Character-Aware Neural Language Models

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Code: https://github.com/yoonkim/lstm-char-cnn

Language Model (LM): probability distribution over a sequence of words.

 $p(w_1, \ldots, w_T)$ for any sequence of length T from a vocabulary \mathcal{V} (with $w_i \in \mathcal{V}$ for all i).

Important for many downstream applications:

- machine translation
- speech recognition
- text generation

By the chain rule, any distribution can be factorized as

$$p(w_1,...,w_T) = \prod_{t=1}^T p(w_t|w_1,...,w_{t-1})$$

Count-based *n*-gram language models make a Markov assumption:

$$p(w_t|w_1,\ldots,w_t) \approx p(w_t|w_{t-n},\ldots,w_{t-1})$$

Need smoothing to deal with rare *n*-grams.

Neural Language Models

Neural Language Models (NLM)

• Represent words as dense vectors in \mathbb{R}^n (word embeddings).

$$\mathbf{w}_t \in \mathbb{R}^{|\mathcal{V}|}$$
: One-hot representation of word $\in \mathcal{V}$ at time $t \Rightarrow \mathbf{x}_t = \mathbf{X}\mathbf{w}_t$: Word embedding $(\mathbf{X} \in \mathbb{R}^{n \times |\mathcal{V}|}, n < |\mathcal{V}|)$

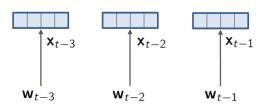
• Train a neural net that composes history to predict next word.

$$p(w_t = j | w_1, \dots, w_{t-1}) = \frac{\exp(\mathbf{p}^j \cdot g(\mathbf{x}_1, \dots, \mathbf{x}_{t-1}) + q^j)}{\sum_{j' \in \mathcal{V}} \exp(\mathbf{p}^{j'} \cdot g(\mathbf{x}_1, \dots, \mathbf{x}_{t-1}) + q^{j'})}$$
$$= \operatorname{softmax}(\mathbf{P}g(\mathbf{x}_1, \dots, \mathbf{x}_{t-1}) + \mathbf{q})$$

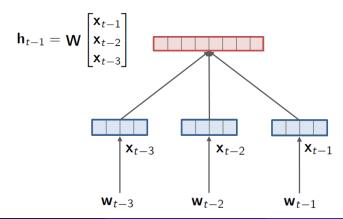
 $\mathbf{p}^j \in \mathbb{R}^m, q^j \in \mathbb{R}$: Output word embedding/bias for word $j \in \mathcal{V}$ g : Composition function

$$\mathbf{W}_{t-3}$$
 \mathbf{W}_{t-2} \mathbf{W}_{t-1}

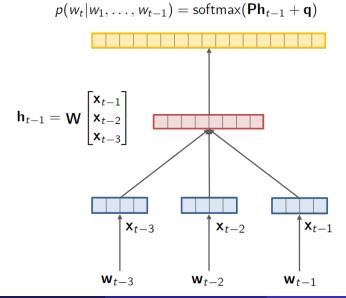
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Character-Aware Neural Language Models



Feed-forward NLM (Bengio, Ducharme, and Vincent 2003)



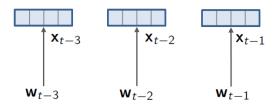
Maintain a hidden state vector \mathbf{h}_t that is recursively calculated.

$$\mathbf{h}_t = f(\mathbf{W}\mathbf{x}_t + \mathbf{U}\mathbf{h}_{t-1} + \mathbf{b})$$

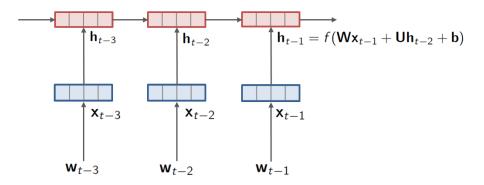
 $\mathbf{h}_t \in \mathbb{R}^m$: Hidden state at time t (summary of history) $\mathbf{W} \in \mathbb{R}^{m \times n}$: Input-to-hidden transformation $\mathbf{U} \in \mathbb{R}^{m \times m}$: Hidden-to-hidden transformation $f(\cdot)$: Non-linearity

Apply softmax to \mathbf{h}_t .

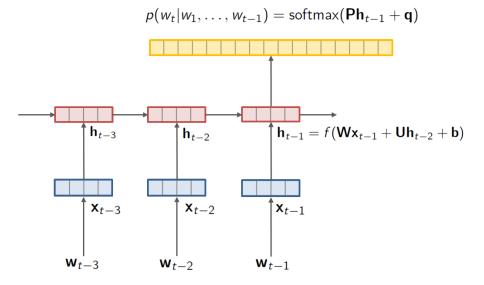
Recurrent Neural Network LM (Mikolov et al. 2011)



Recurrent Neural Network LM (Mikolov et al. 2011)

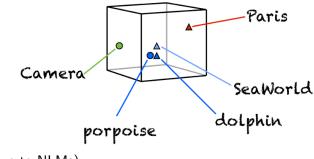


Recurrent Neural Network LM (Mikolov et al. 2011)



Key ingredient in Neural Language Models.

After training, similar words are close in the vector space.



(Not unique to NLMs)

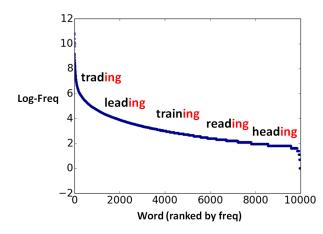
Difficult/expensive to train, but performs well.

Language Model	Perplexity
5-gram count-based (Mikolov and Zweig 2012)	141.2
RNN (Mikolov and Zweig 2012)	124.7
Deep RNN (Pascanu et al. 2013)	107.5
LSTM (Zaremba, Sutskever, and Vinyals 2014)	78.4

Renewed interest in language modeling.

NLM Issue

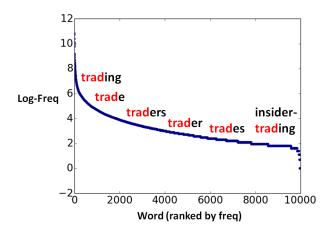
Issue: The fundamental unit of information is still the word



Separate embeddings for "trading", "leading", "training", etc.

NLM Issue

Issue: The fundamental unit of information is still the word



Separate embeddings for "trading", "trade", "trades", etc.

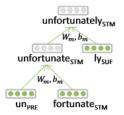
- No parameter sharing across orthographically similar words.
- Orthography contains much semantic/syntactic information.
- How can we leverage subword information for language modeling?

Previous (NLM-based) Work

Use morphological segmenter as a preprocessing step

unfortunately \Rightarrow un_{PRE} - fortunate_{STM} - ly_{SUF}

 Luong, Socher, and Manning 2013: Recursive Neural Network over morpheme embeddings



• Botha and Blunsom 2014: Sum over word/morpheme embeddings

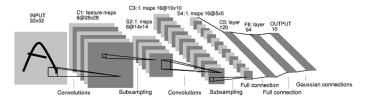
This Work

Main Idea: No morphology, use characters directly.

This Work

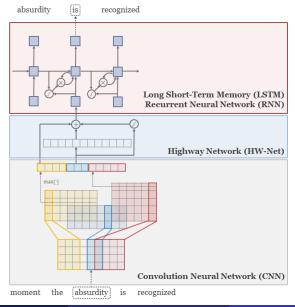
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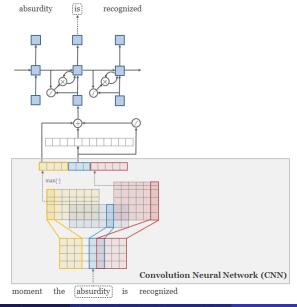
Convolutional Neural Networks (CNN) (LeCun et al. 1989)



- Central to deep learning systems in vision.
- Shown to be effective for NLP tasks (Collobert et al. 2011).
- CNNs in NLP typically involve temporal (rather than spatial) convolutions over words.

Network Architecture: Overview





 $\mathbf{C} \in \mathbb{R}^{d imes l}$: Matrix representation of word (of length l)

 $\mathbf{H} \in \mathbb{R}^{d imes w}$: Convolutional filter matrix

d : Dimensionality of character embeddings (e.g. 15)

w: Width of convolution filter (e.g. 1–7)

 $C \in \mathbb{R}^{d \times l}$: Matrix representation of word (of length *l*) $H \in \mathbb{R}^{d \times w}$: Convolutional filter matrix d: Dimensionality of character embeddings (e.g. 15) w: Width of convolution filter (e.g. 1–7)

1. Apply a convolution between $\boldsymbol{\mathsf{C}}$ and $\boldsymbol{\mathsf{H}}$ to obtain a vector $\boldsymbol{\mathsf{f}} \in \mathbb{R}^{\prime - w + 1}$

$$\mathbf{f}[i] = \langle \mathbf{C}[*, i: i + w - 1], \mathbf{H} \rangle$$

where $\langle \mathbf{A}, \mathbf{B} \rangle = \mathsf{Tr}(\mathbf{A}\mathbf{B}^{\mathsf{T}})$ is the Frobenius inner product.

 $C \in \mathbb{R}^{d \times l}$: Matrix representation of word (of length *l*) $H \in \mathbb{R}^{d \times w}$: Convolutional filter matrix *d*: Dimensionality of character embeddings (e.g. 15) *w*: Width of convolution filter (e.g. 1–7)

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$$\mathbf{f}[i] = \langle \mathbf{C}[*,i:i+w-1], \mathbf{H} \rangle$$

where $\langle \mathbf{A}, \mathbf{B} \rangle = \text{Tr}(\mathbf{AB}^T)$ is the Frobenius inner product. 2. Take the *max-over-time* (with bias and nonlinearity)

$$y = tanh(\max_{i} \{\mathbf{f}[i]\} + b)$$

as the feature corresponding to the filter H (for a particular word).

a b s u r d i t y

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$\mathbf{C} \in \mathbb{R}^{d \times l}$: Representation of *absurdity*

0.4	-0.8	2.2	0.1	0.5	-0.4	0.4	-0.4	0.1
0.1	1.2	1.5	-0.8	-1.5	0.2	0.1	1.2	0.7
0.2	0.1	-1.2	0.2	-0.2	0.3	0.2	-1.3	-0.1
-0.2	-0.5	0.1	0.2	-0.3	0.3	-0.1	1.0	-0.3
	*			• •	• •			
а	b	s	u	r	d	i	t	У

 $\mathbf{H} \in \mathbb{R}^{d imes w}$: Convolutional filter matrix of width w = 3

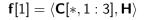
			1 a	l b	s	u	 r	· · d	i	t	Î У	
			-0.2	-0.5	0.1	0.2	-0.3	0.3	-0.1	1.0	-0.3	
3	-0.1	-1.1	0.2	0.1	-1.2	0.2	-0.2	0.3	0.2	-1.3	-0.1	
2	-0.2	0.7	0.1	1.2	1.5	-0.8	-1.5	0.2	0.1	1.2	0.7	
_	0.9	0.3	0.4	-0.8	2.2	0.1	0.5	-0.4	0.4	-0.4	0.1	
1	0.5	2.2	 								••••	
1	0.5	2.2										

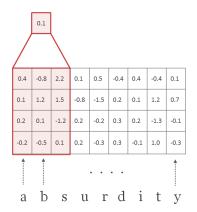
-0.

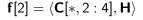
1.3

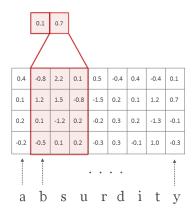
 $\mathbf{f}[1] = \langle \mathbf{C}[*, 1:3], \mathbf{H} \rangle$

0.4	-0.8	2.2	0.1	0.5	-0.4	0.4	-0.4	0.1
0.1	1.2	1.5	-0.8	-1.5	0.2	0.1	1.2	0.7
0.2	0.1	-1.2	0.2	-0.2	0.3	0.2	-1.3	-0.1
-0.2	-0.5	0.1	0.2	-0.3	0.3	-0.1	1.0	-0.3
*	*			• •	• •			
а	b	s	u	r	d	i	t	У

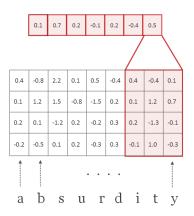




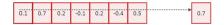




 $\mathbf{f}[T-2] = \langle \mathbf{C}[*, T-2:T], \mathbf{H} \rangle$

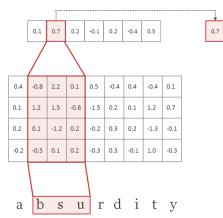


$$y[1] = \max_{i} \{\mathbf{f}[i]\}$$

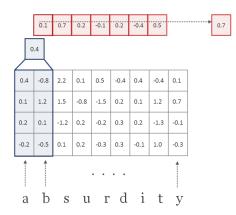


0.4	-0.8	2.2	0.1	0.5	-0.4	0.4	-0.4	0.1
0.1	1.2	1.5	-0.8	-1.5	0.2	0.1	1.2	0.7
0.2	0.1	-1.2	0.2	-0.2	0.3	0.2	-1.3	-0.1
-0.2	-0.5	0.1	0.2	-0.3	0.3	-0.1	1.0	-0.3
				•••	•••			•
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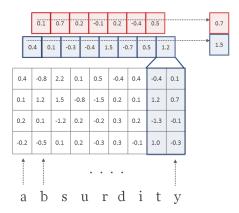
Each filter picks out a character *n*-gram



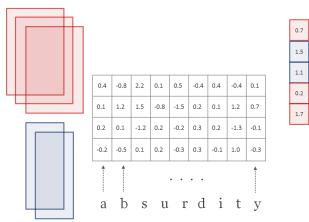
 $\mathbf{f'}[1] = \langle \mathbf{C}[*, 1:2], \mathbf{H'} \rangle$



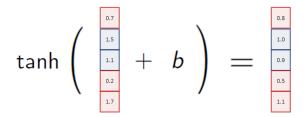
$$y[2] = \max_{i} \{\mathbf{f}'[i]\}$$



Many filter matrices (25–200) per width (1–7)



Add bias, apply nonlinearity

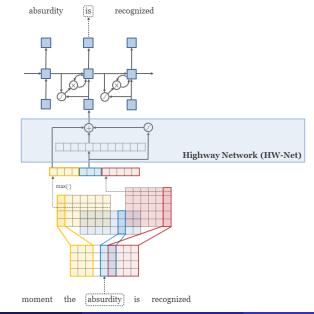


BeforeNowWord embeddingOutput from CharCNNPTB Perplexity: 85.4PTB Perplexity: 84.6

CharCNN is slower, but convolution operations on GPU have been very optimized.

Can we model more complex interactions between character *n*-grams picked up by the filters?

Highway Network



Highway Network

 \boldsymbol{y} : output from CharCNN

Multilayer Perceptron

$$\mathbf{z} = g(\mathbf{W}\mathbf{y} + \mathbf{b})$$

y : output from CharCNN

Multilayer Perceptron

$$\mathbf{z} = g(\mathbf{W}\mathbf{y} + \mathbf{b})$$

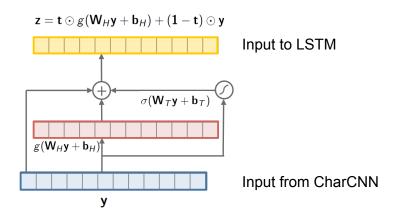
Highway Network

(Srivastava, Greff, and Schmidhuber 2015)

$$\mathsf{z} = \mathsf{t} \odot g(\mathsf{W}_H\mathsf{y} + \mathsf{b}_H) + (1 - \mathsf{t}) \odot \mathsf{y}$$

 $\mathbf{W}_{H}, \mathbf{b}_{H}$: Affine transformation $\mathbf{t} = \sigma(\mathbf{W}_{T}\mathbf{y} + \mathbf{b}_{T})$: transform gate $\mathbf{1} - \mathbf{t}$: carry gate

Hierarchical, adaptive composition of character n-grams.



Model	Perplexity
Word Model	85.4
No Highway Layers	84.6
One MLP Layer	92.6
One Highway Layer	79.7
Two Highway Layers	78.9

No more gains with 2+ layers.

	PPL	Size
KN-5 (Mikolov et al. 2012)	141.2	2 m
RNN (Mikolov et al. 2012)	124.7	6 m
Deep RNN (Pascanu et al. 2013)	107.5	6 m
Sum-Prod Net (Cheng et al. 2014)	100.0	5 m
LSTM-Medium (Zaremba, Sutskever, and Vinyals 2014)	82.7	20 m
LSTM-Huge (Zaremba, Sutskever, and Vinyals 2014)	78.4	52 m
LSTM-Word-Small	97.6	5 m
LSTM-Char-Small	92.3	5 m
LSTM-Word-Large	85.4	20 m
LSTM-Char-Large	78.9	19 m

	Ι	DATA-S			Data-l		
	$ \mathcal{V} $	$ \mathcal{C} $	Т	$ \mathcal{V} $	$ \mathcal{C} $	Т	
English (EN)	10 k	51	1 m	60 k	197	20 m	
$Czech\ (\mathrm{Cs})$	46 k	101	1 m	206 k	195	17 m	
German (DE)	37 k	74	1 m	339 k	260	51 m	
Spanish (Es)	27 k	72	1 m	152 k	222	56 m	
French (FR)	25 k	76	1 m	137 k	225	57 m	
Russian (RU)	62 k	62	1 m	497 k	111	25 m	

- $|\mathcal{V}| = \mathsf{Word} \mathsf{ \ vocab \ Size}$
- $|\mathcal{C}| = \mathsf{Character} \text{ vocab size}$
- T = number of tokens in training set.

	DATA-S			Data-l		
	$ \mathcal{V} $	$ \mathcal{C} $	Т	$ \mathcal{V} $	$ \mathcal{C} $	Т
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 $|\mathcal{V}|$ varies quite a bit by language.

(effectively use the full vocabulary)

Baselines

Kneser-Ney LM: Count-based baseline

Word LSTM: Word embeddings as input

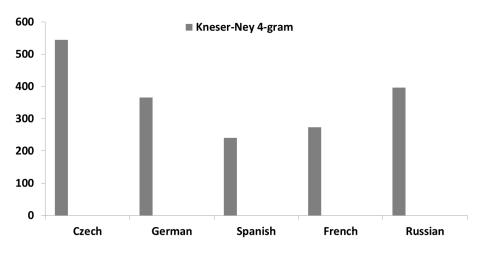
Morpheme LBL (Botha and Blunsom 2014)

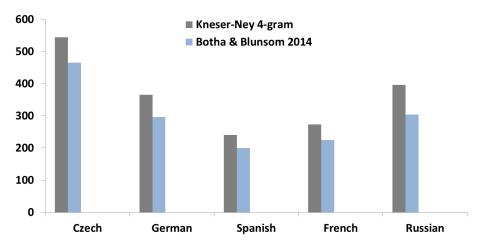
Input for word k is

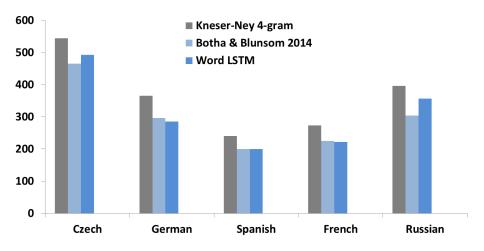


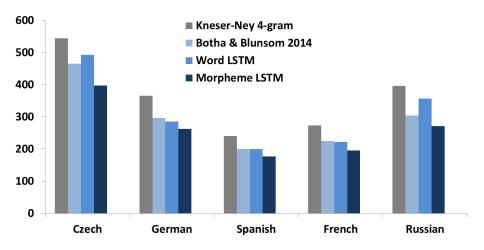
Morpheme LSTM: Same input as above, but with LSTM architecture

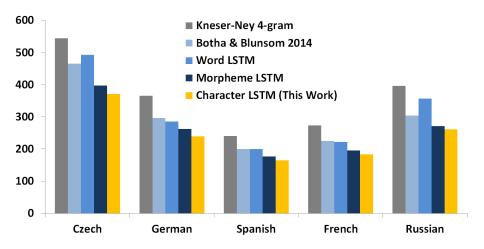
Morphemes obtained from running an unsupervised morphological tagger Morfessor Cat-MAP (Creutz and Lagus 2007).

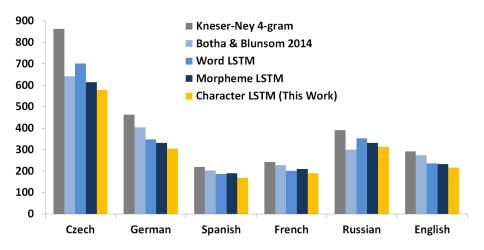




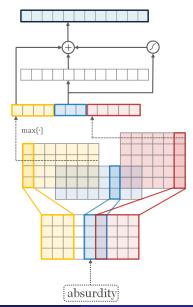




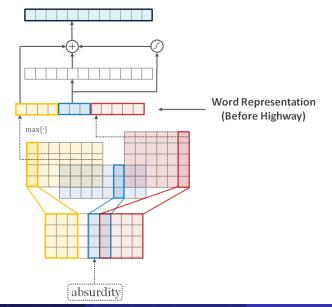




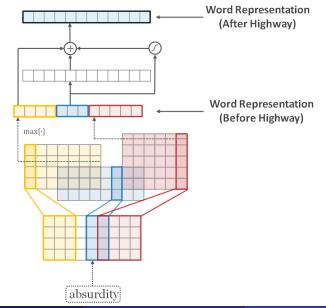
Learned Word Representations



Learned Word Representations



Learned Word Representations



		In Vocabulary			
	while	his	you	richard	trading
Word	although letting	your her	conservatives we	jonathan robert	advertised advertising
Embedding	though	тy	guys	neil	turnover
	minute	their	i	nancy	turnover

	In Vocabulary				
	while	his	you	richard	trading
Word Embedding	although letting though minute	your her my their	conservatives we guys i	jonathan robert neil nancy	advertised advertising turnover turnover
Characters (before highway)	chile whole meanwhile white	this hhs is has	your young four youth	hard rich richer richter	heading training reading leading

	In Vocabulary				
	while	his	you	richard	trading
	although	your	conservatives	jonathan	advertised
Word	letting	her	we	robert	advertising
Embedding	though	тy	guys	neil	turnover
	minute	their	i	nancy	turnover
	chile	this	your	hard	heading
Characters	whole	hhs	young	rich	training
(before highway)	meanwhile	is	four	richer	reading
	white	has	youth	richter	leading
	meanwhile	hhs	we	eduard	trade
Characters	whole	this	your	gerard	training
(after highway)	though	their	doug	edward	traded
,	nevertheless	your	i	carl	trader

	In Vocabulary				
	while	his	you	richard	trading
Word	although letting	your her	conservatives we	jonathan robert	advertised advertising
Embedding	though	my	guys	neil	turnover
-	minute	their	i	nancy	turnover
Characters (before highway)	chile whole meanwhile white	this hhs is has	your young four youth	hard rich richer richter	heading training reading leading
Characters (after highway)	meanwhile whole though nevertheless	hhs this their your	we your doug i	eduard gerard edward carl	trade training traded trader

	In Vocabulary				
	while	his	you	richard	trading
	although	your	conservatives	jonathan	advertised
Word	letting	her	we	robert	advertising
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Characters	whole	hhs	young	rich	training
(before highway)	meanwhile	is	four	richer	reading
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· · · · · · · · · · · · · · · · · · ·	nevertheless	your	i	carl	trader

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	minute	their	i	nancy	turnover
Characters	chile whole	this hhs	your	hard rich	heading training
			young		0
(before highway)	meanwhile	is	four	richer	reading
	white	has	youth	richter	leading
Characters	meanwhile whole	hhs this	we your	eduard gerard	trade training
(after highway)	though	their	doug	edward	traded
(arter ingrivay)	nevertheless		i	carl	trader
	never liteless	your	I	Call	LIAUEI

Learned Word Representations (OOV)

	Out-o computer-aided	of-Vocabulary misinformed	looooook
Characters (before highway)	computer-guided computerized disk-drive computer	informed performed transformed inform	look cook looks shook
Characters (after highway)	computer-guided computer-driven computerized computer	informed performed outperformed transformed	look looks looked looking

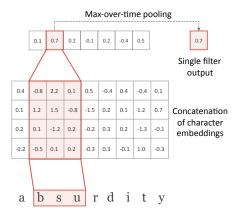
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Characters (before highway)	computer-guided computerized disk-drive computer	informed performed transformed inform	look cook looks shook
Characters (after highway)	computer-guided computer-driven computerized computer	informed performed outperformed transformed	look looks looked looking

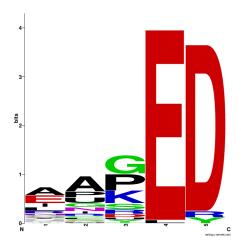
Learned Word Representations (OOV)

	Out-o	looooook	
Characters	computer-aided computer-guided computerized	misinformed informed performed	look cook
(before highway)	disk-drive	transformed	looks
	computer	inform	shook
Characters (after highway)	computer-guided	informed	look
	computer-driven	performed	looks
	computerized	outperformed	looked
	computer	transformed	looking

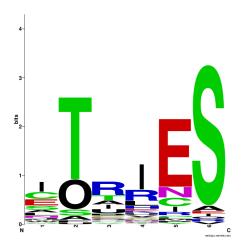
Does each filter truly pick out a character *n*-gram?



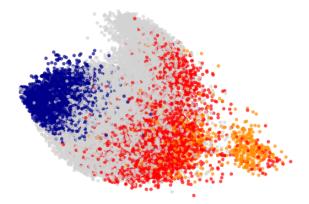
For each filter, visualize 100 substrings with the highest filter response



For each filter, visualize 100 substrings with the highest filter response



Character *N*-gram Representations



Prefixes, Suffixes, Hyphenated, Others

Prefixes: character *n*-grams that start with 'start-of-word' character, such as $\{un, \{mis. Suffixes defined similarly. \}$

A **character-aware** language model that relies only on character-level inputs: CNN over characters + LSTM.

Outperforms strong word/morpheme LSTM baselines.

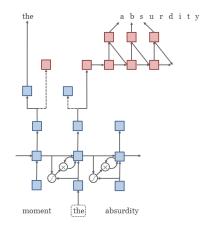
Much recent work on character inputs:

- Santos and Zadrozny 2014: CNN over characters concatenated with word embeddings into CRF.
- Zhang and LeCun 2015: Deep CNN over characters for document classification.
- Ballesteros, Dyer, and Smith 2015: LSTM over characters for parsing.
- Ling et al. 2015: LSTM over characters into another LSTM for language modeling/POS-tagging.

Subword information on the output.

As an encoder/decoder in neural machine translation.

CharCNN + Highway layers for representation learning (e.g. as input into word2vec)



Appendix: Performance vs Corpus/Vocab Size

How does relative performance vary as corpus/vocabulary sizes vary?

Experiment on German large dataset:

- Use the first *T* tokens of the training set.
- Take the most frequent K words as the vocabulary and replace rest with <unk>
- Compare % perplexity reduction going from word to character LSTM.

		Vocabulary Size				
		10 k 25 k 50 k 100 k				
	1 m	17	16	21	_	
Training	5 m	8	14	16	21	
Size	10 m	9	9	12	15	
	25 m	9	8	9	10	

Character model outperforms word model in all scenarios.

		Small	Large
	d	15	15
CNN	W	$\left[1,2,3,4,5,6\right]$	$\left[1,2,3,4,5,6,7\right]$
CININ	h	[25 · w]	$[\min\{200, 50 \cdot w\}]$
	f	tanh	tanh
	Ι	1	2
HW-Net	g	ReLU	ReLU
LSTM	Ι	2	2
	т	300	650

		\mathbf{Cs}	De	Es	$\mathbf{F}\mathbf{R}$	Ru
B&B	KN-4	545	366	241	274	396
	MLBL	465	296	200	225	304
Small	Word	503	305	212	229	352
	Morph	414	278	197	216	290
	Char	401	260	182	189	278
Large	Word	493	286	200	222	357
	Morph	398	263	177	196	271
	Char	371	239	165	184	261

		\mathbf{Cs}	De	\mathbf{Es}	$\mathbf{F}\mathbf{R}$	Ru	En
B&B	KN-4 MLBL						
Small	Word Morph						
	Char	578	305	169	190	313	216

	Small Model	Large Model
No Highway Layers	100.3	84.6
One Highway Layer	92.3	79.7
Two Highway Layers	90.1	78.9
Multilayer Perceptron	111.2	92.6

Long short-term memory (LSTM) (Hochreiter and Schmidhuber 1997): Augment RNN with (latent) cell vectors to allow for learning of long-range dependencies.

$$\mathbf{i}_{t} = \sigma(\mathbf{W}^{i}\mathbf{x}_{t} + \mathbf{U}^{i}\mathbf{h}_{t-1} + \mathbf{b}^{i})$$

$$\mathbf{f}_{t} = \sigma(\mathbf{W}^{f}\mathbf{x}_{t} + \mathbf{U}^{f}\mathbf{h}_{t-1} + \mathbf{b}^{f})$$

$$\mathbf{o}_{t} = \sigma(\mathbf{W}^{o}\mathbf{x}_{t} + \mathbf{U}^{o}\mathbf{h}_{t-1} + \mathbf{b}^{o})$$

$$\mathbf{g}_{t} = \tanh(\mathbf{W}^{g}\mathbf{x}_{t} + \mathbf{U}^{g}\mathbf{h}_{t-1} + \mathbf{b}^{g})$$

$$\mathbf{c}_{t} = \mathbf{f}_{t} \odot \mathbf{c}_{t-1} + \mathbf{i}_{t} \odot \mathbf{g}_{t}$$

$$\mathbf{h}_{t} = \mathbf{o}_{t} \odot \tanh(\mathbf{c}_{t})$$

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