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When taking a picture through a window pane, reflections of objects are often captured.





ransmission

Challenge: in the traditional imaging model I = T + Rsolving the transmission *T* and reflection *R* from a single observation *I* is ill-posed, since both *T* and *R* are natural images and appear the same statistical properties.

Our contribution: separate the reflection layer using the double reflection imaging model [1] with patch-based image prior [2].

Key Idea: Break the Symmetry of T and R using Ghosting





Observation: window reflection often appears multiple times. Occur on double- and single- paned windows. In single-paned windows, each side creates a reflection. The two reflections are separated by the thickness of the glass.

Reflection Removal using Ghosting Cues

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$=T+R\otimes k$



- Parameterize **k** by the separation of the two reflections **d** and an attenuation factor **a** depending on the camera view angle. $k(\mathbf{x}) = \delta(\mathbf{x}) + \alpha \delta(\mathbf{x} - \mathbf{d})$

- Estimate *d* and *a* from the input image *I* using auto-correlation function.

Optimization

To recover the transmission *T* and reflection *R*, we minimize the following:

$$\frac{1}{\sigma^2} \|I - T - R \otimes k\|_2^2 - \sum_i \log(GMM(P_iT))$$

Reconstruction cost Image prior (Gaussian Mixture Model) Non-negativity [3]





We use patch-based Gaussian Mixture Model [2] to regularize image decomposition. Correct decomposition yields higher likelihood.

(a) (b) (c)

Log-likelihood

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- Model ghosting phenomenon using a two-pulse kernel **k**.







 $f(x)) - \sum \log(GMM(P_iR)) \quad \text{s.t. } 0 \le T, R \le 1$





Synthetic input





constraints







14.01 dB 0.5499

26.76 dB 0.9083

The non-negativity constraint regularizes the low-frequency components in the output, and leads to better colors. The above energy is minimized by bounded L-BFGS optimization.



Input image (I)



Limitations: we assume sparially-invariant ghostings. Performance suffers when the transmission layer contains double features. Low frequencies are still challenging.

References

CVPR 2008.

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Transmission layer (T)



Reflection layer (**R**)

Comparisons to single image reflection removal

Levin et al. 2007

Li and Brown 2014

Our method

[1] Y. Diamant and Y. Y. Schechner. Overcoming visual reverberations,

[2] D. Zoran and Y. Weiss. From learning models of natural image patches to whole image restoration, ICCV 2011.

[3] R. Szeliski, S. Avidan, and P. Anandan. Layer extraction from multiple images containing reflections and transparency, CVPR 2000.