

MASSACHUSETTS INSTITUTE OF TECHNOLOGY  
 Department of Electrical Engineering and Computer Science  
 6.001—Structure and Interpretation of Computer Programs  
 Spring Semester, 1999

**Recitation – Wednesday, March 17**

## 0. Administrivia

- Don't miss lecture tomorrow! Really.
- PS #4 is due today (in section or, for Sandia, 36-115, for Hooman, 36-117).
- PS #5 is due on March 31st (not during spring break)

## 1. Functions Aren't Functions Anymore

Up until now, every time we called a procedure with the same arguments, we got the same value back. For example, if `(foo 7)` returned 12, then **every time** we called `(foo 7)` we would get back 12. Consider the example below. Draw the box and pointer diagram and evaluate the following expressions.

<pre>(define count (list 0)) (define (counter)   (set-car! count (+ (car count) 1))   (car count))</pre>	<pre>(counter) ⇒ 1 (counter) ⇒ 2 (counter) ⇒ 3</pre>
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Notice that we're in danger if someone else is using the variable `count`. We'll step on each other's feet. How can we prevent this from happening?

```
(define counter
  (let ((count (list 0)))
    (lambda ()
      (set-car! count (+ (car count) 1))
      (car count))))
)
```

We'll see more tomorrow in lecture on how and why this technique of local state works.

## 2. Buffers

Write a function called `buffer` that takes one argument `x` and at each call, it returns the argument of the previous call to `buffer`. For example:

<pre>(buffer 1) ⇒ #f (buffer 7) ⇒ 1 (buffer 'x) ⇒ 7 (buffer '(2 5)) ⇒ x (buffer +) ⇒ (2 5)</pre>	<pre>(define buffer   (let ((store (list #f)))     (lambda (x)       (let ((result (car store)))         (set-car! store x)         result)))) )</pre>
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## 3. Remembering Values

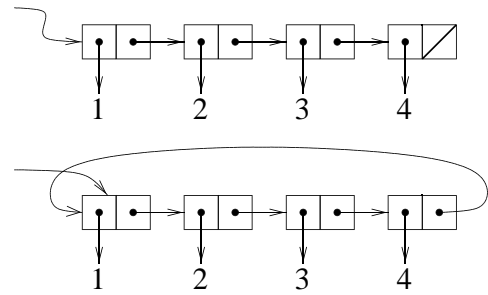
Write a function called `seen?` that takes one argument and returns `#t` only if that function has been called before with that argument. Assume you have the function `element?` that takes an object and a list, and returns `#t` if the object is in the list.

<pre>(seen? 1) ⇒ #f (seen? 'x) ⇒ #f (seen? 1) ⇒ #t (seen? 'y) ⇒ #f (seen? 'x) ⇒ #t (seen? 'y) ⇒ #t</pre>	<pre>(define seen?   (let ((store (list 'values)))     (lambda (x)       (cond ((element? x (cdr store)) #t)             (else (set-cdr! store (cons x (cdr store)))                   #f)))) )</pre>
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## 4. List Mutation – Rings

Rings are circular structures similar to lists. If we define a ring `r`, `(define r (make-ring '(1 2 3 4)))`, the following is true:

```
(nth 0 r)
⇒ 1
(nth 1 r)
⇒ 2
...
(nth 4 r)
⇒ 1
```



Write the function `make-ring!` that takes a list and makes a ring out of it. *Hint: It might be helpful to write a helper function called `last-pair`.*

```
(define (make-ring! ring-list)
  (define (last-pair lst)
    (if (null? (cdr lst))
        lst
        (last-pair (cdr lst))))
  (set-cdr! (last-pair ring-list) ring-list)
  ring-list
)
```

Write the procedure `rotate-left` that takes a ring and returns a ring that has been rotated one to the right.

```
(define (rotate-left ring)
  (cdr ring))

(define r1 (rotate-left r))
⇒ 2
```

We can also rotate a ring to the right. Rotating to the right is harder than rotating to the left. Define a procedure `ring-length` that will tell us the length of the ring (which is the length of the original list). *Hint: remember `eq?`*

```
(define (ring-length ring)
  (define (helper n here)
    (if (eq? here ring)
        n
        (helper (+ 1 n) (cdr here))))
  (helper 1 (cdr ring))
)
```

Now write the procedure `rotate-right`. If you're tired of writing helper procedures, you can use `repeated`.

```
(define (rotate-right ring)
  ((repeated rotate-left
    (- (ring-length ring) 1)) ring))

(define r2 (rotate-right r))
⇒ 4
```

## 5. Append!

Recall the function `append` that takes two lists and returns a list of the two appended. Recall that to do this, we made a **copy** of the first list and `cons`'d it onto the second. Now that we had side effects, we can append two lists without creating a copy of one of them. Assuming you have the function `last-pair` that we wrote above, write the function `append!`.

```
(define (append! x y)
  (set-cdr! (last-pair x) y)
  x
)
```