

MASSACHUSETTS INSTITUTE OF TECHNOLOGY
 Department of Electrical Engineering and Computer Science
 6.001—Structure and Interpretation of Computer Programs
 Spring Semester, 1999

Recitation – Wednesday, March 1

1. Some of the Important Things to Know

- Rules for Evaluation (substitution model) – when in doubt **stop thinking!**
- Rules for Special Forms
- Iteration vs. Recursion
- Pairs, Lists, and Trees (defining, manipulating, contracts, abstractions)
- Higher Order Procedures (procedures returning procedures)
- Abstraction of List Operations (**map**, **accumulate**, and **filter**).

2. Tricky Stuff

What are the values of the following expressions:

`(if 0 1 2) ⇒`

`(define (my-if pred consequent alternate)
 (if (zero? pred) alternate consequent))`

`(my-if 0 1 2) ⇒`

`(define (factorial n)
 (my-if n
 (* n (factorial (- n 1)))
 1))`

`(fact 5) ⇒`

`(define x 5)`

`(define y 6)`

`(let ((x 7)
 (y x))
 (+ x y)) ⇒`

`((lambda (x y) ((y 6) x)) 4
 (lambda (w) (lambda (z) (* 2 z)))) ⇒`

`(list 1 (list 2 list 3) 4)
 ⇒`

`((if + - *) 4 3) ⇒`

3. Writing Some Procedures

Write the following procedures:

The procedure **count-pairs** that counts the number of **cons** pairs in a tree structure.

`(count-pairs (list 2 (list 3 4) (list 5))) ⇒ 6`

`(define (count-pairs tree)`

`)`

The procedure **copy-some** that copies the first **n** elements of a list

`(copy-some 3 (list 1 2 3 4 5)) ⇒ (1 2 3)`

`(define (copy-some n lst)`

`)`

4. Order of Growth

What's the order of growth of the procedure **copy-some** above? $\Theta(\quad)$. Consider the following procedure to copy the last **n** elements of a list. What is the order of growth of **last-n**? $\Theta(\quad)$.

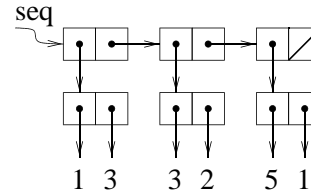
`(define (last-k k lst)
 (if (= (length lst) k)
 lst
 (last-k k (cdr lst))))`

5. Defining a New List Abstraction

Notice that it can take a long time to find the length of one of our list structures. Say we want to define a new sequence abstraction, similar to lists, but that can return the length in constant time. Here's the contract:

```
(head (attach x seq)) = x
(tail (attach x seq)) = seq
(seq-empty? empty-seq) == #t
(seq-empty? (attach x seq)) == #f
(seq-length seq) = the length in  $\Theta(1)$  time.
```

How can we do this? Let's define a sequence as show to the right. The list (1 3 5) would be represented as a list of pairs. The `cars` are the elements of the list, and the `cdrs` are the lengths of the lists. Fill in the blanks below to complete the abstraction.



```
(define empty-seq nil)
(define seq-empty? null?)
```

```
(define (head seq) )
(define (tail seq) )
```

```
(define (seq-length seq)
  (if (seq-empty? seq)
      0
      ))
```

```
(define (attach x seq)
  )
```

```
(define (list->seq lst)
```

```
)
```

```
(define (seq->list seq)
```

```
)
```

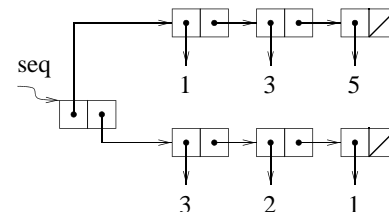
How about another way? Here a sequence is a pair of two things. The `car` is the original list, and the `cdr` stores the lengths of the list. Fill in the blanks below to complete the abstraction.

```
(define empty-seq (cons nil nil))
(define (seq-empty? seq) (null? (car seq)))
```

```
(define (head seq) )
(define (tail seq) )
```

```
(define (seq-length seq)
  (if (seq-empty? seq)
      0
      ))
```

```
(define (attach x seq)
  )
```



```
(define (list->seq lst)
```

```
)
```

```
(define (seq->list seq)
```

```
)
```

Notice that with either of these abstractions, lists behave in the same way as they did before, except that the length of a list can be computed in constant time. We traded time for space.