MASSACHVSETTS INSTITVTE OF TECHNOLOGY
Department of Electrical Engineering and Computer Science
6.001—Structure and Interpretation of Computer Programs
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1. Abstraction using Higher Order Procedures

Let's take a look at using abstraction on common patterns.

```
(* 2 5)
(* 2 8)
(* 2 54)
```

```
(define double
  (lambda (x)
    (* 2 x)))
```

```
(* 3 2)
(* 3 17)
(* 3 4.1)
```

```
(define triple
  (lambda (x)
    (* 3 x)))
```

```
(define make-mult
  (lambda (n)
    (lambda (x)
      (* n x))))
```

3. Higher Order Procedures

Write a function `swap` that takes a function `f`, and returns a function, that takes two arguments, and returns `f` with the variables swapped: `(f x y) == ((swap f) y x)` For example, `((swap -) 4 5)` ⇒ `1`.

```
(define swap




)
```

2. Composing Procedures

Now try to write the function `compose` that takes two functions, `f` and `g`, and returns a function, that takes one argument, and composes `f` and `g` on that argument.

```
(define compose




)
```

Let's trace through the evaluation of the following expression:

```
((compose double cube) 3)
((λ (f g) (λ (x) (f (g x)))) double cube) 3)
((λ (x) (double (cube x))) 3)
(double (cube 3))
54
```

Notice that there's no magic here. We just used the same rules for evaluation that we've been using all along – the substitution model!

Using `compose`, define the function `^5/2` which takes a number `x` and computes $x^{5/2}$.

```
(define ^5/2                                    )
```

5. Repeated Composition of Procedures

We saw how to compose two procedures to produce another procedure. For example, we can define the following.

```
(define fourth-power (compose square square))
(define eight-power (compose square (compose square square)))
... and so on ...
```

Let's write a (very strange) function called `repeated` that takes a function `f` and an integer `n`, and composes `f`, `n` times. For example:

```
(define fourth-power (repeated square 2))
(define eight-power (repeated square 3))
... and so on ...

(define (repeated proc n)




)
```

Let's look at a simple example:

```
(define fourth-power (repeated square 2))
```

6. Iterative Repeated

Guess what.. Now that we've written the recursive version of `repeated`, let's write the iterative version.

```
(define (repeated proc n)




)
```

7. More Higher-Order Procedures

Write a function `snoc` that takes two arguments `a` and `b` and returns a function, that when called with `#t` returns `a` and when called with `#f` returns `b`.

```
(define snoc


)
```

What do we have once we define the following?

```
(define (rac x) (x #t))
(define (rdc x) (x #f))
```

Here's an even more elegant (albeit more obscure) way of doing the same thing. Can you figure out how this is working?

```
(define snoc (lambda (x y) (lambda (f) (f x y))))
(define rac (lambda (p) (p (lambda (a b) a))))
(define rdc (lambda (p) (p (lambda (a b) b))))
```