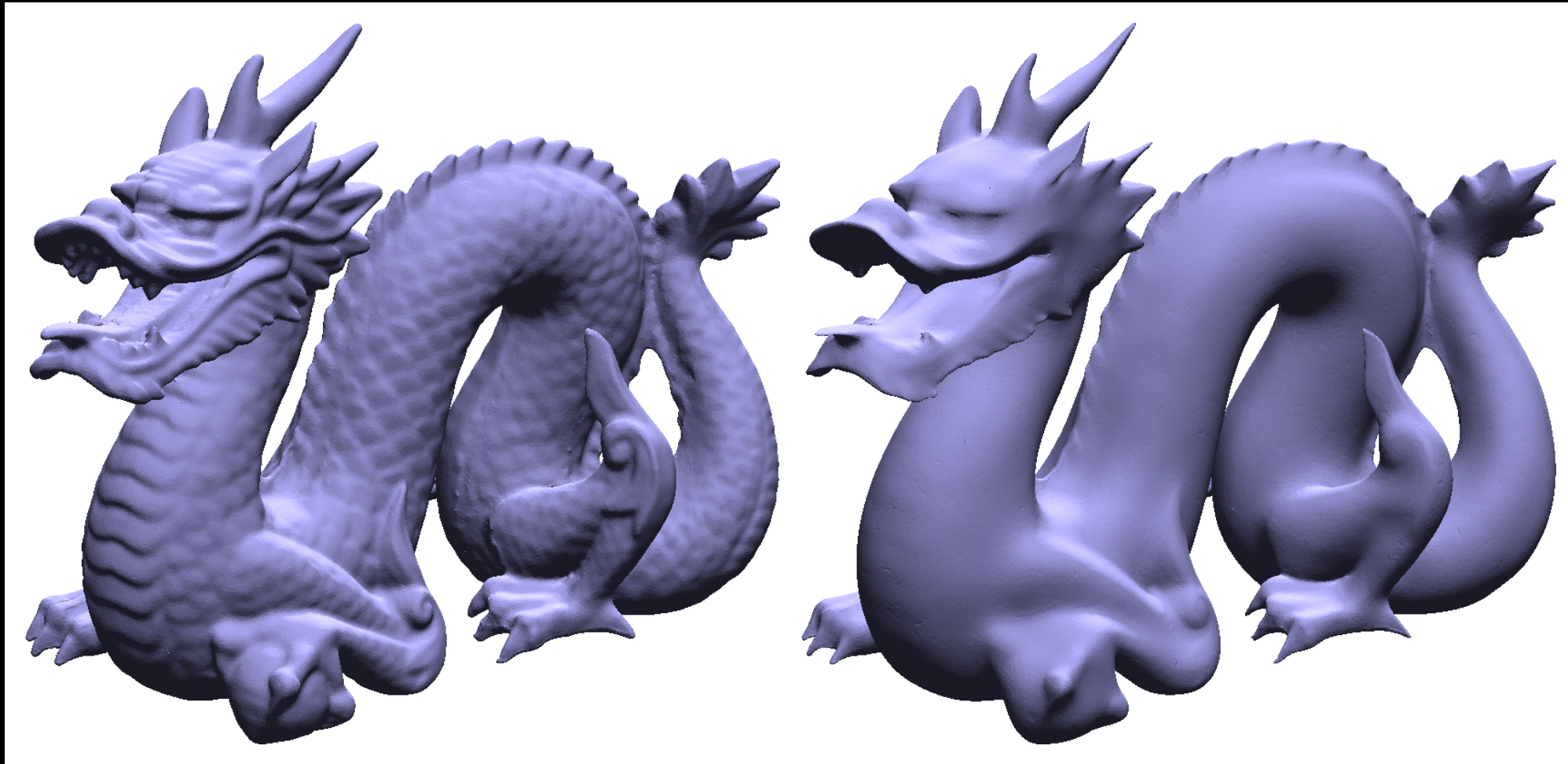


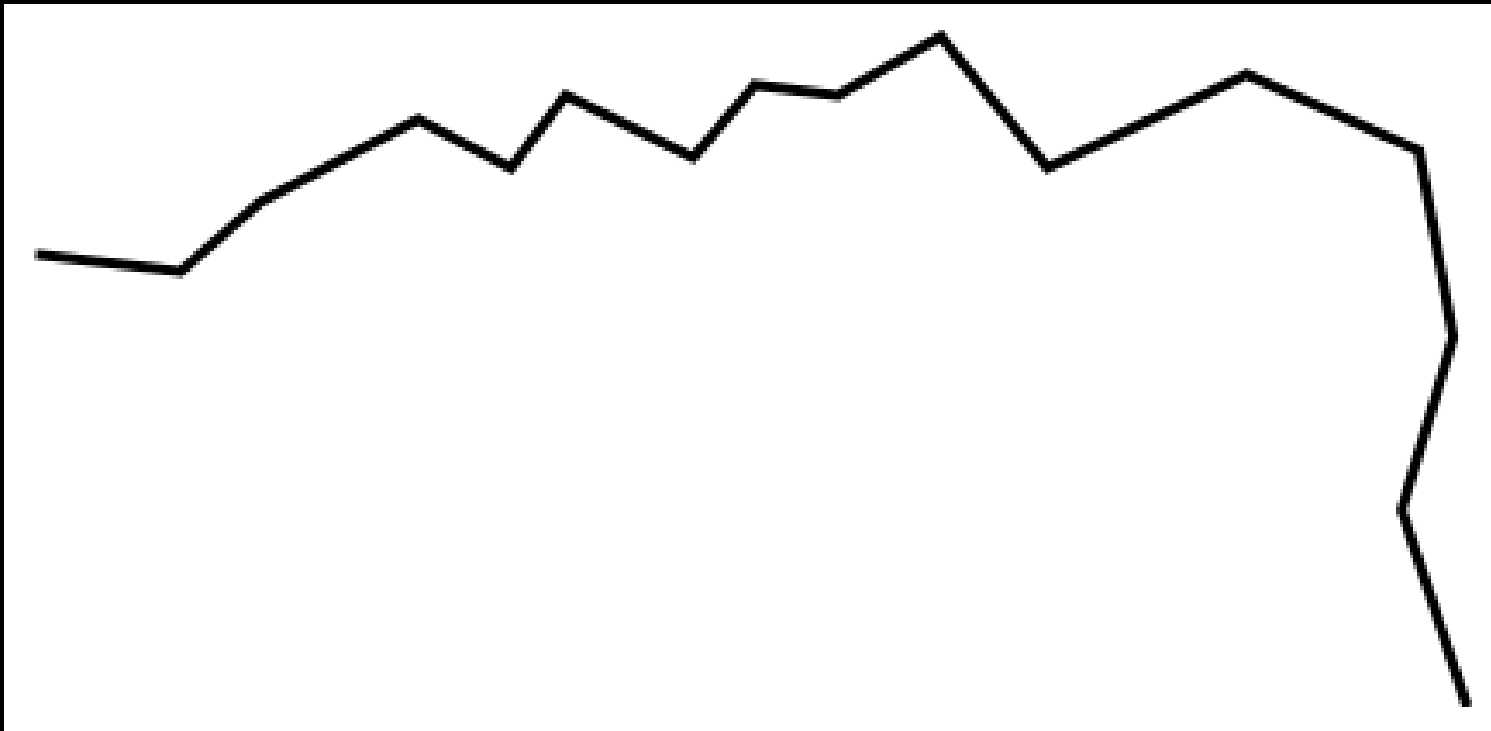
# Non-Iterative, Feature-Preserving Mesh Smoothing



Thouis R. Jones (MIT), Frédo Durand (MIT), Mathieu Desbrun (USC)  
*thouis@graphics.csail.mit.edu, fredod@graphics.csail.mit.edu, desbrun@usc.edu*

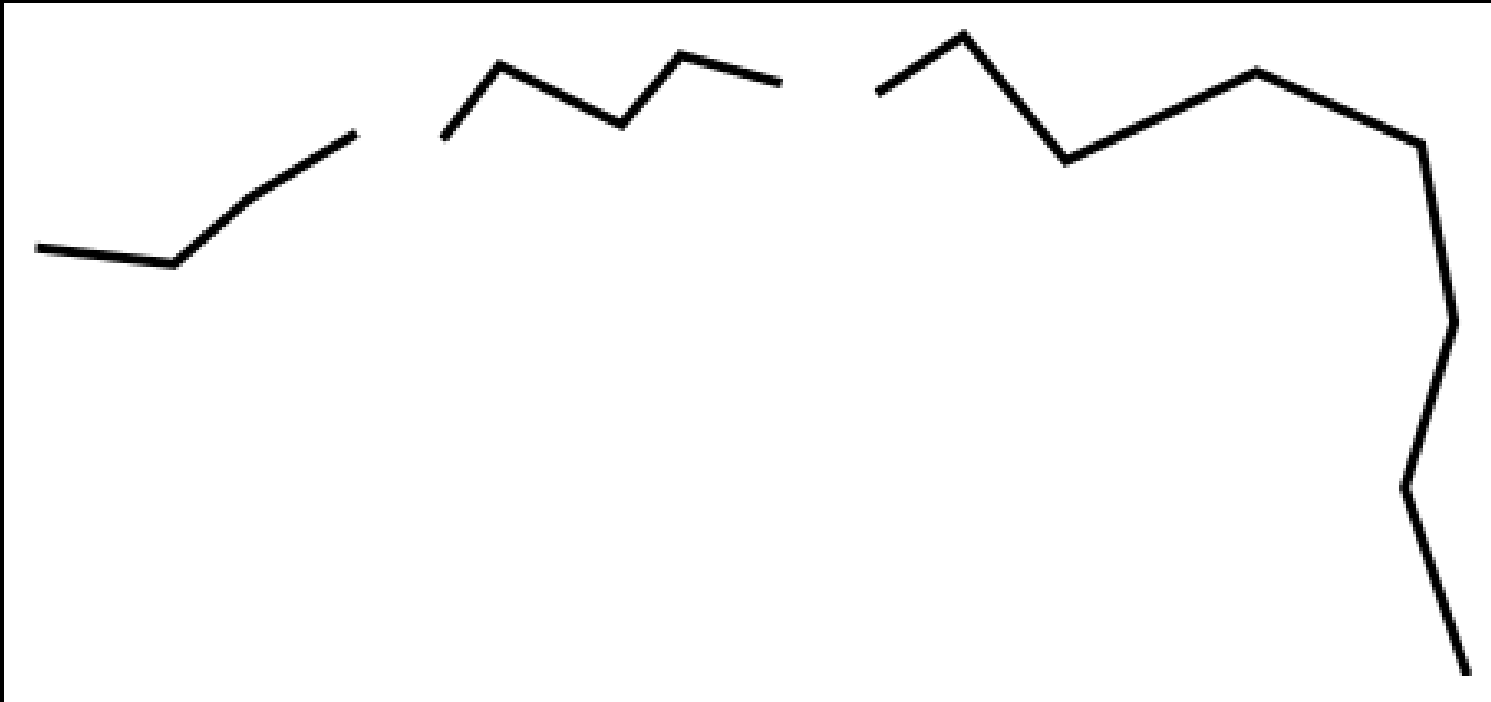
# Why Smooth?

3D scanners are noisy...



# Why Smooth?

3D scanners are noisy...  
and have dropouts...

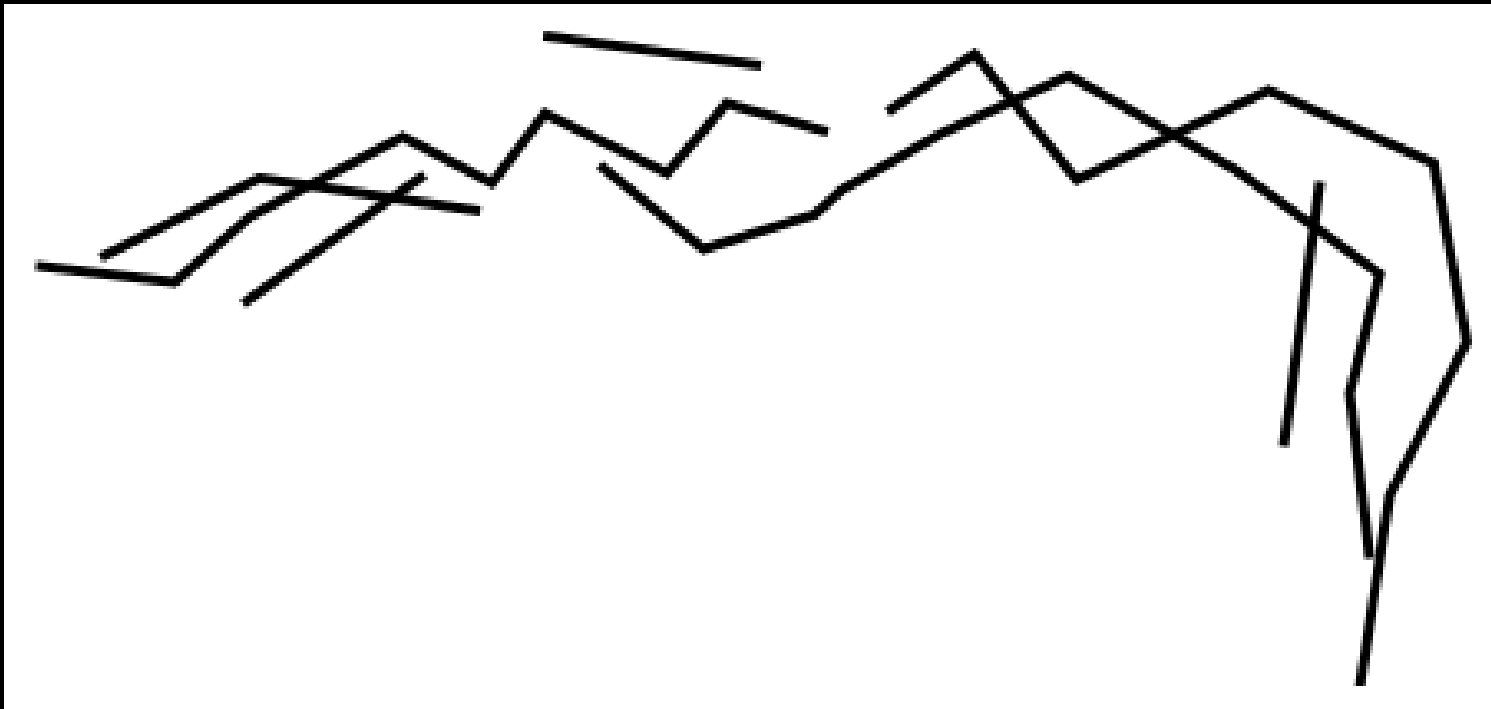


## Why Smooth?

3D scanners are noisy...

and have dropouts...

and usually require multiple scans.



# Goals

Fast smoothing of meshes

Robust

- Geometrically: preserve features
- Topologically: no connectivity information

*Simple to implement*

# Goals

Fast smoothing of ~~meshes~~ polygon soups

Robust

- Geometrically: preserve features
- Topologically: no connectivity information

*Simple to implement*



# Previous Work on Smoothing

## Fast Mesh Smoothing

- Taubin 1995; Desbrun et al. 1999

## Feature Preserving

- Clarenz et al. 2000; Desbrun et al. 2000; Meyer et al. 2002; Zhang and Fiume 2002; Bajaj and Xu 2003

## Diffusion on Normal Field

- Taubin 2001; Belyaev and Ohtake 2001; Ohtake et al. 2002; Tasdizen et al. 2002

## Wiener Filtering of Meshes

- Peng et al. 2001; Alexa 2002; Pauly and Gross 2001 (points)



## Approach

We cast feature-preserving filtering as a robust estimation problem on vertex positions.

Extend Bilateral Filter to 3D.

- Smith and Brady 1997; Tomasi and Manduchi 1998

Use first-order *predictors* based on facets of model.

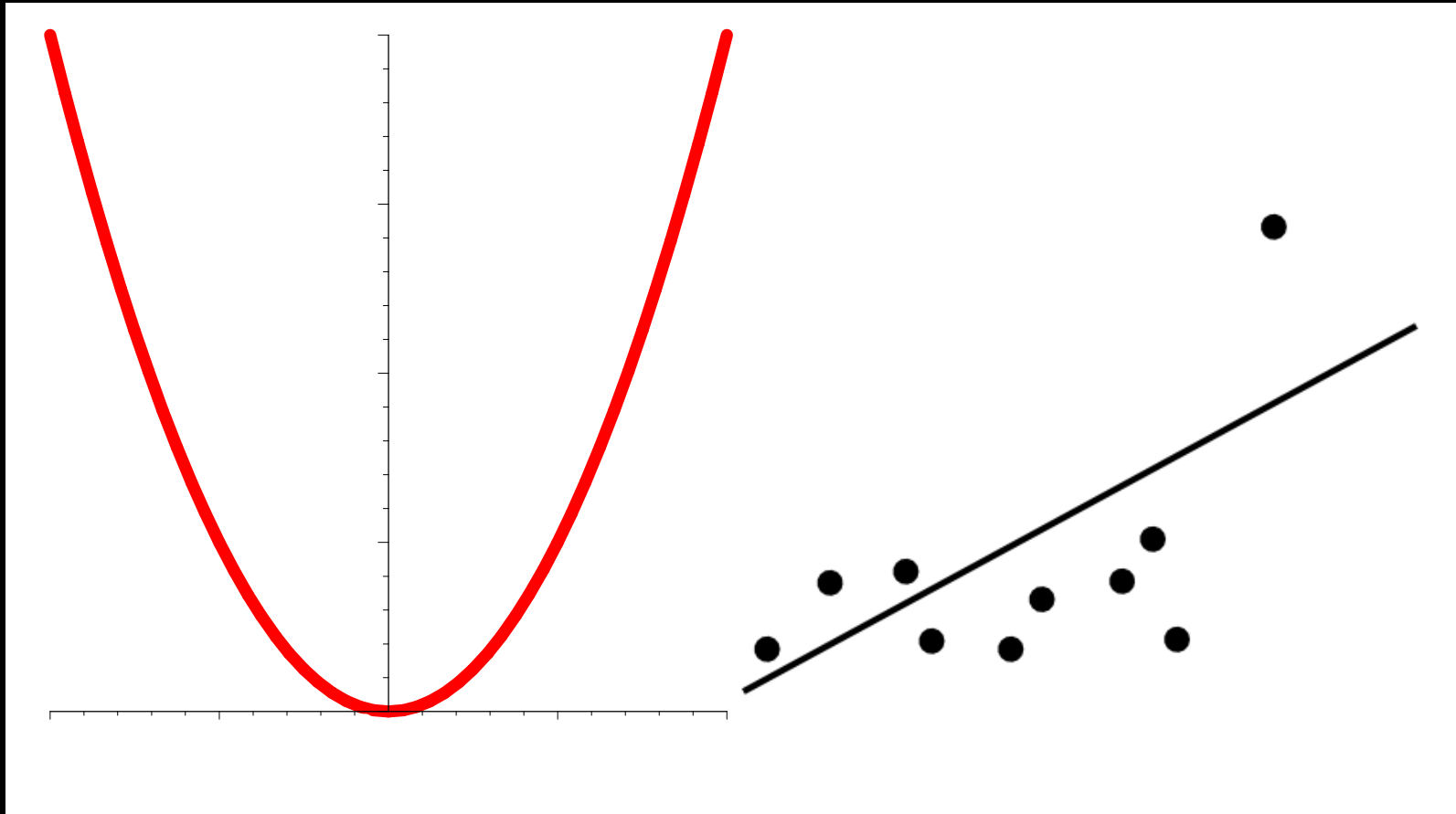
Single pass.





# Non-Robust Estimation

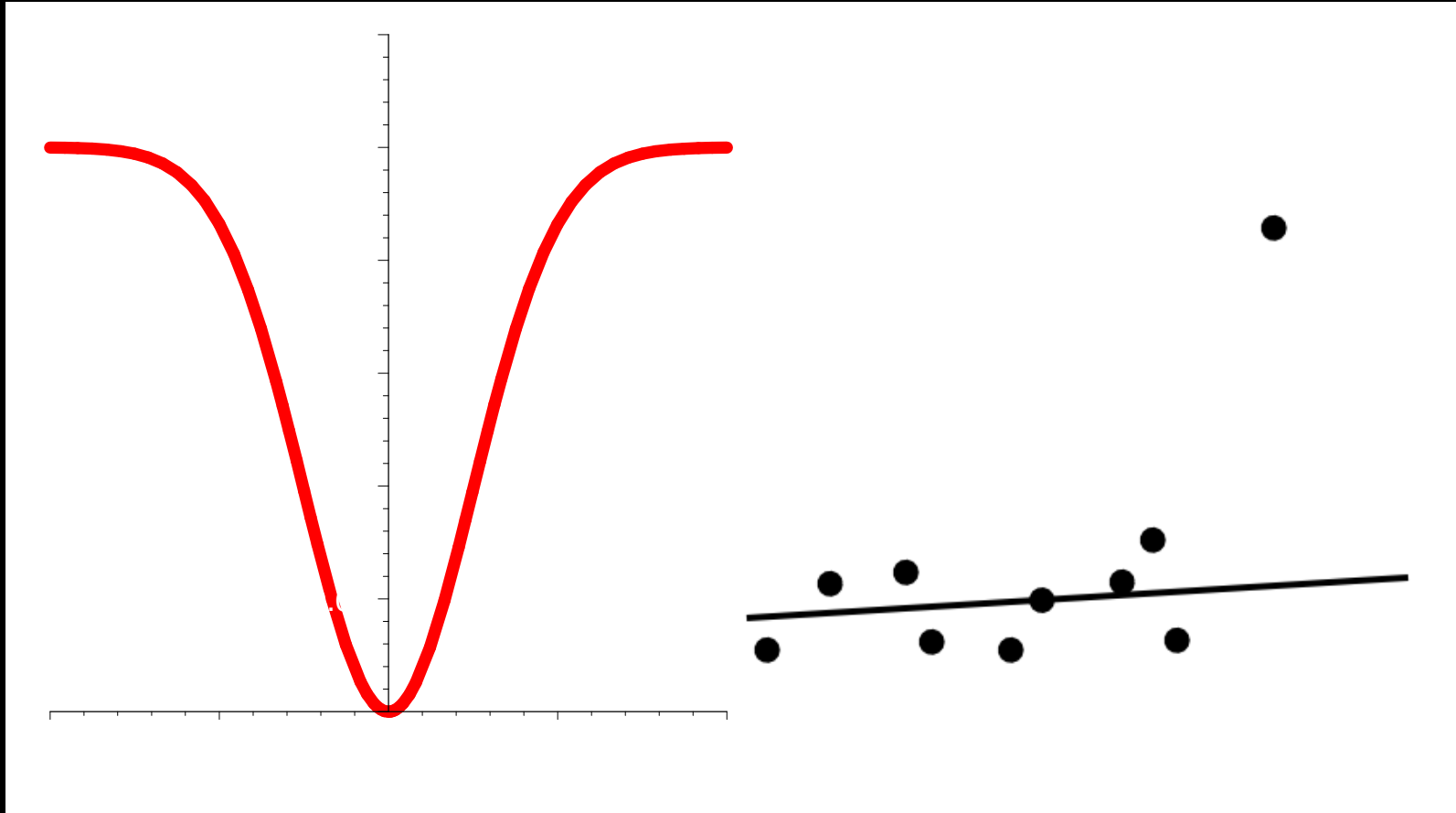
## Least Squares Error Norm



Outliers have unlimited influence on estimate.

# Robust Estimation

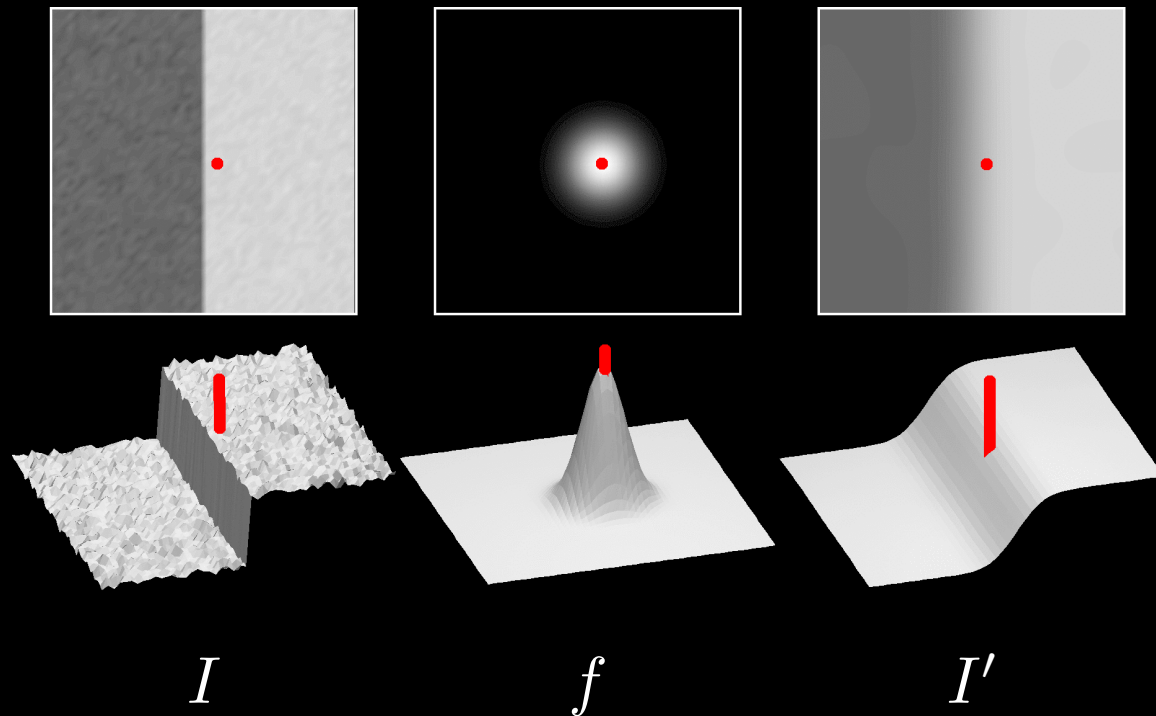
## Robust Error Norm



Outliers have bounded influence on estimate.

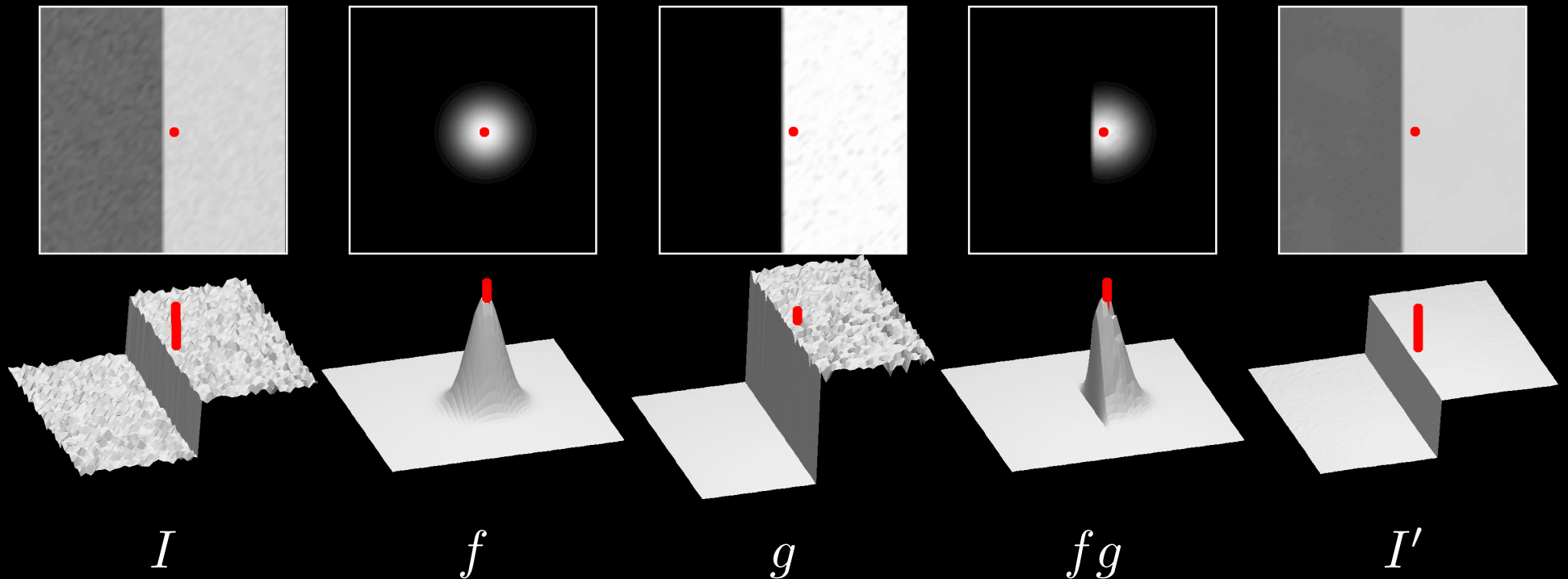
# Gaussian Filter (Non-robust)

$$I'_s = \sum_p \overbrace{I(p)}^{\text{image}} \overbrace{f(s-p)}^{\text{spatial}}$$



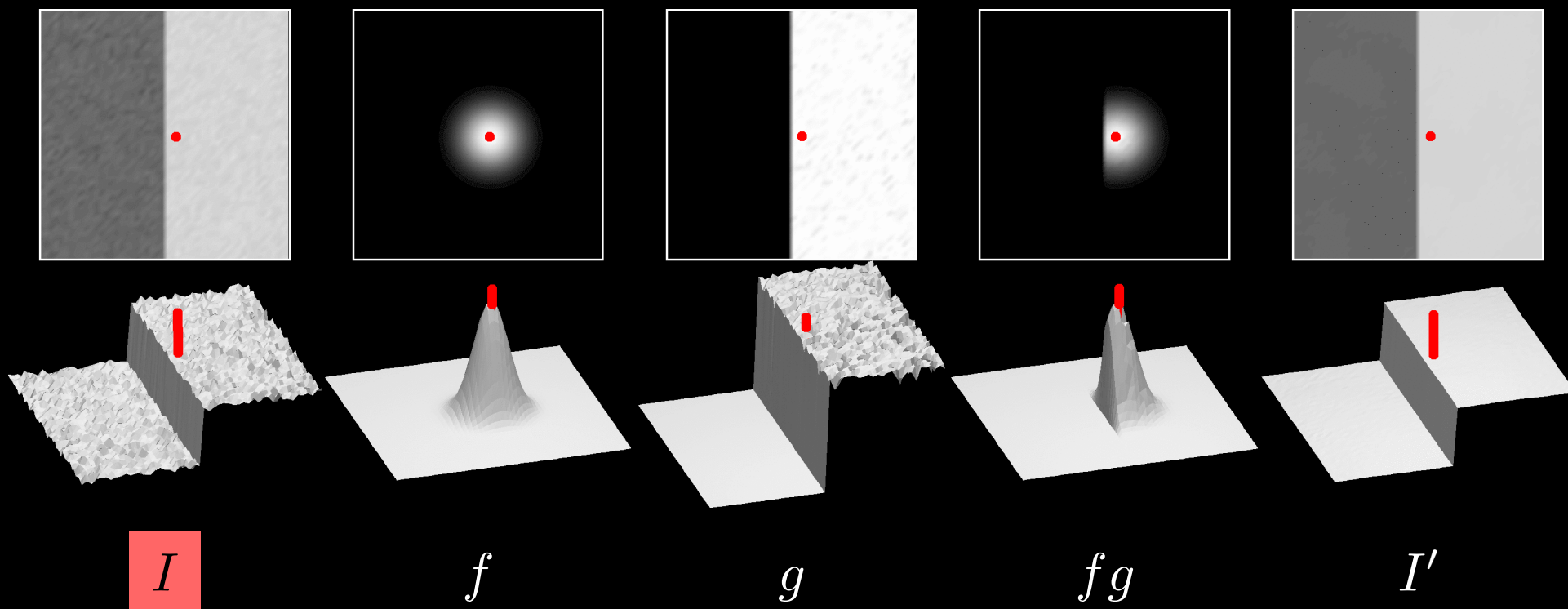
# Bilateral Filter (Robust)

$$I'_s = \frac{1}{k_s} \sum_p \underbrace{I(p)}_{\text{image}} \underbrace{f(s-p)}_{\text{spatial}} \underbrace{g(I_s - I_p)}_{\text{influence}}$$



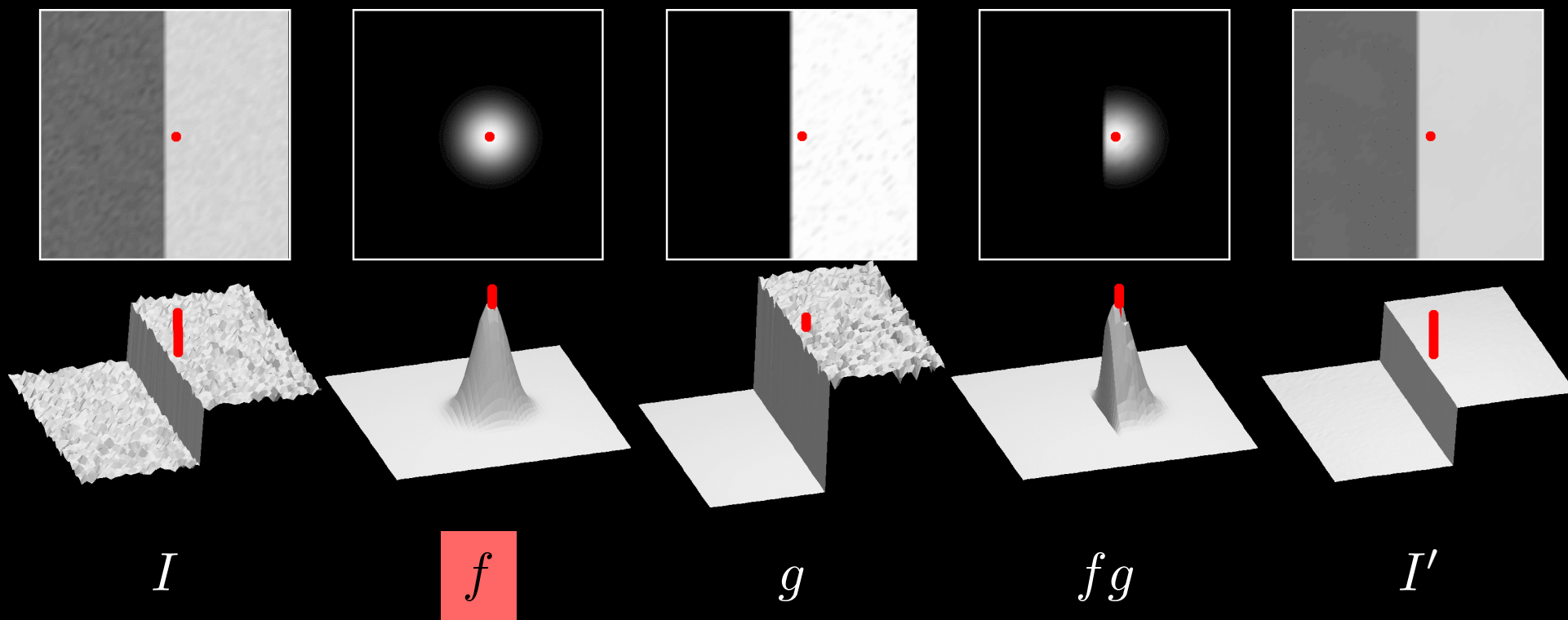
# Bilateral Filter (Robust)

$$I'_s = \frac{1}{k_s} \sum_p \overbrace{I(p)}^{\text{image}} \overbrace{f(s-p)}^{\text{spatial}} \overbrace{g(I_s - I_p)}^{\text{influence}}$$



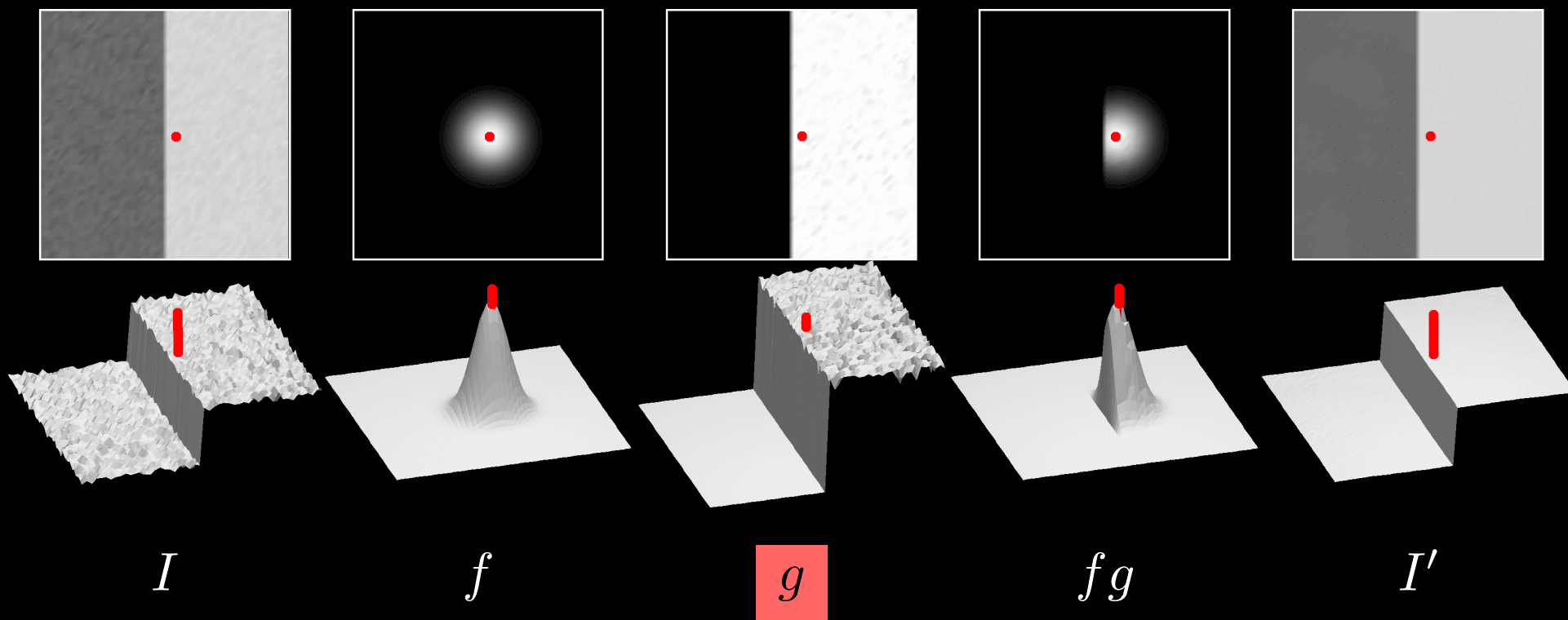
# Bilateral Filter (Robust)

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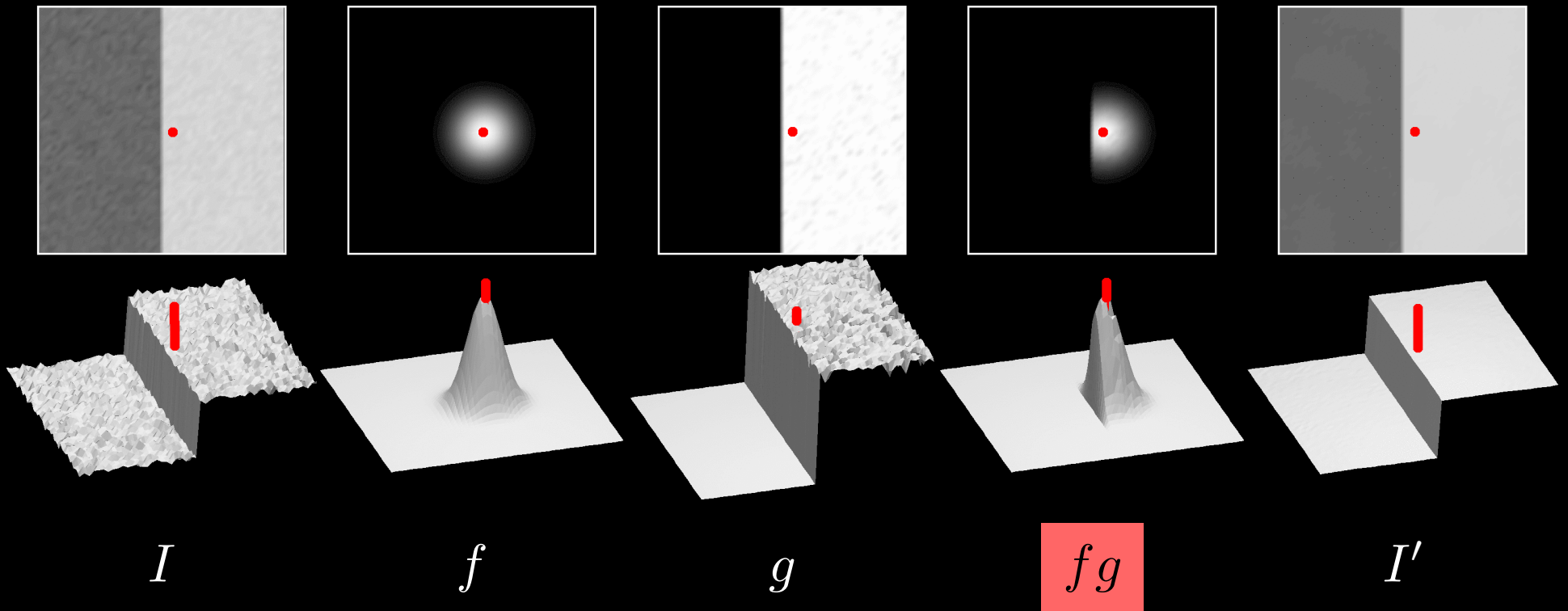
# Bilateral Filter (Robust)

$$I'_s = \frac{1}{k_s} \sum_p \underbrace{I(p)}_{\text{image}} \underbrace{f(s-p)}_{\text{spatial}} \underbrace{g(I_s - I_p)}_{\text{influence}}$$



# Bilateral Filter (Robust)

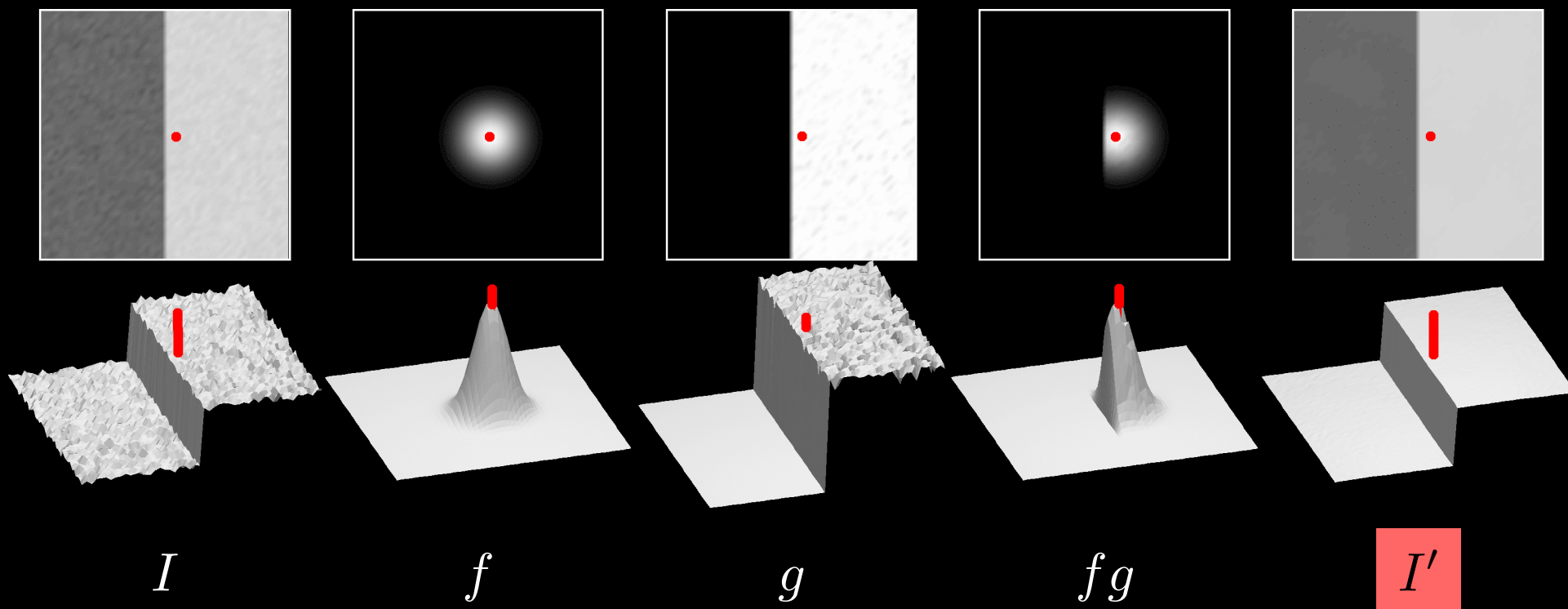
$$I'_s = \frac{1}{k_s} \sum_p \underbrace{I(p)}_{\text{image}} \underbrace{f(s-p)}_{\text{spatial}} \underbrace{g(I_s - I_p)}_{\text{influence}}$$





# Bilateral Filter (Robust)

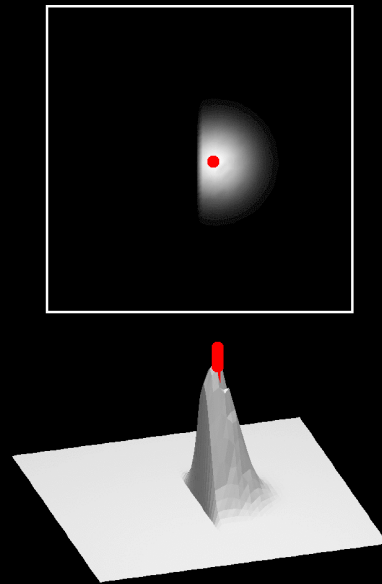
$$I'_s = \frac{1}{k_s} \sum_p \underbrace{I(p)}_{\text{image}} \underbrace{f(s-p)}_{\text{spatial}} \underbrace{g(I_s - I_p)}_{\text{influence}}$$



# Bilateral Filter (Robust)

$$I'_s = \frac{1}{k_s} \sum_p \overbrace{I(p)}^{\text{image}} \overbrace{f(s-p)}^{\text{spatial}} \overbrace{g(I_s - I_p)}^{\text{influence}}$$

$$k_s = \sum_p f(s-p) g(I_s - I_p)$$



# Bilateral Filter



Left: Jones and Jones 2003



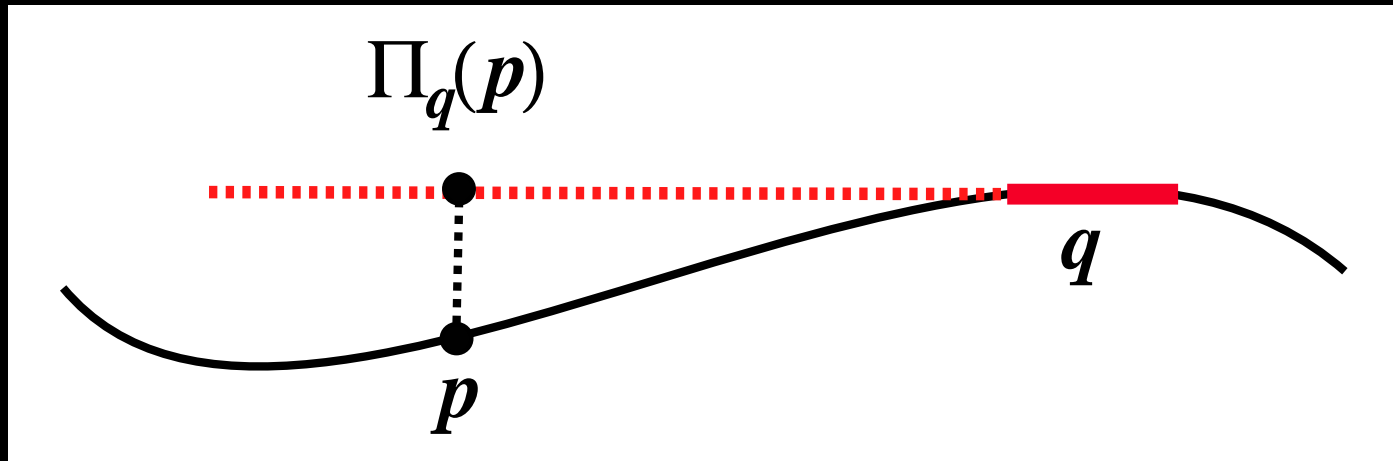
Right: Bilaterally filtered.

# Extending the Bilateral Filter to Meshes

How to separate location and signal in a 3D model?

- Forming local frames requires a connected mesh.

Instead, use first-order predictors based on facets:

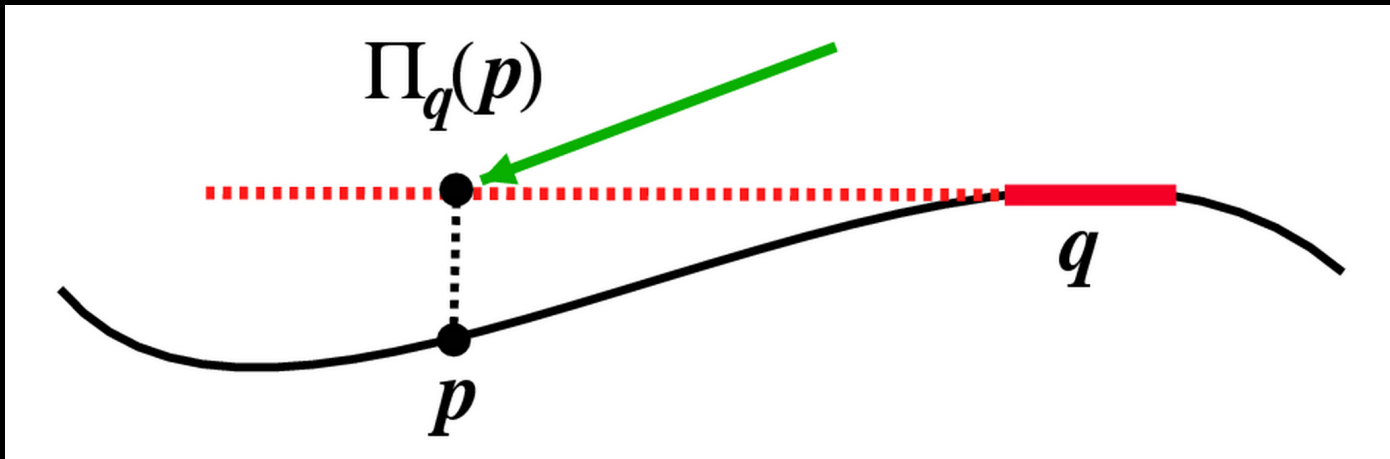


*No connectivity required between facets.*

# Bilateral Filter for Meshes

Estimate  $p'$ , the new position for a vertex  $p$

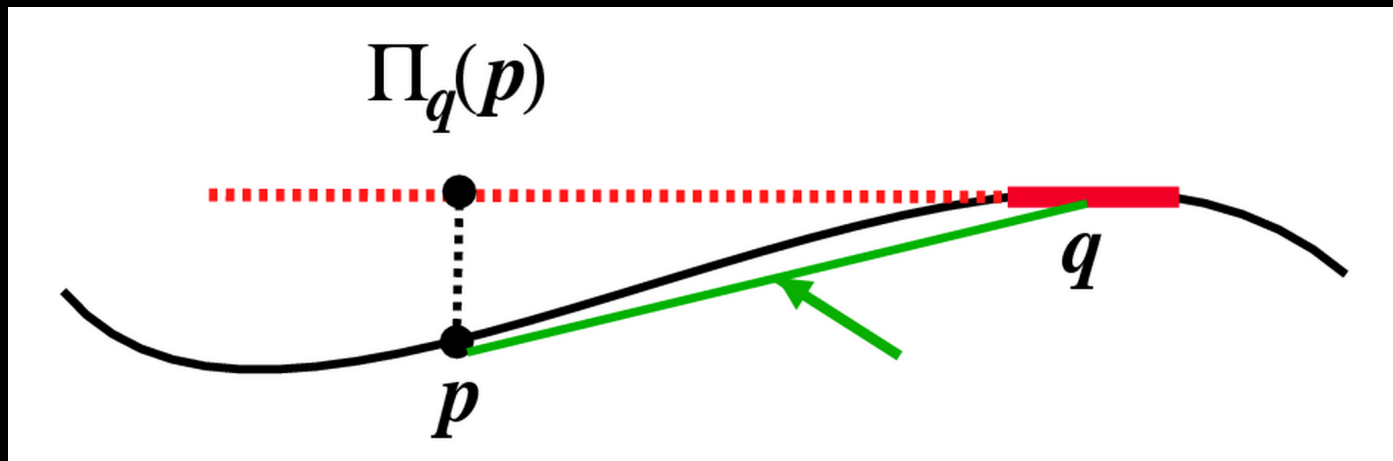
$$p' = \frac{1}{k(p)} \sum_{q \in S} \overbrace{\Pi_q(p)}^{\text{prediction}} \overbrace{f(\|c_q - p\|)}^{\text{spatial}} \overbrace{g(\|\Pi_q(p) - p\|)}^{\text{influence}} \overbrace{a_q}^{\text{area}}$$



# Bilateral Filter for Meshes

Estimate  $p'$ , the new position for a vertex  $p$

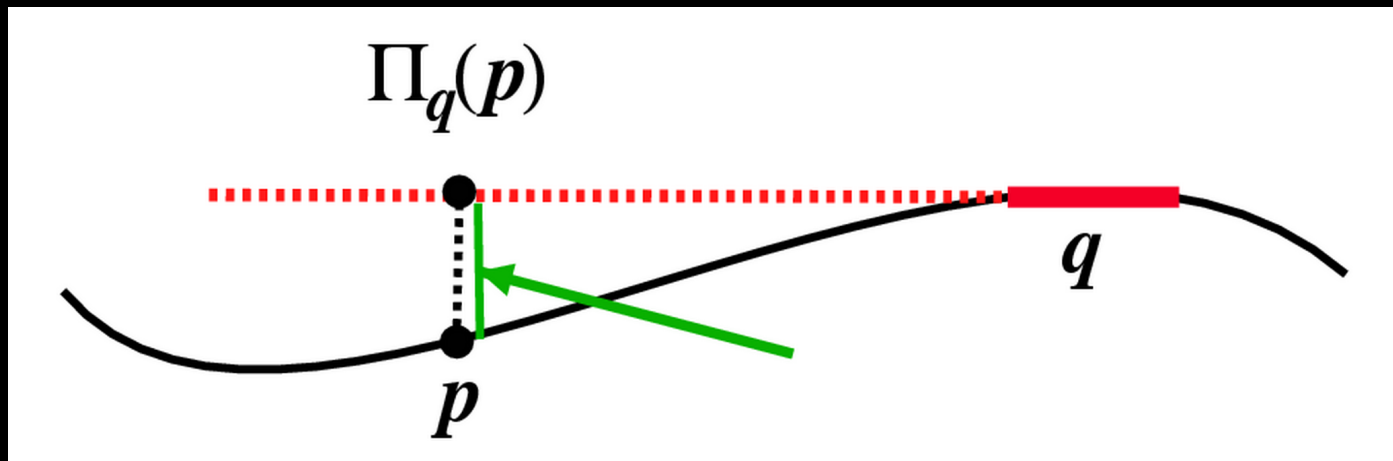
$$p' = \frac{1}{k(p)} \sum_{q \in S} \overbrace{\Pi_q(p)}^{\text{prediction}} \overbrace{f(\|c_q - p\|)}^{\text{spatial}} \overbrace{g(\|\Pi_q(p) - p\|)}^{\text{influence}} \overbrace{a_q}^{\text{area}}$$



# Bilateral Filter for Meshes

Estimate  $p'$ , the new position for a vertex  $p$

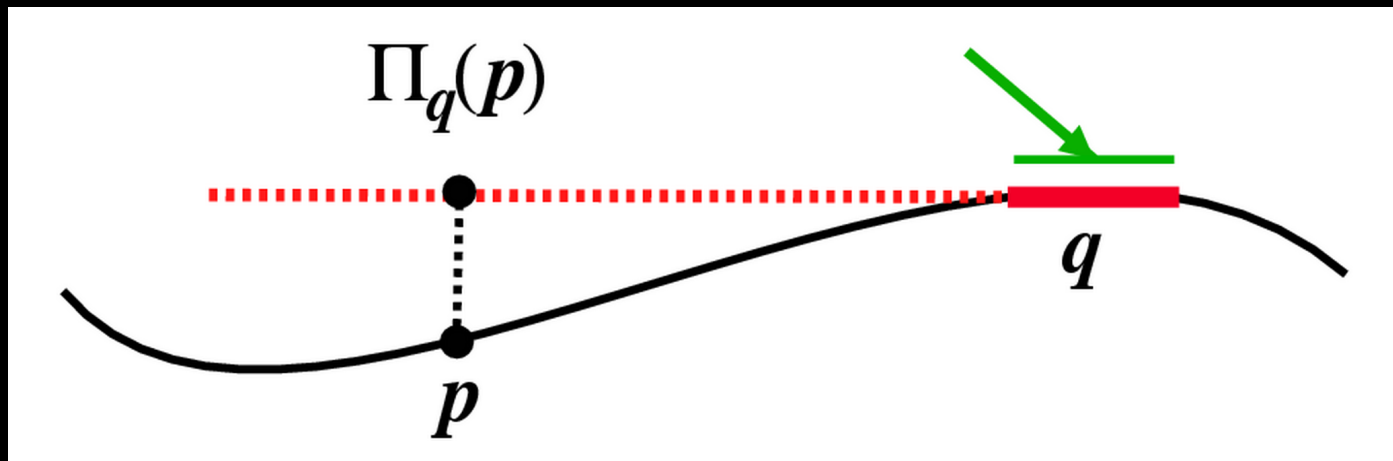
$$p' = \frac{1}{k(p)} \sum_{q \in S} \overbrace{\Pi_q(p)}^{\text{prediction}} \overbrace{f(\|c_q - p\|)}^{\text{spatial}} \overbrace{g(\|\Pi_q(p) - p\|)}^{\text{influence}} \overbrace{a_q}^{\text{area}}$$



# Bilateral Filter for Meshes

Estimate  $p'$ , the new position for a vertex  $p$

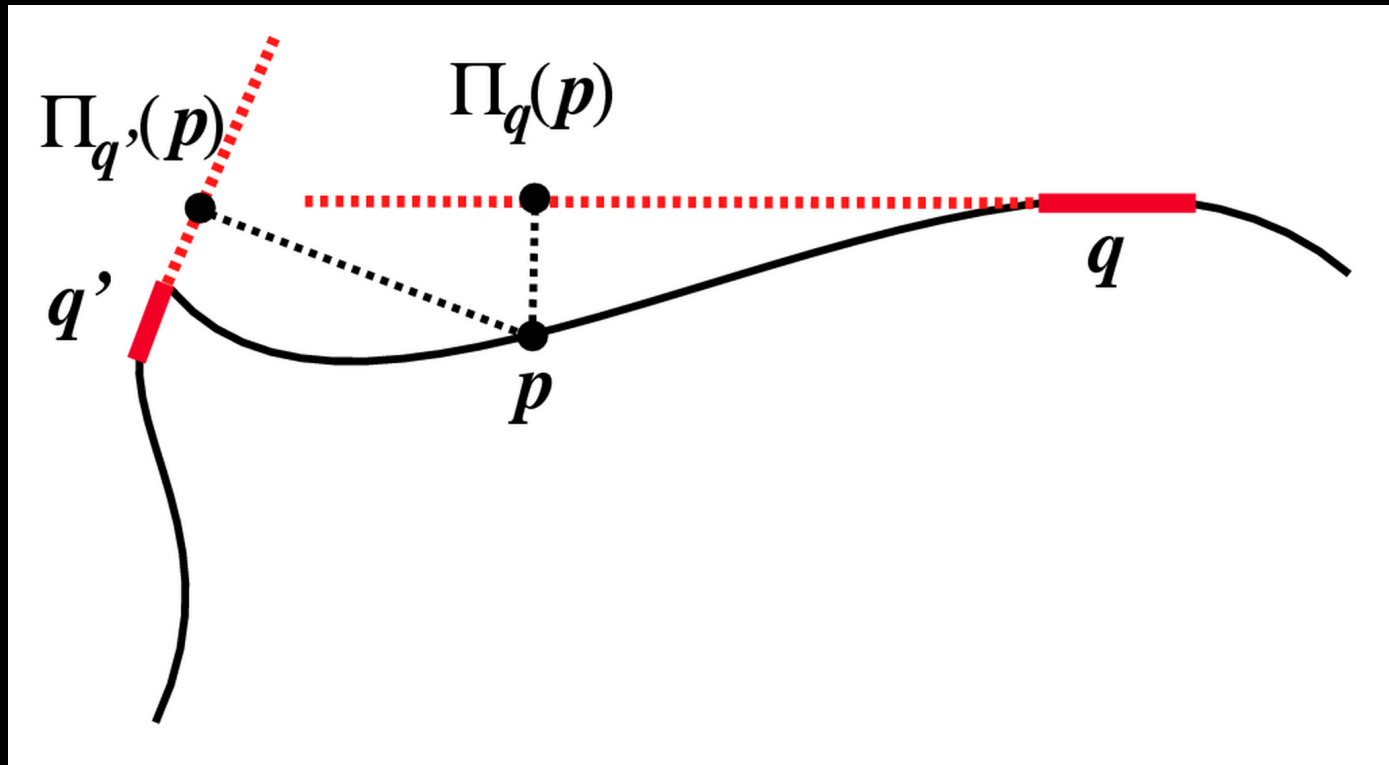
$$p' = \frac{1}{k(p)} \sum_{q \in S} \overbrace{\Pi_q(p)}^{\text{prediction}} \overbrace{f(\|c_q - p\|)}^{\text{spatial}} \overbrace{g(\|\Pi_q(p) - p\|)}^{\text{influence}} \overbrace{a_q}^{\text{area}}$$





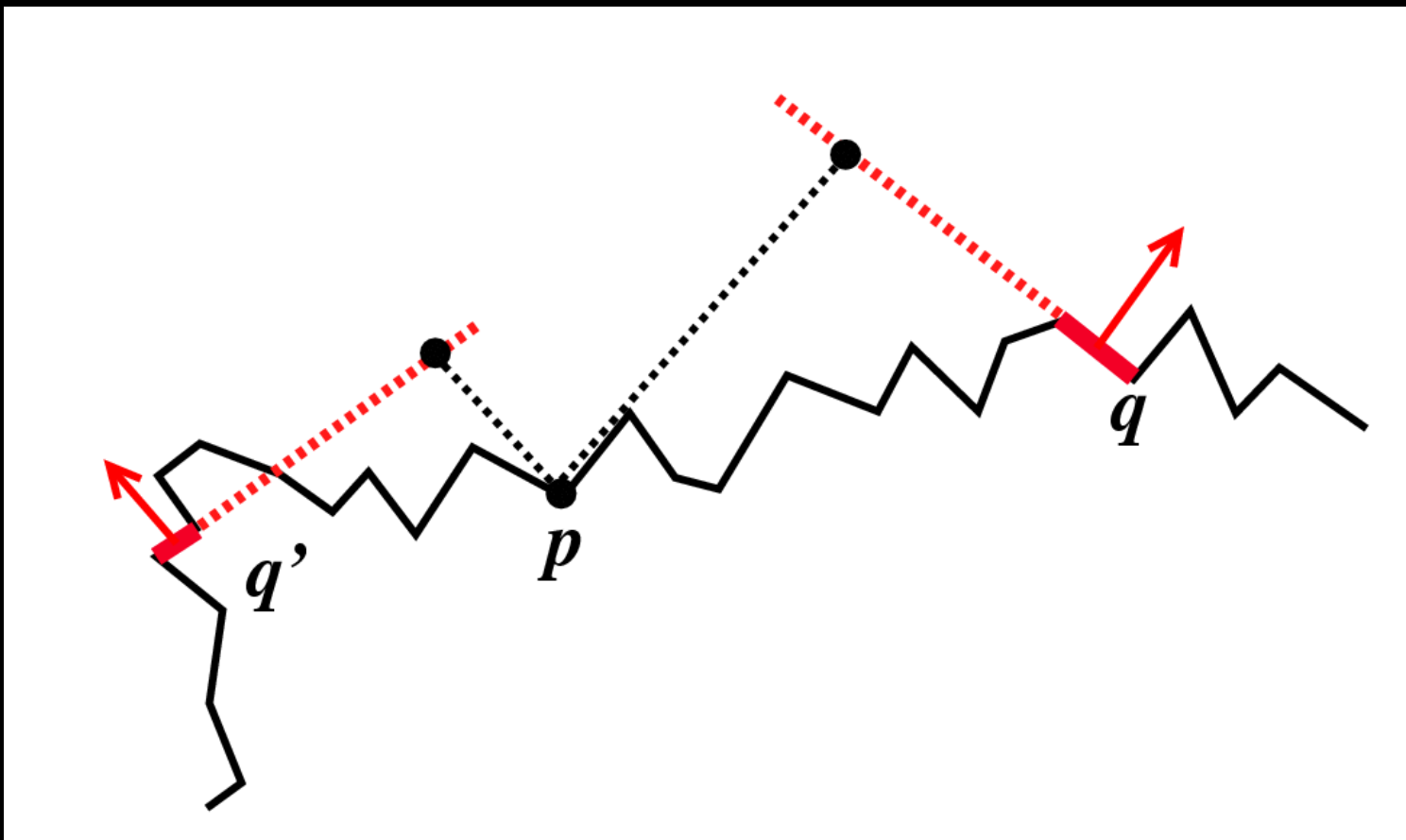
# Why we expect it to work

Predictions across corners are “outliers”.



# Dealing with Noise

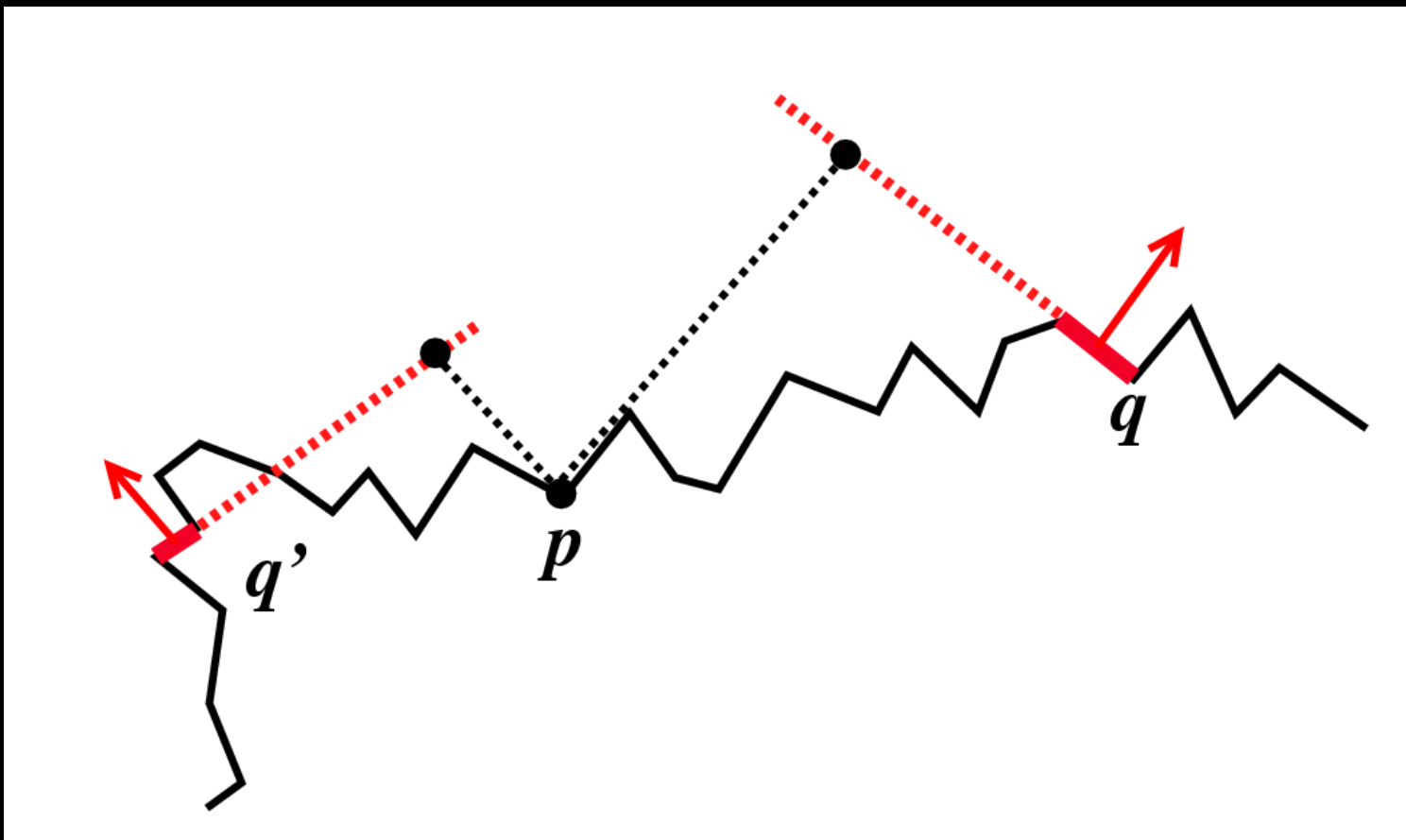
Noise has a nonlinear effect on predictions.



# Dealing with Noise

Noise has a nonlinear effect on predictions.

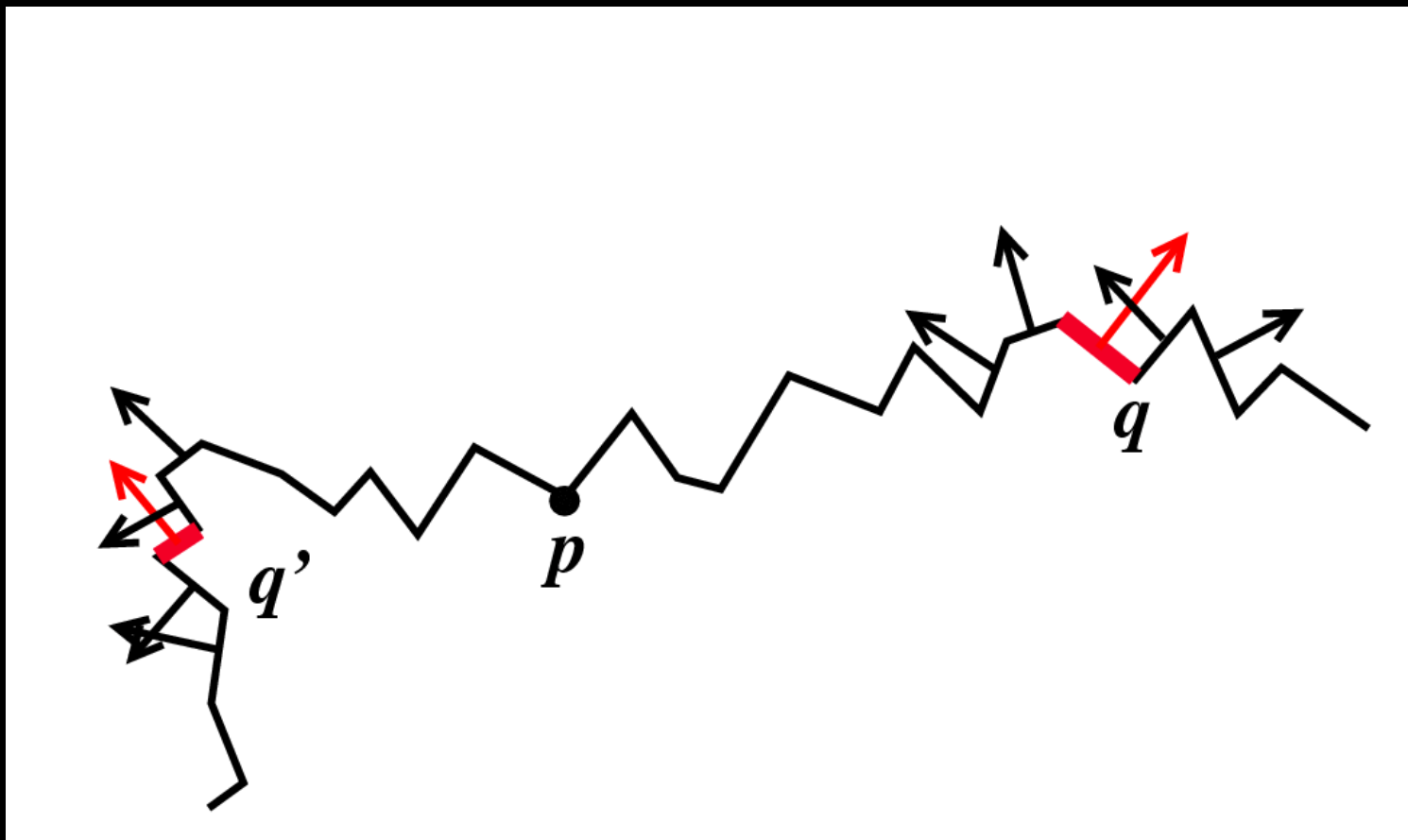
We must *mollify* (pre-smooth) normals.



# Dealing with Noise

Noise has a nonlinear effect on predictions.

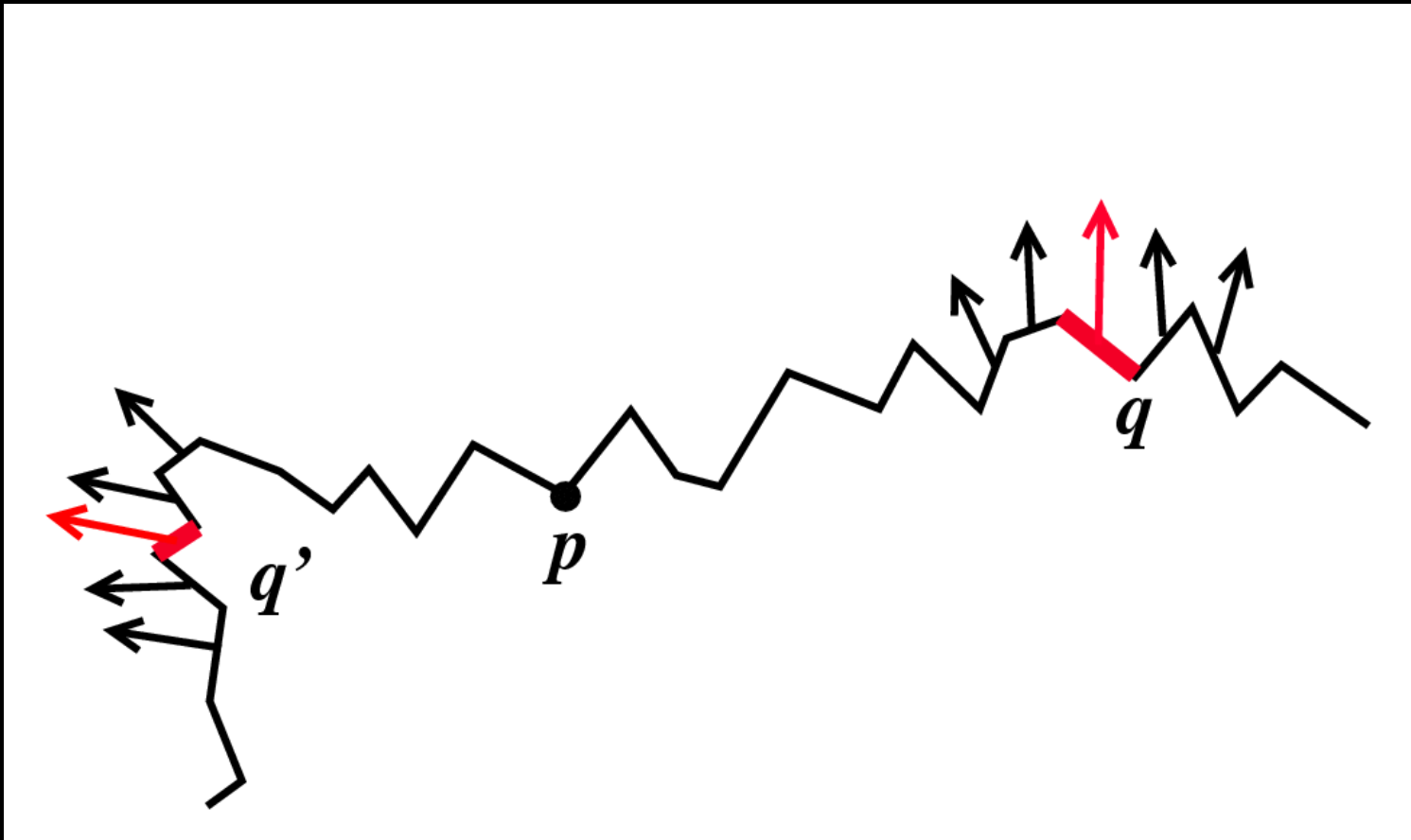
We must *mollify* (pre-smooth) normals.



# Dealing with Noise

Noise has a nonlinear effect on predictions.

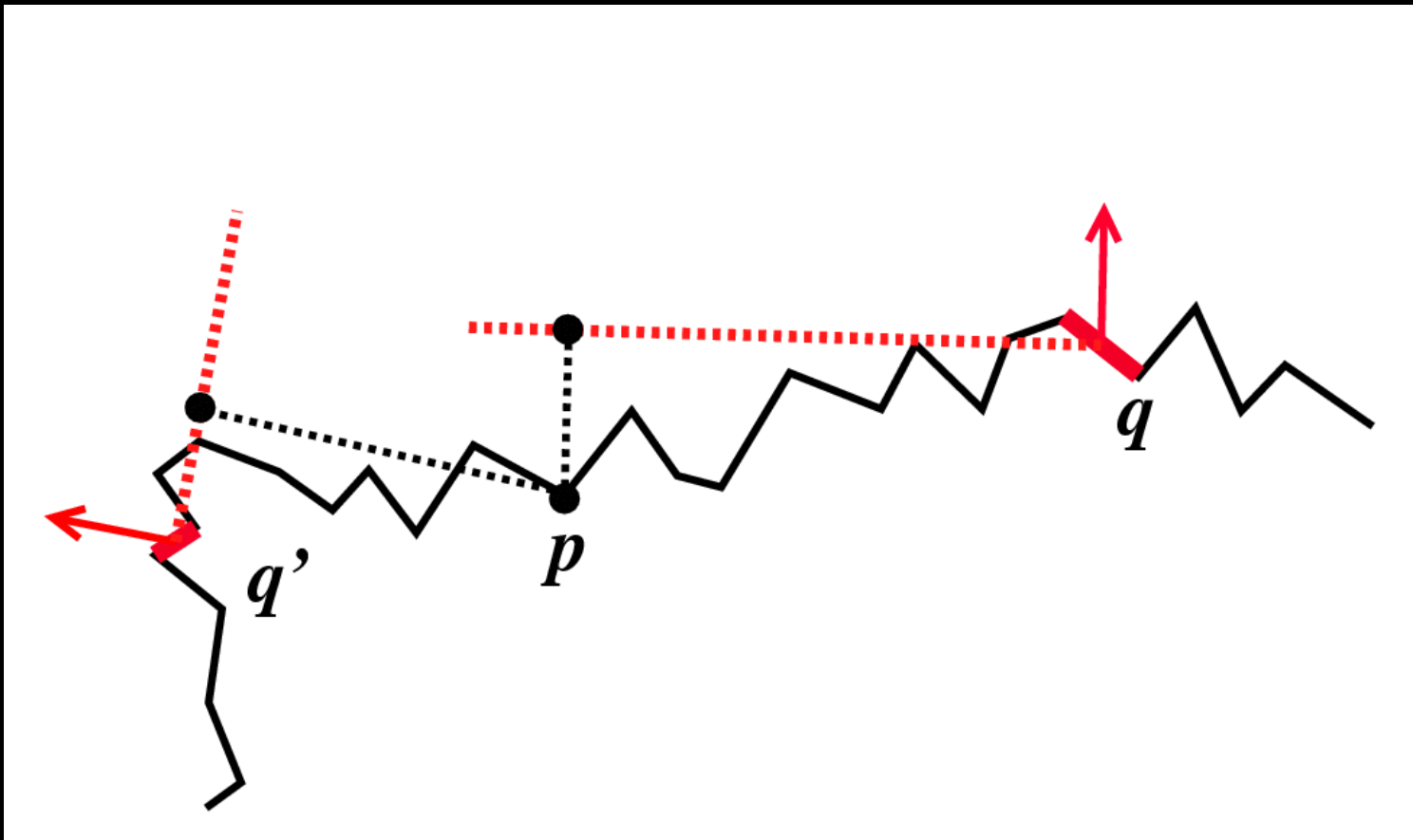
We must *mollify* (pre-smooth) normals.



## Dealing with Noise

Noise has a nonlinear effect on predictions.

We must *mollify* (pre-smooth) normals.



# Implementation

3K vertices / second (typical), 1.4 GHz Athlon.

Gaussians for  $f$  and  $g$ .

## Optimizations

- Cutoff at twice spatial filter radius.
- Binning for spatially coherent computation.

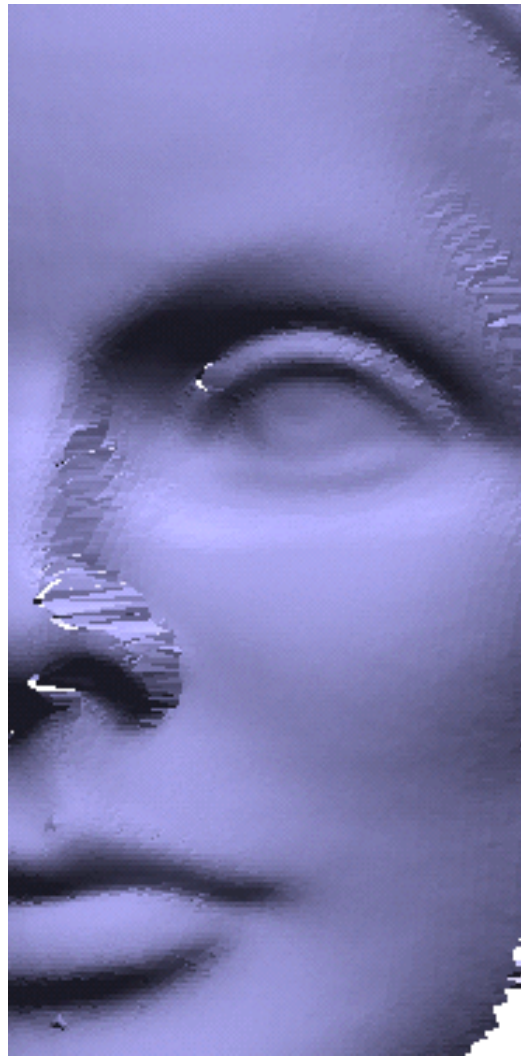
Data and non-optimized code available online.



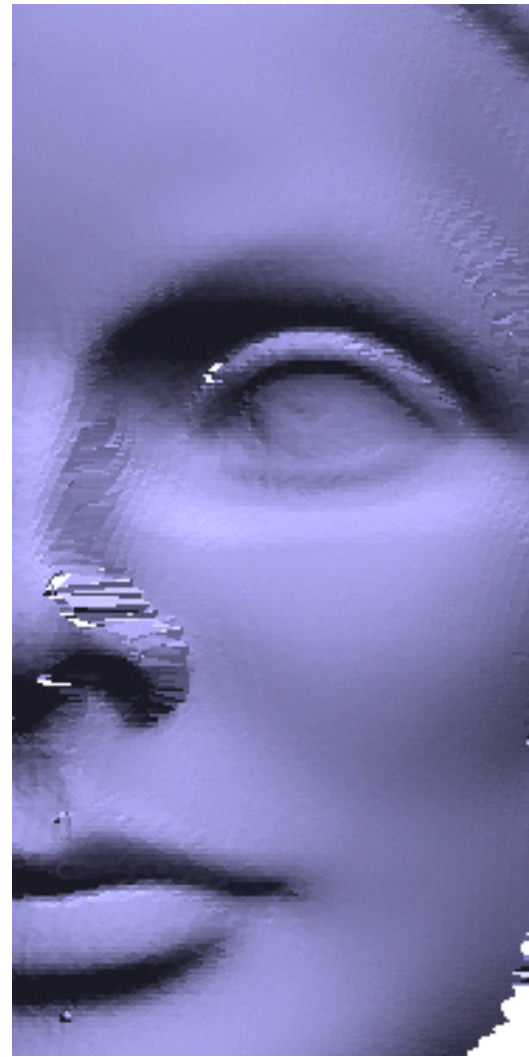
# Results - Smoothing



Original



Desbrun 1999



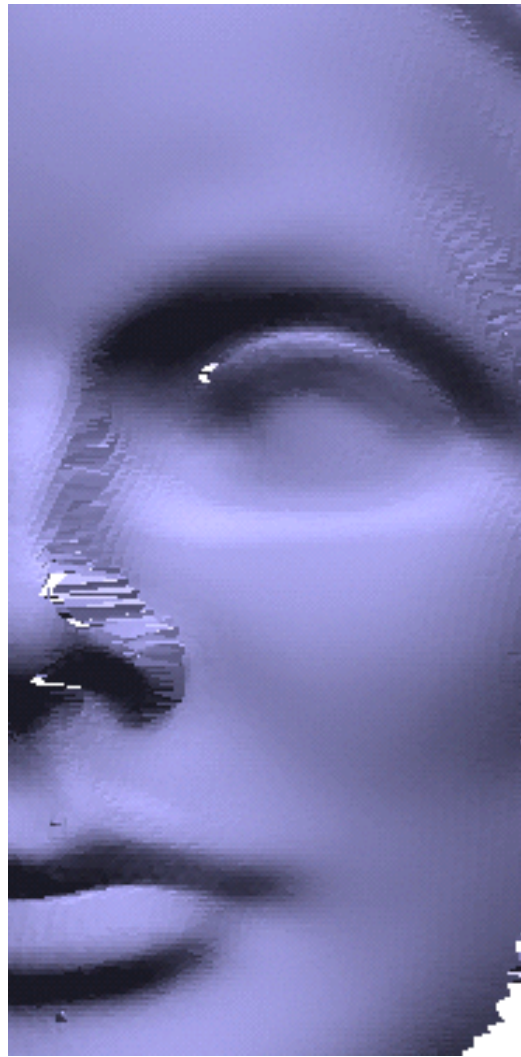
Our result



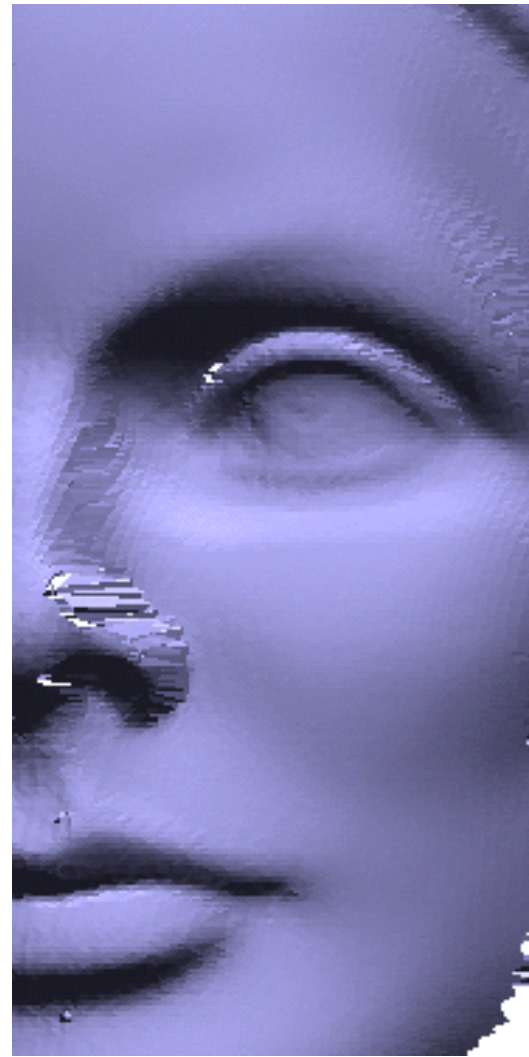
# Results - Effect of $g$



Original



Without  $g$

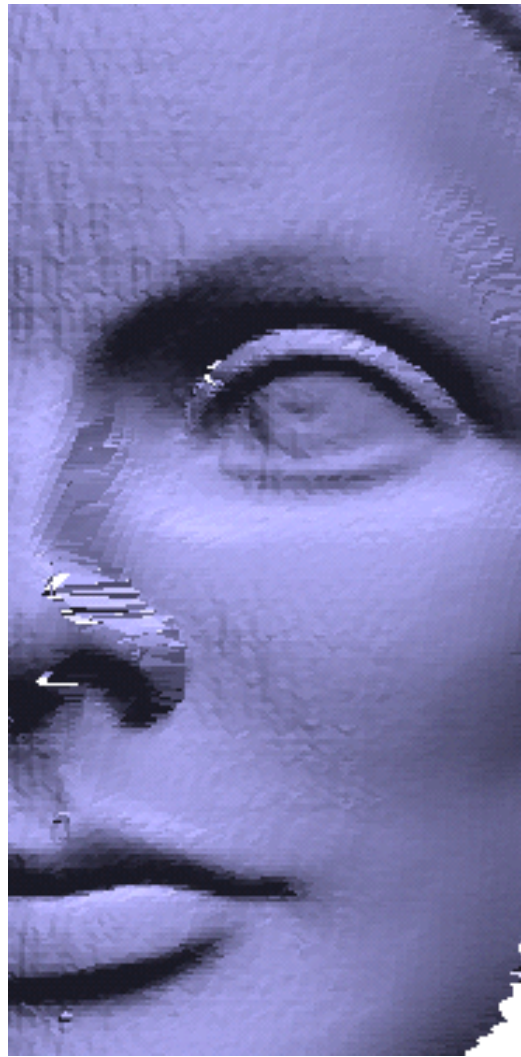


Our result

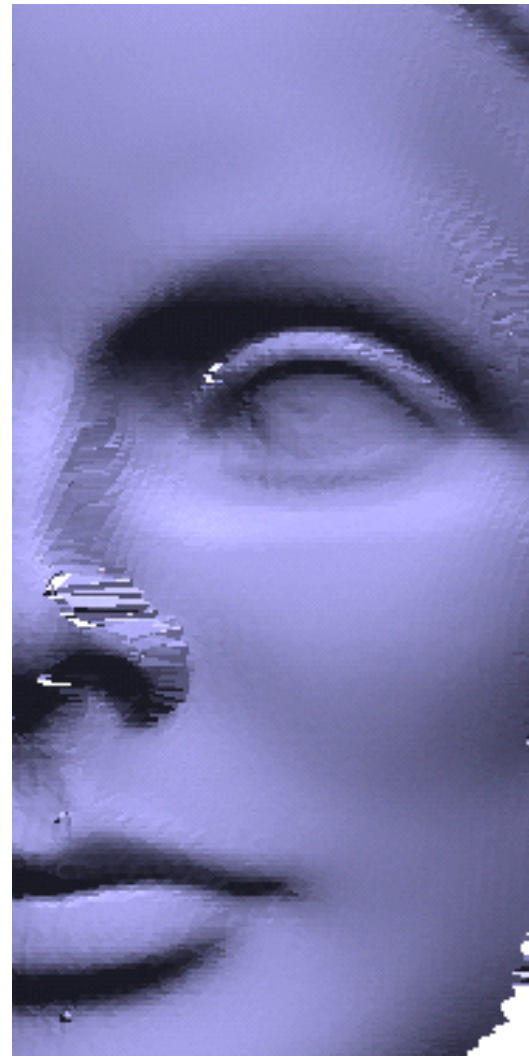
# Results - Effect of Mollification



Original

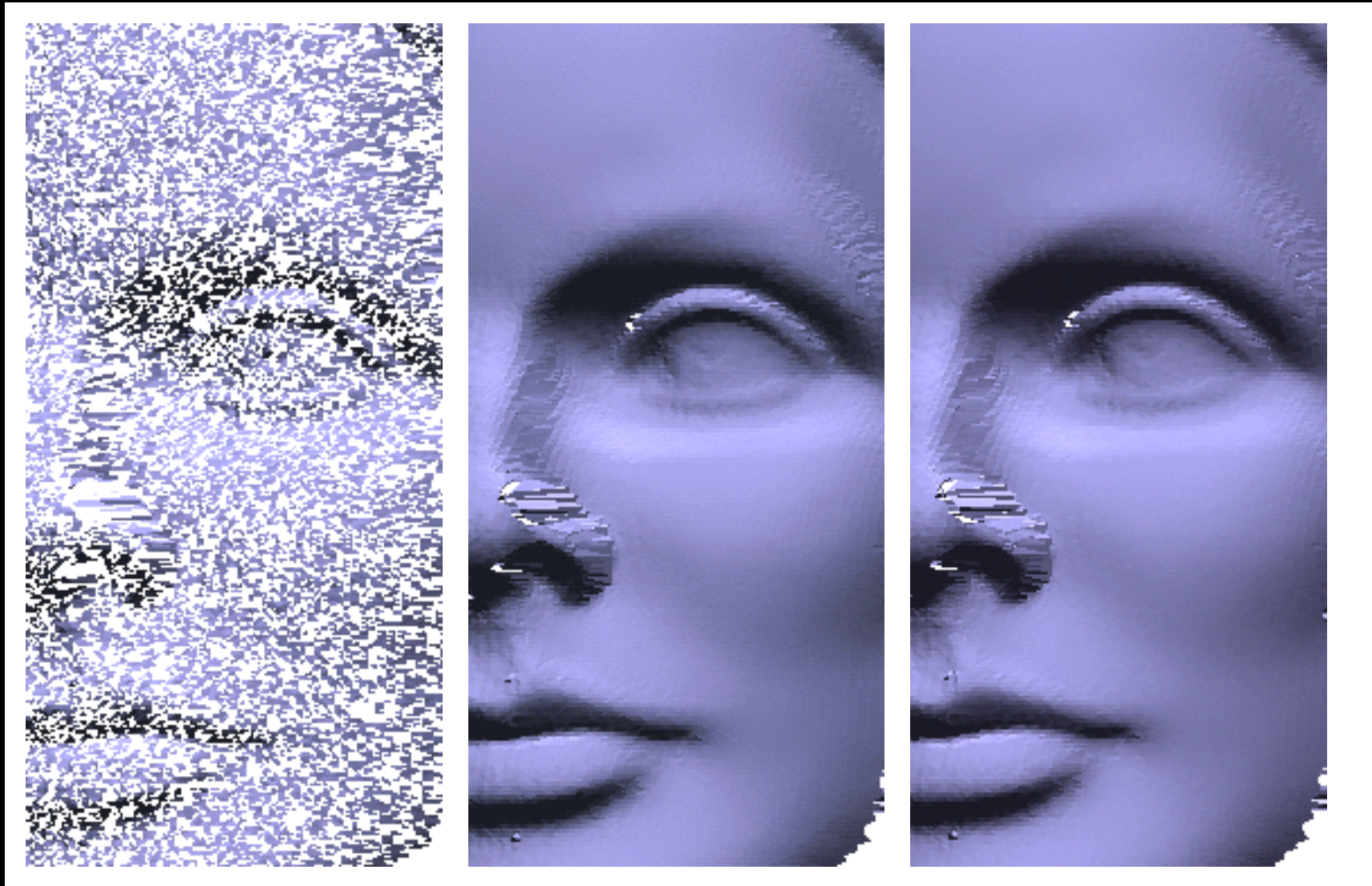


Without mollification



Our result

# Results - Connectivity

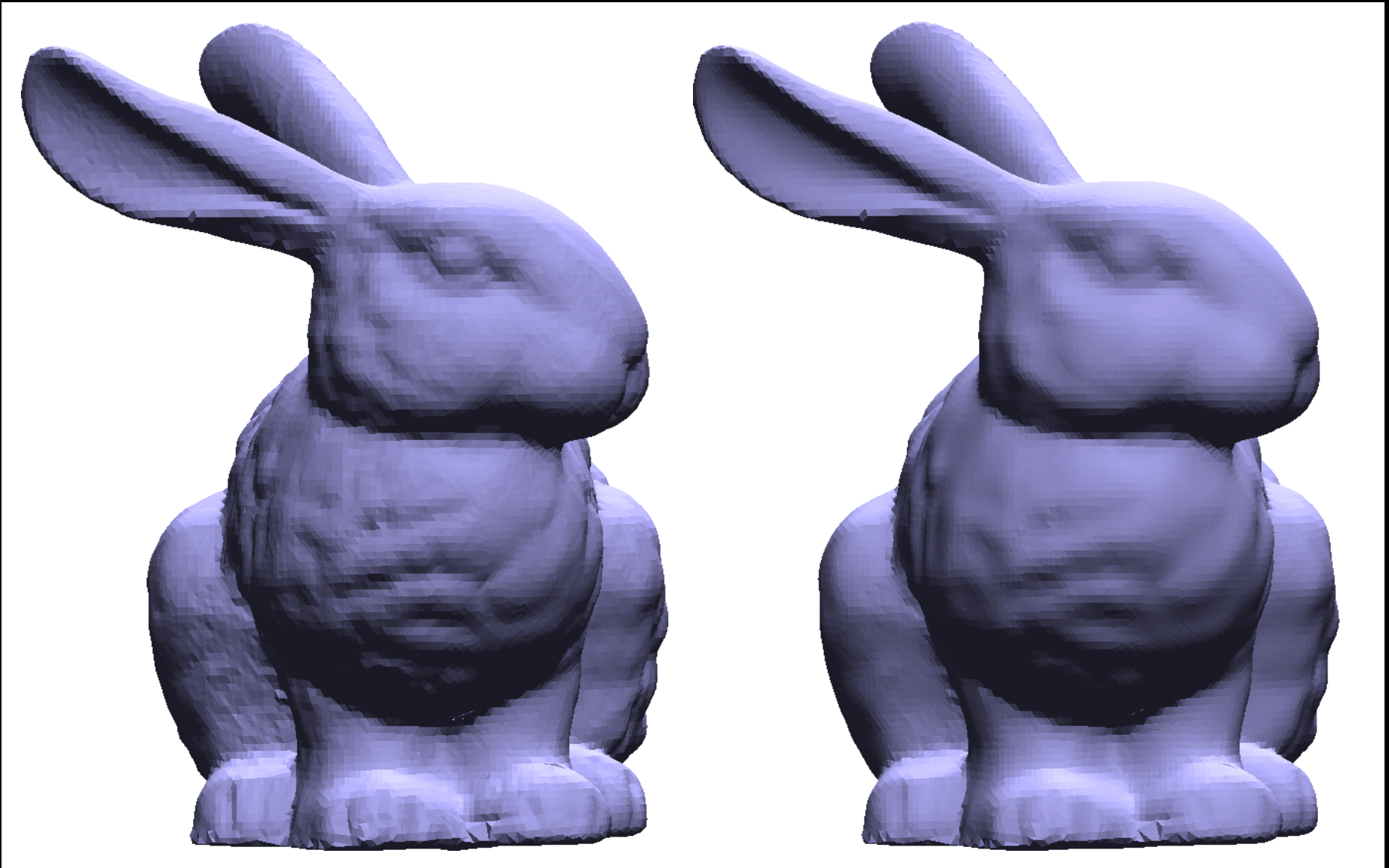


50% Original

Smoothed

All predictors

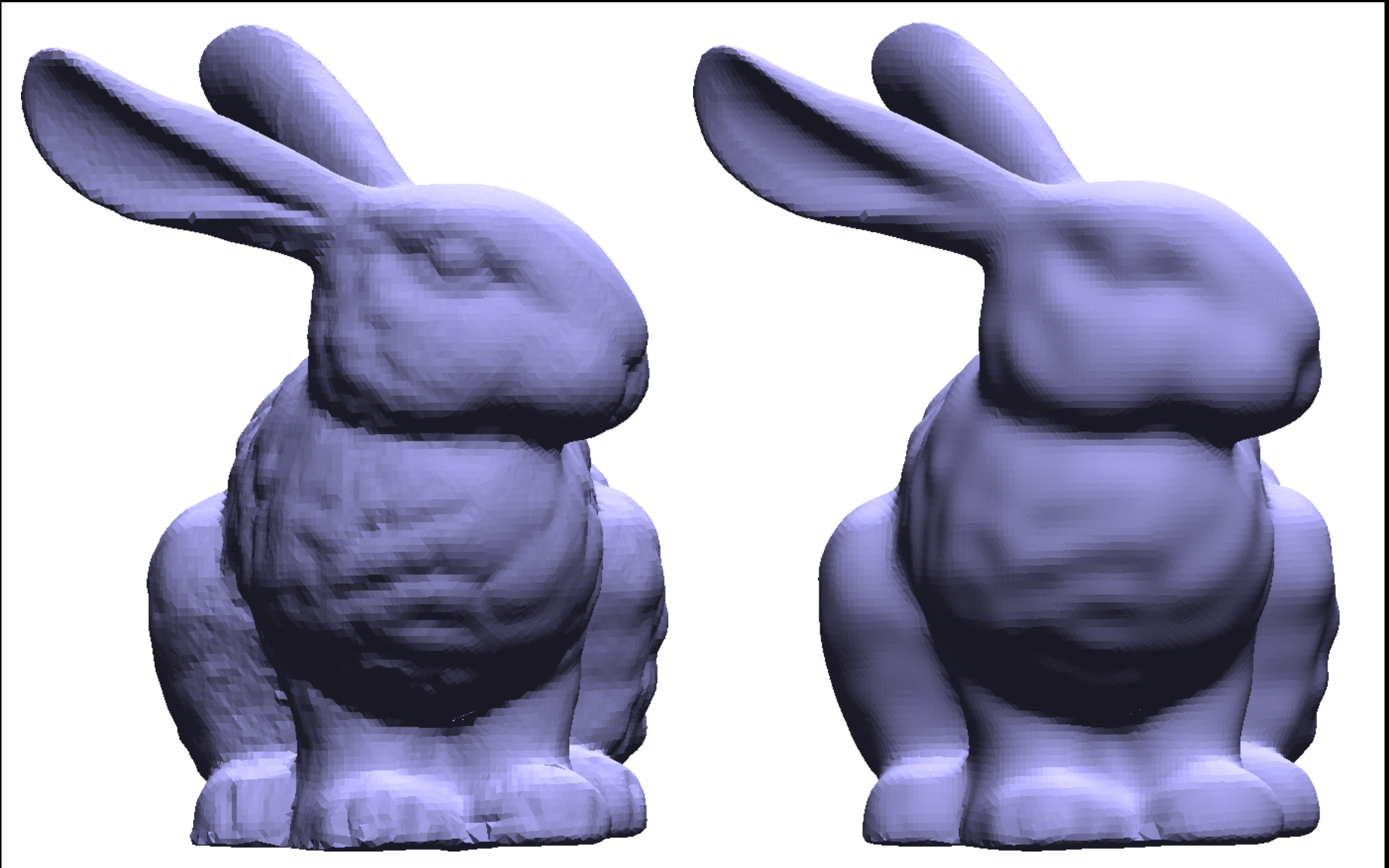
# Results - Varying width of $f$ and $g$



Original

Narrow spatial and influence

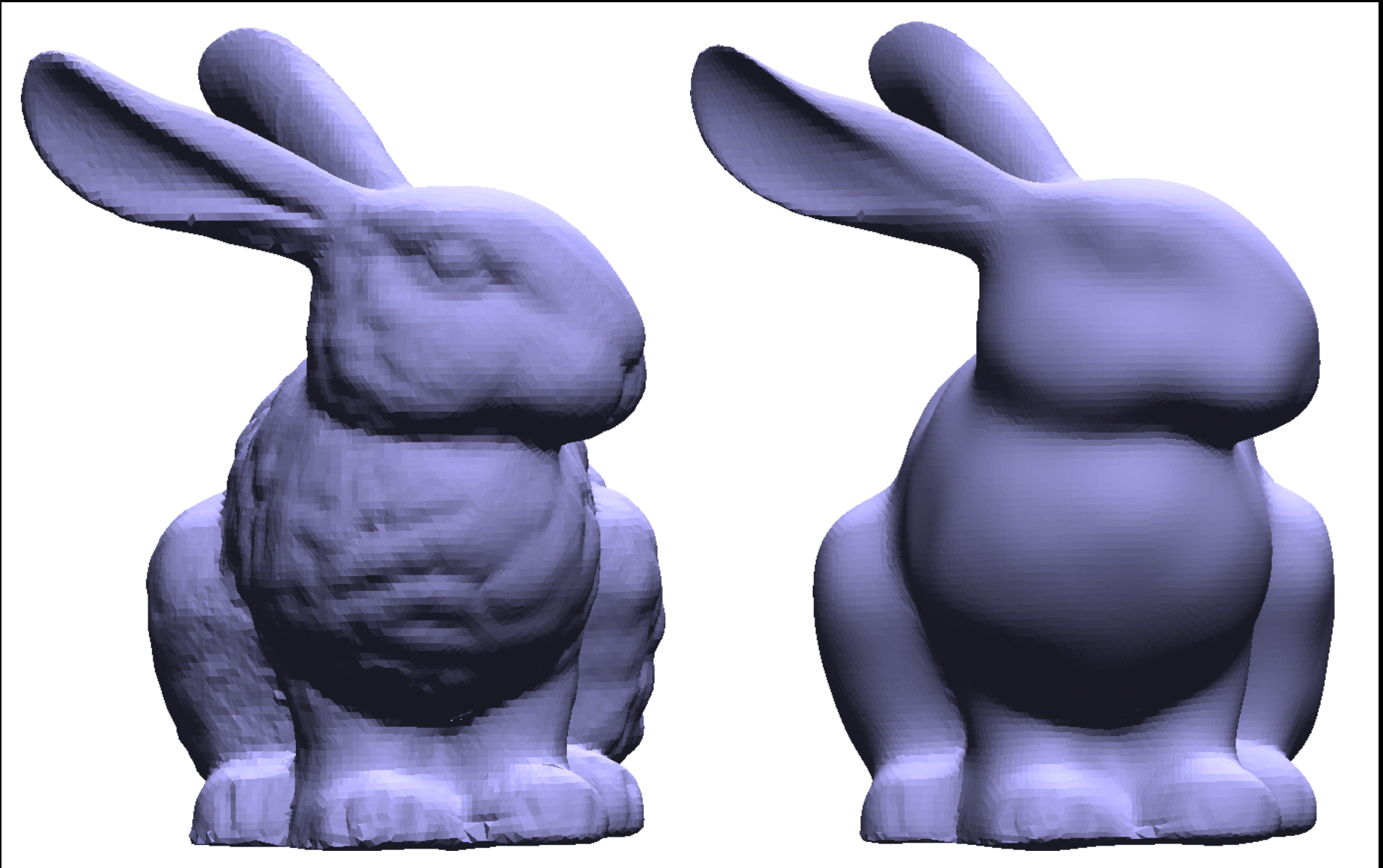
# Results - Varying width of $f$ and $g$



Original

Narrow spatial and wide influence

# Results - Varying width of $f$ and $g$



Original

Wide spatial and influence

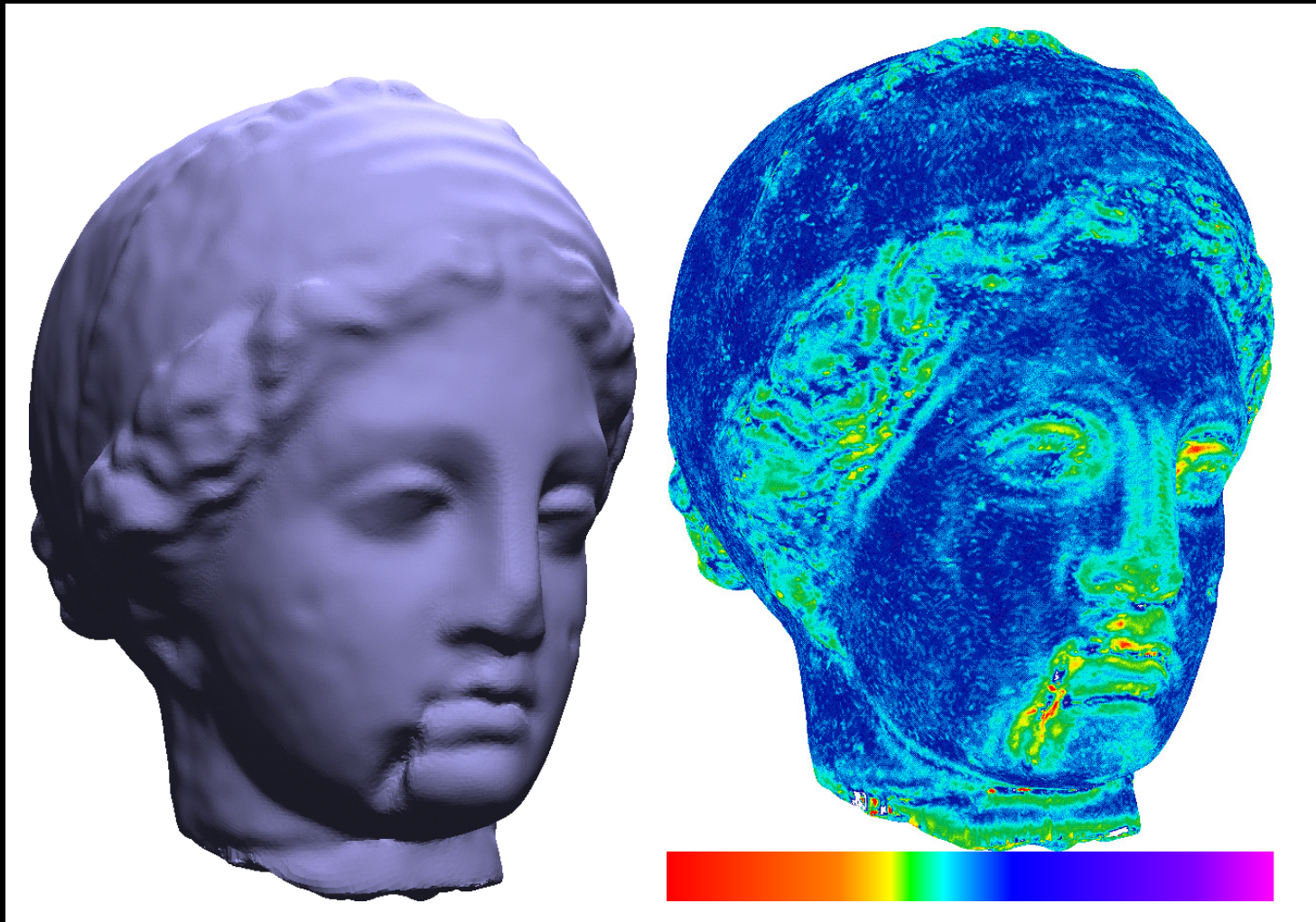
## Normalization factor $k$ as “Confidence”

Normalization term  $k(p)$  is sum of weights, and is a measure of *confidence* in the estimation at  $p$ .

$$p' = \frac{1}{k(p)} \sum_{q \in S} \Pi_q(p) f(\|c_q - p\|) g(\|\Pi_q(p) - p\|) a_q$$

$$k(p) = \sum_{q \in S} f(\|c_q - p\|) g(\|\Pi_q(p) - p\|) a_q$$

# Results - $k$ as Confidence

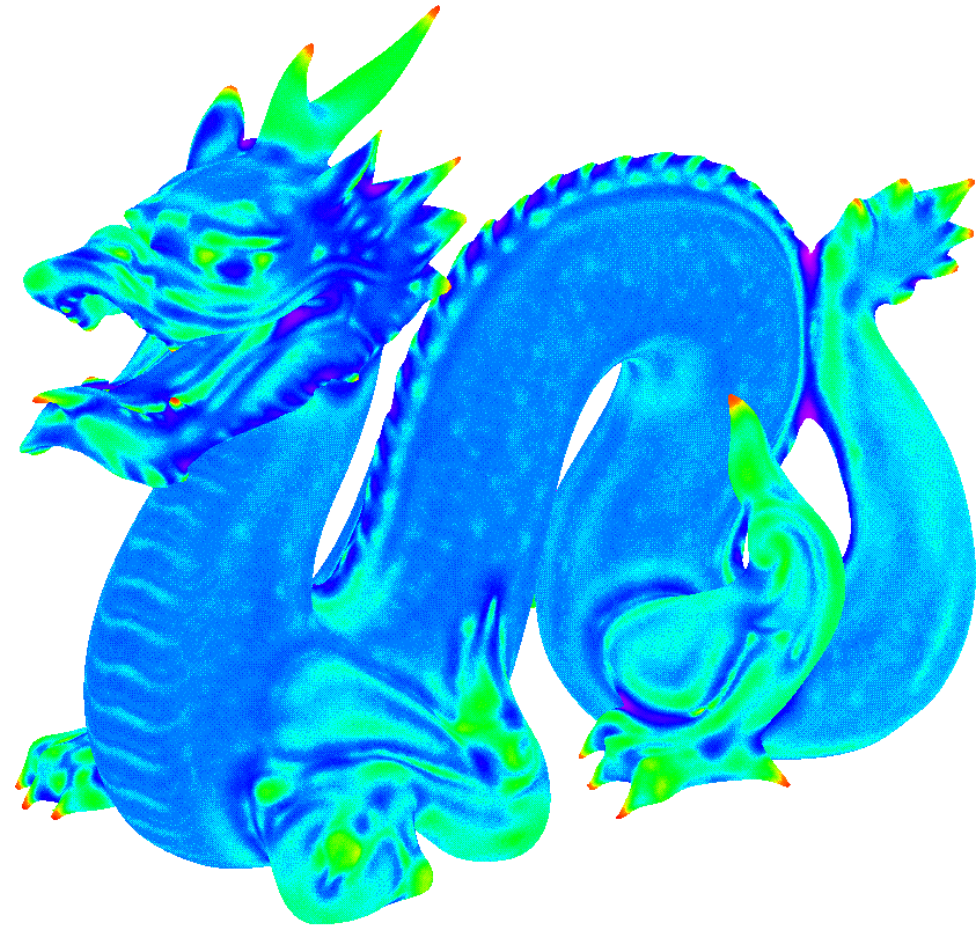


Low

High



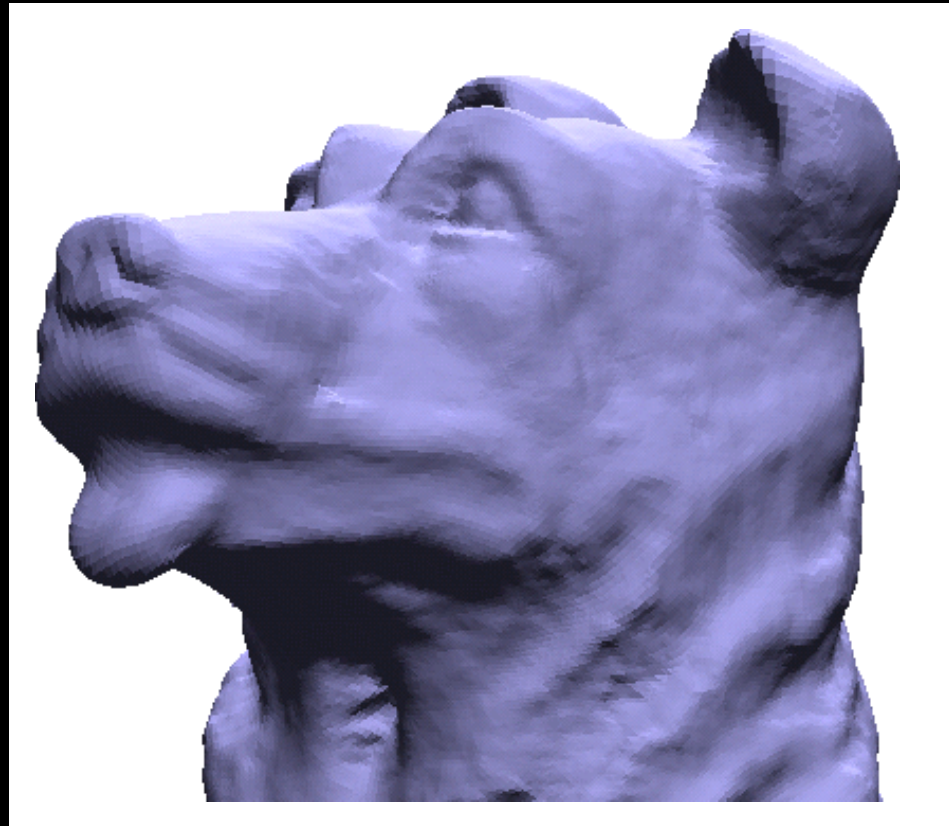
# Results - $k$ as Confidence



Low

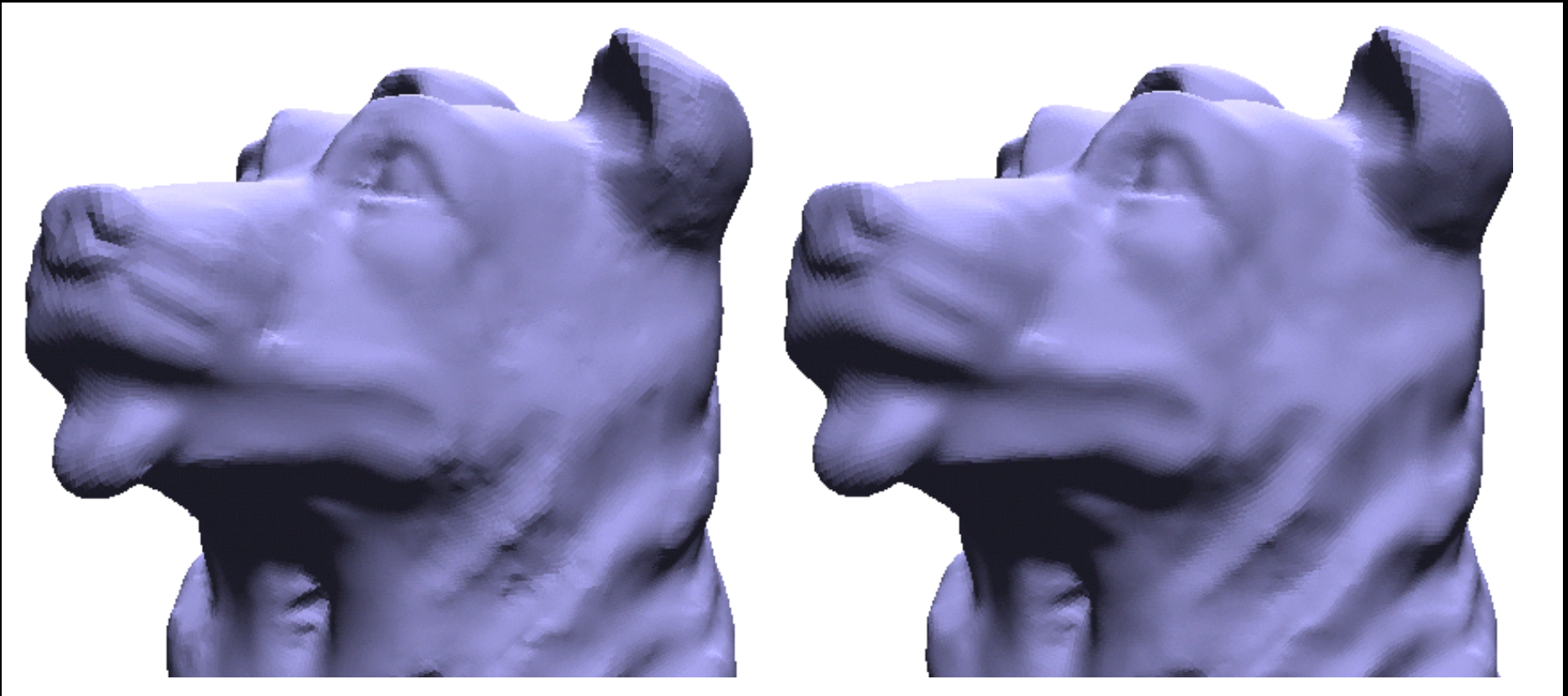
High

# Results - vs Wiener Filtering



Original

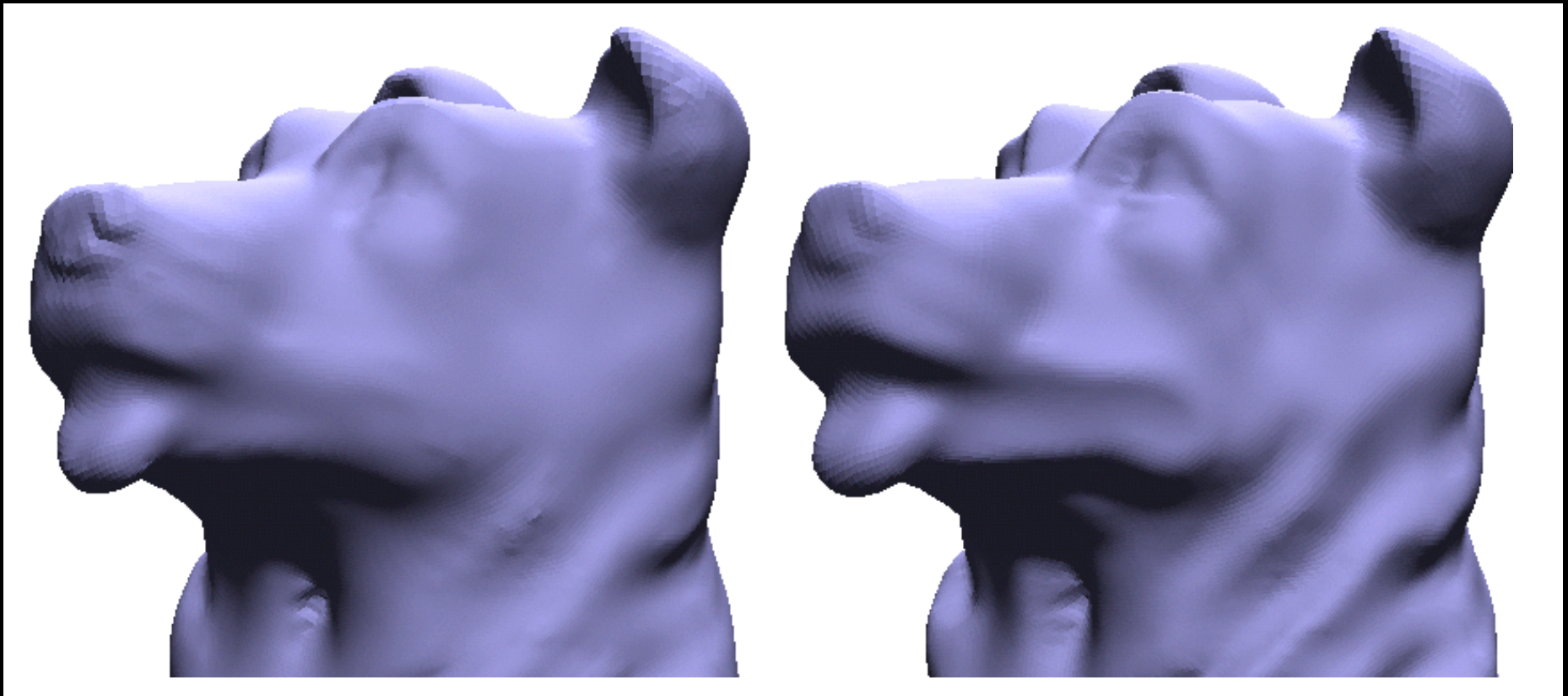
# Results - vs Wiener Filtering (Low Noise)



Peng et al. 2001

Our result

## Results - vs Wiener Filtering (High Noise)



Peng et al. 2001

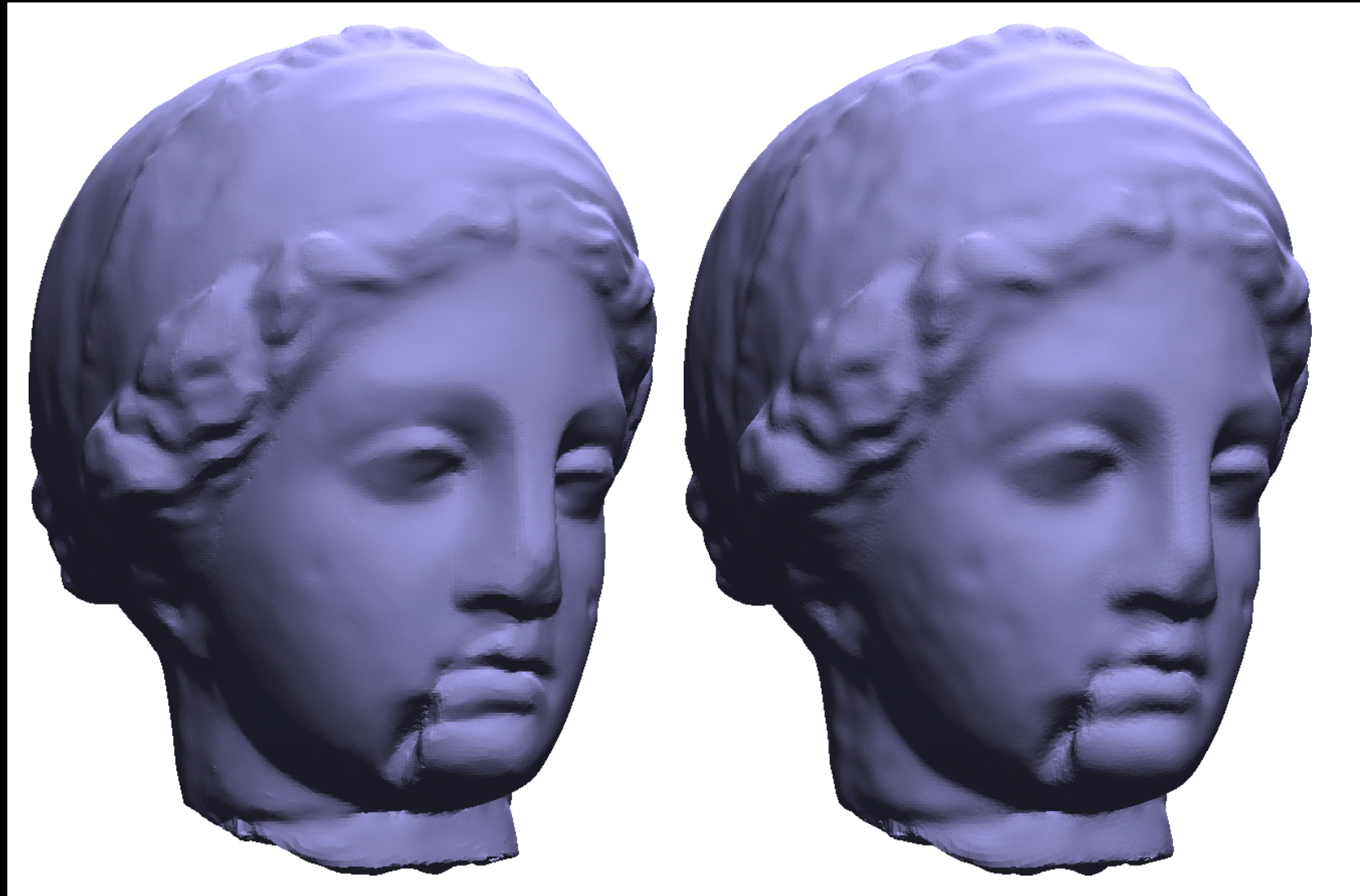
Our result

# Results - vs Anisotropic Diffusion



Original

# Results - vs Anisotropic Diffusion



Clarenz et al. 2000

Our result

## Similar Methods

Bilateral Mesh Denoising, Fleishman et al. 2003  
(next talk)

- Iterative
- Local frame
- No mollification
- Different predictor

Trilateral Filter, Cloudhury and Tumblin 2003  
(EGSR)

- Images and Meshes
- Mollify normals, then vertices
- Different predictor



## Future Work

Extend to other types of data  
(point models, volume data).

Using  $k$  to steer further processing.

Iterative application.





# Conclusions

Fast, feature preserving filter.

Simple to implement.

Applicable to polygon soups.

Take-home message:

- Robust estimation for smoothing.
- Points across features are outliers.
- First-order predictors remove connectivity requirements.



# Acknowledgements

SIGGRAPH reviewers, Caltech SigDraft and MIT pre-reviewers.

Udo Diewald, Martin Rumpf, Jianbo Peng, Denis Zorin, and Jean-Yves Bouguet, and Stanford 3D Scanning Repository for models.

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