

MASSACHUSETTS INSTITUTE OF TECHNOLOGY
 Department of Electrical Engineering and Computer Science
 6.001—Structure and Interpretation of Computer Programs
 Spring Semester, 1999

Recitation – Friday, February 26

1. Warm Up

Write a function **max-err** that takes a list of lists of numbers and computes the **sqrt** of the **maximum** of the **sum** of the **squares** of the sublists. For example,

```
(define data (list (list -1 2) (list 0 -4 3) (list 1 -1 -2)))
(max-err data) ==> 5      (because  $\sqrt{0^2 + (-4)^2 + 3^2} = 5 > \sqrt{(-1)^2 + 2^2}$  and  $\sqrt{1^2 + (-1)^2 + (-2)^2}$ )
(define (max-err data)
```

```
)
```

2. Uniqueness

Say we have a list of numbers, and we want to get back a list where each number in the original list appears exactly once. For example,

```
(define x (list 1 2 2 3 1 5 4 3 4))
(unique x) ==> (1 2 3 5 4)
```

Let's write the function **unique** to do this. But first, write the function **remove** that removes all instances of an element from a list. (e.g. **(remove 3 (list 1 3 2 3 4 3))** ==> **(1 2 4)**).

```
(define (remove elt seq)
```

```
)
```

Now write **unique**, using **remove**. When writing **unique**, first think in English (or language of choice) about how you'd do this, then translate to Scheme.

```
(define (unique seq)
```

```
)
```

3. All Pairs

Write the function **all-pairs** that takes a list and returns a list of all pairs of the elements in the list. For example, **(all-pairs (list 1 2 3 4))** ==> **((1 2) (1 3) (1 4) (2 3) (2 4) (3 4))**

Again, first think about how you'd do this, and then translate into Scheme. Maybe start with trying to just get the pairs **((1 2) (1 3) (1 4))**, and then build up from there.

```
(define (all-pairs s)
```

```
)
```

4. Deep Reverse

So far, we've been working on lists, while we've ignored the elements of the list. What does the following return? `(reverse (list 1 (list 2 3) (list 4 5 6)))`

Write a function `deep-reverse` that when called on the above tree will reverse all the elements. `(deep-reverse (list 1 (list 2 3) (list 4 5 6))) ==> ((6 5 4) (3 2) 1)`

```
(define (deep-reverse x)
```

```
)
```

Now write `deep-reverse` using `map` (hint: you can use `reverse`)...

```
(define (deep-reverse x)
```

```
)
```

5. Flatten

Write the function `flatten` that takes a tree structure and returns a flat list of the leaves of the tree. For example `(fringe (list 1 (list 2) 3)) ==> (1 2 3)`

```
(define (flatten x)
```

```
)
```

Now try writing `flatten` using `map` and `accumulate`.

```
(define (flatten x)
```

```
)
```

6. Occurrences

Write the function `occurrences` that takes a number and a tree and counts the number of times that number appears in the tree. For example,

```
(define tree (list 1 2 (list (list 3 1) (list 1 2) 1)))
(occurrences 1 tree) ==> 4
```

```
(define (occurrences elt tree)
```

```
)
```

Now write `occurrences` using `map` and `accumulate`.

```
(define (occurrences elt tree)
```

```
)
```