MASSACHVSETTS INSTITUTE OF TECHNOLOGY

Department of Electrical Engineering and Computer Science 6.001—Structure and Interpretation of Computer Programs Spring Semester, 1999

Recitation – Friday, February 19

1. Abstraction using Higher Order Procedures

Let's take a look at using abstraction on common patterns.

(* 2 5)	(double 5)	(* 3 2)	(triple 2)
(* 2 8)	(double 8)	(* 3 17)	(triple 17)
(* 2 54)	(double 54)	(* 3 4.1)	(triple 4.1)
(define double (lambda (x) (* 2 x)))	(define double (make-mult 2))	(define triple (lambda (x) (* 3 x)))	(define triple (make-mult 3))

(define make-mult (lambda (n) (lambda (x) (* n x))))

3. Higher Order Procedures

Write a function swap that takes a function f, and returns a function, that takes two arguments, and returns f with the variables swapped: $(f \times y) = ((swap f) \times y)$ For example, $((swap -) \times 4) = 1$.

2. Composing Procedures

Now try to write the function compose that takes two functions, f and g, and returns a function, that takes one argument, and composes f and g on that argument.

Let's trace through the evaluation of the following expression:

```
((compose double cube) 3)

(((\lambda \text{ (f g)} (\lambda \text{ (x) (f (g x))})) double cube) 3)

(((\lambda \text{ (x) (double (cube x))}) 3)
(double (cube 3))
```

Notice that there's no magic here. We just used the same rules for evaluation that we've been using all along – the substitution model!

Using compose, define the function $^5/2$ which takes a number x and computes $x^{5/2}$.

```
(define ^5/2 (compose sqrt cube)
```

5. Repeated Composition of Procedures

We saw how to compose two procedures to produce another procedure. For example, we can define the following.

```
(define fourth-power (compose square square))
(define eight-power (compose square (compose square square)))
... and so on ...
```

Let's write a (very strange) function called **repeated** that takes a function **f** and an integer **n**, and composes **f**, **n** times. For example:

6. Iterative Repeated

Guess what.. Now that we've written the recursive version of repeated, let's write the iterative version.

7. More Higher-Order Procedures

Write a function snoc that takes two arguments a and b and returns a function, that when called with #t returns a and when called with #f returns b.

Here's an even more elegant (albeit more obscure) way of doing the same thing. Can you figure out how this is working?

```
(define snoc (lambda (x y) (lambda (f) (f x y))))
(define rac (lambda (p) (p (lambda (a b) a))))
(define rdc (lambda (p) (p (lambda (a b) b))))
```