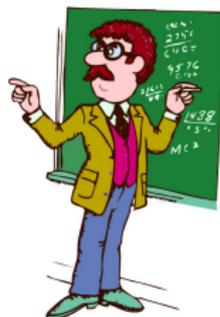


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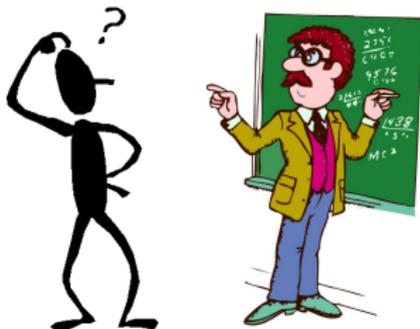
I can convince you

Zero-Knowledge Proofs



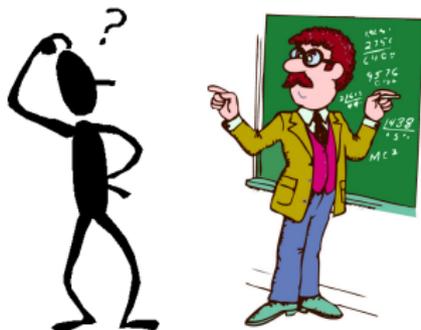
*I can convince you
I know a solution
to a hard problem*

Zero-Knowledge Proofs



*I can convince you
I know a solution
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while telling you nothing
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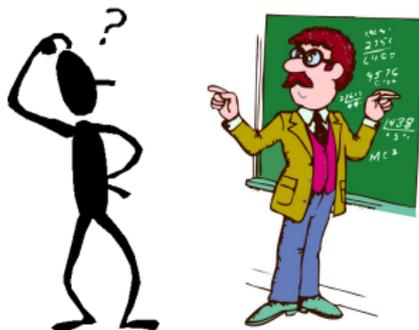
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*Goldwasser, Micali, Rackoff (1985)
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An enormously useful capability!

Payment Systems

- ▶ *Probabilistic payments* (Micali and Rivest, 2001).
“Peppercoin” payments. Paying you ten cents is like paying you one dollar with probability $1/10$.

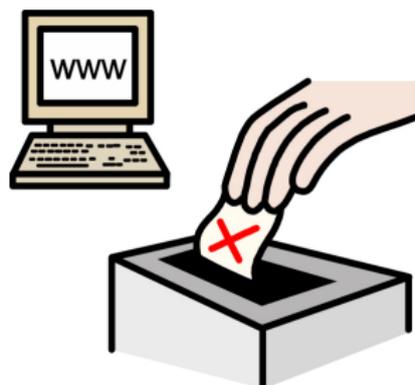
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- ▶ *Bitcoin* (Nakamoto, 2009). The “blockchain” for decentralized consensus.
- ▶ Ethereum, Dogecoin, Litecoin, Zero-cash, ...

Voting Systems



New “end-to-end” cryptographic voting systems (Chaum, Neff, Benaloh, Ryan, Rivest, Adida, ...):

- ▶ all ballots posted on web (encrypted)
- ▶ voters verify their votes are correct (while preventing vote-selling and coercion)
- ▶ anyone can verify final tally
- ▶ may be done with paper ballots

Cryptography *increases* transparency and verifiability!

Fully Homomorphic Encryption



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Fully Homomorphic Encryption



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- ▶ In 2009, Craig Gentry (Stanford, IBM) gave solution based on use of lattices. If efficiency can be greatly improved, could be huge implications (e.g. for cloud computing).

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Invention of Public-Key Crypto and RSA

Early steps

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Crypto policy

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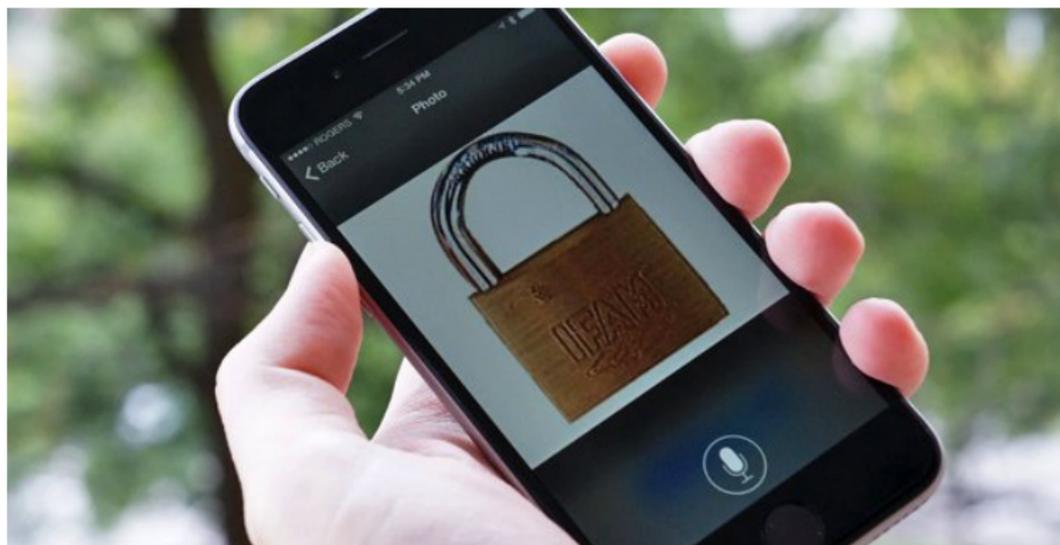
More New Directions

Crypto Wars 2.0

What Next?

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Crypto Wars 2.0



- ▶ Apple / FBI iPhone debate...
- ▶ Should LE have ability to unlock any iPhone or encryption content?
- ▶ Read “Keys Under Doormats” report (Abelson et al. 2015)

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- ▶ Show $P \neq NP$!
- ▶ Is quantum computing practical?
- ▶ Give Alice and Bob smartphones!
- ▶ Ground crypto practice better in vulnerable computer systems; prepare better for worst-case scenarios.

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- ▶ Cryptography is fun!

Thank You!

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