MASSACHVSETTS INSTITVTE OF TECHNOLOGY

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> Recitation – Friday, May 7 Final Review Handout ¹

Iterative vs. Recursive Processes and Order of Growth

Consider the two procedures below. Assume the arguments passed in are always positive integers.

Given the above definitions, when the expression (odd? 24) is evaluated, does that generate a recursive or iterative process? Why?



What is the order of growth of in time of the procedure even??



What is the order of growth of in space of the procedure odd??



Change one of the two functions above to make the process the opposite of what it currently is (eg. If it's a recursive process, make it iterative and if it's an iterative process, make it recursive).



Consider the function below:

Does the function power-of-2? generate a recursive or iterative process? Why?



What is the order of growth of in time of the procedure power-of-2??



What is the order of growth of in space of the procedure power-of-2??



¹Disclaimer: This handout was created as a study guide for the final. It is NOT necessarily complete. There could be other material not covered in this handout that is still fair game for the final. This is also NOT a practice final, in that I didn't time how long it should take. I just tried to come up with some problems that would help in reviewing for the final.

Higher Order Procedures and Tree Structures

We'd like to write an evaluator for simple in-fix numerical expressions. For example, consider the trees generated by the following expressions. Careful: Notice that the operators are **not** quoted.

```
(define exp1 (list 3 + 5))
  (define exp2 (list 3 * (list (list 4 + (list 6 - 2)) / 2)))
How does exp1 print when evaluated?
```

Draw the box and pointer diagram for the tree structure of exp2



Write a function infix that evaluates these types of expressions. For example,

```
(infix 4) ==> 4
(infix exp1) ==> 8
(infix exp2) ==> 12
```

Consider a function infix->prefix that takes an infix expression like exp1 and exp2 above, and transforms the expression into prefix form (e.g. it swaps the order of the operator and first operand). For example, the expression (infix->prefix (list (list 3 * 2) + 4)) will produce the same list structure as (i.e. will be equal? with) the value of following expression:

```
(list + (list * 3 2) 4).
```

Write the function infix->prefix.



Local State

Assume scheme has the following special form time, which takes one argument and times how long it takes to evaluate the argument. Time returns a list of two elements, the first is the amount of time it took to evaluate the expression, and the second is the value of the expression. For example,

```
(time (sqrt 4)) ==> (20 2)
(time (sqr 5)) ==> (10 25)
(time (list 1 2 3)) ==> (7 (1 2 3))
(time (/ 1 0)) ==> Error: divide by zero
```

(define tsqrt (make-timed-procedure sqrt))

Assume, for simplicity, that (sqrt x) always takes 20 time units to compute and (sqr x) always takes 10 time units to compute for all positive numbers.

Louis has a program that he wants to make run faster. He wants to see what procedures are eating up the most amount of time. He decides to write a procedure called make-timed-procedure which takes a procedure and returns a procedure that does the same thing as the original, but also keeps track of the total time spent in the procedure. For example,

```
(define tsqr (make-timed-procedure sqr))
     (tsqrt 'time) ==> 0
                                                       (tsqr 'time)
     (tsqrt 4)
                   ==> 2
                                                       (tsqr 10)
                                                                     ==> 100
     (tsqrt 'time) ==> 20
                                                       (tsqr 'time)
                                                                   ==> 10
                                                      (tsqr 10)
     (tsqrt 4)
                   ==> 2
                                                                     ==> 100
     (tsqrt 'time) ==> 40
                                                       (tsqr 'time) ==> 20
Louis writes the following procedure:
   (define make-timed-procedure-1
     (let ((total-time 0))
       (lambda (proc)
          (lambda (x)
           (if (eq? x 'time)
               total-time
                (let ((result (time (proc x))))
                  (set! total-time (+ total-time (car result)))
                  (cadr result))))))
```

After defining the following two functions, Louis trys out his code. Show the output of each of the following expressions, assuming that each call to sqrt takes 20 and each call to sqr takes 10 time units.

This isn't quite the behavior we wanted. What change needs to be made to make-timed-procedure so that we get the correct behavior?



Object Oriented Programming and Environment Diagrams

Below is the object oriented system from the March 19th Lecture Notes (just included for reference)

```
(define (get-method object message)
     (object message))
   (define (no-method name)
     (list 'no-method name))
   (define (no-method? x)
     (if (pair? x)
        (eq? (car x) 'no-method)
       false))
   (define (method? x)
     (not (no-method? x)))
   (define (ask object message . args)
     (let ((method (get-method object message)))
      (if (method? method)
         (apply method (cons object args))
         (error "No method" message (cadr method)))))
Consider the following expressions:
   (define (create-counter)
      (let ((count 0))
         (lambda (message)
             (case message
               ((VALUE) (lambda (self) count))
               ((INCR) (lambda (self)
                          (set! count (+ 1 count))
                          count))
               ((DECR) (lambda (self)
                          (set! count (- count 1))
                          count))))))
   (define c1 (create-counter))
   (define c2 (create-counter))
Draw the environment diagram for the above three expressions.
```



Write the expression that you would use to get the value of counter c1.



Write the expression that you would use to increment counter c1.



Streams and Higher Order Procedures

In this part, we are going to create an infinite stream of higher-order procedures. First, here are some simple functions that we are going to be using.

```
(define (compose f g) (lambda (x) (f (g x))))
(define (incr x) (+ x 1))
(define (sqr x) (* x x)
```

Now, Consider the function compose-fstreams that takes two streams-of-functions, fs1 and fs2, and returns another stream-of-functions where each element is the result of composing the corresponding elements of fs1 and fs2.

We define the following two infinite streams of functions, one that increments and one that squares.

```
(define fs-incr (cons-stream incr fs-incr))
(define fs-sqr (cons-stream sqr fs-sqr))
```

We can now define another infinite stream-of-functions fs (Hint: this is similar to how we defined integers in terms of ones).

```
(define fs
  (cons-stream incr (compose-fstreams fs-incr fs)))
```

What is the first element of the stream fs?



What is the second element of the stream fs?



Consider the function apply-fstream and the definition of the stream s, below.

```
(define (apply-fstream fs x)
    (cons-stream
          ((stream-car fs) x)
          (apply-fstream (stream-cdr fs) x)))
(define s (apply-fstream fs 0))
What are the first 10 elements of the stream s?
```

Consider the following two streams that are defined.

```
(define t1 (apply-fstream (compose-fstreams fs fs-sqr) 0))
(define t2 (apply-fstream (compose-fstreams fs-sqr fs) 0))
```

What are the first 5 elements of the stream t1?



What are the first 5 elements of the stream t2?



Meta Circular Evaluator

We would like to introduce a new special form to our evaluator called same?. Same? always takes three arguments, and returns #t if all three arguments are eq?. Same?, however is smart in that if the first two arguments are different, then the third argument is not evaluated. Here are some examples of using same?.

```
(same? 'x 'x 'x) ==> #t
(same? 'x 'x 'y) ==> #f
(same? 'x 'y 'y) ==> #f
(same? 'x 'y (/ 1 0)) ==> #f
(same? 'x 'x (/ 1 0)) ==> Divide by Zero Error
```

To add this special form to the evaluator, we need to define some data abstraction.

Define the function same?? that checks to see if an expression is a same? expression.



Define the functions same?-first and same?-second that select out the first and second sub-expressions (assume someone else defined same?-third).





Next, write the appropriate clause to add to the cond clause of eval, assuming that we have the function eval-same? that will evaluate a same? expression.



Finally, write the eval-same? function that takes a same? expression and an environment and implements the special form as described above.



Fill in the blanks:

We need to make same? a special form in our language because our language has ______ evaluation. If, instead, our language had ______ evaluation, then we could simply define same? as a function.

Assuming our Scheme has the alternative method of evaluation (stated in the previous paragraph), define same? as a function.



Explicit Control Evaluator

The special form same? from the previous example was so helpful that we decided to add it to the explicit control evaluator. Assume that in addition to the registers we've used in the past, we've also got the register TMP. Fill in the blanks in the following code that evaluates a same? expression.

```
1. ev-same?
       2.
            (assign unev (reg exp))
       З.
            (assign exp ((op same?-first) (reg exp)))
       4.
            (save continue)
       5.
       6.
            (save unev)
      7.
            (assign
      8.
            (goto .
      9. eval-after-first
            (restore unev)
      10.
      11.
      12.
            (assign tmp (reg val))
            (assign exp ((op same?-second) (reg unev)))
      13.
      14.
            (save tmp)
      15.
            (save unev)
      16.
      17.
            (assign continue eval-after-second)
      18.
      19. eval-after-second
      20.
            (restore unev)
      21.
      22.
            (restore tmp)
     23.
            (test (op eq?)
            (branch (label eval-third-arg))
      24.
            (assign val #f)
      25.
      26.
            (goto (reg continue))
      27.
      28. eval-third-arg
      29.
            (assign exp ((op same?-third) (reg unev)))
     30.
      31.
            (save tmp)
      32.
            (goto -
      33. eval-after-third
      34.
            (restore tmp)
      35.
            (test (op eq?)
     36.
      37.
            (branch (label all-same))
      38.
            (assign val #f)
      39.
            (goto (reg continue))
      40. all-same
            (assign val #t)
      41.
            (goto (reg continue))
Does this same? operation handle tail recursion? Why or why not?
For example, is the following recursive or iterative?
(define (foo x y)
  (same? (even? x) (even? y) (foo x (/ y 2))))
```

Concurrency

Consider the following definitions of x and y

```
(define x 2)
(define y 3)
```

In the table below, list all possible final values of z after the following expressions are evaluated.

```
(parallel-execute
  (lambda () (set! x (+ y y)))
   (lambda () (set! y (* x y))))

(define z (list x y))
```

Implementing Put and Get

Assume that we have one global put and get table called *global-put-table*. Define (a simplified version of) put and get as follows².

```
(put keys value) -- Places the value in the global table indexed by keys
   (get keys)
                     ==> value
For example,
   (put '(6001 is) 'fun)
   (put '(the season is) 'spring)
   (get '(6001 is))
   (put '(6001 is) '(almost over))
   (put 'year 1999)
   (get 'house)
                                         #f
   (get '(6001 is))
                                         (almost over)
   (get 'year)
                                         1999
Complete the following three definitions for put and get.
                                                  )
   (define *global-put-table*
   (define (put keys value)
   (define (get keys)
```

²Note that the put we used before took any number of keys such as (put 'a 'b '(c d) 5) and then to retrieve, (get 'a 'b '(c d)) ==> 5. For this example, we'll be simplifying it to take one list of keys.

Register Machines

Draw the Data Paths AND Controller for a machine to compute whether the input x is odd by successively subtracting 1 from the input. You can assume that the input will be a positive integer. Assume the only primitive operations you have are subtraction, logical not, and testing equality. After your machine finishes running, the result in the answer register should be either #t or #f.





Compilers

Consider the following compiled code:

```
(assign val (op make-compiled-procedure) (label entry23) (reg env))
         (goto (label after-lambda22))
     3. entry23
         (assign env (op compiled-procedure-env) (reg proc))
         (assign env (op extend-environment) (const (f c)) (reg argl) (reg env))
     6.
         (save continue)
     7.
         (save env)
     8.
         (assign proc (op lookup-variable-value) (const c) (reg env))
     9.
          (assign val (op lookup-variable-value) (const f) (reg env))
          (assign argl (op list) (reg val))
    10.
          (test (op primitive-procedure?) (reg proc))
    11.
          (branch (label primitive-branch29))
    12.
    13. compiled-branch28
          (assign continue (label proc-return30))
          (assign val (op compiled-procedure-entry) (reg proc))
    15.
    16.
         (goto (reg val))
    17. proc-return30
    18.
          (assign proc (reg val))
    19.
          (goto (label after-call27))
    20. primitive-branch29
         (assign proc (op apply-primitive-procedure) (reg proc) (reg argl))
    21.
    22. after-call27
    23.
          (restore env)
    24.
          (restore continue)
    25.
          (assign val (op lookup-variable-value) (const f) (reg env))
          (test (op false?) (reg val))
    27.
          (branch (label false-branch25))
    28. true-branch26
    29.
          (assign val (const 1))
          (goto (label after-if24))
    30.
    31. false-branch25
    32. (assign val (const 2))
    33. after-if24
    34.
         (assign argl (op list) (reg val))
         (assign val (op lookup-variable-value) (const a) (reg env))
    35.
         (assign argl (op cons) (reg val) (reg argl))
    36.
    37.
          (test (op primitive-procedure?) (reg proc))
          (branch (label primitive-branch33))
    38.
    39. compiled-branch32
         (assign val (op compiled-procedure-entry) (reg proc))
         (goto (reg val))
    41.
    42. primitive-branch33
    43.
          (assign val (op apply-primitive-procedure) (reg proc) (reg argl))
    44. (goto (reg continue))
    45. after-call31
    46. after-lambda22
          (perform (op define-variable!) (const a) (reg val) (reg env))
          (assign val (const ok))
Decompile the following groups of code. (Hint: Don't worry if the overall code looks a bit unusual.)
\implies Lines 8–22:
\implies Lines 25–33:
     > Lines 8–45:
     > Lines 1–48:
```